

CH5440: MULTIVARIATE DATA ANALYSIS

QUIZ 1      04/03/22      9:00-9:50 AM      ROLL NO: MM17B113

**NOTE: FILL IN YOUR ANSWERS IN THE QUESTION PAPER ITSELF AND UPLOAD IT**

The life expectancy in a country is considered to be strongly correlated with its average per capita expenditure on health. The annual per capita expenditure on health spent by a country (in terms of equivalent 2017 US \$) and the corresponding average life expectancy in some of the years within the period 1970-2015 is given in the data set. Assume the following linear relation exists between life expectancy ( $y$ ) and average per capita expenditure ( $x$ ) :  $y = ax + b$

- (a) The sample mean of life expectancy is 79.08 years and average per capita expenditure is 3162.74 US \$
- (b) The sample standard deviation of life expectancy is 2.53 years and per capita expenditure is 753.19 US \$
- (c) The OLS estimate of parameter  $a$  is 0.003 and  $b$  is 68.61
- (d) The TLS estimate of parameter  $a$  is 0.003 and  $b$  is 68.61
- (e) The additional per capita amount required to be spent by the country to increase life expectancy by an additional 5 years is 1691.6 US \$
- (f) If the country spends US \$ 1000 on health, the life expectancy is known to be exactly 70 years. If the OLS regression line has to pass through this data then the estimate of parameter  $a$  is 0.0035
- (g) The lower and upper bounds on the estimate for parameter  $a$  are 0.003313223 and 0.003313222 respectively
- (h) The estimated standard deviation of error in the measurements of life expectancy using OLS is 0.47 years
- (i) Assuming that the errors in life expectancy data are normally distributed, the 95% confidence interval for the parameter  $a$  obtained using OLS is between -205.95 and 205.95