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AI1110 Assignment 2 in LATEX

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12.13.6.16: Bag I contains 3 red balls and 4 black balls and Bag II contains 4 red and 5 black balls. One ball is transfered from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be red in colour. Find the probability that the transfered ball is black. **Solution**:

 $\begin{tabular}{ll} TABLE \ 0 \\ Random \ variables \ and \ their \ distribution \end{tabular}$

Random variable	Description	Values
X	Colour of transferred ball	0 for red,1 for black
Y	Colour of drawn ball	0 for red,1 for black

By using Bayes' theorem, the probability that the transferred ball is black given that the drawn ball is red

$$\Pr(X = 1|Y = 0) = \frac{\Pr(Y = 0|X = 1) \times \Pr(X = 1)}{\Pr(Y = 0)}$$
(1)

where P(Y = 0|X = 1) is the probability of drawing a red ball from Bag II given that the transferred ball is black, P(X = 1) is the probability of transferring a black ball from Bag I to Bag II, and P(Y = 0) is the probability of drawing a red ball from Bag II.

We can calculate each of these probabilities as follows:

$$\Pr(Y = 0|X = 1) = \frac{4}{10} \tag{2}$$

$$\implies \Pr(Y = 0|X = 1) = \frac{2}{5} \tag{3}$$

$$\Pr(X = 1) = \frac{4}{7} \tag{4}$$

$$Pr(Y = 0) = Pr(Y = 0|X = 0) \times Pr(X = 0) + Pr(Y = 0|X = 1) \times Pr(X = 1)$$
(5)

$$\implies \Pr(Y = 0) = \frac{5}{10} \times \frac{3}{7} + \frac{4}{10} \times \frac{4}{7}$$
 (6)

$$\implies \Pr(Y = 0) = \frac{15}{70} + \frac{16}{70} \tag{7}$$

$$\implies \Pr(Y=0) = \frac{31}{70} \tag{8}$$

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TABLE 0 EVENT AND PROBABILITY TABLE

Event	Probability
Y = 0 X = 1	2/5
X = 1	4/7
Y = 0	31/70

Substituting these values in equation number (1),

$$\Pr(X = 1 | Y = 0) = \frac{\frac{4}{10} \times \frac{4}{7}}{\frac{31}{70}}$$
 (9)

$$\Pr(X = 1|Y = 0) = \frac{\frac{4}{10} \times \frac{4}{7}}{\frac{31}{70}}$$

$$\implies \Pr(X = 1|Y = 0) = \frac{\frac{16}{70}}{\frac{31}{70}}$$

$$\implies \Pr(X = 1|Y = 0) = \frac{16}{31}$$
(10)
$$\implies \Pr(X = 1|Y = 0) = \frac{16}{31}$$
(11)

$$\implies \Pr(X = 1|Y = 0) = \frac{16}{31}$$
 (11)

 \therefore The probability that the transferred ball is black given that the drawn ball is red is $\frac{16}{31}$.