01 KNAPSACK VARIATIONS

01.) 0 1 KNAPSACK

RECURSION

MEMOIZATION

TABULATION

2.) SUBSET SUM PROBLEM

RECURSIVE

```
class Solution{
public:
    bool func(vector<int> &arr, int n, int sum){
        if(n==0 && sum==0)
        return true;

        if(sum==0)
        return true;

        if(n==0)
        return false;

        if(arr[n-1]<=sum){
            return func(arr, n-1, sum-arr[n-1]) || func(arr, n-1, sum);
        }
        return func(arr, n-1, sum);
    }

    bool isSubsetSum(vector<int>arr, int sum){
        int n=arr.size();
        return func(arr, n, sum);
    }
};
```

MEMOIZATION

```
class Solution{
public:
              vector<vector<int>> &dp) {
        if(n==0 \&\& sum==0)
        if(sum==0)
        return true;
        if(n==0)
        if(dp[n][sum]!=-1)
        return dp[n][sum];
        if (arr[n-1] <= sum) {</pre>
            return dp[n][sum]=func(arr, n-1, sum-arr[n-1], dp) ||
                                     func(arr, n-1, sum, dp);
        return dp[n][sum]=func(arr, n-1, sum, dp);
    bool isSubsetSum(vector<int>arr, int sum){
        int n=arr.size();
        vector<vector<int>> dp(n+1, vector<int> (sum+1, -1));
        return func(arr, n, sum, dp);
```

TABULATION

03.) PARTITION EQUAL SUBSET SUM

MEMOIZATION

```
class Solution {
public:
    bool func(vector<int> &arr, int n, int sum,
              vector<vector<int>> &dp){
        if(n==0 \&\& sum==0)
        return true;
        if(sum==0)
        return true;
        if(n==0)
        return false;
        if(dp[n][sum]!=-1)
        return dp[n][sum];
        if(arr[n-1]<=sum){</pre>
            return dp[n][sum]=func(arr, n-1, sum-arr[n-1], dp) ||
                                     func(arr, n-1, sum, dp);
        return dp[n][sum]=func(arr, n-1, sum, dp);
    bool isSubsetSum(vector<int>&arr, int sum){
        int n=arr.size();
        vector<vector<int>> dp(n+1, vector<int> (sum+1, -1));
        return func(arr, n, sum, dp);
    bool canPartition(vector<int>& nums) {
        int n=nums.size();
        int sum=accumulate(nums.begin(), nums.end(), 0);
        if(sum&1)
        return false;
        int req sum=sum/2;
        return isSubsetSum(nums, req_sum);
```

TABULATION

```
class Solution {
public:
    bool isSubsetSum(vector<int>arr, int sum){
        int n=arr.size();
        vector<vector<int>> dp(n+1, vector<int> (sum+1, 0));
        for(int i=0;i<n+1;i++){</pre>
            dp[i][0]=1;
        for(int i=1;i<n+1;i++){</pre>
            for(int j=1;j<sum+1;j++){</pre>
                 if(arr[i-1]<=j)</pre>
                 dp[i][j]=dp[i-1][j-arr[i-1]] || dp[i-1][j];
                 dp[i][j]=dp[i-1][j];
        return dp[n][sum];
    bool canPartition(vector<int>& nums) {
        int n=nums.size();
        int sum=accumulate(nums.begin(), nums.end(), 0);
        if(sum&1)
        return false;
        int req_sum=sum/2;
        return isSubsetSum(nums, req_sum);
```

04.) COUNT OF A SUBSET WITH A GIVEN SUM

```
class Solution {
public:
    int mod = 1e9 + 7;
    int func(int arr[], int n, int sum) {
        vector<vector<int>> dp(n + 1, vector<int>(sum + 1, 0));
        for (int i = 0; i <= n; i++) {
            dp[i][0] = 1;
        for (int i = 1; i <= n; i++) {
            for (int j = 0; j <= sum; j++) {
                if (arr[i - 1] <= j) {
                    dp[i][j] = (dp[i - 1][j - arr[i - 1]] + dp[i - 1][j])
                                % mod;
                    dp[i][j] = dp[i - 1][j];
        return dp[n][sum];
    int perfectSum(int arr[], int n, int sum) {
        return func(arr, n, sum);
```

05.) TARGET SUM

```
class Solution {
public:
    int func(vector<int> &arr, int sum) {
        int n=arr.size();
        vector<vector<int>> dp(n + 1, vector<int>(sum + 1, 0));
        for (int i = 0; i <= n; i++) {
            dp[i][0] = 1;
        for (int i = 1; i <= n; i++) {
            for (int j = 0; j <= sum; j++) {
                if (arr[i - 1] <= j) {
                    dp[i][j] = (dp[i - 1][j - arr[i - 1]] + dp[i - 1][j]);
                } else {
                    dp[i][j] = dp[i - 1][j];
        return dp[n][sum];
    int findTargetSumWays(vector<int>& nums, int target) {
        int sum=accumulate(nums.begin(), nums.end(), 0);
        if(target>sum)
        return 0;
        if((target+sum)%2!=0)
        return 0;
        sum=(sum-target)/2;
        return func(nums, sum);
```

UNBOUNDED KNAPSACK

1.) UNBOUNDED KNAPSACK

RECURSION

MEMOIZATION

TABULATION

2.) ROD CUTTING PROBLEM

```
int cutRod(vector<int> &price, int n)
{
    vector<vector<int>> dp(n+1, vector<int>(n+1, 0));
    for(int i = 1; i <= n; i++) {
        for(int j = 1; j <= n; j++) {
            int notTake = dp[i-1][j];
            int take = 0;
            if(j >= i) {
                take = price[i-1] + dp[i][j-i];
            }
            dp[i][j] = max(take, notTake);
        }
    }
    return dp[n][n];
}
```

3.) COIN CHANGE II

4.) COIN CHANGE I

```
class Solution {
public:
    int coinChange(vector<int>& coins, int sum) {
        int n=coins.size();
        vector<vector<int>> dp(n+1, vector<int> (sum+1, INT_MAX-1));
        for(int i=0;i<=n;i++){</pre>
             if(i!=0)
             dp[i][0]=0;
        for(int i=1;i<=n;i++){</pre>
             for(int j=1;j<=sum;j++){</pre>
                 if(coins[i-1]<=j){</pre>
                     dp[i][j]=min(1+dp[i][j-coins[i-1]], dp[i-1][j]);
                 else{
                     dp[i][j]=dp[i-1][j];
        if(dp[n][sum]==INT_MAX-1)
        return -1;
        return dp[n][sum];
```

LONGEST COMMON SUBSEQUENCE

1.) LONGEST COMMON SUBSEQUENCE

RECURSIVE

```
class Solution {
public:
    int LCS(string a, string b, int n, int m){
        if(n==0 || m==0)
        return 0;
        if(a[n-1]==b[m-1])
        return 1+LCS(a, b, n-1, m-1);
        else
        return max(LCS(a, b, n, m-1), LCS(a, b, n-1, m));
    }
    int longestCommonSubsequence(string text1, string text2) {
        int n=text1.size();
        int m=text2.size();
        return LCS(text1, text2, n, m);
    }
};
```

MEMOIZATION (TLE)

```
class Solution {
public:
    int LCS(string a, string b, int n, int m, vector<vector<int>> &dp){
        if(n==0 || m==0)
        return 0;

        if(dp[n][m]!=-1)
        return dp[n][m];

        if(a[n-1]==b[m-1])
        return dp[n][m]=1+LCS(a, b, n-1, m-1, dp);
        else
        return dp[n][m]=max(LCS(a, b, n, m-1, dp), LCS(a, b, n-1, m, dp));
    }

int longestCommonSubsequence(string text1, string text2) {
        int n=text1.size();
        int m=text2.size();
        vector<vector<int>> dp(n+1, vector<int> (m+1, -1));
        return LCS(text1, text2, n, m, dp);
    }
};
```

MEMOIZATION (GOOD)

TABULATION

```
class Solution {
public:
    int longestCommonSubsequence(string text1, string text2) {
        int n=text1.size();
        int m=text2.size();
        vector<vector<int>> dp(n+1, vector<int> (m+1, 0));
        for(int i=1;i<n+1;i++){
            for(int j=1;j<m+1;j++){
                if(text1[i-1]==text2[j-1])
                dp[i][j]=1+dp[i-1][j-1];
                else
                dp[i][j]=max(dp[i][j-1], dp[i-1][j]);
            }
        }
        return dp[n][m];
    }
};</pre>
```

2.) LONGEST COMMON SUBSTRING

```
int LCSubStr(string &text1, string &text2) {
    int n=text1.size();
    int m=text2.size();
    vector<vector<int>> dp(n+1, vector<int> (m+1, 0));

    int ans=0;
    for(int i=1;i<n+1;i++) {
        for(int j=1;j<m+1;j++) {
            if(text1[i-1]==text2[j-1]) {
                int val=1+dp[i-1][j-1];
               dp[i][j]=val;
                ans=max(ans, val);
        }
        else {
            dp[i][j]=0;
        }
    }
    return ans;
}</pre>
```

3.) SHORTEST COMMON SUPERSEQUENCE (ONLY LENGTH)

```
class Solution
{
   public:
    int shortestCommonSupersequence(string text1, string text2, int n, int m)
   {
      vector<vector<int>> dp(n+1, vector<int>> (m+1, 0));
      for(int i=1;i<n+1;i++){
            for(int j=1;j<m+1;j++){
                if(text1[i-1]==text2[j-1])
                dp[i][j]=1+dp[i-1][j-1];
                else
                dp[i][j]=max(dp[i][j-1], dp[i-1][j]);
            }
      }
      return m+n-dp[n][m];
   }
};</pre>
```

4.) MINIMUM NUMBER OF DELETIONS AND INSERTIONS TO MAKE STRING A TO B

```
int canYouMake(string &text1, string &text2){
    int n=text1.length();
    int m=text2.length();
    vector<vector<int>> dp(n+1, vector<int>> (m+1, 0));
    for(int i=1;i<n+1;i++){
        for(int j=1;j<m+1;j++){
            if(text1[i-1]==text2[j-1])
            dp[i][j]=1+dp[i-1][j-1];
            else
            dp[i][j]=max(dp[i][j-1], dp[i-1][j]);
        }
    }
    return m+n-(2*dp[n][m]);
}</pre>
```

5.) DELETE OPERATIONS FOR TWO STRINGS

SAME AS ABOVE

6.) LONGEST PALINDROMIC SUBSEQUENCE

```
class Solution {
public:
    int longestPalindromeSubseq(string text1) {
        string text2=text1;
        reverse(text2.begin(), text2.end());
        int n=text1.length();
        int m=text2.length();
        vector<vector<int>> dp(n+1, vector<int> (m+1, 0));
        for(int i=1;i<n+1;i++){</pre>
            for(int j=1;j<m+1;j++){</pre>
                if(text1[i-1]==text2[j-1])
                dp[i][j]=1+dp[i-1][j-1];
                else
                dp[i][j]=max(dp[i][j-1], dp[i-1][j]);
        }
        return dp[n][m];
```

7.) MINIMUM INSERTION STEPS TO MAKE STRING PALINDROME

```
class Solution {
public:
    int minInsertions(string text1) {
        string text2=text1;
        reverse(text2.begin(), text2.end());
        int n=text1.length();
        int m=text2.length();
        vector<vector<int>> dp(n+1, vector<int> (m+1, 0));
        for(int i=1;i<n+1;i++){</pre>
            for(int j=1;j<m+1;j++){</pre>
                if(text1[i-1]==text2[j-1])
                dp[i][j]=1+dp[i-1][j-1];
                else
                dp[i][j]=max(dp[i][j-1], dp[i-1][j]);
        }
        return n-dp[n][m];
```

8.) LONGEST REPEATING SUBSEQUENCE

9.) IS SUBSEQUENCE

10.) NUMBER OF MATCHING SUBSEQUENCES

```
class Solution {
public:
    int LCS(string &word, string &s){
        int index=-1;
        for(int i=0;i<word.size();i++){</pre>
            index=s.find(word[i], index+1);
            if(index==-1){
                return false;
        return true;
    int numMatchingSubseq(string s, vector<string>& words) {
        int count=0;
        for(int i=0;i<words.size();i++){</pre>
            string s2=words[i];
            if(LCS(s2, s))
            count++;
        return count;
```

MATRIX CHAIN MULTIPLICATION

01.) BASIC MCM

RECURSIVE

MEMOIZATION

02.) PALINDROME PARTITIONING II

```
class Solution {
public:
    bool isPalindrome(string &s, int i, int j){
        while(i<=j){</pre>
            if(s[i]==s[j]){
                i++;
                j--;
            else
            return false;
        return true;
    int mcm(string &s, int i, int j, vector<int> &dp){
        if(i>=j)
        return 0;
        if(isPalindrome(s, i, j))
        return 0;
        if(dp[i]!=-1)
        return dp[i];
        int mini=INT_MAX;
        for(int k=i;k<=j-1;k++){</pre>
            if(isPalindrome(s, i, k)){
                int temp=mcm(s, k+1, j, dp)+1;
                mini=min(mini, temp);
        return dp[i]=mini;
    int minCut(string s) {
        int n=s.length();
        vector<int> dp(n+1, -1);
        return mcm(s, 0, n-1, dp);
```

03.) BOOLEAN PARENTHESIZATION

EVALUATE EXPRESSIONS TO TRUE

```
const int mod = 1000000007;
int f(int i, int j, int isTrue, string& s, vector<vector<vector<long lo
ng>>>& dp) {
    if(i>j) return 0;
    if(i==j) {
       if(isTrue) return s[i]=='T';
        else return s[i] == 'F';
    if (dp[i][j][isTrue] != -1)
    return dp[i][j][isTrue];
    long long ways = 0;
    for(int k=i; k<j; k++) {</pre>
        long long leftTrue = f(i, k-1, 1, s, dp);
        long long leftFalse = f(i, k-1, 0, s, dp);
        long long rightTrue = f(k+1, j, 1, s, dp);
        long long rightFalse = f(k+1, j, 0, s, dp);
        if(s[k] == '&') {
            if(isTrue)
            ways = (ways + (leftTrue*rightTrue)%mod)%mod;
            ways = (ways + (leftFalse*rightTrue)%mod + (leftFalse*right
False) % mod + (leftTrue * rightFalse) % mod) % mod;
        else if(s[k] == '|') {
            if(isTrue)
            ways = (ways + (leftTrue*rightTrue)%mod + (leftTrue*rightFa
lse)%mod + (leftFalse*rightTrue)%mod)%mod;
            ways = (ways + (leftFalse*rightFalse)%mod)%mod;
            if(isTrue)
            ways = (ways + (leftTrue*rightFalse)%mod + (leftFalse*right
True) %mod) %mod;
            ways = (ways + (leftTrue*rightTrue)%mod + (leftFalse*rightF
alse)%mod)%mod;
    return dp[i][j][isTrue] = ways;
```

```
int evaluateExp(string & exp) {
    int n = exp.size();
    vector<vector<long long>>> dp(n, vector<vector<long long>>(n
, vector<long long>(2, -1)));
    return f(0,n-1, 1, exp, dp);
}
```

THANK YOU!