1

02-24-2021-shift-2-1-15

AI24BTECH11011 - Himani Gourishetty

- 1) Let $a, b \in \mathbb{R}$. If the mirror image of the point P(a, 6, 9) with respect to the line $\frac{(x-3)}{7} = \frac{(y-2)}{5} = \frac{(z-1)}{-9}$ is (20, b, -a, -9), then |a + b| is equal to:
 - a) 86
 - b) 88
 - c) 84
 - d) 90
- 2) Let f be a twice differentiable function defined on \mathbb{R} such that f(0) = 1, f'(0) = 2 and $f'(x) \neq 0$ for all $x \in \mathbb{R}$. If |f(x) f'(x) f'(x) f''(x)| = 0, for all $x \in \mathbb{R}$, then the value of f(1) lies in the interval:
 - a) (9, 12)
 - b) (6,9)
 - c) (3,6)
 - d) (0,3)
- 3) A possible value of $\tan\left(\frac{1}{4}\sin^{-1}\frac{\sqrt{63}}{8}\right)$ is :
 - a) $\frac{1}{2\sqrt{2}}$ b) $\frac{1}{\sqrt{7}}$

 - c) $\sqrt[7]{7} 1$
 - d) $2\sqrt{2} 1$
- 4) The probability that two randomly selected subsets of the set $\{1, 2, 3, 4, 5\}$ have exactly two elements in their intersection, is:
 - a) $\frac{65}{27}$ b) $\frac{135}{29}$ c) $\frac{65}{28}$ d) $\frac{35}{27}$
- 5) The vector equation of the plane passing through the intersection of the planes $\mathbf{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 1$ and $\mathbf{r}(\hat{i}-2\hat{j}) = -2$ and the points(1,0,2) is:
 - a) $\mathbf{r} \cdot (\hat{i} 7\hat{j} + 3\hat{k}) = \frac{7}{3}$ b) $\mathbf{r} \cdot (\hat{i} + 7\hat{j} + 3\hat{k}) = 7$

 - c) $\mathbf{r} \cdot (3\hat{i} + 7\hat{j} + 3\hat{k}) = 7$
 - d) $\mathbf{r} \cdot (\hat{i} + 7\hat{j} + 3\hat{k}) = \frac{7}{3}$
- 6) If P is a point on the parabola $y = x^2 + 4$ which is closest to the straight line y = 4x 1, then the co-ordinates of P are:
 - a) (-2, 8)
 - b) (1,5)
 - c) (3, 13)
 - d) (2,8)
- 7) Let a, b, c be in arithmetic progression. Let the centroid of the triangle with vertices (a, c), (2, b) and (a,b) be $\left(\frac{10}{3},\frac{7}{3}\right)$. If α,β are the roots of the equation $ax^2 + bx + 1 = 0$, then the value of $\alpha^2 + \beta^2 - \alpha\beta$ is:

- 8) The value of the integral, $\int_1^3 \lfloor x^2 2x 2 \rfloor dx$ where $\lfloor x \rfloor$ denotes the greatest integer less than or equal
 - a) -4
 - b) -5
 - c) $-\sqrt{2} \sqrt{3} 1$
 - d) $-\sqrt{2}-\sqrt{3}+1$
- 9) Let $f: \mathbb{R} \to \mathbb{R}$ be defined as

$$f(x) = \begin{cases} -55x, & \text{if } x < -5\\ 2x^3 - 3x^2 - 120x, & \text{if } -5 \le x \le 4\\ 2x^3 - 3x^2 - 36x - 336, & \text{if } x > 4 \end{cases}$$

Let $A = \{x \in \mathbb{R} : f \text{ is increasing}\}$. Then A is equal to :

- a) $(-5,4) \cup (4,\infty)$
- b) $(-5, \infty)$
- c) $(-\infty, -5) \cup (4, \infty)$
- d) $(-\infty, -5) \cup (-4, \infty)$
- 10) If the curve $y = ax^2 + bx + c$, $x \in \mathbb{R}$ passes through the point (1,2) and the tangent line to this curve at origin is y = x, then the possible values of a, b, c are:
 - a) a = 1, b = 1, c = 0
 - b) a = -1, b = 1, c = 1
 - c) a = 1, b = 0, c = 1
 - d) $a = \frac{1}{2}, b = \frac{1}{2}, c = 1$
- 11) The negation of the statement $\neg p \land (p \lor q)$ is:
 - a) $\neg p \land q$
 - b) $p \wedge \neg q$
 - c) $\neg p \lor q$
 - d) $p \vee \neg q$
- 12) For the system of linear equations: x 2y = 1, x y + kz = -2, ky + 4z = 6, $k \in \mathbb{R}$ Consider the following statements:
 - (A) The system has a unique solution if $k \neq 2, k \neq -2$.
 - (B) The system has a unique solution if k = -2.
 - (C) The system has a unique solution if k = 2.
 - (D) The system has no solution if k = 2.
 - (E) The system has an infinite number of solutions if $k \neq -2$.
 - a) (B) and (E) only
 - b) (C) and (D) only
 - c) (A) and (D) only
 - d) (A) and (E) only
- 13) For which of the following curves, the line $x + \sqrt{3}y = 2\sqrt{3}$ is the tangent at the point $\left(\frac{3\sqrt{3}}{2}, \frac{1}{2}\right)$?
 - a) $x^2 + 9y^2 = 9$
 - b) $2x^2 18y^2 = 9$ c) $y^2 = \frac{x}{6\sqrt{3}}$ d) $x^2 + y^2 = 7$

- 14) The angle of elevation of a jet plane from a point A on the ground is 60° . After a flight of 20 seconds at the speed of $432 \frac{km}{hour}$, the angle of elevation changes to 30° . If the jet plane is flying at a constant height, then its height is:
 - a) $1200 \sqrt{3}m$
 - b) $1800 \sqrt{3}m$
 - c) $3600 \sqrt{3}m$
 - d) $2400 \sqrt{3}m$
- 15) For the statements p and q, consider the following compound statements:
 - (a) $(\neg q \land (p \rightarrow q)) \rightarrow \neg p$
 - (b) $((p \lor q) \land \neg p) \rightarrow q$
 - a) (a) is a tautology but not (b)
 - b) (a) and (b) both are not tautologies
 - c) (a) and (b) both are tautologies
 - d) (a) is a tautology but not (b)