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- 1) Let A and B be two events such that the probability that exactly one of them occurs is $\frac{2}{5}$ and the probability that A or B occurs is $\frac{1}{2}$, then the probability of both of them occur together is
 - a) 0.10
 - b) 0.20
 - c) 0.01
 - d) 0.02
- 2) Let S be the set of all real roots of the equation, $3^x(3^x - 1) + 2 = |3^x - 1| + |3^x - 2|$. Then S :
 - a) is a singleton.
 - b) is an empty set.
 - c) contains at least four elements.
 - d) contains exactly two elements.
- 3) The mean and variance of 20 observations are found to be 10 and 4, respectively. On rechecking, it was found that an observation 9 was incorrect and the correct observation was 11. Then the correct variance is:
 - a) 4.01
 - b) 3.99
 - c) 3.98
 - d) 4.02
- 4) Let $\mathbf{a} = \hat{i} - 2\hat{j} + \hat{k}$, $\mathbf{b} = \hat{i} - \hat{j} + \hat{k}$ be two vectors. If \mathbf{c} is a vector such that $\mathbf{b} \times \mathbf{c} = \mathbf{b} \times \mathbf{a}$ and $\mathbf{a} \cdot \mathbf{b} = 0$ then $\mathbf{c} \cdot \mathbf{b}$ is equal to:
 - a) $\frac{1}{2}$
 - b) $\frac{-3}{2}$
 - c) $\frac{-1}{2}$
 - d) -1
- 5) Let $f : (1, 3) \rightarrow \mathbb{R}$ be a function defined by $f(x) = \frac{x[x]}{x^2+1}$, where $[x]$ denotes the greatest integer $\leq x$. Then the range of f is:
 - a) $(\frac{2}{5}, \frac{3}{5}] \cup (\frac{3}{4}, \frac{4}{5})$
 - b) $(\frac{2}{5}, \frac{4}{5}]$
 - c) $(\frac{3}{5}, \frac{4}{5})$
 - d) $(\frac{2}{5}, \frac{1}{2}) \cup (\frac{3}{5}, \frac{4}{5}]$
- 6) If α and β be the coefficients of x^4 and x^2 respectively in the expansion of $(x + \sqrt{x^2 - 1})^6 + (x - \sqrt{x^2 - 1})^6$, then:
 - a) $\alpha + \beta = -30$
 - b) $\alpha - \beta = -132$
 - c) $\alpha + \beta = 60$
 - d) $\alpha - \beta = 60$
- 7) If a hyperbola passes through the point (10, 16) and it has vertices at $(\pm 6, 0)$, then the equation of the normal at \mathbf{P} is:
 - a) $3x + 4y = 94$
 - b) $x + 2y = 42$

- c) $2x + 5y = 100$
d) $x + 3y = 58$
- 8) $\lim_{x \rightarrow 0} \frac{\int_0^x t \sin(10t) dt}{x}$ is equal to:
a) 0
b) $\frac{1}{10}$
c) $\frac{-1}{10}$
d) $\frac{-1}{5}$
- 9) If a line, $y = mx + c$ is a tangent to the circle, $(x - 3)^2 + y^2 = 1$ and it is perpendicular to a line L_1 , where L_1 is the tangent to the circle, $x^2 + y^2 = 1$ at the point $(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}})$; then:
a) $c^2 + 7c + 6 = 0$
b) $c^2 - 6c + 7 = 0$
c) $c^2 - 7c + 6 = 0$
d) $c^2 + 6c + 7 = 0$
- 10) Let $\alpha = \frac{(-1+i\sqrt{3})}{2}$. If $\alpha = (1 + \alpha) \sum_{k=0}^{100} a^{2k}$ and $b = \sum_{k=0}^{100} a^{3k}$, then a and b are the roots of the quadratic equation:
a) $x^2 + 101x + 100 = 0$
b) $x^2 + 102x + 101 = 0$
c) $x^2 - 102x + 101 = 0$
d) $x^2 - 101x + 100 = 0$
- 11) The mirror image of the point $(1, 2, 3)$ in a plane is $(\frac{-7}{3}, \frac{-4}{3}, \frac{-1}{3})$. Which of the following points lies on this plane?
a) $(1, -1, 1)$
b) $(-1, -1, 1)$
c) $(1, 1, 1)$
d) $(-1, -1, -1)$
- 12) The length of the perpendicular from the origin, on the normal to the curve, $x^2 + 2xy - 3y^2 = 0$ at the point $(2, 2)$ is
a) 2
b) $2\sqrt{2}$
c) $4\sqrt{2}$
d) $\sqrt{2}$
- 13) Which of the following statements is a tautology?
a) $\neg(p \wedge \neg q) \rightarrow (p \vee q)$
b) $(\neg p \vee \neg q) \rightarrow (p \wedge q)$
c) $p \wedge (\neg q) \rightarrow (p \wedge q)$
d) $\neg(p \vee \neg q) \rightarrow (p \vee q)$
- 14) If $I = \int_1^2 \frac{dx}{\sqrt{2x^3 - 9x^2 + 12x + 4}}$, then:
a) $\frac{1}{6} < I^2 < \frac{1}{2}$
b) $\frac{1}{8} < I^2 < \frac{1}{4}$
c) $\frac{1}{9} < I^2 < \frac{1}{8}$
d) $\frac{1}{16} < I^2 < \frac{1}{9}$
- 15) If $A = \begin{pmatrix} 2 & 2 \\ 9 & 4 \end{pmatrix}$ and $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$, then $10A^{-1}$ is equal to:
a) $6I - A$
b) $A - 6I$
c) $4I - A$

d) A-4I