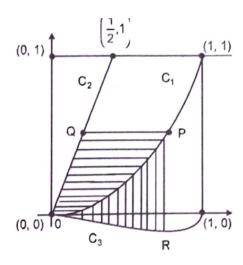
## 18/A/E/36-49

## AI24BTECH11011 - HIMANI GOURISHETTY

Let  $C_1$  and  $C_2$  be the graphs of the functions  $y = x^2$  and  $y = 2x, 0 \le x \le 1$  respectively.Let  $C_3$  be graph of a function  $y=f(x), 0 \le x \le 1$ , f(0)=0. For a point P on  $C_1$ , let the lines through P,parallel to the axes, meet  $C_2$  and  $C_3$  at Q and R respectively(see figure). If for every position of P(on  $C_1$ ), the areas of the shaded regions OPQ and ORP are equal, determine the function of f(x). (1998-8 Marks) Integrate



(1999-2 Marks) Let f(x) be a continuos function given by

$$f(x) = \begin{cases} 2x, & |x| \le 1\\ x^2 + ax + b, & |x| > 1 \end{cases}$$

Find the area of the region in the third quadrant bounded by the curves  $x=-2y^2$  and y=f(x) lying on the left of the line 8x + 1 = 0. (1999-10marks)

For x > 0,  $let f(x) = \int_e^x \frac{lnt}{1+t}$  Find the function  $f(x) + f(\frac{1}{x})$  and show that  $f(e) + f(\frac{1}{e}) = \frac{1}{2}$ . Here log t. (2000-5Marks) Let  $b \neq 0$  and for j=0,1,2,...,n,  $S_i$  be the area of the region bounded by the y-axis and the curve  $xe^{ay} = \sin by \frac{jr}{b} \le y \le \frac{(j+1)\pi}{b}$ . Show that  $S_0, S_1, S_2, \dots, S_n$  are in geometric progression . Also, find their sum for a=-1 and b=pi.

(2001-5Marks) Find the area of the region bounded by the curves  $y = x^2$ , y = |2 - x| and y = 2, which lies to the right of the line x = 1. Marks) If f is an even function then prove that  $\int_0^{\frac{\pi}{2}} f(\cos 2x) \cos x = \sqrt{2} \int_0^{\frac{\pi}{4}} f(\sin 2x) \cos x$   $(2003-2\text{Marks}) \text{ If } y(x) = \int_{\frac{\pi^2}{16}}^{x^2} \frac{\cos x \cos \sqrt{\theta}}{1+\sin^2 \sqrt{\theta}}, \text{ then }$ (2004-2Marks) Find the value of

. (2004-4Marks) Evaluate  $\int_0^{\pi} e^{\cos x} (2\sin(\frac{1}{2}\cos x) + 3\cos(\frac{1}{2}\cos x)) \sin x$ . (2005-2Marks) Find the area bounded by the

 $x^2 = y$ ,  $x^2 = -y$  and  $y^2 = 4x - 3$ (2005 -4Marks) f(x) is a differentiable function and g(x) is double differentiable function such that  $|f(x)| \le 1$  and f'(x) = g(x). if  $f^2(0) + g^2(0) = 9$ . Prove that there exist some  $c \in (-3,3)$  such that g(c).g''(c) < 0.

 $\begin{bmatrix} 4a^2 & 4a & 1 \\ 4b^2 & 4b & 1 \\ 4c^2 & 4c & 1 \end{bmatrix} \begin{bmatrix} f(-1) \\ f(1) \\ f(2) \end{bmatrix} = \begin{bmatrix} 3a^2 + 3a \\ 3b^2 + 3b \\ 3c^2 + 3c \end{bmatrix}$ 

(2005-6Marks)

f(x) is a quadratic function and its maximum value occurs at a point V.A is a point of intersection of y=f(x) with x axis and point B is such that chord AB subtends a right angle at V . Find the area enclosed by f(x) and chord AB. (2005-6Marks) The value of 5050  $\int_0^1 (1-x^50)^1 00$ 2006-6M  $\int 0^{1}(1-x^{5}0)^{1}01$