

Introduction to Scientific Computing with Python

What Is Python?

Python is an interpreted programming language that allows you to do almost anything possible with a compiled language (C/C++/Fortran) without requiring all the complexity.

PYTHON HIGHLIGHTS

- **Interpreted and interactive**
- **Object-oriented**
- **“Batteries Included”**
- **Free**
- **Portable**
- **Easy to Learn and Use**
- **Truly Modular**

Interactive Calculator

```
# adding two values
```

```
>>> 1 + 1
```

```
2
```

```
# setting a variable
```

```
>>> a = 1
```

```
>>> a
```

```
1
```

```
# checking a variables type
```

```
>>> type(a)
```

```
<type 'int'>
```

```
# an arbitrarily long integer
```

```
>>> a = 1203405503201
```

```
>>> a
```

```
1203405503201L
```

```
>>> type(a)
```

```
<type 'long'>
```

```
# real numbers
```

```
>>> b = 1.2 + 3.1
```

```
>>> b
```

```
4.2999999999999998
```

```
>>> type(b)
```

```
<type 'float'>
```

```
# complex numbers
```

```
>>> c = 2+1.5j
```

```
>>> c
```

```
(2+1.5j)
```

Complex Numbers

CREATING COMPLEX NUMBERS

```
# Use "j" or "J" for imaginary
# part. Create by "(real+imagj)",
# or "complex(real, imag)" .
>>> 1j * 1J
(-1+0j)
>>> 1j * complex(0,1)
(-1+0j)
>>> (1+2j) / (1+1j)
(1.5+0.5j)
```

EXTRACTING COMPONENTS

```
# to extract real and im
# component
>>> a=1.5+0.5j
>>> a.real
1.5
>>> a.imag
0.5
```

Strings

CREATING STRINGS

```
# using double quotes
>>> s = "hello world"
>>> print s
hello world
# single quotes also work
>>> s = 'hello world'
>>> print s
hello world
```

STRING OPERATIONS

```
# concatenating two strings
>>> "hello " + "world"
'hello world'

# repeating a string
>>> "hello " * 3
'hello hello hello '
```

STRING LENGTH

```
>>> s = "12345"
>>> len(s)
5
```

FORMAT STRINGS

```
# the % operator allows you
# to supply values to a
# format string. The format
# string follows
# C conventions.
>>> s = "some numbers:"
>>> x = 1.34
>>> y = 2
>>> s = "%s %f, %d" % (s,x,y)
>>> print s
some numbers: 1.34, 2
```

Multi-line Strings

```
# triple quotes are used
# for mutli-line strings
>>> a = """hello
... world"""
>>> print a
hello
world
```

```
# multi-line strings using
# "\" to indicate
continuation
>>> a = "hello " \
...     "world"
>>> print a
hello world
```

```
# including the new line
>>> a = "hello\n" \
...     "world"
>>> print a
hello
world
```

List objects

LIST CREATION WITH BRACKETS

```
>>> l = [10,11,12,13,14]
>>> print l
[10, 11, 12, 13, 14]
```

CONCATENATING LIST

```
# simply use the + operator
>>> [10, 11] + [12,13]
[10, 11, 12, 13]
```

REPEATING ELEMENTS IN LISTS

```
# the multiply operator
# does the trick.
>>> [10, 11] * 3
[10, 11, 10, 11, 10, 11]
```

range(start, stop, step)

```
# the range method is helpful
# for creating a sequence
```

```
>>> range(5)
[0, 1, 2, 3, 4]
```

```
>>> range(2,7)
[2, 3, 4, 5, 6]
```

```
>>> range(2,7,2)
[2, 4, 6]
```

Indexing

RETRIEVING AN ELEMENT

```
# list
# indices: 0  1  2  3  4
>>> l = [10,11,12,13,14]
>>> l[0]
10
```

SETTING AN ELEMENT

```
>>> l[1] = 21
>>> print l
[10, 21, 12, 13, 14]
```

OUT OF BOUNDS

```
>>> l[10]
Traceback (innermost last):
File "<interactive input>",line 1,in ?
IndexError: list index out of range
```

NEGATIVE INDICES

```
# negative indices count
# backward from the end of
# the list.
#
# indices: -5 -4 -3 -2 -1
>>> l = [10,11,12,13,14]

>>> l[-1]
14
>>> l[-2]
13
```


More on list objects

LIST CONTAINING MULTIPLE TYPES

```
# list containing integer,  
# string, and another list.  
>>> l = [10, 'eleven', [12, 13]]  
>>> l[1]  
'eleven'  
>>> l[2]  
[12, 13]
```

```
# use multiple indices to  
# retrieve elements from  
# nested lists.  
>>> l[2][0]  
12
```

LENGTH OF A LIST

```
>>> len(l)  
3
```

DELETING OBJECT FROM LIST

```
# use the del keyword  
>>> del l[2]  
>>> l  
[10, 'eleven']
```

DOES THE LIST CONTAIN x ?

```
# use in or not in  
>>> l = [10, 11, 12, 13, 14]  
>>> 13 in l  
1  
>>> 13 not in l  
0
```

Slicing

`var[lower:upper]`

SLICING LISTS

```
# indices: 0  1  2  3  4
>>> l = [10,11,12,13,14]
# [10,11,12,13,14]
>>> l[1:3]
[11, 12]

# negative indices work also
>>> l[1:-2]
[11, 12]
>>> l[-4:3]
[11, 12]
```

OMITTING INDICES

```
# omitted boundaries are
# assumed to be the beginning
# (or end) of the list.

# grab first three elements
>>> l[:3]
[10,11,12]
# grab last two elements
>>> l[-2:]
[13,14]
```

List methods in action

```
>>> l = [10,21,23,11,24]
```

```
# add an element to the list
```

```
>>> l.append(11)
```

```
>>> print l
```

```
[10,21,23,11,24,11]
```

```
# how many 11s are there?
```

```
>>> l.count(11)
```

```
2
```

```
# where does 11 first occur?
```

```
>>> l.index(11)
```

```
3
```

```
# remove the first 11
```

```
>>> l.remove(11)
```

```
>>> print l
```

```
[10,21,23,24,11]
```

```
# sort the list
```

```
>>> l.sort()
```

```
>>> print l
```

```
[10,11,21,23,24]
```

```
# reverse the list
```

```
>>> l.reverse()
```

```
>>> print l
```

```
[24,23,21,11,10]
```

Dictionaries

Dictionaries store *key/value* pairs. Indexing a dictionary by a *key* returns the *value* associated with it.

DICTIONARY EXAMPLE

```
# create an empty dictionary using curly brackets
>>> record = {}
>>> record['first'] = 'Jmes'
>>> record['last'] = 'Maxwell'
>>> record['born'] = 1831
>>> print record
{'first': 'Jmes', 'born': 1831, 'last': 'Maxwell'}
```

Dictionary methods in action

```
>>> d = {'cows': 1, 'dogs': 5,  
...      'cats': 3}
```

```
# get a list of all keys  
>>> d.keys()  
['cats', 'dogs', 'cows']
```

```
# get a list of all values  
>>> d.values()  
[3, 5, 1]
```

```
# clear the dictionary  
>>> d.clear()  
>>> print d  
{}
```

If statements

`if/elif/else` provide conditional execution of code blocks.

IF STATEMENT FORMAT

```
if <condition>:  
    <statements>  
elif <condition>:  
    <statements>  
else:  
    <statements>
```

IF EXAMPLE

```
# a simple if statement  
>>> x = 10  
>>> if x > 0:  
...     print 1  
... elif x == 0:  
...     print 0  
... else:  
...     print -1  
... < hit return >  
1
```

Test Values

- True means any non-zero number or non-empty object
- False means not true: zero, empty object, or **None**

EMPTY OBJECTS

```
# empty objects evaluate false
>>> x = []
>>> if x:
...     print 1
... else:
...     print 0
... < hit return >
0
```

For loops

For loops iterate over a sequence of objects.

```
for <loop_var> in <sequence>:  
    <statements>
```

TYPICAL SCENARIO

```
>>> for i in range(5):  
...     print i,  
... < hit return >  
0 1 2 3 4
```

LOOPING OVER A STRING

```
>>> for i in 'abcde':  
...     print i,  
... < hit return >  
a b c d e
```

LOOPING OVER A LIST

```
>>> l=['dogs','cats','bears']  
>>> accum = ''  
>>> for item in l:  
...     accum = accum + item  
...     accum = accum + ' '  
... < hit return >  
>>> print accum  
dogs cats bears
```


While loops

While loops iterate until a condition is met.

```
while <condition>:  
    <statements>
```

WHILE LOOP

```
# the condition tested is  
# whether lst is empty.  
>>> lst = range(3)  
>>> while lst:  
...     print lst  
...     lst = lst[1:]  
... < hit return >  
[0, 1, 2]  
[1, 2]  
[2]
```

BREAKING OUT OF A LOOP

```
# breaking from an infinite  
# loop.  
>>> i = 0  
>>> while 1:  
...     if i < 3:  
...         print i,  
...     else:  
...         break  
...     i = i + 1  
... < hit return >  
0 1 2
```

Anatomy of a function

The keyword **def** indicates the start of a function.

Function arguments are listed separated by commas. They are passed by *assignment*. More on this later.

Indentation is used to indicate the contents of the function. It is *not* optional, but a part of the syntax.

```
def add(arg0, arg1):  
    a = arg0 + arg1  
    return a
```

A colon (**:**) terminates the function definition.

An optional return statement specifies the value returned from the function. If return is omitted, the function returns the special value **None**.

Our new function in action

```
# We'll create our function
# on the fly in the
# interpreter.
>>> def add(x,y):
...     a = x + y
...     return a
```

```
# test it out with numbers
>>> x = 2
>>> y = 3
>>> add(x,y)
5
```

```
# how about strings?
>>> x = 'foo'
>>> y = 'bar'
>>> add(x,y)
'foobar'
```

```
# functions can be assigned
# to variables
>>> func = add
>>> func(x,y)
'foobar'
```

```
# how about numbers and strings?
```

```
>>> add('abc',1)
```

```
Traceback (innermost last):
```

```
File "<interactive input>", line 1, in ?
```

```
File "<interactive input>", line 2, in add
```

```
TypeError: cannot add type "int" to string
```

Modules

EX1.PY

```
# ex1.py

PI = 3.1416

def sum(lst):
    tot = lst[0]
    for value in lst[1:]:
        tot = tot + value
    return tot

l = [0,1,2,3]
print sum(l), PI
```

FROM SHELL

```
[ej@bull ej]$ python ex1.py
6, 3.1416
```

NumPy

NumPy

IMPORT NUMPY

```
>>> from numpy import *  
>>> import numpy
```

Array Operations

SIMPLE ARRAY MATH

```
>>> a = array([1,2,3,4])
>>> b = array([2,3,4,5])
>>> a + b
array([3, 5, 7, 9])
```

```
# multiply entire array by
# scalar value
>>> a = (2*pi)/10.
>>> a
0.628318530718
```

MATH FUNCTIONS

```
>>> a*x
array([ 0., 0.628, ..., 6.283])

# apply functions to array.
>>> y = sin(a*x)
```

Introducing Numeric Arrays

SIMPLE ARRAY CREATION

```
>>> a = array([0,1,2,3])
>>> a
array([0, 1, 2, 3])
```

CHECKING THE TYPE

```
>>> type(a)
<type 'array'>
```

NUMERIC TYPE OF ELEMENTS

```
>>> a.typecode()
'1'      # '1' = Int
```

BYTES IN AN ARRAY ELEMENT

```
>>>
a.itemsize()
```

4

ARRAY SHAPE

```
>>> a.shape
(4,)
>>> shape(a)
(4,)
```

CONVERT TO PYTHON LIST

```
>>> a.tolist()
[0, 1, 2, 3]
```

ARRAY INDEXING

```
>>> a[0]
0
>>> a[0] = 10
>>> a
[10, 1, 2, 3]
```


Multi-Dimensional Arrays

MULTI-DIMENSIONAL ARRAYS

```
>>> a = array([[ 0, 1, 2, 3],
               [10,11,12,13]])


>>> a
array([[ 0, 1, 2, 3],
       [10,11,12,13]])
```

(ROWS,COLUMNS)

```
>>> shape(a)
(2, 4)
```

GET/SET ELEMENTS

```
>>> a[1,3]
13
```



```
>>> a[1,3] = -1
>>> a
array([[ 0, 1, 2, 3],
       [10,11,12,-1]])
```

ADDRESS FIRST ROW USING SINGLE INDEX

```
>>> a[1]
array([10, 11, 12, 13])
```

FLATTEN TO 1D ARRAY

```
>>> a.flat
array(0,1,2,3,10,11,12,-1)
```

Array Slicing

**SLICING WORKS MUCH LIKE
STANDARD PYTHON SLICING**

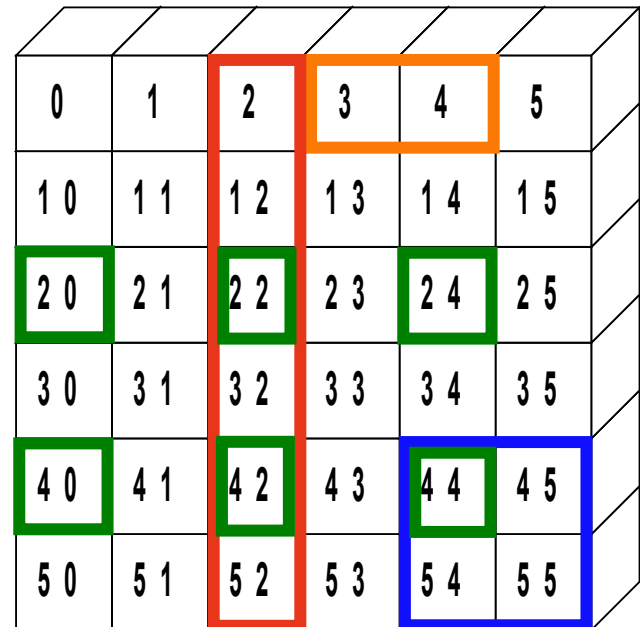
```
>>> a[0,3:5]  
array([3, 4])
```

```
>>> a[4:,4:]  
array([[44, 45],  
       [54, 55]])
```

```
>>> a[:,2]  
array([2, 12, 22, 32, 42, 52])
```

STRIDES ARE ALSO POSSIBLE

```
>>> a[2::2,::2]  
array([[20, 22, 24],  
       [40, 42, 44]])
```



A 3D visualization of a 6x6 array grid. The grid is shown from an isometric perspective. The top face of the cube shows the array indices 0 to 5 for both rows and columns. The grid is divided into four colored regions: a red vertical strip for column 2, an orange horizontal strip for row 3, a green vertical strip for column 4, and a blue vertical strip for column 5. The intersection of these strips is highlighted in the center of the grid.

0	1	2	3	4	5
1 0	1 1	1 2	1 3	1 4	1 5
2 0	2 1	2 2	2 3	2 4	2 5
3 0	3 1	3 2	3 3	3 4	3 5
4 0	4 1	4 2	4 3	4 4	4 5
5 0	5 1	5 2	5 3	5 4	5 5

Mathematic Binary Operators

$a + b \rightarrow \text{add}(a,b)$
 $a - b \rightarrow \text{subtract}(a,b)$
 $a \% b \rightarrow \text{remainder}(a,b)$

$a * b \rightarrow \text{multiply}(a,b)$
 $a / b \rightarrow \text{divide}(a,b)$
 $a ** b \rightarrow \text{power}(a,b)$

MULTIPLY BY A SCALAR

```
>>> a = array((1,2))  
>>> a*3.  
array([3., 6.] )
```

ELEMENT BY ELEMENT ADDITION

```
>>> a = array([1,2])  
>>> b = array([3,4])  
>>> a + b  
array([4, 6])
```

ADDITION USING AN OPERATOR FUNCTION

```
>>> add(a,b)  
array([4, 6])
```

Comparison and Logical Operators

<code>equal</code>	<code>(==)</code>	<code>not_equal</code>	<code>(!=)</code>	<code>greater</code>	<code>(>)</code>
<code>greater_equal</code>	<code>(>=)</code>	<code>less</code>	<code>(<)</code>	<code>less_equal</code>	<code>(<=)</code>
<code>logical_and</code>	<code>(and)</code>	<code>logical_or</code>	<code>(or)</code>	<code>logical_xor</code>	
<code>logical_not</code>	<code>(not)</code>				

2D EXAMPLE

```
>>> a = array(((1,2,3,4) , (2,3,4,5)))
>>> b = array(((1,2,5,4) , (1,3,4,5)))
>>> a == b
array([[1, 1, 0, 1],
       [0, 1, 1, 1]])
# functional equivalent
>>> equal(a,b)
array([[1, 1, 0, 1],
       [0, 1, 1, 1]])
```