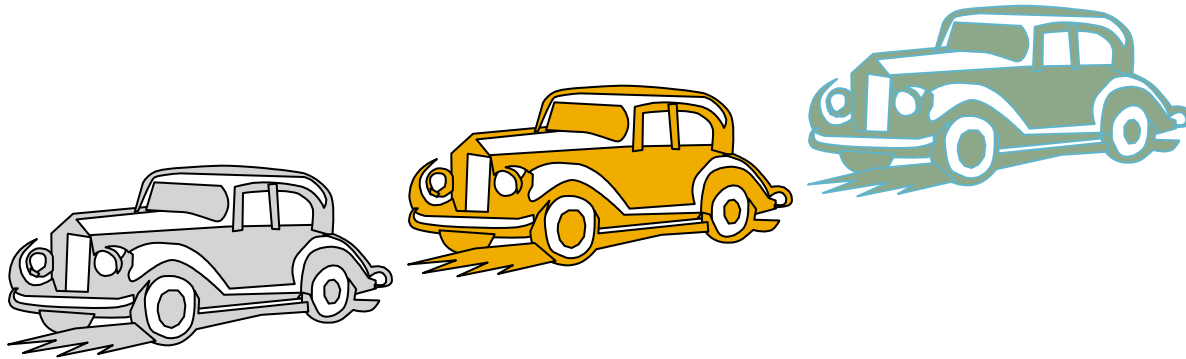


Queues

Algorithms & Data Structures
ITCS 6114/8114

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Queues



Outline and Reading

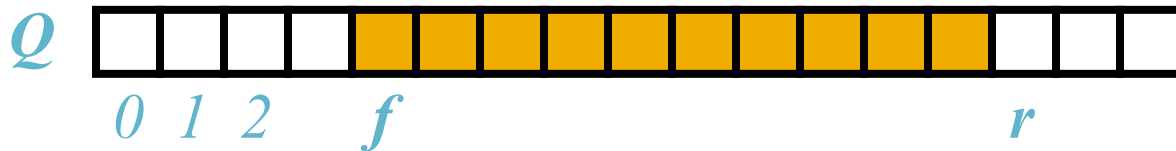
3

- The Queue ADT (§2.1.2)
- Implementation with a circular array (§2.1.2)
- Growable array-based queue
- Queue interface in Java

The Queue ADT

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- Stores arbitrary objects
- Insertions and deletions follow the first-in first-out (FIFO) scheme
- Insertions are at the rear of the queue and removals are at the front of the queue



- Main queue operations:
 - `enqueue(object)`: inserts an element at the end of the queue
 - `object dequeue()`: removes and returns the element at the front of the queue

The Queue ADT (cont.)

- Auxiliary queue operations:
 - ▣ `object front()`: returns the element at the front without removing it
 - ▣ `integer size()`: returns the number of elements stored
 - ▣ `boolean isEmpty()`: indicates whether no elements are stored
- Exceptions
 - ▣ Attempting the execution of `dequeue` or `front` on an empty queue throws an `EmptyQueueException`

Applications of Queues

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- Direct applications
 - ▣ Waiting lists, bureaucracy
 - ▣ Access to shared resources (e.g., printer)
 - ▣ Multiprogramming
- Indirect applications
 - ▣ Auxiliary data structure for algorithms
 - ▣ Component of other data structures

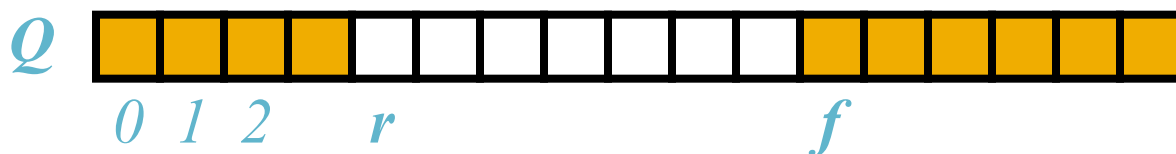
Array-based Queue

- Use an array of size N in a circular fashion
- Two variables keep track of the front and rear
 - f index of the front element
 - r index immediately past the rear element
- Array location r is kept empty

normal configuration



wrapped-around configuration



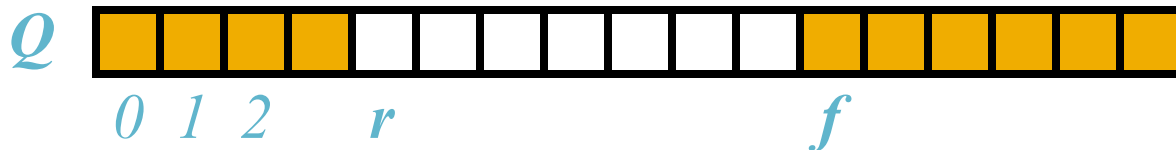
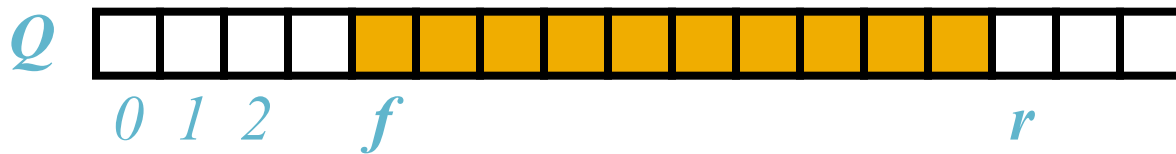
Queue Operations

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- We use the modulo operator (remainder of division)

```
Algorithm size()  
    return (N - f + r) mod N
```

```
Algorithm isEmpty()  
    return (f = r)
```

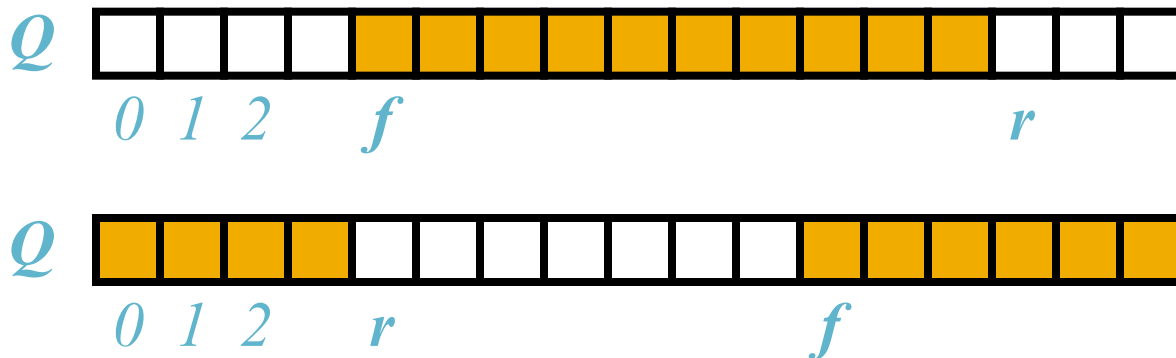


Queue Operations (cont.)

9

- Discussion on size $N - 1$!!
- Operation enqueue throws an exception if the array is full
- This exception is implementation-dependent

```
Algorithm enqueue(o)
  if size() = N - 1 then
    throw FullQueueException
  else
    Q[r] ← o
    r ← (r + 1) mod N
```

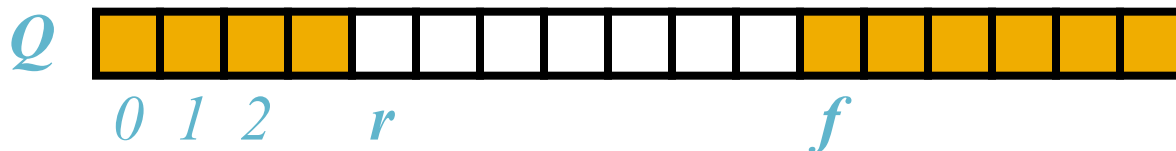
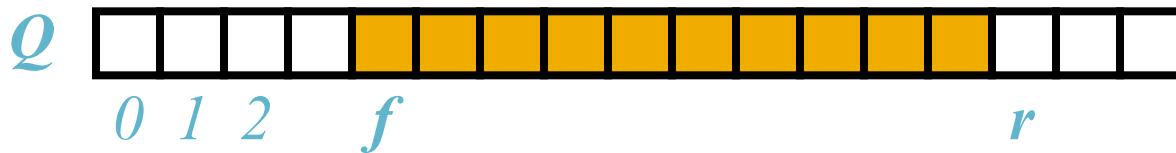


Queue Operations (cont.)

10

- Operation dequeue throws an exception if the queue is empty
- This exception is specified in the queue ADT

```
Algorithm dequeue()  
  if isEmpty() then  
    throw EmptyQueueException  
  else  
    o ← Q[f]  
    f ← (f + 1) mod N  
    return o
```



Growable Array-based Queue

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- In an enqueue operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one
- Similar to what we did for an array-based stack
- The enqueue operation has amortized running time
 - ▣ $O(n)$ with the incremental strategy
 - ▣ $O(1)$ with the doubling strategy

Reference

12

- **Algorithm Design: Foundations, Analysis, and Internet Examples.** Michael T. Goodrich and Roberto Tamassia. John Wiley & Sons.
- **Introduction to Algorithms.** Thomas H. Cormen, Charles E. Leiserson, Ronald L. Rivest, Clifford Stein.

Thank you!