



PES University, Bangalore

UE18MA251- Linear Algebra (Jamuna S Murthy)

Session: Jan 2020 – May 2020

**Scilab Assignment 4**

1. Write a Sci-Lab Program to implement the Gram- Schmidt Orthogonalization in  $\mathbb{R}^3$ .

**Procedure:** Given a set of mutually independent vectors  $a, b, c$  in  $\mathbb{R}^3$ , we produce a set of orthonormal vectors  $q_1, q_2, q_3$  by applying the Gram – Schmidt process.

2. Write a Sci-Lab Program to find the Eigen values and Eigen vectors of any square matrix of size  $3 \times 3$ .

**Procedure:** Given a square matrix  $A$ , we find the characteristic polynomial of  $A$  by expanding the matrix equation  $|A - \lambda I|$ . The Eigen values of  $A$  are obtained solving the characteristic equation  $|A - \lambda I| = 0$ . The corresponding Eigen vectors are obtained by solving the system of equations  $Ax = \lambda x$ .

3. Write a Sci-Lab Program to find the numerically Largest Eigen value of  $A$  using Rayleigh Power Method for any  $3 \times 3$  matrix.

**Procedure:** Given a square matrix  $A$  and an initial vector  $x_0$ , to find the numerically largest Eigen value of  $A$ , we compute the product  $Ax_0$  and rewrite it in the form  $\lambda_1 x_1$  where  $\lambda_1$  is the first approximation to the numerically largest Eigen value  $\lambda$  and  $x_1$  is the corresponding Eigen vector which is the first approximation to the actual Eigen vector. We then find  $Ax_1$  and rewrite it in the form  $\lambda_2 x_2$ . This process is continued until we get the two successive values of  $\lambda$  to be nearly the same.

Deadline: 5<sup>th</sup> April 2020