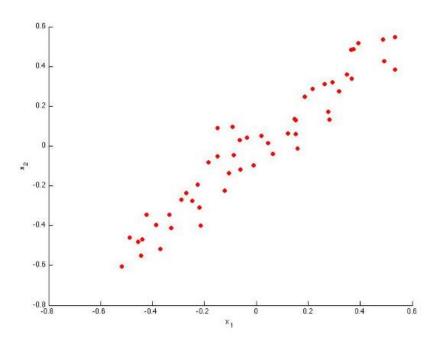
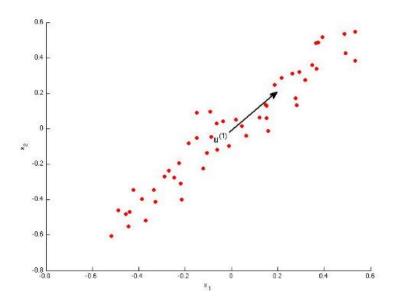
1. Consider the following 2D dataset:

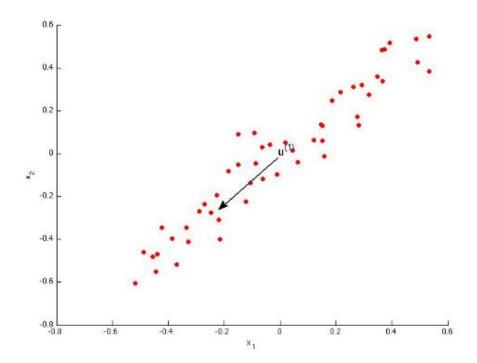
1 point

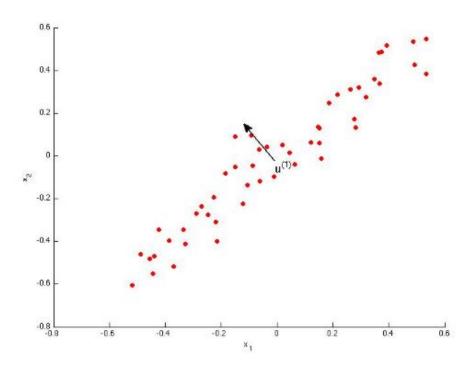


Which of the following figures correspond to possible values that PCA may return for $u^{(1)}$ (the first eigenvector / first principal component)? Check all that apply (you may have to check more than one figure).









1 point 2. Which of the following is a reasonable way to select the number of principal components k? (Recall that n is the dimensionality of the input data and m is the number of input examples.)

- Choose ${\it k}$ to be the largest value so that at least 99% of the variance is retained
- Use the elbow method.
- lacksquare Choose k to be the smallest value so that at least 99% of the variance is retained.
- Choose k to be 99% of m (i.e., k=0.99*m, rounded to the nearest integer).

1 point **3.** Suppose someone tells you that they ran PCA in such a way that "95% of the variance was retained." What is an equivalent statement to this?

$$\frac{\frac{1}{m}\sum_{i=1}^{m}||x^{(i)}||^2}{\frac{1}{m}\sum_{i=1}^{m}||x^{(i)}-x_{\text{approx}}^{(i)}||^2} \leq 0.05$$

$$\qquad \frac{\frac{1}{m}\sum_{i=1}^{m}||x^{(i)}||^2}{\frac{1}{m}\sum_{i=1}^{m}||x^{(i)}-x_{\mathrm{approx}}^{(i)}||^2} \geq 0.05$$

$$\qquad \qquad \frac{\frac{1}{m} \sum_{i=1}^{m} ||x^{(i)} - x_{\text{approx}}^{(i)}||^2}{\frac{1}{m} \sum_{i=1}^{m} ||x^{(i)}||^2} \leq 0.05$$

$$\frac{\frac{1}{m}\sum_{i=1}^{m}||x^{(i)}||^2}{\frac{1}{m}\sum_{i=1}^{m}||x^{(i)}-x_{\mathrm{approx}}^{(i)}||^2} \leq 0.95$$

1 point	4.	Which of the following statements are true? Check all that apply.
		Feature scaling is not useful for PCA, since the eigenvector calculation (such as using Octave's svd(Sigma) routine) takes care of this automatically.
		Given an input $x\in\mathbb{R}^n$, PCA compresses it to a lower-dimensional vector $z\in\mathbb{R}^k$.
		PCA can be used only to reduce the dimensionality of data by 1 (such as 3D to 2D, or 2D to 1D).
		If the input features are on very different scales, it is a good idea to perform feature scaling before applying PCA.
1 point	5.	Which of the following are recommended applications of PCA? Select all that apply.
		To get more features to feed into a learning algorithm.
		Preventing overfitting: Reduce the number of features (in a supervised learning problem), so that there are fewer parameters to learn.
		Data visualization: Reduce data to 2D (or 3D) so that it can be plotted.
		Data compression: Reduce the dimension of your data, so that it takes up less memory / disk space.