Natural Language Processing with Deep Learning



Representation of words

1) One hot vector

Problem:

- Orthogonal
- Highly Sparse
- No natural inheritance meaning

2) word2vec

Language model: Assign probability to a sequence of tokens.

- Unigram model $P(w_1, w_2, w_3, ... w_m) = P(w_1)P(w_2)...P(w_m)$ not good model, no reference of past or future of the language.
- Bigram model $P(w_1, w_2, w_3, ... w_m) = \prod_{i=2}^{m} P(w_i | w_{i-1})$
- n-gram model $P(w_1, w_2, w_3, ... w_m) = \prod_{i=1}^{m} P(w_i | w_{i-n+1} ... w_{i-1})$

Skip-gram

the cat is eating the mouse eating here

"eating" is the centre word, "cat is" and "the mouse" are the context words. Input takes one-hot vector $Z^{(1)} = w^{(1)} X$ //no activation function Go through each position 't' in the Corpus, which has centre word 'c' and context word 'o'.

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

$$L = -\frac{1}{T} \sum_{t=1}^{T} \sum_{j=-m, j \neq 0}^{m} \log \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

Also can be look as maximizing data likelihood.

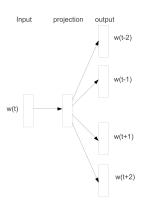
$$L = \prod_{t=1}^{T} \prod_{j=-c, j \neq 0}^{c} P(w_{t+j}|w_{t}; \theta)$$

 $\text{Objective function} \! = \! -\frac{1}{T} \log L(\theta)$

$$\begin{split} \frac{\delta}{\delta v_c} \log \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)} &= \frac{\delta}{\delta v_c} \log \exp(u_o^T v_c) - \frac{\delta}{\delta v_c} \log \sum_{w \in V} \exp(u_w^T v_c) \\ &= u_o - \sum_w^V \frac{\exp(u_w^T v_c)}{\sum_w^V \exp(u_w^T v_c)} u_w \\ &= u_o - \sum_w^V P(w|c) u_w \end{split}$$

Problem: In this function the denominator is expensive to compute Solution:

- Sub sampling frequent words
- Context position Weighting
- Negative sampling



<u>Sub-sampling frequent words</u>: frequent words provide less information than rare words. To counter imbalance created by frequent words against rare, discard some frequent from the training dataset. Heuristics: *w*_i is the discarded with probability

$$P(w_i) = 1 - \left(\frac{t}{f(w_i)}\right)^{\frac{1}{2}}$$

<u>Negative sampling</u> Subsampling frequent words and context position waiting helps, but can we do better? Noise Contrast estimation: posits a good model should be able to differentiate data from noise by means of Logistic regression.

Changing objective function for learning word vectors.

pair (w,c)coming from Data? 1 if yes, 0 if no

Maximize that all pairs come from data and minimise that does not come from data.

$$\begin{split} &= \underset{\theta}{\operatorname{argmax}} \prod_{(w,c) \in D} P(D = 1 | w,c,\theta) \prod_{(w,c) \in \widetilde{D}} P(D = 0 | w,c,\theta) \\ &= \underset{\theta}{\operatorname{argmax}} \sum_{(w,c) \in D} \log \frac{1}{1 + \exp(-v_w^{'T}v_c)} + \sum_{(w,c) \in \widetilde{D}} \log \frac{1}{1 + \exp(v_w^{'T}v_c)} \end{split}$$

for negative sampling, $(w,c) \in \widetilde{D}$ we can choose a 'k' word pair, where k ranges from 5 to 20.

$$\log \sigma(v_{w_o}^{'T}v_{w_i}) + \sum_{i=1}^{K} \underbrace{E}_{w_i \sim P_n(w)} [\log \sigma(-v_{w_i}^{'T}v_{w_i})]$$

$$J_{\textit{Negative-sampling}}(u_o, v_c) = -\log \sigma(u_o^T v_c) - \sum_{k \in K \text{ sampling Indices}} \log(-u_k^T v_c)$$

How to choose words from negative sampling?

$$P(w_i) = \frac{f(w_i)^{\frac{3}{4}}}{\sum_{i=1}^{V} f(w_i)^{\frac{3}{4}}}$$

Continuous Bag of Words

predict the centre word given words in the context window. Here the input will be sum of one-hot vector of the context word.

Maximize
$$P(w_c|w_{c-m}, w_{c-m+1}, ..., w_{c-1}, w_{c+1}, ..., w_{c+m})$$

Hierarchical Softmax: Another method to improve calculation of probability of Predicting words. Binary tree representation of output layers. A random walk from the root to nodes assign probability to words. No output representation of words.

$$P(w|w_{I}) = \prod_{j=1}^{L(w)-1} \sigma([n(w, j+1) = ch(n(w, j))].v_{n}'(w, j)^{T}v_{w_{I}})$$

||x|| = 1 if x = True else - 1

 v_{w_I} Input representation of w_I

L(w) No. Of Nodes in the path to w

One representation of each were w, one for every inner node of the binary tree. The paper uses binary Huffman tree, short codes for frequent words.

GloVe Word-Word Co-occurence Matrix

Capture global information, simpler objectives/cost function. Ratio probabilities carry better information

 X_{ij} = No. of word j occurs in context of word i. $X \leftarrow |V| \times |V|$ dimension

We want,
$$F(w_i, e_j, \widetilde{w}_k) = \frac{P_{ik}}{P_{ik}}$$

Finding appropriate function which help us find useful/good word embeddings. Word Embeddings are relative so absolute value of word embeddings does not matter much their difference does

$$F(w_i - w_j; \widetilde{w}_k) = \frac{P_{ik}}{P_{ik}}$$

F could be complicate function like neural networks another choice dot product

$$F((w_i - w_j)^T \widetilde{w}_k) = \frac{P_{ik}}{P_{jk}}$$

Reaching Symmetry

$$w_i^T \widetilde{w}_k + b_i + \widetilde{b}_k = \log(X_{ik})$$

 w_i Input word Embedding

 \widetilde{w}_k Context word Embedding

 b_i Bias

 $\widetilde{b_k}$ Bias Context

$$\widetilde{w_i}^T w_k + \widetilde{b_i} + b_k = \log(X_{ki})$$

We want
$$F((w_i - w_j)^T \widetilde{w}_k) = \frac{F(w_i^T \widetilde{w}_k)}{F(w_i^T \widetilde{w}_k)}$$

To above equation, exponent function is a solution

$$\exp(w_i^T \widetilde{w}_k) = \frac{X_{ik}}{X_i}$$

$$w_i^T \widetilde{w}_k = \log\left(\frac{X_{ik}}{X_i}\right)$$

Cost function
$$J = \left(\underbrace{w_i^T \widetilde{w}_k + b_i + \widetilde{b}_k}_{\text{Prediction from Algo}} - \underbrace{\log(X_{ik})}_{\text{From data}}\right)^2$$

Problem, if $X_{ij} = 0$; $\log(x_{ij})$ is not define

$$J = \sum_{i,j=1}^{|V|} f(X_{ij}) \left(w_i^T \widetilde{w}_j + b_i + \widetilde{b}_j - \log(X_{ij}) \right)^2$$

Properties of F():

- F(0) = 0, it should vanish as x tends to 0; $\lim_{x\to 0} f(x)\log^2(x)$ = finite
- F(x) is non-decreasing
- F(x) relatively small for large values

$$f(x) = \begin{cases} (x/x_{max})^{\alpha}, & \text{if } x < x_{max} \\ 1, & \text{otherise} \end{cases}$$

Perplexity: Standard evaluation metric for Language Models

Perplexity =
$$\prod_{t=1}^{T} \left[\frac{1}{P_{LM}(x^{(t+1)}|x^{(t)},...,x^{(1)})} \right]^{\frac{1}{T}}$$

This is equal to exponential of cross entropy

$$\prod_{t=1}^{T} \left(\frac{1}{\hat{y}_{x_{t+1}}^{(t)}} \right)^{\frac{1}{T}} = \exp \left[\frac{-1}{T} \sum_{t=1}^{T} \log \hat{y}_{x_{t+1}}^{(t)} \right]$$

The lower perplexity, the better

Neural Network

Non-linearities:

• Sigmoid $(1+\exp(-z))^{-1}$

•
$$\tanh \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

• hard
$$tanh$$

$$\begin{cases} 1, & x \ge 1 \\ x, & -1 \le x \le 1 \\ -1, & x \le 1 \end{cases}$$

- ReLU max(z,0)
- Leaky ReLU
- Swish $x.\sigma(x)$
- GeLU $x.P(X \le x)$ $X \sim N(0,1)$ $\approx x. \sigma(1.702 x)$

Regularization

Classical view: Regularization works to prevent over-fitting when we have a lot of features.

Now: Regularization produces model that generalize well when we have a "big" model we don't care that our model overfits on the training data even though they are hugely overfit.

DropOut: It prevents feature co-adaptation = good regulation

Parameter Initialization

- Zero Initialization (does not work) leads to identical gradient and prevents neuron from learning diverse features
- Uniform Initialization can work but effectiveness depends upon architecture and problem. The choice of range is critical for training. If it is too small, gradients during backpropagation may vanish.
- Xavier Initialization: Variance inversely proportional to fan in(n_{in}) and fan out (n_{out})

$$var(w) = \frac{2}{n_{in} + n_{out}}$$

Optimizer

- SGD (Works just fine)
- Adagrad (Simplest, but tend to "stall early")
- RMSprop
- Adam (Fairly good, safe place to begin in many cases)
- AdamW
- NadamW

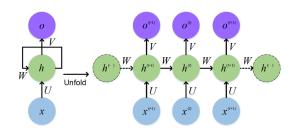
Recurrent Neural Network (RNN)

$$h^{(t)} = \sigma(W h^{(t-1)} + U x^{(t)} + b_1)$$
$$o^{(t)} = V h^{(t)} + b_2$$

Advantages:

- Can process any length input
- Model size does not increase for longer context
- In theory, computation for step t, can use information from many step back
- Same weights applied on every time step

Disadvantages:



Computation is slow.

Loss function on step t

$$\begin{split} J^{(t)}(\theta) &= -\sum_{w \in V} y_w^{(t)} \log y_w^{(t)} = -\log \hat{y}_{x_{t+1}}^{(t)} \\ J(\theta) &= \frac{1}{T} \sum_{t=1}^{T} J^{(t)}(\theta) = -\frac{1}{T} \sum_{t=1}^{T} \hat{y}_{x_{t+1}}^{(t)} \end{split}$$

RNNs can greatly improve perplexity over what came before.

Problems with RNN

Vanishing Gradient Problem: Gradient signal from far away is lost because its much smaller than gradient signal from close by. So model weights are basically updated only wrt near effects, not long term effects. Exploding gradient problem can be fixed by gradient clipping but vanishing gradient is still a problem. (Difficult to preserve information over many time steps)

Long Short Term Memory (LSTM)

$$f^{(t)} = \sigma(W_f h^{(t-1)} + U_f x^{(t)} + b_f)$$

$$i^{(t)} = \sigma(W_i h^{(t-1)} + U_i x^{(t)} + b_i)$$

$$o^{(t)} = \sigma(W_o h^{(t-1)} + U_o x^{(t)} + b_o)$$

Forget Gate: Control what is kept vs forgotten from previous cell state.

Legend:

Input Gate: Control what part of new cell content are written to cell Output Gate: Control what part of cell are output to hidden state.

$$\widetilde{c}^{(t)} = \tanh(W_c h^{(t-1)} + U_c x^{(t)} + b_c)
c^{(t)} = f^{(t)} \odot c^{(t-1)} + i^{(t)} \odot \widetilde{c}^{(t)}
h^{(t)} = o^{(t)} \odot \tanh c^{(t)}$$

LSTMs solve vanishing Gradients?

LSTM architecture make it much easier for an RNN to preserve information over many timesteps. If forgot gate is set to 1 for a cell and input gate is set to 0, then all the information of that cell is preserve indefinitely. In contrast its harder for Vanilla RNN and to learn current weight Matrix W_h that preserve info in hidden state.

Multi layer or stacked RNN allow a network to compute more complex representation, they work better than just have one layer of hidden dimensional encodings.

Neural Machine Translation e2e NN

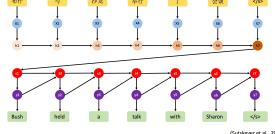
Architecture seq2seq (involves to RNN)

How do we evaluate machine translation?

BLEU (Bilingual Evaluation Understudy)

BLEU compare machine written translation to one or

several human return translations and compare a similar score based on:



- 1) Geometric mean of n-gram precision (1-, 2-, 3-, 4- gram)
- 2) Plus a penalty for two short system translation

BLEU is useful but imperfect, many ways to translate a sentence, a good translation can get a poor BLEU because it has low n-gram overlap with human evaluation.

Attention

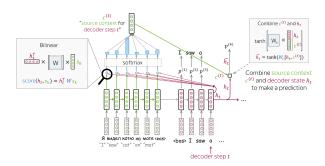
Core idea: On each step of decoder, use a direct connection to the encoder to focus on a particular part of source sequence

 $h_1, h_2, ..., h_N \in \mathfrak{R}^n$ //Encoder Hidden state $s_t \in \mathfrak{R}^n$ //Decoder hidden state at step t We get attention score

$$e^{t} = [s_{t}^{T} h_{w}, ..., s_{t}^{T} h_{N}] \in \Re^{N}$$

$$\alpha^{t} = \operatorname{softmax}(e^{t}) \in \Re^{N}$$

$$a_{t} = \sum_{i=1}^{N} \alpha_{i}^{t} h_{i} \in \Re^{n}$$



We use α^t to take a weighted sum of the encoder hidden state to get attention output a_t . We concatenate attention output a_t with decoder hidden state s_t and proceed as in non-attention seq2seq models

$$[a_t;s_t] \in \Re^{2n}$$

Attention Variants:

Several ways to compute $e \in \mathbb{R}^N$ from $h_1, \dots, h_N \in \mathbb{R}^{d_1}$ and $s \in \mathbb{R}^{d_2}$

- 1) Basic dot product: Assume $d_1 = d_2 :: e_i = s^T h_i \in \Re$
- 2) Multiplicative attention (better called as Bi-linear attention) $e_i = s^T W h_i \in \Re$; $W \in \Re^{d_2 \times d_1}$ is weight matrix.
- 3) Reduce-Rank multiplicative attention $e_i = s^T (U^T V) h_i = (U s)^T (V h_i) :: U \in \mathfrak{R}^{k \times d_1} V \in \mathfrak{R}^{k \times d_1} k \ll d_1, d_2$
- 4) Additive attention $e_i = V^T \tanh(W_1 h_1 + W_2 s) :: W_1 \in \Re^{d_3 \times d_1} W_2 \in \Re^{d_3 \times d_2} V \in \Re^{d_3}$

More general definition of attention: Given a set of factor values and query. Attention is a technique to compute a weighted sum of the values, dependent on the query Issues with RNN/LSTM:

- 1) Linear Interactive Distance: Nearby words often affect each others meaning. O(seq_length) steps for distant word pair to interact. Which means hard to lean long-distance dependencies
- 2) Lack of parallelizability: Forward and backward passes have O(seq_length) unparallelizable operations but future RNN hidden states can't be computed in full before past RNN hidden states have been computed. You can think of attention as performing fuzzy lookup in a key-value store. In a lookup table we have table of keys that map to a value. The query matches one of the keys returning its value. In attention the query matches all key softly to a weight between 0 and 1, the keys values are multiplied by weights and summed.

Self-attention

 $W_{1:n}$ be the sequence of word in vocabulary V. For each word w_i , let $x_i = Ew_i$; $E \in \Re^{d \times |V|}$ Embedding Matrix.

- 1) Transform each word embedding with weight matrix Q, K, V each in $\Re^{d\times d}$
- 2) Compute pairwise-similarities between keys and queries, normalize with softmax

$$\alpha_{ij} = q_i^T k_j$$

$$\alpha_{ij} = \frac{\exp(e_{ij})}{\sum_{l} \exp(e_{il})}$$

3) computer output for each word as weighted sum of values

$$o_i = \sum_j \alpha_{ij} v_j$$

Fixing first self attention problem:

1) Sequence order: since self attention does not built in order information we need to encode the order of the sentence in our keys queries and value. Considered representing each sequence index as a vector $p_i \in \mathbb{R}^d$ $i \in \{1,2,...,n\}$ $\widetilde{x}_i = x_i + p_i$

Sinusoidal position representation

$$p_{i} = \begin{bmatrix} \sin(i/10000^{\frac{2*1}{d}}) \\ \cos(i/10000^{\frac{2*1}{d}}) \\ \vdots \\ \sin(i/10000^{\frac{2*d/2}{d}}) \\ \cos(i/10000^{\frac{2*d/2}{d}}) \end{bmatrix}$$

Pros:

- Priodicity indicates that maybe "absolute position" isn't as important.
- maybe we can extrapolate to longer sequence as periods restart!

Cons:

• not learnable; extrapotion does not really work!

Learned absolute positional representation

Let all p_i be learnable parameters. $p \in \Re^{d \times n}$ p_i : column of p

Pros:

• Flexibility: each position gets to be learnt to fit the data.

Cons:

- Definitely can't extrapolate the indices outside 1 ... n
- 2) Adding non-linearities in Self Attention, since there are no non-linearity in self attention adding MLP layer post self attention $m_i = MLP(output) = W_2 ReLU(W_1 output_i + b_1) + b_2$

We can stack self attention + MLP on top of each other

3) Masking future in self attention: To enable parallelisation for future words by setting attention score to $-\infty$

Transformers

Decoder-only Transformers: Replace self attention with Masked multi-head attention.

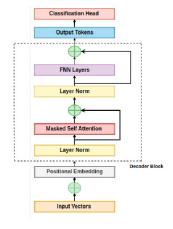
Sequence stack from attention $X = [x_1, x_2, ..., x_n] \in \Re^{n \times d}$ be concatenation of input vectors.

$$XK \in \mathfrak{R}^{n \times d}$$
 $XQ \in \mathfrak{R}^{n \times d}$ $XV \in \mathfrak{R}^{n \times d}$.

The output is defined as $softmax(XQ(XK)^T)XV \in \Re^{n \times d}$

Multihead Attention

For token 'i', self attention looks where $X_iQ^TKX_j$ is high, but maybe we ant to focus on different j for different reasons.



$$Q_l, K_l, V_l \in \mathbb{R}^{n \times \frac{d}{h}}$$
 where 'h' is number of heads, $l \in \{1, 2, ..., h\}$ output $_l = softmax(XQ_lK_l^TX^T)XV_l$. Output of all heads are combined $output = [output_1, output_2, ..., output_h]Y, Y \in \mathbb{R}^{d \times d}$

Even though we compute 'h' many attention had it is not really more costly. Compute $XQ \in \mathfrak{R}^{n \times d}$,

reshape to $\mathfrak{R}^{n \times h \times \frac{d}{h}}$ likewise for XV and XK. Transpose to $\mathfrak{R}^{h \times n \times \frac{d}{h}}$ (head axis is like batch axis). Everything else identical and matrices are of same size.

Scaled dot product

When dimensionality 'd' becomes large, dot product between vectors tend to become large, because of this, input to softmax can be large making gradient small. We divide attention score by $\sqrt{d/h}$ to stop the score from being large.

$$output_{l} = softmax \left(\frac{XQ_{l}K_{l}^{T}X^{T}}{\sqrt{d/h}} \right) XV_{l}$$

Two optimization tricks:

- Residual connection
- Layer normalization

These are often written as "add and norm"

Layer normalization Cut down on uninformative variation in hidden vector values by normalizing to unit mean and standard deviation within each layer

Encoder-decoder Transformers

We use normal transformer encoder but Decoder modified to perform cross attention to the output of the encoder. Let $h_1, h_2, \dots h_n$ be output vector from Transformer encoder. Let z_1, z_2, \dots, z_n be input vector from Transformer decoder, then keys and values are drawn from encoder $k_i = Kh_i$ $v_i = Vh_i$. Queries are drawn from decoder

Drawbacks of Transformers:

- Quadratic compute in self attention: Computing all interactions means are computation grows quadratic with sequence length, for RNN/LSTM it goes linearly
- Positional representation

Efficient Transformers

N: Sequence length h: No. of heads d_{model} : Embedding size

 $d_k : d_{model}/h$ $dim(X) = N \times d_{model}$

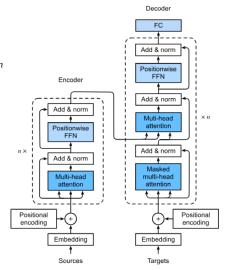
$$dim(W^{Q}) = dim(W^{K}) = dim(W^{V}) = d_{model} \times d_{k}$$

$$Attention(Q, K, V) = softmax \left(\frac{QK^{T}}{\sqrt{d}}\right)V$$

 $dim(QK) = N^2 O(N^2 d)$ Time comlexity to calculate QK Storing Attention matrix for each head $O(N^2 h)$ If $N \gg d_k$, space and time complexity $O(N^2)$

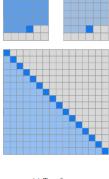
Sparse Transformers

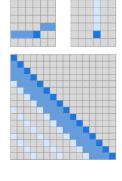
$$S = S_1, S_2, ..., S_n; S_i$$
:Input vector that i^{th} vector attends to $Attend(X, S)\{a(x_i, S_i)\}_{i \in [1,2,..n]}$

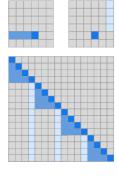


$$a(x_{i}, S_{i}) = softmax \left(\frac{(W^{Q}x_{i})K_{S_{i}}^{T}}{\sqrt{d}}\right)V_{S_{i}}$$
$$\begin{cases}K_{S_{i}} = (W^{K}S_{j})_{j \in S_{i}}\\V_{S_{i}} = (W^{V}S_{j})_{j \in S_{i}}\end{cases}$$

There can be 'P' separate attention heads, attending to different subsets of input tokens. The paper chose $|S_i^m| \propto \sqrt[p]{n}$







(b) Sparse Transformer (strided)

(c) Sparse Transformer (fixed)

1) Strided Attention: Each tokens attends to every kth token.

$$S_i^1 = \{t, t+1, ...i \text{ for } t = max(0, i-l)\}\$$

 $S_i^2 = \{j: (i-j) mod l = 0\}$

2) Fixed Attention

$$S_{i}^{1} = \left\{ j : \left\lfloor \frac{j}{l} \right\rfloor = \left\lfloor \frac{i}{l} \right\rfloor \right\}$$

$$S_{i}^{2} = \left\{ j : j \mod l \ l \in \{t, t+1, \dots, l\} \right\}$$

Time complexity reduces from O(N²d) to O(Nkd)

Linformer

Project K_i and V_i with E_i and $F_i \in \Re^{k \times n}$ into $\hat{k_i} = E_i K_i$, $\hat{v_i} = F_i V_i \in \Re^{k \times d_k}$ Softmax requires O(Nk) computational cost

Dimension of Attention matrix $N \times k$. Hence Storage O(Nkh) which is linear in $N(k, h \ll N)$

Theorem: For any Q_i , K_i , $V_i \in \Re^{n \times d}$ and W_i^Q , W_i^K , $W_i^V \in \Re^{d \times d}$, if $k = min\{\Theta(9 d \log(d))/\epsilon^2\}$, then exist matrices E_i and $F_i \in \Re^{n \times k}$ such that for any row vector w of matrix $QW_i^Q(KW_i^K)^T/\sqrt{d}$, we have

 $Pr(\|\operatorname{softamx}(wE_i^T)F_iVW_i^V - \operatorname{softmax}(w)VW_i^V\| < \epsilon \|\operatorname{softmax}(w)\|\|VW_i^V\| > 1 - o(1)$

Linearized Attention

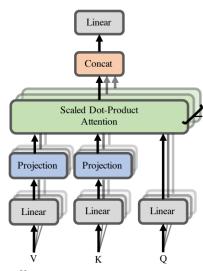
$$Y_{i} = softmax \left(\frac{Q_{i}K}{\sqrt{d_{k}}}\right)V$$

$$Y_{i} = \frac{\exp\left(\frac{Q_{i}K}{\sqrt{d_{k}}}\right)V}{\sum_{j=1}^{N} \exp\left(\frac{Q_{i}K_{j}}{\sqrt{d_{k}}}\right)}$$

$$Y_{i} = \frac{\sum_{j=1}^{N} \sin\left(Q_{i}, K_{j}\right)V_{j}}{\sum_{j=1}^{N} \sin\left(Q_{i}, K_{j}\right)}$$

where
$$sim(q,k) = exp(\frac{q.k}{\sqrt{d_k}})$$

The only constraint on sim(.) is no negativity, Any $K(x,y): \Re^{2 \times d_{model}} \rightarrow \Re_+$ works



Let $\phi(x)$ be feature representation of such a kernel, then

$$Y_{i} = \frac{\sum_{j=1}^{N} \phi(Q_{i})^{T} \phi(K_{j}) V_{j}}{\sum_{j=1}^{N} \phi(Q_{i})^{T} \phi(K_{j})}$$

$$Y_{i} = \frac{\phi(Q_{i}) \sum_{j=1}^{N} \phi(K_{j}) V_{j}^{T}}{\phi(Q_{i})^{T} \sum_{j=1}^{N} \phi(K_{j})}$$

Now, $\sum_{j=1}^{N} \phi(K_j) V_j^T$ and $\sum_{j=1}^{N} \phi(K_j)$ can be computed once and reused.

Causal Masking: Maskign Attention computation such that ith position can only be influenced by position j, if and only if $j \le i$

$$Y_{i} = \frac{\phi(Q_{i}) \sum_{j=1}^{i} \phi(K_{j}) V_{j}^{T}}{\phi(Q_{i})^{T} \sum_{j=1}^{i} \phi(K_{j})} = \frac{\phi(Q_{i})^{T} S_{i}}{\phi(Q_{i})^{T} Z_{i}}$$

$$S_{i} = \sum_{j=1}^{i} \phi(K_{j}) V_{j}^{T}$$

$$Z_{i} = \sum_{j=1}^{i} \phi(K_{j})$$

Byte-Pair encoding algorithm

- Start with vocabulary containing only characters and an "and of word" symbol
- Using Corpus of text find the most common adjacent character
- Replace instances of character pair with new subwords, repeat until desired vocabulary size Subword Modelling paradigm is to learn vocabulary of part of words. At training and testing time each word is split into a sequence known as subword

Earlier we had pre-trained word embeddings on which a model (RNN/LSTM/Transformer) has been trained. Issues :

- Training data from downstream task must be sufficient to teach all contextual aspect of language.
- Parameters in our network are randomly initialise.

In modern NLP, all parameters are initialized via pre training pre-training. Pre-training method hide parts of input from the model and train the model to reconstruct these part. This has been exceptionally efficient at building strong:

- Representation of language
- Parameter initialization for strong NLP model
- Probability distribution over language that we can sample from

Why should pre-training and fine-tuning help from "training Network network" perspective

- Provide $\hat{\theta}$ by approximating $\min \mathscr{L}_{\textit{pretrain}}(\theta)$
- Then fine-tune by approximating $\min_{\theta} \mathscr{L}_{\mathit{finetuning}}(\theta)$, starting at $\hat{\theta}$

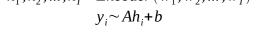
The pre-training may matter because SGD stick close to $\hat{\theta}$ during fine-tuning. So maybe fine-tuning local minimum near $\hat{\theta}$ tend to generalize well and/or maybe gradient of fine-tuning loss near $\hat{\theta}$ propagate nicely. went

Pre-training Encoders

Encoder gets bi-directional context, so we can't do language modelling! Replace some fraction of words in input with special mask [MASK] token predict these words.

$$h_1, h_2, \dots, h_T = Encoder(w_1, w_2, \dots, w_T)$$

 $y_i \sim Ah_i + b$



BERT Bi-directional Encoder Representation from

Transformer

Mask LM for BERT, predict random 15% of (sub)words tokens

- Replace input word with [MASK] 80% of the time
- Replace input word with a random token 10% of the time
- Leave input word unchanged 10% of the time (but still predict it)

If you are task involve generating sequences, consider using decoder BERT and other don't naturally lead to nice auto-regressive generation method.



The encoder model benefit from bi-directional context. Decoder portion is used to train the whole network through language modelling.

Pre-training Decoder

When using language model, pre-trained decoded we can ignore that they were trained to model $P(w_t|w_{1:t-1})$. We can fine-tune them by training a classifier on the last word hidden state.

$$h_1, h_2, \dots, h_T = Decoder(w_1, w_2, \dots, w_T)$$

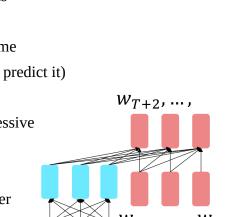
 $y \sim Ah_T + b$

t is natural to pre-train Decoder as a language model then use them as generator, fine-tune with $p_{\theta}(w_t|w_{1:t-1})$. This will helpful in task where output is a sequence with vocabulary like that at pre-training time

- Dialogue (context = Dialogue history)
- Summarization (context = document)

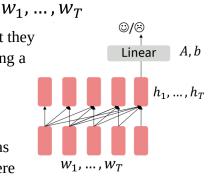
GPT Generative pre-train Transformers

- 12 layers, 117M parameters
- 768 dimensional hidden state, 3072 dimensional feed forward layer



[M] to the [M]

 h_1, \ldots, h_T



- Byte-pair Encoding with 40000 mergers
- Trained on book Corpus (7000 books)

GPT-2 (1.5B) trained on more data

GPT-3 (175B) seems to perform some kind of learning without grading steps simply from examples you provide within the contexts. The incontext example seems to specify the task to be performed and the conditional distribution mocks performing the task to certain extent

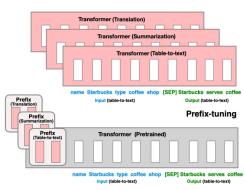
Fine-tuning vs Parameter Efficient Fine-Tuning

Fine-Tuning every parameter on a pre-trained model works well, but it's memory intensive. But

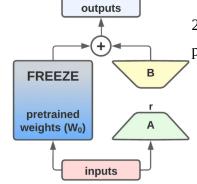
light-weight fine-tuning methods adapts pre-trained model in a constrained way, leads to less over-fitting and/or more efficient find tuning and inference

Parameter Efficient Fine-Tuning

1) Prefix tuning adds a prefix to parameters and freeze all the pre-trained parameters. The prefix is processed by the model just like real words would be. Advantage: each element of the batch at inference could run a different tune model.



LoRA adaptation



2) Low Rank Adaptation : Learns a low rank difference between pre trained and fine-tuned weight matrices

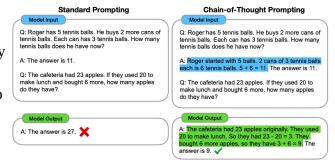
Post Training

Language model made to rudimentary modelling of agents, believes an actions

1) Emergent zero short learning: One key emergent ability in GPT-2 is zero short learning, ability to

do many task with no example and no gradient updates.

- 2) Emergent few short learning: Specify a task by simply prepending examples of the task before your examples. Also called in-context learning to stress that gradient up dates are performed when learning and new task.
- 3) Chain of thought prompting
- 4)Zero-shot chain of tought prompting Zero-shot and few-shot in-context learning:
 - No fine tuning needed, prompt engineering (CoT) can improve performance.
 - Limits to what you can fit in context.



(d) Zero-shot-CoT (Ours)

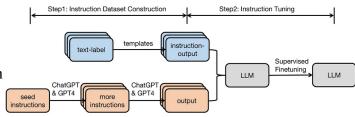
Q: A juggler can juggle 16 balls. Half of the balls are golf balls, and half of the golf balls are blue. How many blue golf balls are there?

A: Let's think step by step.

(Output) There are 16 balls in total. Half of the balls are golf balls. That means that there are 8 golf balls. Half of the golf balls are blue. That means that there are 4 blue golf balls.

• Complex task will probably need gradient steps.

Instruction fine tuning: Supervised finetuning trains models on input examples and their corresponding outputs, instruction tuning augments input-output examples with instructions, which enables instructiontuned models to generalize more easily to new tasks.



- 1) You can generate data synthetically from bigger LLMs
- 2) You don't need many samples to instruction tune.
- 3) Crowdsourcing can be pretty effective

Limitation of instruction fine tuning:

- It is expensive to collect ground truth data for tasks.
- Tasks like open ended creative generation have no right answer.
- Language modelling penalize all the token level mistake equally but some errors are worse than other.
- Human generate sub optical answers.

Optimising for human preferences

We are training LM on some task, for an instruction 'x' and the LM sample 'y'. we have a better way to obtain a human reward of summary $R(x, y) \in \Re$ (higher is better).

Maximize expected reward of samples from our LM

$$\mathop{E}_{\hat{y} \sim p_{\theta}(y|x)}[R(x,\hat{y})]$$

High level instantiation 'RLHF' pipeline



