

# Example to test Installation of MatTuGames

Consult also the file `getting_started.m` in the doc-folder.

< M A T L A B (R) >  
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R2013a (8.1.0.604) 64-bit (glnxa64)  
February 15, 2013

To get started, type one of these: `helpwin`, `helpdesk`, or `demo`.  
For product information, visit [www.mathworks.com](http://www.mathworks.com).

Checking Basic Installation of MatTuGames.  
The claims vector is specified by:

d =

40.0000 32.0000 11.0000 73.3000 54.9500 81.1000

and the estate by:

E =

176

The Talmudic distribution is given by:  
`t1m_rl=Talmudic_Rule(E,d)`

t1m\_rl =

20.0000 16.0000 5.5000 48.3500 30.0000 56.1500

The corresponding bankruptcy game is given by:  
`bv=bankruptcy_game(E,d)`

bv =

Columns 1 through 14

0	0	0	0	0	0	0	0	0	0	0	28.9500	0	7.9500	0
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Columns 15 through 28

39.9500	0	0	0	10.6000	0	0	0	21.6000	11.9000	51.9000	43.9000	83.9000	22.9000
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Columns 29 through 42

62.9000	54.9000	94.9000	0	4.7500	0	36.7500	0	15.7500	7.7500	47.7500	38.0500	78.0500	70.0500
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Columns 43 through 56

110.0500	49.0500	89.0500	81.0500	121.0500	19.7000	59.7000	51.7000	91.7000	30.7000	70.7000	62.7000	102.7000	93.0000
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Columns 57 through 63

133.0000	125.0000	165.0000	104.0000	144.0000	136.0000	176.0000
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Is the game convex?

cvQ=convex\_gameQ(bv)

cvQ =

1

Is the core non-empty?

crQ=coreQ(bv)

Exiting: The constraints are overly stringent; no feasible starting point found.

crQ =

1

Is the game monotone?

mQ=monotone\_gameQ(bv)

mQ =

1

Is the game zero-monotone?  
zmQ=zero\_monotonicQ(bv)

zmQ =  
1

Is the game average convex?  
acvQ=average\_convexQ(bv)

acvQ =  
1

Is the game super additive?  
sadQ=super\_additiveQ(bv)

sadQ =  
1

Is the game semi convex?  
scvQ=semi\_convexQ(bv)

scvQ =  
1

The Harsanyi dividends are given by:  
hd=harsanyi\_dividends(bv)

hd =

Columns 1 through 14

0	0	0	0	0	0	0	0	0	0	0	28.9500	0	7.9500	0
---	---	---	---	---	---	---	---	---	---	---	---------	---	--------	---

Columns 15 through 28

3.0500	0	0	0	10.6000	0	0	0	11.0000	11.9000	40.0000	32.0000	-39.5500	11.0000
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Columns 29 through 42

-7.9500	0	-14.0500	0	4.7500	0	32.0000	0	11.0000	7.7500	-7.7500	38.0500	35.2500	32.0000
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Columns 43 through 56

-60.9500	11.0000	-18.9500	-7.7500	4.7000	19.7000	35.2500	32.0000	-42.6000	11.0000	-11.0000	-7.7500	-3.2500	23.3500
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Columns 57 through 63

-75.2500	-64.0000	71.5500	-22.0000	18.9500	7.7500	6.3000
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We get the following game from the Harsanyi dividends:

v=getgame(hd)

v =

Columns 1 through 14

0	0	0	0	0	0	0	0	0	0	28.9500	0	7.9500	0
---	---	---	---	---	---	---	---	---	---	---------	---	--------	---

Columns 15 through 28

39.9500	0	0	0	10.6000	0	0	0	21.6000	11.9000	51.9000	43.9000	83.9000	22.9000
---------	---	---	---	---------	---	---	---	---------	---------	---------	---------	---------	---------

Columns 29 through 42

62.9000	54.9000	94.9000	0	4.7500	0	36.7500	0	15.7500	7.7500	47.7500	38.0500	78.0500	70.0500
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Columns 43 through 56

110.0500	49.0500	89.0500	81.0500	121.0500	19.7000	59.7000	51.7000	91.7000	30.7000	70.7000	62.7000	102.7000	93.0000
----------	---------	---------	---------	----------	---------	---------	---------	---------	---------	---------	---------	----------	---------

Columns 57 through 63

133.0000	125.0000	165.0000	104.0000	144.0000	136.0000	176.0000
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Coincides this game with the original game bv?

geqQ1 =

1

The Shapley value of the game is:

sh\_v=ShapleyValue(bv)

sh\_v =

23.5175	18.7483	6.4950	44.3008	33.3317	49.6067
---------	---------	--------	---------	---------	---------

The Tau value of the game is:

tau\_v=TauValue(bv)

tau\_v =

24.0807	19.2646	6.6222	44.1279	33.0809	48.8237
---------	---------	--------	---------	---------	---------

The solidarity value of the game is:

sl\_vl=SolidarityValue(bv)

sl\_vl =

28.0285	27.0297	24.5264	32.5247	30.1952	33.6954
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A pre-kernel element of the game is:

prk\_v=PreKernel(bv)

prk\_v =

20.0000	16.0000	5.5000	48.3500	30.0000	56.1500
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A kernel element of the game is:

kr\_v=Kernel(bv)

kr\_v =

20.0000	16.0000	5.5000	48.3500	30.0000	56.1500
---------	---------	--------	---------	---------	---------

The pre-nucleolus of the game is:

prn\_v=PreNucl(bv)

Optimization terminated.

Optimization terminated.

Optimization terminated.

Optimization terminated.

Optimization terminated.  
Optimization terminated.  
Optimization terminated.

prn\_v =

20.0000	16.0000	5.5000	48.3500	30.0000	56.1500
---------	---------	--------	---------	---------	---------

The nucleolus of the game is:

nuc\_v=nuc1(bv)

Optimization terminated.  
Optimization terminated.  
Optimization terminated.  
Optimization terminated.  
Optimization terminated.  
Optimization terminated.

nuc\_v =

20.0000	16.0000	5.5000	48.3500	30.0000	56.1500
---------	---------	--------	---------	---------	---------

The vector of excesses w.r.t. the pre-kernel is:

ex\_prk=excess(bv,prk\_v)

ex\_prk =

Columns 1 through 14

-20.0000	-16.0000	-36.0000	-5.5000	-25.5000	-21.5000	-41.5000	-48.3500	-68.3500	-64.3500	-55.4000	-53.8500	-65.9000	-69.8500
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Columns 15 through 28

-49.9000	-30.0000	-50.0000	-46.0000	-55.4000	-35.5000	-55.5000	-51.5000	-49.9000	-66.4500	-46.4500	-50.4500	-30.4500	-60.9500
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Columns 29 through 42

-40.9500	-44.9500	-24.9500	-56.1500	-71.4000	-72.1500	-55.4000	-61.6500	-65.9000	-69.9000	-49.9000	-66.4500	-46.4500	-50.4500
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Columns 43 through 56

-30.4500	-60.9500	-40.9500	-44.9500	-24.9500	-66.4500	-46.4500	-50.4500	-30.4500	-60.9500	-40.9500	-44.9500	-24.9500	-41.5000
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Columns 57 through 63

-21.5000   -25.5000   -5.5000   -36.0000   -16.0000   -20.0000   0

Is the vector  $\text{prk } v$  a pre-kernel element?

```
prkQ=PrekernelQ(bv,prk_v)
```

$$\text{prkQ} =$$

1

The anti-pre-kernel element of the game is given by:

```
aprk=Anti PreKernel(bv)
```

apr<sub>k</sub> =

22.6550    17.9050    7.3050    41.8600    37.1100    49.1650

The dual game is:

```
dv=dual_game(bv)
```

$$dv =$$

Columns 1 through 14

40.0000	32.0000	72.0000	11.0000	51.0000	43.0000	83.0000	73.3000	113.3000	105.3000	145.3000	84.3000	124.3000	116.3000
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Columns 15 through 28

156.3000    54.9500    94.9500    86.9500    126.9500    65.9500    105.9500    97.9500    137.9500    128.2500    168.2500    160.2500    176.0000    139.2500

Columns 29 through 42

176.0000 171.2500 176.0000 81.1000 121.1000 113.1000 153.1000 92.1000 132.1000 124.1000 164.1000 154.4000 176.0000 176.0000

Columns 43 through 56

176.0000 165.4000 176.0000 176.0000 176.0000 136.0500 176.0000 168.0500 176.0000 147.0500 176.0000 176.0000 176.0000 176.0000

Columns 57 through 63

176.0000 176.0000 176.0000 176.0000 176.0000 176.0000 176.0000

The greedy bankruptcy game is specified by:

gv=greedy\_bankruptcy(E,d)

gv =

Columns 1 through 14

40.0000	32.0000	72.0000	11.0000	51.0000	43.0000	83.0000	73.3000	113.3000	105.3000	145.3000	84.3000	124.3000	116.3000
---------	---------	---------	---------	---------	---------	---------	---------	----------	----------	----------	---------	----------	----------

Columns 15 through 28

156.3000	54.9500	94.9500	86.9500	126.9500	65.9500	105.9500	97.9500	137.9500	128.2500	168.2500	160.2500	176.0000	139.2500
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Columns 29 through 42

176.0000	171.2500	176.0000	81.1000	121.1000	113.1000	153.1000	92.1000	132.1000	124.1000	164.1000	154.4000	176.0000	176.0000
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Columns 43 through 56

176.0000	165.4000	176.0000	176.0000	176.0000	136.0500	176.0000	168.0500	176.0000	147.0500	176.0000	176.0000	176.0000	176.0000
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Columns 57 through 63

176.0000	176.0000	176.0000	176.0000	176.0000	176.0000	176.0000
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Is the greedy game equal to the dual?

geqQ2 =

1

A pre-kernel element of the dual is given by:

prk\_dv=PreKernel(dv)

prk\_dv =

22.6550	17.9050	7.3050	41.8600	37.1100	49.1650
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An anti-pre-kernel element of the dual is given by:

apr\_kdv=Anti\_PreKernel(dv)

apr\_kdv =



20.0000	16.0000	5.5000	48.3500	30.0000	56.1500
---------	---------	--------	---------	---------	---------

Satisfies the pre-kernel consistency?

```
[RGP RGPC]=Reduced_game_propertyQ(bv,prk_v,'PRK');
```

```
echo off;
```

RGP =

rgpQ: 1

[illegible]

Satisfies the pre-kernel converse consistency?

```
[CRGP CRGPC]=Converse_RGP_Q(bv,prk_v,'PRK');
```

```
echo off;
```

CRGP =

CrgpQ: 1

```
crgpQ: [1 1 1 1 1 1 1 1 1 1 1 1 1 1]
```

Satisfies the pre-kernel element the reconfirmation property?

```
[RCP RPCP]=Reconfirmation_propertyQ(bv,prk_v,'PRK');
```

```
echo off;
```

RCP =

RCPQ: 1

[illegible]

Is the pre-kernel element replicable for some related games?

```
RepSol=replicate_prk(bv,prk_v,2,1)
```

RepSol =

[illegible]

```
V SPC: [57x63 double]
```

[illegible]

SBC: [1x1 struct]

```
Mat W: [16x63 double]
```

P Basis: [57x63 double]

```
VarP_Basis: [57x63 double]
```

Select a partition of the player set by:

$P=\{[1\ 3],[2\ 4\ 5],[6]\}$

P =

[1x2 double] [1x3 double] [6]

Transcribe it to its unique integer representation through:

$pm=clToMatlab(P)$

pm =

5 26 32

The Owen value w.r.t. a priori unions pm is:

$ow\_vl=OwenValue(bv,pm)$

ow\_vl =

21.7083 22.3667 6.4167 46.8500 35.4833 43.1750

The weighted Owen value w.r.t. a priori unions pm is:

$wow\_vl=weightedOwen(bv,pm)$

wow\_vl =

20.4708 29.9500 5.1792 54.4333 43.0667 22.9000

The coalition solidarity value w.r.t. a priori unions pm is:

$csl\_vl=CoalitionSolidarity(bv,pm)$

csl\_vl =

17.8854 29.8231 10.2396 39.7704 35.1065 43.1750

Define a communication structure by:

$CS=\{[1\ 2],[1\ 3],[1\ 4],[2\ 3],[2\ 4],[3\ 4],[4\ 5],[4\ 6],[5\ 6]\}$

CS =

Columns 1 through 8

[1x2 double] [1x2 double] [1x2 double] [1x2 double] [1x2 double] [1x2 double] [1x2 double] [1x2 double]

Column 9

[1x2 double]

Transform it to its unique integer representation by:

csm=clToMatlab(CS)

csm =

3 5 6 9 10 12 24 40 48

The Myerson value w.r.t. communication structure csm is specified by:

my\_vl=MyersonValue(bv,csm)

my\_vl =

20.7142 17.1158 7.6658 54.7892 31.3200 44.3950