# Factor Oracle for Machine Improvisation

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## **Preliminaries**

#### Word

A word s is a finite sequence  $s = s_1 s_2 \dots s_m$  of length |s| = m on a finite alphabet  $\Sigma$ .

#### **Factor**

A word  $x \in \Sigma^*$  is a factor of s if and only if s can be written s = uxv with  $u, v \in \Sigma^*$ . Given integers i, j where  $1 \le i \le j \le m$ , we denote a factor of s as  $s[i...j] = s_i s_{i+1} ... s_j$ .

## **Preliminaries**

#### **Prefix**

A factor x of s is a prefix of s if s = xu with  $u \in \Sigma^*$ . The ith prefix of s, denoted  $pref_s(i)$ , is the prefix s[1 ... i].

#### **Suffix**

A factor x of s is a suffix of s if s = ux with  $u \in \Sigma^*$ . The ith suffix of s, denoted  $suff_s(i)$ , is the suffix s[i ... m].

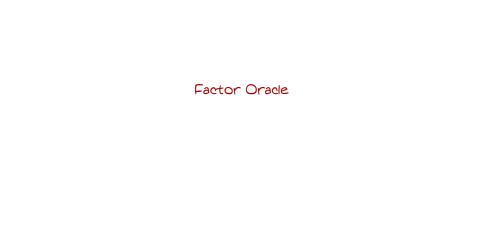
## **Preliminaries**

## Longest Repeated Suffix (LRS)

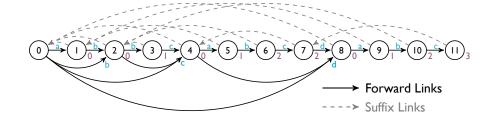
A factor x of s is the longest repeated suffix of s if x is a suffix of s and |x| is maximal.

$$s = \begin{bmatrix} a & b & b & c & d & a & b & c \end{bmatrix}$$

$$Irs(s)$$



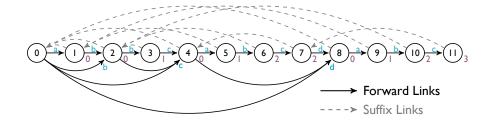
Overview



#### **Factor Oracle**

The factor oracle of a word s of length m is a deterministic finite automaton  $(Q, q_0, F, \delta)$  where  $Q = \{0, 1, \dots, m\}$  is the set of states,  $q_0 = 0$  is the starting state, F = Q is the set of terminal states and  $\delta$  is the transition function.

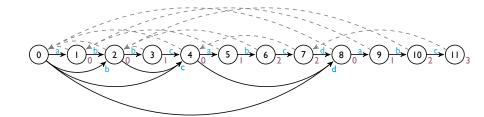
Overview



#### Suffix Link

The suffix link of a state i of the factor oracle of a word s, is equal to the state in which the *longest repeated suffix* (lrs) of s[1 ... i] is recognized.

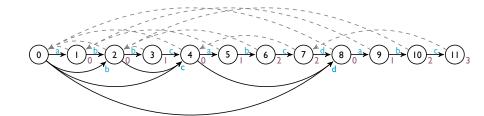
Overview



## **Suffix Links**

• s = abbcabcdabc

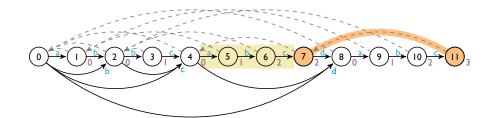
Overview



## **Suffix Links**

- s = abbcabcdabc
- lrs(s) = abc

Overview



## **Suffix Links**

- s = abbcabcdabc
- lrs(s) = abc
- S(11) = 7

Algorithm

#### **Algorithm I** Construction of a Factor Oracle

```
1: function FactorOracle(p = p_1p_2 \dots p_m)
2: Create a new oracle P with an initial state 0
3: S_P(0) \leftarrow -1
4: for i \leftarrow 1, m do
5: Oracle(p = p_1p_2 \dots p_i) \leftarrow AddLetter(Oracle(p = p_1p_2 \dots p_{i-1}), p_i)
6: end for
7: return Oracle(p = p_1p_2 \dots p_m)
8: end function
```

#### Algorithm

## Algorithm 2 Incremental update of Factor Oracle

```
1: function AddLetter(Oracle(p = p_1, p_2 ... p_m), \sigma)
 2:
          Create state m+1
 3:
                                                                                                  \triangleright \delta(m, \sigma) = m + 1
          Create a new transition from m to m+1 labeled by \sigma
 4:
          k \leftarrow S_p(m)
 5:
          i \leftarrow m
 6:
          while k > -1 and there is no transition from k by \sigma do
               Create a new transition from k to m+1 by \sigma
 7:
                                                                                                   \triangleright \delta(k, \sigma) = m + 1
 8:
              i \leftarrow k
 9:
               k \leftarrow S_p(k)
10:
          end while
          if k = -1 then
11:
12:
              S_{p\sigma} \leftarrow 0
13:
              Irs_{n\sigma} \leftarrow 0
14:
          else
15:
               S_{p\sigma} \leftarrow state that leads the transition from k by \sigma
               Irs_{p\sigma} \leftarrow \text{LengthCommonSuffix}(i, S(m+1)-1) + I
16:
17:
          end if
```

Algorithm

## Algorithm 3 Incremental update of Factor Oracle

```
18: k \leftarrow \text{FindBetter}(m+1, p[m+1-lrs(m+1)])

19: if k \neq 0 then

20: lrs_{p\sigma} \leftarrow lrs(m+1) + 1

21: S_{p\sigma} \leftarrow k

22: end if

23: T(S_{p\sigma}) \leftarrow T(S(m+1) \cup \{i\})

24: return Oracle(p = p_1p_2 ... p_m\sigma)

25: end function
```

Algorithm

#### Algorithm 4 Find Better Algorithm

```
    function FindBetter(i, a)
    for all the elements j of T(i) in increasing order do
    if Irs(j) = Irs(i) and p[j - Irs(i)] = a then
    return j
    end if
    end for
    return 0
    end function
```

Algorithm

## Algorithm 5 Length Common Suffix Algorithm

```
function LengthCommonSuffix(i, j)
 2:
        if S(i) = i then
 3:
           return Irs(i)
4:
       else
 5:
           while S(i) \neq S(j) do
 6:
              j \leftarrow S(j)
 7:
           end while
8:
        end if
 9:
       return min(lrs(i), lrs(j))
10: end function
```

Thank you for your attention! ©

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