

Logical Agents Homework

1. Unicorn Problem

Mythical = M

Mortal = R

Mammal = L

Horned = H

Magical = G

Knowledge Base:

R1: $M \Rightarrow \neg R$

R2: $\neg M \Rightarrow (R \wedge L)$

R3: $(\neg M \vee L) \Rightarrow H$

R4: $H \Rightarrow G$

Proofs:

R5: $\neg M \vee \neg R$ - implication elimination R1

R6: $(M \vee R) \wedge (M \vee L)$ - implication elimination R2

R7: $M \vee R$ - separate compound statement R6

R8: $M \vee L$ - separate compound statement R6

R9: $\neg R \vee L$ - resolution R5, R8

R10: H - Modus Ponens R3, R9

R11: G - Modus Ponens R4, R10

R12: M - Cannot prove

2. True / False

- False \models True: **TRUE**, anything implying True will be True
- $(A \wedge B) \models (A \Leftrightarrow B)$: **TRUE**, this is given by its truth table. In every instance that $(A \wedge B)$ is True, $(A \Leftrightarrow B)$ is True

| A | B | $(A \wedge B)$ | $(A \Leftrightarrow B)$ |
|---|---|----------------|-------------------------|
| T | T | T | T |
| T | F | F | F |
| F | T | F | F |
| F | F | F | T |

- c. $A \Leftrightarrow B \models (A \vee B)$: **FALSE**, the last condition leads a non-entailment relationship between these two

| A | B | $(A \Leftrightarrow B)$ | $(A \vee B)$ |
|---|---|-------------------------|--------------|
| T | T | T | T |
| T | F | F | T |
| F | T | F | T |
| F | F | T | F |

- d. $A \Leftrightarrow B \models \neg A \vee B$: **TRUE**, for each True condition leads to a True entailment

| A | B | $\neg A$ | $A \Leftrightarrow B$ | $\neg A \vee B$ |
|---|---|----------|-----------------------|-----------------|
| T | T | F | T | T |
| T | F | F | F | F |
| F | T | T | F | T |
| F | F | T | T | T |

- e. $(A \vee B) \wedge (\neg A \vee B)$ is satisfiable: **TRUE**, this is satisfiable by some model since it has true values in 2 positions.

| A | B | $\neg A$ | $A \vee B$ | $\neg A \vee B$ | $(A \vee B) \wedge (\neg A \vee B)$ |
|---|---|----------|------------|-----------------|-------------------------------------|
| T | T | F | T | T | T |
| T | F | F | T | F | F |
| F | T | T | T | T | T |
| F | F | T | F | T | F |