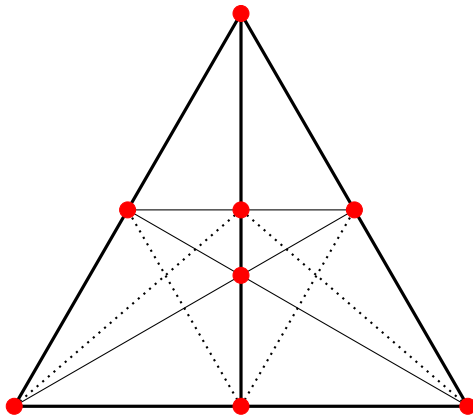


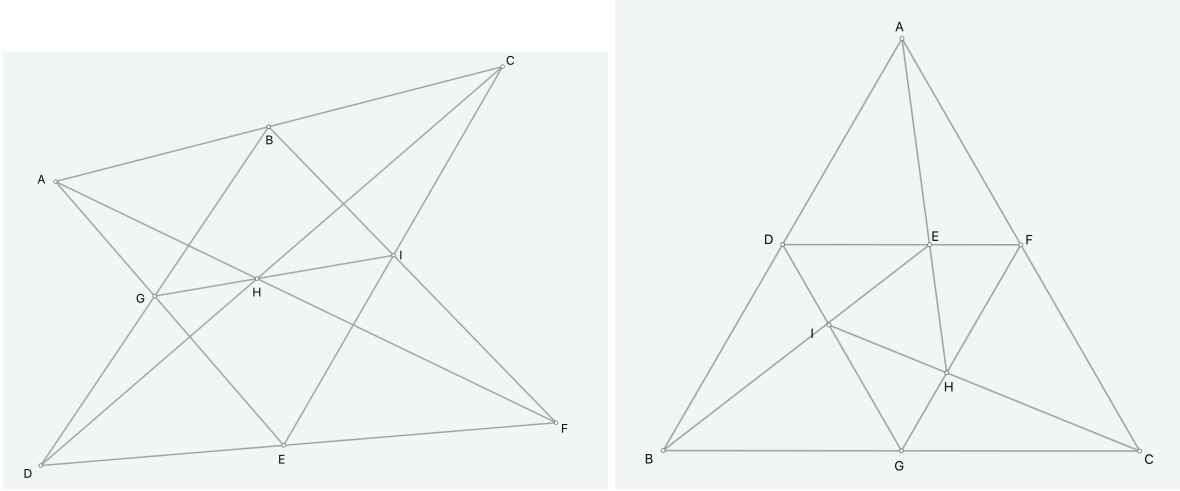
**Q1:**



As indicated in the figure, the 8 points consist of 3 vertices of an equilateral triangle, 3 midpoints of edges, the mass center and the midpoint of the height. The 4 dotted lines are the ordinary lines.

**Q2:** We borrow the ideas from graph theory. For each configuration  $X$ , we associate it with a matrix  $m(X)$  with rows labeled by points and columns labeled by lines and with the entry value 1 if the point lies on the line and 0 if not. Relabeling and moving vertices around for a fixed configuration  $X$  only permutes rows and columns of  $m(X)$ . In other words, if  $X$  and  $Y$  are two isomorphic combinatorial configurations, then there is a permutation matrix  $P$  such that  $m(Y) = P \cdot m(X)$ . In particular, this means  $m(X)$  and  $m(Y)$  have the same rank.

Now label the Pappus configuration and another configuration as in the figure.



Then the associated matrices are

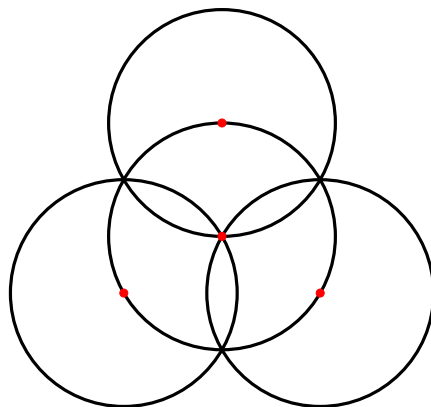
$$\begin{matrix} & \begin{matrix} ABC & AHF & AGE & BGD & BIF & CHD & CIE & GHI & DEF \end{matrix} \\ \begin{matrix} A \\ B \\ C \\ D \\ E \\ F \\ G \\ H \\ I \end{matrix} & \begin{pmatrix} 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 \end{pmatrix} \end{matrix} = m(X)$$

and

$$\begin{matrix} & \begin{matrix} ADB & AEH & AFC & BGC & BIE & CHI & DEF & DIG & GHF \end{matrix} \\ \begin{matrix} A \\ B \\ C \\ D \\ E \\ F \\ G \\ H \\ I \end{matrix} & \begin{pmatrix} 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 \end{pmatrix} \end{matrix} = m(Y).$$

But a straightforward calculation gives  $\det(m(X)) = 0$  and  $\det(m(Y)) = 27$ . It follows that  $m(X)$  and  $m(Y)$  do not have the same rank and these two configurations are not isomorphic.

**Q3:**



As shown in the figure, the centers of the unit circles are  $(0, 0)$ ,  $(\sqrt{3}, 0)$ ,  $(\frac{\sqrt{3}}{2}, \frac{1}{2})$  and  $(\frac{\sqrt{3}}{2}, \frac{3}{2})$ .

**Q4:**

**Q5:**

**Q6:**

**Q7:**