

(Eigen vector & values

vectors has magnitude and  
<sup>(size)</sup> direction

Magnitude of  $(a, b)$

eigenvalues

$$\| (a, b) \| = \sqrt{a^2 + b^2}$$

Direction  $(a, b)$

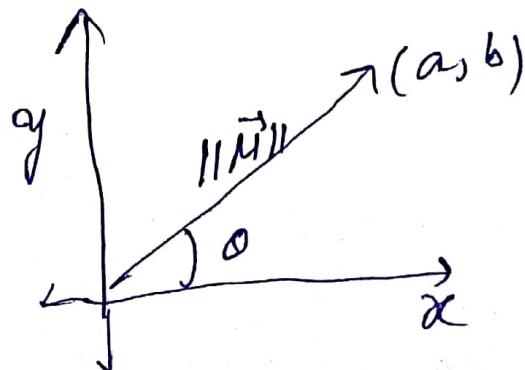
$$\theta = \tan^{-1} \left( \frac{b}{a} \right)$$

Components from magnitude  $\| \vec{u} \|$  and direction

$$(\| \vec{u} \| \cos(\theta), \| \vec{u} \| \sin(\theta))$$

Vectors can be represented in component format.

- \* We can plot vectors on the coordinate plane by drawing a directed line segment from the origin to the point that ~~coordinates~~ corresponds to the vector's components.



- \* Magnitude of a vector  $\vec{v}$  is written as  $\| \vec{v} \|$

$$\Rightarrow \text{Magnitude of } (3, 4) \text{ is } \sqrt{3^2 + 4^2} = \sqrt{25} = 5$$

## Direction from components

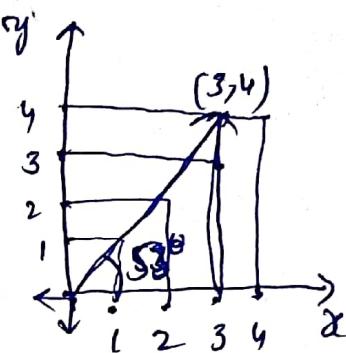
eigen vector

$$\theta \Rightarrow \tan^{-1}\left(\frac{b}{a}\right)$$

① direction of  $(3, 4)$

$$\tan^{-1}\left(\frac{4}{3}\right) \approx 53^\circ$$

Quadrant-I



② quadrant-II,  $(3, -4)$

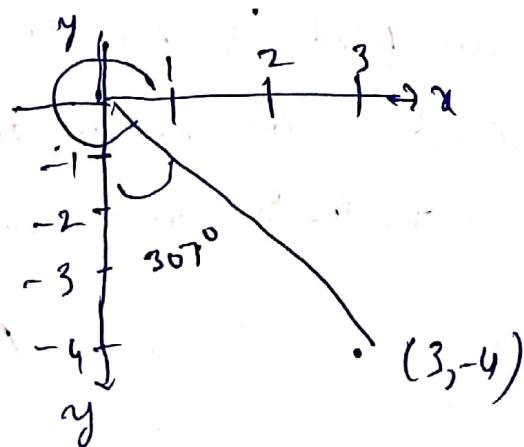
$$\tan^{-1}\left(-\frac{4}{3}\right) \approx -53^\circ$$

the calculator returned negative angle.

But it is common to use positive value for the direction

of a vector, add  $360^\circ$

$$-53 + 360^\circ = 307^\circ$$



③

If the eigen vectors represent the directions for the  
whereas eigenvalues represent the magnitudes  
for the directions.