

$$(c) \quad W \in \mathbb{R}^{d_2 \times d_1} \quad x \in \mathbb{R}^{d_1} \quad Wx = y \quad d_2 \times 1.$$

$$w \in \mathbb{R}^{1 \times d_1} \quad \mathbb{E}(y) = \mathbb{E}(wx) = \mathbb{E}(w) \mathbb{E}(x) = 0.$$

$$\text{Var}(y) = \mathbb{E}(y^2) - \mathbb{E}(y)^2 = \mathbb{E}(w^2 x^2)$$

$$\frac{1}{\sqrt{\frac{1}{d_1} \sum_i x_i^2}} w x$$

$$\text{Var} = \text{Var} \left( \frac{d_1}{\sum_i x_i^2} \left( \sum_i w_i x_i \right)^2 \right) = \frac{d_1^2}{\left( \sum_i x_i^2 \right)^2}$$

$$= d_1^2 \left( \frac{\left( \sum_i w_i x_i \right)^2}{\left( \sum_i x_i^2 \right)^2} \right) = \frac{d_1^2}{d_1} = d_1.$$