MLP Tensorflow

September 16, 2020

0.1 MLP: Initializations

```
[0]: ## MLP: Initializations# https://leonardoaraujosantos.gitbooks.io/
     →artificial-inteligence/content/multi_layer_perceptron_mnist.html
     # https://github.com/wagonhelm/NaNmnist/blob/master/NaNmnist.ipynb
     # https://github.com/aymericdamien/TensorFlow-Examples/blob/master/notebooks/
     →3_NeuralNetworks/neural_network.ipynb
     from tensorflow.examples.tutorials.mnist import input_data
     import tensorflow as tf
     mnist = input_data.read_data_sets("MNIST_data/", one_hot=True)
    WARNING:tensorflow:From <ipython-input-1-0db05428d778>:4: read data_sets (from
    tensorflow.contrib.learn.python.learn.datasets.mnist) is deprecated and will be
    removed in a future version.
    Instructions for updating:
    Please use alternatives such as official/mnist/dataset.py from
    tensorflow/models.
    WARNING:tensorflow:From /usr/local/lib/python3.6/dist-
    packages/tensorflow/contrib/learn/python/learn/datasets/mnist.py:260:
    maybe_download (from tensorflow.contrib.learn.python.learn.datasets.base) is
    deprecated and will be removed in a future version.
    Instructions for updating:
    Please write your own downloading logic.
    WARNING:tensorflow:From /usr/local/lib/python3.6/dist-
    packages/tensorflow/contrib/learn/python/learn/datasets/mnist.py:262:
    extract_images (from tensorflow.contrib.learn.python.learn.datasets.mnist) is
    deprecated and will be removed in a future version.
    Instructions for updating:
    Please use tf.data to implement this functionality.
    Extracting MNIST_data/train-images-idx3-ubyte.gz
    WARNING:tensorflow:From /usr/local/lib/python3.6/dist-
    packages/tensorflow/contrib/learn/python/learn/datasets/mnist.py:267:
    extract_labels (from tensorflow.contrib.learn.python.learn.datasets.mnist) is
    deprecated and will be removed in a future version.
    Instructions for updating:
    Please use tf.data to implement this functionality.
    Extracting MNIST_data/train-labels-idx1-ubyte.gz
```

```
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-
packages/tensorflow/contrib/learn/python/learn/datasets/mnist.py:110:
dense_to_one_hot (from tensorflow.contrib.learn.python.learn.datasets.mnist) is
deprecated and will be removed in a future version.
Instructions for updating:
Please use tf.one_hot on tensors.
Extracting MNIST_data/t10k-images-idx3-ubyte.gz
Extracting MNIST_data/t10k-labels-idx1-ubyte.gz
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-
packages/tensorflow/contrib/learn/python/learn/datasets/mnist.py:290:
DataSet.__init__ (from tensorflow.contrib.learn.python.learn.datasets.mnist) is
deprecated and will be removed in a future version.
Instructions for updating:
Please use alternatives such as official/mnist/dataset.py from
tensorflow/models.

# *mathlotlib notebook*
```

```
[0]: # %matplotlib notebook
import matplotlib.pyplot as plt
import numpy as np
import time
# https://gist.github.com/greydanus/f6eee59eaf1d90fcb3b534a25362cea4
# https://stackoverflow.com/a/14434334
# this function is used to update the plots for each epoch and error
def plt_dynamic(x, y, y_1, ax, ticks,title, colors=['b']):
    ax.plot(x, y, 'b', label="Train Loss")
    ax.plot(x, y_1, 'r', label="Test Loss")
    if len(x)=Fkee=1:
        plt.legend()
        plt.title(title)
    plt.yticks(ticks)
    fig.canvas.draw()
```

```
[0]: # Network Parameters

n_hidden_1 = 512 # 1st layer number of neurons

n_hidden_2 = 128 # 2nd layer number of neurons

n_input = 784 # MNIST data input (img shape: 28*28)

n_classes = 10 # MNIST total classes (0-9 digits)
```

```
# keep_prob: we will be using these placeholders when we use dropouts, while training model

keep_prob_input: we will be using these placeholders when we use dropouts, while training model

keep_prob_input = tf.placeholder(tf.float32)
```

```
[0]: # Weight initialization
     # https://arxiv.org/pdf/1707.09725.pdf#page=95
     # https://www.tensorflow.org/api docs/python/tf/random normal
     # Outputs random values from a normal distribution mean=0 std=1
     # If we sample weights from a normal distribution N(0, ) we satisfy this.
      \rightarrow condition with =\sqrt{(2/(ni+ni+1))}.
     # h1 \Rightarrow =\sqrt{(2/(fan_in+fan_out+1))} = 0.039 \Rightarrow N(0, ) = N(0, 0.039)
     # h2 \Rightarrow =\sqrt{2/(fan \ in+fan \ out+1)} = 0.055 \Rightarrow N(0, ) = N(0, 0.055)
     # out => =\sqrt{(2/(fan_in+fan_out+1))} = 0.120 => N(0, 0.120)
     # SGD: Xavier/Glorot Normal initialization.
     weights_sgd = {
          'h1': tf.Variable(tf.random_normal([n_input, n_hidden_1],stddev=0.039,
      \rightarrowmean=0)),
                    \#784x512 \# sqrt(2/(784+512)) = 0.039
          'h2': tf.Variable(tf.random_normal([n_hidden_1, n_hidden_2],stddev=0.055,_
      \rightarrowmean=0)), #512x128 # sqrt(2/(512+128)) = 0.055
          'out': tf. Variable(tf.random normal([n hidden 2, n classes], stddev=0.120,
      \rightarrowmean=0)) #128x10
     }
     # https://arxiv.org/pdf/1707.09725.pdf#page=95
     # for relu lates
     # If we sample weights from a normal distribution N(0, ) we satisfy this.
     \rightarrow condition with =\sqrt{(2/(ni))}.
     # h1 \Rightarrow =\sqrt{(2/(fan_in+1))} = 0.062 \Rightarrow N(0, ) = N(0, 0.062)
     # h2 \Rightarrow =\sqrt{(2/(fan in+1) = 0.125} => N(0, ) = N(0, 0.125)
     # out => =\sqrt{(2/(fan_in+1))} = 0.120 => N(0, 0.120)
     # He Normal initialization.
     weights_relu = {
          'h1': tf.Variable(tf.random_normal([n_input, n_hidden_1],stddev=0.062,_
                      #784x512
          'h2': tf.Variable(tf.random_normal([n_hidden_1, n_hidden_2],stddev=0.125,__
      \rightarrowmean=0)), #512x128
          'out': tf. Variable(tf.random_normal([n_hidden_2, n_classes],stddev=0.120,__
      \rightarrowmean=0)) #128x10
     }
```

```
biases = {
    'b1': tf.Variable(tf.random_normal([n_hidden_1])), #512x1
    'b2': tf.Variable(tf.random_normal([n_hidden_2])), #128x1
    'out': tf.Variable(tf.random_normal([n_classes])) #10x1
}
```

```
[0]: # Parameters
    training_epochs = 15
    learning_rate = 0.001
    batch_size = 100
    display_step = 1
```

Model 1: input (784) - sigmoid(512) - sigmoid(128) - softmax(output 10)

```
[0]: # https://leonardoaraujosantos.gitbooks.io/artificial-inteligence/content/
     → multi_layer_perceptron_mnist.html
     # Create model
    def multilayer_perceptron(x, weights, biases):
         # Use tf.matmul instead of "*" because tf.matmul can change it's dimensions.
     \rightarrow on the fly (broadcast)
        print( 'x:', x.get_shape(), 'W[h1]:', weights['h1'].get_shape(), 'b[h1]:', u
     →biases['b1'].get shape())
         # Hidden layer with Sigmoid activation
        layer_1 = tf.add(tf.matmul(x, weights['h1']), biases['b1'])__
     \rightarrow#(x*weights['h1']) + biases['b1']
        layer_1 = tf.nn.sigmoid(layer_1)
        print( 'layer_1:', layer_1.get_shape(), 'W[h2]:', weights['h2'].

→get_shape(), 'b[h2]:', biases['b2'].get_shape())
         # Hidden layer with Sigmoid activation
        layer_2 = tf.add(tf.matmul(layer_1, weights['h2']), biases['b2']) #__
     \rightarrow (layer_1 * weights['h2']) + biases['b2']
        layer 2 = tf.nn.sigmoid(layer 2)
        print( 'layer_2:', layer_2.get_shape(), 'W[out]:', weights['out'].
      # Output layer with Sigmoid activation
        out_layer = tf.matmul(layer_2, weights['out']) + biases['out'] # (layer_2 *_
     →weights['out']) + biases['out']
        out_layer = tf.nn.sigmoid(out_layer)
        print('out_layer:',out_layer.get_shape())
        return out_layer
```

 $\underline{\hspace{1cm}}$ Model 1 + AdamOptimizer $\underline{\hspace{1cm}}$

```
[0]: # Since we are using sigmoid activations in hiden layers we will be using.
      →weights that are initalized as weights_sgd
     y_sgd = multilayer_perceptron(x, weights_sgd, biases)
     # https://www.tensorflow.org/api_docs/python/tf/nn/
     ⇒softmax_cross_entropy_with_logits
     cost_sgd = tf.reduce_mean(tf.nn.softmax_cross_entropy_with_logits(logits = ___
      \rightarrowy_sgd, labels = y_))
     # https://qithub.com/amitmac/Question-Answering/issues/2
     # there are many optimizers available: https://www.tensorflow.org/versions/r1.2/
      → api_guides/python/train#Optimizers
     optimizer_adam = tf.train.AdamOptimizer(learning_rate=learning_rate).
     →minimize(cost_sgd)
     optimizer_sgdc = tf.train.GradientDescentOptimizer(learning_rate=learning_rate).
      →minimize(cost_sgd)
     with tf.Session() as sess:
         tf.global_variables_initializer().run()
         fig,ax = plt.subplots(1,1)
         ax.set_xlabel('epoch') ; ax.set_ylabel('Soft Max Cross Entropy loss')
         xs, ytrs, ytes = [], [], []
         for epoch in range(training_epochs):
             train_avg_cost = 0.
             test_avg_cost = 0.
             total batch = int(mnist.train.num examples/batch size)
             # Loop over all batches
             for i in range(total_batch):
                 batch_xs, batch_ys = mnist.train.next_batch(batch_size)
                 # here c: corresponds to the parameter cost_sqd
                 # w : correspondse to the parameter weights_sqd
                 # c = sess.run() return the cost after every bath during train
                 \# w = sess.run() return the weights that are modified after every
      →batch through Back prop
                 # w is dict w = \{ h1': updated h1 weight vector after the current_{11} \}
      \rightarrow batch,
                                   'h2': updated h2 weight vector after the current
      \rightarrow batch,
                                   'out': updated output weight vector after the
      \hookrightarrow current batch,
                 #
                 # you check these w matrix for every iteration, and check whatsu
      → happening during back prop
```

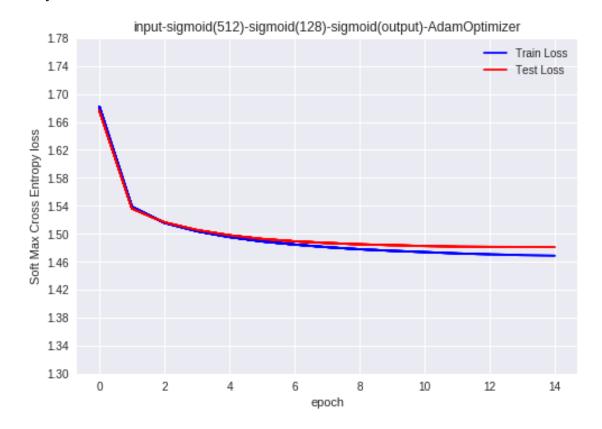
```
# note: sess.run() returns parameter values based on the input_
 \rightarrow parameters
             # _, c, w = sess.run([optimizer_adam, cost_sgd,weights_sgd]) it_
 →returns three parameters
             # _, c = sess.run([optimizer_adam, cost_sqd ]) it returns two___
 \rightarrow parameters
             # _ = sess.run([optimizer_adam]) it returns one paramter (for the_
 → input optimizer it return none)
             \# c = sess.run([cost sqd]) it returns one paramter (for the input
 →cost return error after the batch)
             # feed\_dict=\{x: batch\_xs, y\_: batch\_ys\} here x, y\_ should be
 \rightarrow placeholders
             # x, y are the input parameters on which the models gets trained
             # here we use AdamOptimizer
             _, c, w = sess.run([optimizer_adam, cost_sgd,weights_sgd],_
 →feed_dict={x: batch_xs, y_: batch_ys})
             train avg cost += c / total batch
             c = sess.run(cost_sgd, feed_dict={x: mnist.test.images, y_: mnist.
 →test.labels})
            test_avg_cost += c / total_batch
        xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test_avg_cost)
        plt_dynamic(xs, ytrs, ytes, ax, np.arange(1.3, 1.8, step=0.04),__
 →"input-sigmoid(512)-sigmoid(128)-sigmoid(output)-AdamOptimizer")
        if epoch%display_step == 0:
             print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 -format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    plt dynamic(xs, ytrs, ytes, ax, np.arange(1.3, 1.8, step=0.04),
 →"input-sigmoid(512)-sigmoid(128)-sigmoid(output)-AdamOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(y_sgd,1), tf.argmax(y_,1))
    accuracy = tf.reduce mean(tf.cast(correct_prediction, tf.float32))
    print("Accuracy:", accuracy.eval({x: mnist.test.images, y: mnist.test.
 →labels}))
x: (?, 784) W[h1]: (784, 512) b[h1]: (512,)
layer_1: (?, 512) W[h2]: (512, 128) b[h2]: (128,)
layer_2: (?, 128) W[out]: (128, 10) b3: (10,)
out_layer: (?, 10)
WARNING:tensorflow:From <ipython-input-8-743a1d69c459>:4:
softmax_cross_entropy_with_logits (from tensorflow.python.ops.nn_ops) is
```

deprecated and will be removed in a future version. Instructions for updating:

Future major versions of TensorFlow will allow gradients to flow into the labels input on backprop by default.

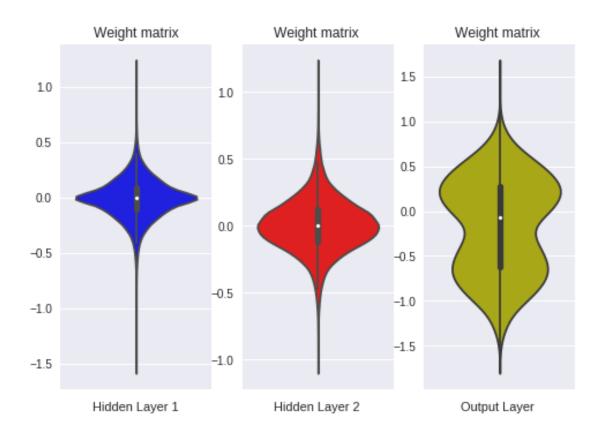
See tf.nn.softmax_cross_entropy_with_logits_v2.

Epoch: 0001 train cost=1.681823547 test cost=1.676311211 Epoch: 0002 train cost=1.538490382 test cost=1.536218471 Epoch: 0003 train cost=1.515721546 test cost=1.516237581 Epoch: 0004 train cost=1.503663794 test cost=1.505241357 Epoch: 0005 train cost=1.495330883 test cost=1.497797373 Epoch: 0006 train cost=1.489064606 test cost=1.492622907 Epoch: 0007 train cost=1.484618232 test cost=1.489168651 Epoch: 0008 train cost=1.480839387 test cost=1.486846633 Epoch: 0009 train cost=1.477865693 test cost=1.484905369 Epoch: 0010 train cost=1.475599988 test cost=1.483736856 Epoch: 0011 train cost=1.473791684 test cost=1.482444747 Epoch: 0012 train cost=1.471931230 test cost=1.481658286 Epoch: 0013 train cost=1.470603549 test cost=1.481347544 Epoch: 0014 train cost=1.469495951 test cost=1.481273373 Epoch: 0015 train cost=1.468627278 test cost=1.480902303 Accuracy: 0.9792



```
[0]: # Plot weight distribution at the end of training.
     import seaborn as sns
     h1_w = w['h1'].flatten().reshape(-1,1)
     h2_w = w['h2'].flatten().reshape(-1,1)
     out_w = w['out'].flatten().reshape(-1,1)
     fig = plt.figure()
     plt.subplot(1, 3, 1)
     plt.title("Weight matrix")
     ax = sns.violinplot(y=h1_w,color='b')
     plt.xlabel('Hidden Layer 1')
     plt.subplot(1, 3, 2)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=h2_w, color='r')
     plt.xlabel('Hidden Layer 2 ')
     plt.subplot(1, 3, 3)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=out w,color='y')
     plt.xlabel('Output Layer ')
     plt.show()
```

```
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:588:
FutureWarning: remove_na is deprecated and is a private function. Do not use.
  kde_data = remove_na(group_data)
/usr/local/lib/python3.6/dist-packages/seaborn/categorical.py:816:
FutureWarning: remove_na is deprecated and is a private function. Do not use.
  violin_data = remove_na(group_data)
```

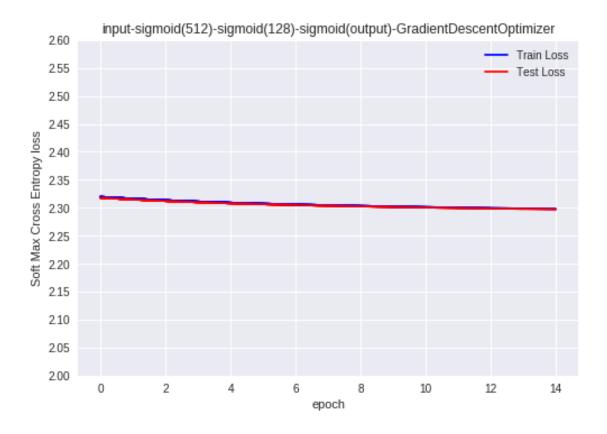


Model 1 + GradientDescentOptimizer

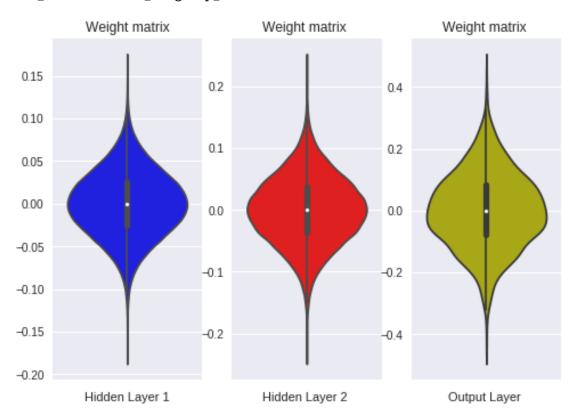
```
[0]: # We can now launch the model in an InteractiveSession
     # We first have to create an operation to initialize the variables we created:
     # https://github.com/amitmac/Question-Answering/issues/2
     # Note: make sure you initialize variables.
     with tf.Session() as sess:
         tf.global_variables_initializer().run()
         fig,ax = plt.subplots(1,1)
         ax.set_xlabel('epoch') ; ax.set_ylabel('Soft Max Cross Entropy loss')
         xs, ytrs, ytes = [], [], []
         for epoch in range(training_epochs):
             train_avg_cost = 0.
             test_avg_cost = 0.
             total_batch = int(mnist.train.num_examples/batch_size)
             # Loop over all batches
             for i in range(total_batch):
                 batch_xs, batch_ys = mnist.train.next_batch(batch_size)
```

```
# here we use GradientDescentOptimizer
             _, c, w = sess.run([optimizer_sgdc, cost_sgd, weights_sgd],__
 →feed_dict={x: batch_xs, y_: batch_ys})
            train_avg_cost += c / total_batch
            c = sess.run(cost sgd, feed dict={x: mnist.test.images, y : mnist.
 →test.labels})
            test_avg_cost += c / total_batch
        xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test avg cost)
        plt_dynamic(xs, ytrs, ytes, ax, np.arange(2, 2.6, step=0.05),_
 →"input-sigmoid(512)-sigmoid(128)-sigmoid(output)-GradientDescentOptimizer")
        if epoch%display step == 0:
            print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 →format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    plt_dynamic(xs, ytrs, ytes, ax, np.arange(2, 2.6, step=0.05),__
 →"input-sigmoid(512)-sigmoid(128)-sigmoid(output)-GradientDescentOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(y_sgd,1), tf.argmax(y_,1))
    accuracy = tf.reduce mean(tf.cast(correct_prediction, tf.float32))
    print("Accuracy:", accuracy.eval({x: mnist.test.images, y_: mnist.test.
 →labels}))
Epoch: 0001 train cost=2.319404572 test cost=2.318047826
```

```
Epoch: 0001 train cost=2.319404572 test cost=2.318047826 Epoch: 0002 train cost=2.316184991 test cost=2.314944556 Epoch: 0003 train cost=2.313415619 test cost=2.312310369 Epoch: 0004 train cost=2.311047141 test cost=2.310042647 Epoch: 0005 train cost=2.309026067 test cost=2.308095952 Epoch: 0006 train cost=2.307287374 test cost=2.306472156 Epoch: 0007 train cost=2.305776415 test cost=2.305014431 Epoch: 0008 train cost=2.304444027 test cost=2.303744715 Epoch: 0009 train cost=2.303249972 test cost=2.302621931 Epoch: 0010 train cost=2.302166392 test cost=2.301561712 Epoch: 0011 train cost=2.301172580 test cost=2.301561712 Epoch: 0012 train cost=2.300254010 test cost=2.299707088 Epoch: 0013 train cost=2.299401874 test cost=2.298892814 Epoch: 0014 train cost=2.298614489 test cost=2.298106769 Epoch: 0015 train cost=2.297889533 test cost=2.297402518 Accuracy: 0.0974
```



```
[0]: h1_w = w['h1'].flatten().reshape(-1,1)
     h2_w = w['h2'].flatten().reshape(-1,1)
     out_w = w['out'].flatten().reshape(-1,1)
     fig = plt.figure()
     plt.subplot(1, 3, 1)
     plt.title("Weight matrix")
     ax = sns.violinplot(y=h1_w,color='b')
     plt.xlabel('Hidden Layer 1')
     plt.subplot(1, 3, 2)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=h2_w, color='r')
     plt.xlabel('Hidden Layer 2 ')
     plt.subplot(1, 3, 3)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=out_w,color='y')
     plt.xlabel('Output Layer ')
     plt.show()
```



Model 2: input (784) - ReLu(512) - ReLu(128) - sigmoid(output 10)

Input-ReLu(512)-ReLu(128)-sigmoid(output) - AdamOptimizer ____

```
[0]: # Since we are using Relu activations in hiden layers we will be using weights.
     → that are initalized as weights_relu
     yrelu = multilayer_perceptron_relu(x, weights_relu, biases)
     # https://www.tensorflow.org/api_docs/python/tf/nn/
     \hookrightarrow softmax_cross_entropy_with_logits
     cost_relu = tf.reduce_mean(tf.nn.softmax_cross_entropy_with_logits(logits =_
     # https://qithub.com/amitmac/Question-Answering/issues/2
     # there are many optimizers available: https://www.tensorflow.org/versions/r1.2/
     \rightarrow api_guides/python/train#Optimizers
     optimizer relu adam = tf.train.AdamOptimizer(learning rate=learning rate).
     →minimize(cost_relu)
     optimizer_relu_sgdc = tf.train.
     →GradientDescentOptimizer(learning_rate=learning_rate).minimize(cost_relu)
     with tf.Session() as sess:
         tf.global_variables_initializer().run()
         fig,ax = plt.subplots(1,1)
         ax.set_xlabel('epoch') ; ax.set_ylabel('Soft Max Cross Entropy loss')
         xs, ytrs, ytes = [], [], []
         for epoch in range(training_epochs):
            train_avg_cost = 0.
            test_avg_cost = 0.
             total_batch = int(mnist.train.num_examples/batch_size)
```

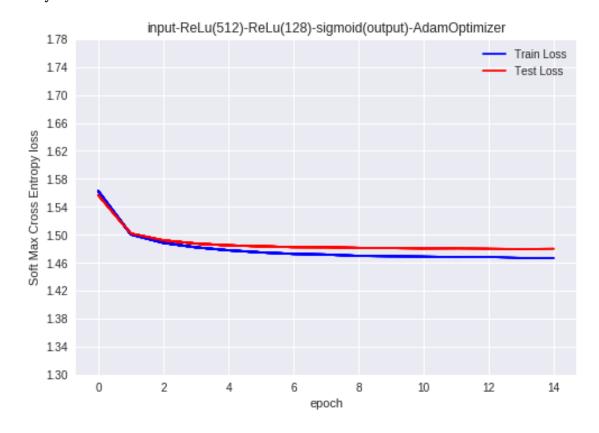
```
# Loop over all batches
        for i in range(total_batch):
            batch_xs, batch_ys = mnist.train.next_batch(batch_size)
            # here we use AdamOptimizer
            _, c, w = sess.run([optimizer_relu_adam, cost_relu, weights_relu],_
 →feed_dict={x: batch_xs, y_: batch_ys})
            train_avg_cost += c / total_batch
            c = sess.run(cost_relu, feed_dict={x: mnist.test.images, y_: mnist.
 →test.labels})
            test_avg_cost += c / total_batch
        xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test_avg_cost)
        plt_dynamic(xs, ytrs, ytes, ax, np.arange(1.3, 1.8, step=0.04),__

¬"input-ReLu(512)-ReLu(128)-sigmoid(output)-AdamOptimizer")

        if epoch%display_step == 0:
            print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 →format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    # plot final results
    plt_dynamic(xs, ytrs, ytes, ax,np.arange(1.3, 1.8, step=0.04),__

¬"input-ReLu(512)-ReLu(128)-sigmoid(output)-AdamOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(yrelu,1), tf.argmax(y_,1))
    accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
    print("Accuracy:", accuracy.eval({x: mnist.test.images, y_: mnist.test.
 →labels}))
x: (?, 784) W[h1]: (784, 512) b[h1]: (512,)
layer_1: (?, 512) W[h2]: (512, 128) b[h2]: (128,)
layer_2: (?, 128) W[out]: (128, 10) b3: (10,)
out_layer: (?, 10)
Epoch: 0001 train cost=1.562207396 test cost=1.556652784
Epoch: 0002 train cost=1.500463881 test cost=1.501601754
Epoch: 0003 train cost=1.488371294 test cost=1.492026712
Epoch: 0004 train cost=1.482039372 test cost=1.487420058
Epoch: 0005 train cost=1.477783545 test cost=1.484849013
Epoch: 0006 train cost=1.474736516 test cost=1.483547766
Epoch: 0007 train cost=1.472646466 test cost=1.482295828
Epoch: 0008 train cost=1.471696293 test cost=1.482177148
Epoch: 0009 train cost=1.469835149 test cost=1.481312513
Epoch: 0010 train cost=1.469276900 test cost=1.480974347
```

Epoch: 0011 train cost=1.468788507 test cost=1.480446307 Epoch: 0012 train cost=1.468029417 test cost=1.480591303 Epoch: 0013 train cost=1.468475725 test cost=1.480107398 Epoch: 0014 train cost=1.466739849 test cost=1.479299975 Epoch: 0015 train cost=1.466718120 test cost=1.480001667 Accuracy: 0.9785

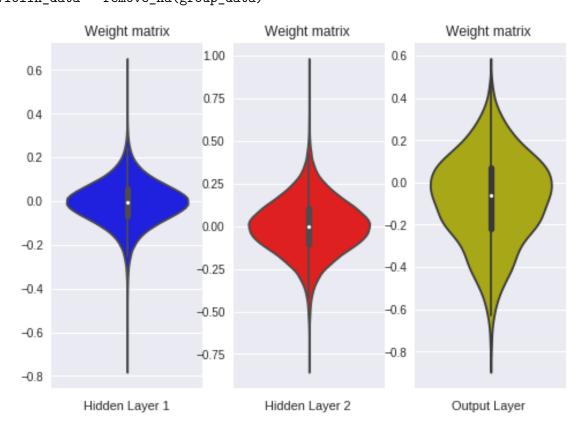


```
[0]: h1_w = w['h1'].flatten().reshape(-1,1)
h2_w = w['h2'].flatten().reshape(-1,1)
out_w = w['out'].flatten().reshape(-1,1)

fig = plt.figure()
plt.subplot(1, 3, 1)
plt.title("Weight matrix")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')

plt.subplot(1, 3, 2)
plt.title("Weight matrix ")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')
```

```
plt.subplot(1, 3, 3)
plt.title("Weight matrix ")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```



Input-ReLu(512)-ReLu(128)-sigmoid(output) - GradientDescentOptimizer

```
[0]: # We can now launch the model in an InteractiveSession

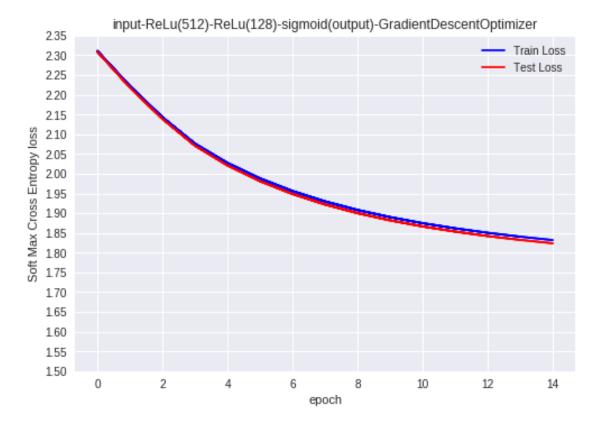
# We first have to create an operation to initialize the variables we created:
# https://github.com/amitmac/Question-Answering/issues/2

# Note: make sure you initialize variables after AdamOptimizer
```

```
with tf.Session() as sess:
   tf.global_variables_initializer().run()
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Soft Max Cross Entropy loss')
   xs, ytrs, ytes = [], [], []
   for epoch in range(training_epochs):
       train_avg_cost = 0.
       test avg cost = 0.
       total_batch = int(mnist.train.num_examples/batch_size)
        # Loop over all batches
        for i in range(total_batch):
            batch_xs, batch_ys = mnist.train.next_batch(batch_size)
            # here we use GradientDescentOptimizer
            _, c, w = sess.run([optimizer_relu_sgdc, cost_relu, weights_relu],_
 →feed_dict={x: batch_xs, y_: batch_ys})
            train avg cost += c / total batch
            c = sess.run(cost_relu, feed_dict={x: mnist.test.images, y_: mnist.
 →test.labels})
            test_avg_cost += c / total_batch
       xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test_avg_cost)
       plt_dynamic(xs, ytrs, ytes, ax, np.arange(1.5, 2.4, step=0.05),
→"input-ReLu(512)-ReLu(128)-sigmoid(output)-GradientDescentOptimizer")
        if epoch%display_step == 0:
            print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 →format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    # plot final results
   plt dynamic(xs, ytrs, ytes, ax, np.arange(1.5, 2.4, step=0.05),
→"input-ReLu(512)-ReLu(128)-sigmoid(output)-GradientDescentOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(yrelu,1), tf.argmax(y_,1))
    accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
   print("Accuracy:", accuracy.eval({x: mnist.test.images, y: mnist.test.
 →labels}))
```

Epoch: 0001 train cost=2.310429324 test cost=2.309331124 Epoch: 0002 train cost=2.221610156 test cost=2.218818418 Epoch: 0003 train cost=2.142771041 test cost=2.139230260 Epoch: 0004 train cost=2.075905863 test cost=2.071342851

```
Epoch: 0005 train cost=2.027072112 test cost=2.021270330 Epoch: 0006 train cost=1.987932869 test cost=1.981295761 Epoch: 0007 train cost=1.956008127 test cost=1.948708092 Epoch: 0008 train cost=1.929796880 test cost=1.922126883 Epoch: 0009 train cost=1.908102709 test cost=1.900147488 Epoch: 0010 train cost=1.889981364 test cost=1.881854080 Epoch: 0011 train cost=1.874673119 test cost=1.866476579 Epoch: 0012 train cost=1.861609627 test cost=1.853379037 Epoch: 0013 train cost=1.850336982 test cost=1.842097878 Epoch: 0014 train cost=1.840515356 test cost=1.832302262 Epoch: 0015 train cost=1.831871038 test cost=1.823694615 Accuracy: 0.1066
```



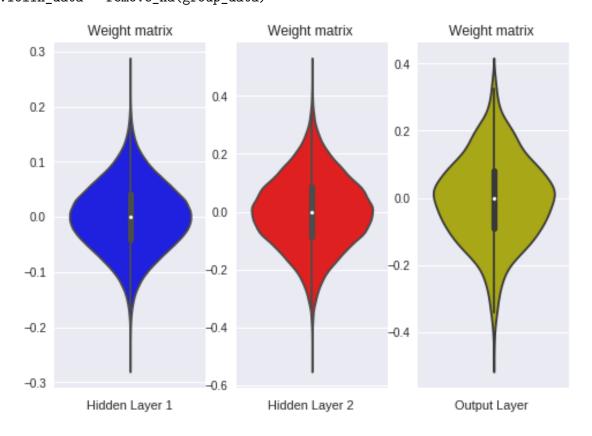
```
[0]: h1_w = w['h1'].flatten().reshape(-1,1)
h2_w = w['h2'].flatten().reshape(-1,1)
out_w = w['out'].flatten().reshape(-1,1)

fig = plt.figure()
plt.subplot(1, 3, 1)
plt.title("Weight matrix")
ax = sns.violinplot(y=h1_w,color='b')
```

```
plt.xlabel('Hidden Layer 1')

plt.subplot(1, 3, 2)
plt.title("Weight matrix ")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')

plt.subplot(1, 3, 3)
plt.title("Weight matrix ")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
plt.show()
```



 $\label{eq:model} \mbox{Model 3: Input - Sigmoid(BatchNormalization(512)) - Sigmoid(BatchNormalization(128))- Sigmoid(output)} \\$

```
[0]: # https://www.tensorflow.org/api_docs/python/tf/nn/batch_normalization
    \# \ https://r2rt.com/implementing-batch-normalization-in-tensorflow.html
    epsilon = 1e-3
    def multilayer_perceptron_batch(x, weights, biases):
        # Use tf.matmul instead of "*" because tf.matmul can change it's dimensions.
     \rightarrow on the fly (broadcast)
        print( 'x:', x.get_shape(), 'W[h1]:', weights['h1'].get_shape(), 'b[h1]:', u
     →biases['b1'].get_shape())
        # Hidden layer with Sigmoid activation and batch normalization
        layer_1 = tf.add(tf.matmul(x, weights['h1']), biases['b1'])__
     \rightarrow#(x*weights['h1']) + biases['b1']
        # https://www.tensorflow.org/api_docs/python/tf/nn/moments
        # Calculate the mean and variance of x.
        batch_mean_1, batch_var_1 = tf.nn.moments(layer_1,[0])
        scale_1 = tf.Variable(tf.ones([n_hidden_1]))
        beta_1 = tf.Variable(tf.zeros([n_hidden_1]))
        # https://www.tensorflow.org/api_docs/python/tf/nn/batch_normalization
        layer_1 = tf.nn.batch_normalization(layer_1, batch_mean_1, batch_var_1,__
     →beta_1, scale_1, epsilon)
        layer_1 = tf.nn.sigmoid(layer_1)
        print( 'layer_1:', layer_1.get_shape(), 'W[h2]:', weights['h2'].

¬get_shape(), 'b[h2]:', biases['b2'].get_shape())
     # Hidden layer with Sigmoid activation and batch normalization
        layer_2 = tf.add(tf.matmul(layer_1, weights['h2']), biases['b2']) #__
     \hookrightarrow (layer_1 * weights['h2']) + biases['b2']
        {\it \# https://www.tensorflow.org/api\_docs/python/tf/nn/moments}
        # Calculate the mean and variance of x.
        batch_mean_2, batch_var_2 = tf.nn.moments(layer_2, [0])
        scale_2 = tf.Variable(tf.ones([n_hidden_2]))
        beta_2 = tf.Variable(tf.zeros([n_hidden_2]))
        layer_2 = tf.nn.batch_normalization(layer_2, batch_mean_2, batch_var_2,_u
     →beta_2, scale_2, epsilon)
        layer_2 = tf.nn.sigmoid(layer_2)
```

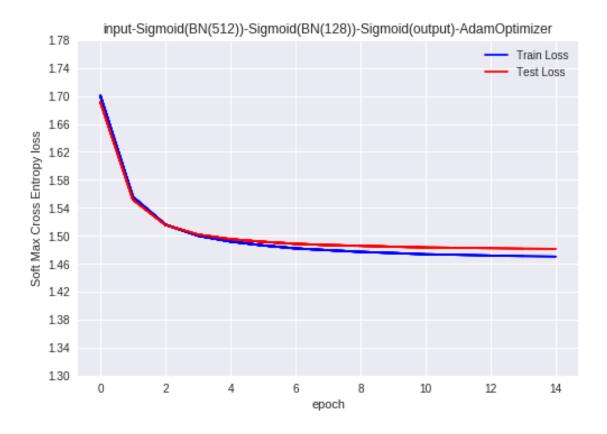
___ Model 3+ AdamOptimizer ___

```
[0]: # Since we are using sigmoid activations in hiden layers we will be using.
     →weights that are initalized as weights_sqd
     ybatch = multilayer_perceptron_batch(x, weights_sgd, biases)
     # https://www.tensorflow.org/api_docs/python/tf/nn/
     ⇒softmax_cross_entropy_with_logits
     cost_batch = tf.reduce_mean(tf.nn.softmax_cross_entropy_with_logits(logits = __
     →ybatch, labels = y_))
     # https://github.com/amitmac/Question-Answering/issues/2
     # there are many optimizers available: https://www.tensorflow.org/versions/r1.2/
     → api_quides/python/train#Optimizers
     optimizer_batch_adam = tf.train.AdamOptimizer(learning_rate=learning_rate).
     →minimize(cost_batch)
     optimizer batch sgdc = tf.train.
     → GradientDescentOptimizer(learning rate=learning rate).minimize(cost batch)
     with tf.Session() as sess:
         tf.global_variables_initializer().run()
         fig,ax = plt.subplots(1,1)
         ax.set_xlabel('epoch') ; ax.set_ylabel('Soft Max Cross Entropy loss')
         xs, ytrs, ytes = [], [], []
         for epoch in range(training_epochs):
            train_avg_cost = 0.
            test avg cost = 0.
            total_batch = int(mnist.train.num_examples/batch_size)
             # Loop over all batches
             for i in range(total_batch):
                 batch_xs, batch_ys = mnist.train.next_batch(batch_size)
                 # here we use AdamOptimizer
```

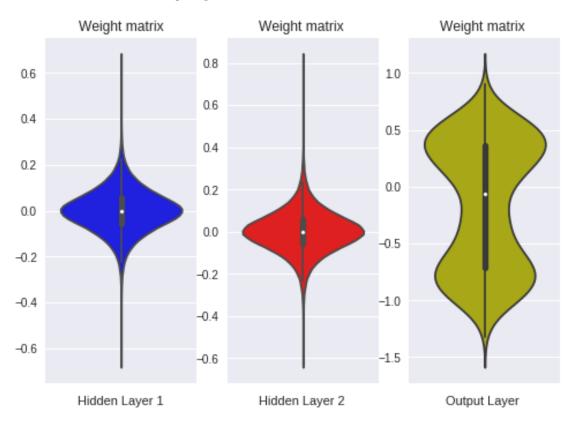
```
_, c, w = sess.run([optimizer_batch_adam, cost_batch, weights_sgd],__

→feed_dict={x: batch_xs, y_: batch_ys})
            train_avg_cost += c / total_batch
            c = sess.run(cost batch, feed dict={x: mnist.test.images, y : mnist.
 →test.labels})
            test_avg_cost += c / total_batch
        xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test_avg_cost)
        plt_dynamic(xs, ytrs, ytes, ax, np.arange(1.3, 1.8, step=0.04),__
 →"input-Sigmoid(BN(512))-Sigmoid(BN(128))-Sigmoid(output)-AdamOptimizer")
        if epoch%display_step == 0:
            print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 →format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    # plot final results
    plt_dynamic(xs, ytrs, ytes, ax, np.arange(1.3, 1.8, step=0.04),__
 →"input-Sigmoid(BN(512))-Sigmoid(BN(128))-Sigmoid(output)-AdamOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(ybatch,1), tf.argmax(y_,1))
    accuracy = tf.reduce mean(tf.cast(correct_prediction, tf.float32))
    print("Accuracy:", accuracy.eval({x: mnist.test.images, y_: mnist.test.
 →labels}))
x: (?, 784) W[h1]: (784, 512) b[h1]: (512,)
layer_1: (?, 512) W[h2]: (512, 128) b[h2]: (128,)
layer_2: (?, 128) W[out]: (128, 10) b3: (10,)
out_layer: (?, 10)
Epoch: 0001 train cost=1.700068553 test cost=1.691480070
Epoch: 0002 train cost=1.555593932 test cost=1.551793572
Epoch: 0003 train cost=1.515948518 test cost=1.515595129
Epoch: 0004 train cost=1.500090736 test cost=1.501608725
Epoch: 0005 train cost=1.491691740 test cost=1.495176234
Epoch: 0006 train cost=1.486215817 test cost=1.491377480
Epoch: 0007 train cost=1.481944979 test cost=1.488477005
Epoch: 0008 train cost=1.479413016 test cost=1.486683784
Epoch: 0009 train cost=1.476976019 test cost=1.485592169
Epoch: 0010 train cost=1.475328626 test cost=1.484361933
Epoch: 0011 train cost=1.473508603 test cost=1.483245888
Epoch: 0012 train cost=1.472790788 test cost=1.482792196
Epoch: 0013 train cost=1.471692099 test cost=1.482280265
Epoch: 0014 train cost=1.470980778 test cost=1.481615747
Epoch: 0015 train cost=1.470204555 test cost=1.481264244
```

Accuracy: 0.9811



```
[0]: h1_w = w['h1'].flatten().reshape(-1,1)
     h2_w = w['h2'].flatten().reshape(-1,1)
     out_w = w['out'].flatten().reshape(-1,1)
     fig = plt.figure()
     plt.subplot(1, 3, 1)
     plt.title("Weight matrix")
     ax = sns.violinplot(y=h1_w,color='b')
     plt.xlabel('Hidden Layer 1')
     plt.subplot(1, 3, 2)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=h2_w, color='r')
     plt.xlabel('Hidden Layer 2 ')
     plt.subplot(1, 3, 3)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=out_w,color='y')
     plt.xlabel('Output Layer ')
     plt.show()
```

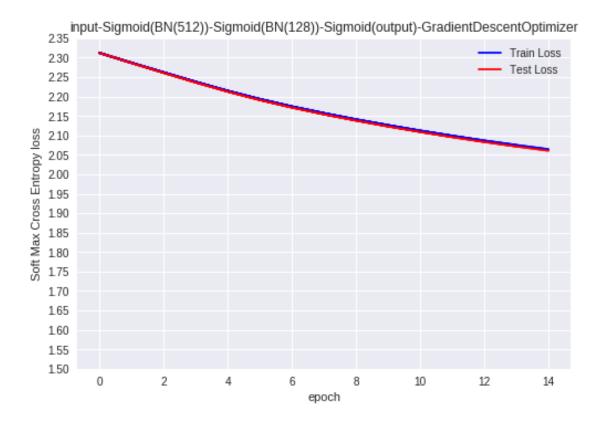


$_$ Model 3 + GradientDescentOptimizer $_$

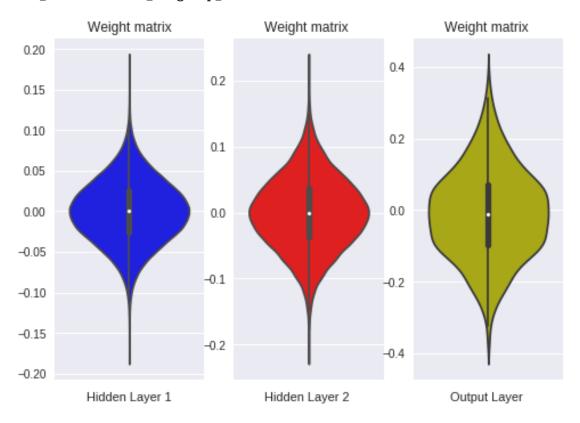
```
[0]: with tf.Session() as sess:
    tf.global_variables_initializer().run()
    fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch') ; ax.set_ylabel('Soft Max Cross Entropy loss')
    xs, ytrs, ytes = [], [], []
    for epoch in range(training_epochs):
        train_avg_cost = 0.
        test_avg_cost = 0.
        total_batch = int(mnist.train.num_examples/batch_size)

# Loop over all batches
    for i in range(total_batch):
        batch_xs, batch_ys = mnist.train.next_batch(batch_size)
```

```
# here we use GradientDescentOptimizer
             _, c, w = sess.run([optimizer_batch_sgdc, cost_batch, weights_sgd],_
 →feed_dict={x: batch_xs, y_: batch_ys})
            train_avg_cost += c / total_batch
            c = sess.run(cost batch, feed dict={x: mnist.test.images, y : mnist.
 →test.labels})
            test_avg_cost += c / total_batch
        xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test avg cost)
        plt_dynamic(xs, ytrs, ytes, ax,np.arange(1.5, 2.4, step=0.05),__
 →"input-Sigmoid(BN(512))-Sigmoid(BN(128))-Sigmoid(output)-GradientDescentOptimizer")
        if epoch%display step == 0:
            print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 →format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    # plot final results
    plt_dynamic(xs, ytrs, ytes, ax, np.arange(1.5, 2.4, step=0.05),_
 →"input-Sigmoid(BN(512))-Sigmoid(BN(128))-Sigmoid(output)-GradientDescentOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(ybatch,1), tf.argmax(y_,1))
    accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
    print("Accuracy:", accuracy.eval({x: mnist.test.images, y_: mnist.test.
 →labels}))
Epoch: 0001 train cost=2.312056991 test cost=2.312045197
Epoch: 0002 train cost=2.286723345 test cost=2.286289722
Epoch: 0003 train cost=2.262095340 test cost=2.261143614
Epoch: 0004 train cost=2.237721429 test cost=2.236359837
Epoch: 0005 train cost=2.214522683 test cost=2.212769454
Epoch: 0006 train cost=2.193412623 test cost=2.191231863
Epoch: 0007 train cost=2.174389078 test cost=2.171921795
Epoch: 0008 train cost=2.157141389 test cost=2.154426692
Epoch: 0009 train cost=2.141131058 test cost=2.138286440
Epoch: 0010 train cost=2.126325870 test cost=2.123236751
Epoch: 0011 train cost=2.112224244 test cost=2.109058378
Epoch: 0012 train cost=2.099121217 test cost=2.095732109
Epoch: 0013 train cost=2.086694297 test cost=2.083267775
Epoch: 0014 train cost=2.075242446 test cost=2.071594143
Epoch: 0015 train cost=2.064474456 test cost=2.060690631
Accuracy: 0.125
```



```
[0]: h1_w = w['h1'].flatten().reshape(-1,1)
     h2_w = w['h2'].flatten().reshape(-1,1)
     out_w = w['out'].flatten().reshape(-1,1)
     fig = plt.figure()
     plt.subplot(1, 3, 1)
     plt.title("Weight matrix")
     ax = sns.violinplot(y=h1_w,color='b')
     plt.xlabel('Hidden Layer 1')
     plt.subplot(1, 3, 2)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=h2_w, color='r')
     plt.xlabel('Hidden Layer 2 ')
     plt.subplot(1, 3, 3)
     plt.title("Weight matrix ")
     ax = sns.violinplot(y=out_w,color='y')
     plt.xlabel('Output Layer ')
     plt.show()
```



 $\label{eq:model 4: Input - ReLu(512) - Dropout - ReLu(128) - Dropout - Sigmoid(output)} \\$

```
layer_1 = tf.add(tf.matmul(x, weights['h1']), biases['b1'])__
\rightarrow#(x*weights['h1']) + biases['b1']
   layer_1 = tf.nn.relu(layer_1)
   # we are adding a drop out layer after the first hidden layer with parameter_
\rightarrow keep\_prob
   layer_1_drop = tf.nn.dropout(layer_1, keep_prob)
   print( 'layer_1:', layer_1.get_shape(), 'W[h2]:', weights['h2'].

¬get_shape(), 'b[h2]:', biases['b2'].get_shape())
   # Hidden layer with ReLu activation
   layer_2 = tf.add(tf.matmul(layer_1_drop, weights['h2']), biases['b2']) #__
\rightarrow (layer_1 * weights['h2']) + biases['b2']
   layer 2 = tf.nn.relu(layer 2)
   # we are adding a drop out layer after the first hidden layer with parameter_

→ keep_prob

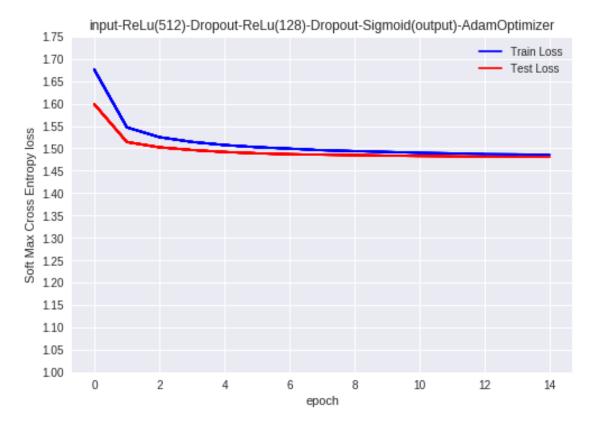
   layer_2_drop = tf.nn.dropout(layer_2, keep_prob)
   print( 'layer_2:', layer_2.get_shape(), 'W[out]:', weights['out'].

→get_shape(), 'b3:', biases['out'].get_shape())
   # Output layer with Sigmoid activation
   out_layer = tf.matmul(layer_2_drop, weights['out']) + biases['out'] #__
→(layer_2 * weights['out']) + biases['out']
   out_layer = tf.nn.sigmoid(out_layer)
   print('out_layer:',out_layer.get_shape())
   return out_layer
```

$_$ Model 4 + AdamOptimizer $_$

```
with tf.Session() as sess:
    tf.global variables initializer().run()
    fig,ax = plt.subplots(1,1)
    ax.set_xlabel('epoch') ; ax.set_ylabel('Soft Max Cross Entropy loss')
    xs, ytrs, ytes = [], [], []
    for epoch in range(training_epochs):
        train_avg_cost = 0.
        test_avg_cost = 0.
        total batch = int(mnist.train.num examples/batch size)
        # Loop over all batches
        for i in range(total_batch):
            batch_xs, batch_ys = mnist.train.next_batch(batch_size)
            # here we use AdamOptimizer
            _, c, w = sess.run([optimizer_drop_adam, cost_drop, weights_relu],_
 →feed_dict={x: batch_xs, y_: batch_ys, keep_prob: 0.5})
            train_avg_cost += c / total_batch
            c = sess.run(cost_drop, feed_dict={x: mnist.test.images, y_: mnist.
 →test.labels, keep_prob: 1.0})
            test_avg_cost += c / total_batch
        xs.append(epoch)
        ytrs.append(train_avg_cost)
        ytes.append(test_avg_cost)
        plt_dynamic(xs, ytrs, ytes, ax,np.arange(1, 1.8, step=0.05),__
 →"input-ReLu(512)-Dropout-ReLu(128)-Dropout-Sigmoid(output)-AdamOptimizer")
        if epoch%display_step == 0:
            print("Epoch:", '%04d' % (epoch+1), "train cost={:.9f}".
 →format(train_avg_cost), "test cost={:.9f}".format(test_avg_cost))
    # plot final results
    plt_dynamic(xs, ytrs, ytes, ax,np.arange(1, 1.8, step=0.05),__
 →"input-ReLu(512)-Dropout-ReLu(128)-Dropout-Sigmoid(output)-AdamOptimizer")
    # we are calculating the final accuracy on the test data
    correct_prediction = tf.equal(tf.argmax(ydrop,1), tf.argmax(y_,1))
    accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
    print("Accuracy:", accuracy.eval({x: mnist.test.images, y: mnist.test.
 →labels, keep_prob: 1.0 }))
x: (?, 784) W[h1]: (784, 512) b[h1]: (512,)
layer_1: (?, 512) W[h2]: (512, 128) b[h2]: (128,)
layer_2: (?, 128) W[out]: (128, 10) b3: (10,)
out_layer: (?, 10)
Epoch: 0001 train cost=1.675481348 test cost=1.598583966
```

```
Epoch: 0002 train cost=1.546939785 test cost=1.514125155 Epoch: 0003 train cost=1.524996623 test cost=1.502378711 Epoch: 0004 train cost=1.514395935 test cost=1.496348261 Epoch: 0005 train cost=1.507464443 test cost=1.491901992 Epoch: 0006 train cost=1.502681051 test cost=1.488922666 Epoch: 0007 train cost=1.499395829 test cost=1.486873763 Epoch: 0008 train cost=1.495856912 test cost=1.485843970 Epoch: 0009 train cost=1.493913886 test cost=1.484971796 Epoch: 0010 train cost=1.491971510 test cost=1.483862281 Epoch: 0011 train cost=1.490074936 test cost=1.482910818 Epoch: 0012 train cost=1.488904240 test cost=1.482207586 Epoch: 0013 train cost=1.487357789 test cost=1.481696167 Epoch: 0014 train cost=1.486711373 test cost=1.480950590 Epoch: 0015 train cost=1.485781125 test cost=1.480801912 Accuracy: 0.9736
```



```
[0]: h1_w = w['h1'].flatten().reshape(-1,1)
h2_w = w['h2'].flatten().reshape(-1,1)
out_w = w['out'].flatten().reshape(-1,1)
fig = plt.figure()
```

```
plt.subplot(1, 3, 1)
plt.title("Weight matrix")
ax = sns.violinplot(y=h1_w,color='b')
plt.xlabel('Hidden Layer 1')

plt.subplot(1, 3, 2)
plt.title("Weight matrix ")
ax = sns.violinplot(y=h2_w, color='r')
plt.xlabel('Hidden Layer 2 ')

plt.subplot(1, 3, 3)
plt.title("Weight matrix ")
ax = sns.violinplot(y=out_w,color='y')
plt.xlabel('Output Layer ')
# plt.show()
```

[0]: Text(0.5,0,'Output Layer ')

