#### **Kinematics** Unit 2

#### 1. What is Mechanics?

Mechanics is the branch of physics that deals with the **motion** of objects and the **forces** that change it.

#### 2. What are the branches of Mechanics?

Mechanics is generally divided into two branches:

**Kinematics** – The study of motion without referring to forces.

### **Dynamics** – The study of forces and their effect on motion.

### \*\* 3. Define scalar and vector quantities. Give 5 examples each for scalar and vector quantities.

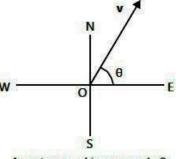
Scalar Quantity	Vector Quantity
A scalar is that physical quantity which can be described completely by its magnitude only.	A vector is that physical quantity which needs magnitude as well as direction to describe it completely.
Examples of scalers are distance, length, time, speed, energy, temperature.	Examples of vectors are displacement, velocity, acceleration, weight, force.
For example, mass of sugar (5 kg) is completely described by its magnitude.  Scalars can be added like numbers (e.g., 5 m + 3 m =	For example, velocity of a car $(25 ms^{-1})$ towards north) needs both magnitude and direction.  Vectors cannot be added like scalars; their
8 m).	directions must be considered.
Represented by a single numerical value with a unit.	Represented using a ows to show both magnitude and direction

### \*4. How is a vector represented symbolically?

In the textbook, a vector is represented by a boldface letter such as A, v, F etc. Since bold face cannot be written on paper, a vector is written with a small arrow over it, i.e.,  $\vec{A}$ ,  $\vec{v}$ ,  $\vec{F}$ ,  $\vec{d}$ . The magnitude of a vector is represented by an italic letter without an arrowhead.

### \*\* 5. How can a vector be represented graphically?

"A vector is graphically represented by drawing a straight line with arrowhead at one end. The th of the line represents the magnitude of the vector according to a suitable scale, while the arrowhead indicates the direction of the vector."

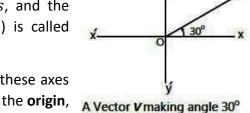


vector v making an angle θ towards north from east

Note: To represent the direction of a vector, two mutually perpendicular lines are required. One line represents the east-west direction, and the other represents the north-south direction as shown in figure. The direction of a vector can be given with respect to these lines. Mostly, we use any two lines which are perpendicular to each other.

### \*6. What are the reference axes, and what is the origin?

The horizontal line (XX') is called the x-axis, and the vertical line (YY') is called the *y-axis*.



The point where these axes meet is known as the origin, usually denoted by O. These

axes are called reference axes.

with x-axis

### 7. How is the direction of a vector specified

A vector is drawn from the origin of the reference axes towards the given direction. The direction is usually given by an angle  $oldsymbol{ heta}$  (theta) with the x-ax This angle is always measured from the right side of the x-axis in the anticlockwise direction.

### \*8. What is a resultant vector, and how is vector addition different from scalar addition?

A **resultant vector** is a single vector obtained by adding two or more vectors. It has the same effect as the combined effect of all the vectors being added.

Unlike scalar addition, where only magnitudes added, vector addition requires determining both nagnitude and direction. One method of adding vectors is the graphical method.

#### \*\* 9. State head-to-tail rule for addition of vectors.

To add a number of vectors, redraw their representative lines such that the **head** of one line coincides with the tail of the other. The resultant vector is given by a single **vector** which is directed from the **tail** of the first vector to the **head** of the **last vector**.

### 10. How can we add two or more vectors using the headto-tail rule?

Let us add two vectors  $v_1$  and  $v_2$  having magnitudes of 300 N and 400 N acting at angles of 30° and 60° with the x-axis. By selecting a suitable scale (100N = 1cm), we can draw the vectors as shown in fig. (a).

fig. (b)

The measured length of the resultant vector is 6.8 cm fig. (b). According to the selected scale, the magnitude of the resultant vector v is 680 N,

and its direction is  $49^{\circ}$  with the *x-axis*. We can find the resultant vector of more than two vectors by adding them in the same way using the **head-to-tail rule**.

#### \*\* 11. What is difference between rest and motion?

11. What is difference be					
Rest	Motion				
If a body does not change	If a body continuously				
its position with respect to	changes its position with				
its surroundings, it is said	respect to its				
to be <b>at rest</b> .	surroundings, it is said to				
	be <b>in motion</b> .				
Example: A motorcyclist	Example: A <b>moving</b>				
standing on the road is at	motorcyclist is in motion				
rest because he is not	because he is				
changing his position with	continuously changing his				
respect to nearby	position with respect to				
buildings, trees, or poles.	his surroundings.				
Objects like <b>buildings</b> ,	A moving car, running				
trees, and electric poles	water, or a flying bird are				
are in a state of rest as	examples of motion.				
they do not change their					
position.					
Rest and motion are	Rest and motion are				
relative. A person sitting	relative. The same person				
inside a moving train is at	is in motion with respect				
rest <b>relative to other</b>	to someone standing				
passengers but in motion	outside the train.				
relative to an observer on					
the platform.					

### \*\* 12. What are the different types of motion? Explain with examples.

We observe different types of motion in our daily life. Generally, there are **three types of motion:** 

**Translatory Motion:** If the motion of a body is such that every particle of the body moves uniformly in the same direction, it is called translatory motion.

For example, the motion of a train or a car.

**Rotatory Motion:** If each point of a body moves around a fixed point (axis), the motion of this body is called rotatory motion.

For example, the motion of an electric fan or a spinning top.

**Vibratory Motion:** When a body repeats its to and fro motion about a fixed position, the motion is called vibratory motion.

For example, a swing in a children's park.

### 13. What are the types of translatory motion? Explain with examples.

Translatory motion can be of three types:

**Linear Motion:** If the body moves along a straight line, it is called linear motion.

For example, a freely falling body.

**Random Motion:** If the body moves along an irregular path, the motion is called random motion.

For example, the motion of a bee.

**Circular Motion:** The motion of a body along a circle is called circular motion.

For example, a Ferris wheel or a ball tied to a string and whirled in a circle.

### \*14. What is the difference between distance and displacement? Explain with examples.

**Distance:** The distance is the length of the actual path of the motion.

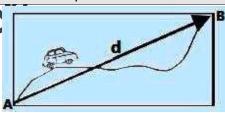
**Example:** Let a person be travelling from **Lahore to Multan** in a car. On reaching **Multan**, he reads the speedometer and notices that he has travelled a **distance of 320 km**. This is the total distance he travelled. However, this is **not the shortest distance**, as the car took many turns along the way and did not travel in a straight line.

**Displacement:** The displacement of an object is a vector quantity whose magnitude is the shortest distance between the initial and final positions of the motion. Its direction is from the initial position to the final position. We can also call this the change in position.

OR

The shortest distance between the initial and final positions of a body is called its displacement.

car travels from a position A to The curved line is the actual path followed by the par as shown



in figure, which represents the **distance**. The **displacement** (d) is the straight line from A to B, as indicated by the arrow.

**Position:** Position of any object is its distance and direction from a fixed point.

### **Key Points:**

- (a) Distance is a scalar quantity, while displacement is a vector quantity.
- **(b)** The **SI unit** for displacement is the same as that of distance (*meters*, *m*).

#### \*\* 15. What is speed? Write its formula and SI unit.

Speed is the distance covered in unit time. It tells us how fast a body is moving.

The formula for **speed (v)** is:

$$Speed = \frac{Distance}{Time}$$
$$v = \frac{S}{t}$$

Speed is a scalar quantity, and its SI unit is  $ms^{-1}$  or  $kmh^{-1}$ .

### \*16. Differentiate between instantaneous speed and average speed.

**Instantaneous Speed:** The speed of a vehicle at any given instant is called instantaneous speed. It is the reading shown on a speedometer at that moment.

Prepared By: M. Tayyab, SSE(Math) Govt Christian High School, Daska. Mobile: 03338114798

Average Speed: Since speed is not constant during a journey, we often use average speed, which is defined as:

ey, we often use average speed, which is define 
$$Average\ speed = rac{Total\ distance\ covered}{Total\ time\ taken}$$
  $v_{av} = rac{S}{t}$ 

This helps us determine how fast an object moves on average over a period of time.

### \*\* 17. What is velocity? Write its formula and SI unit.

Velocity is the net displacement of a body in unit time.

It is a vector quantity, meaning it has both magnitude and direction. The formula for average velocity is:

Average velocity 
$$=$$
  $\frac{Displacement}{Time}$   $v_{av} = \frac{d}{t}$  The **SI unit** of velocity is  $ms^{-1}$  or  $kmh^{-1}$ .

### 18. How is velocity different from speed?

- Speed only tells how fast an object is moving; it does not include direction.
- **Velocity** tells both how fast and in which direction an object is moving.
- Speed is a scalar quantity, while velocity is a vector

For example, if a car moves towards north at  $70 \text{ kmh}^{-1}$ , its speed is  $70 \, kmh^{-1}$  (scalar), but its velocity is  $70 \; kmh^{-1}$ towards north (vector).

### \*19. What is uniform and non-uniform velocity? Giv example.

The velocity is said to be uniform if the speed and direction of a moving body do not change. If the speed or direction or both of them change, it is known as variable velocity or non-uniform velocity.

For example, the downward motor of a paratrooper is an example of uniform velocity. When a paratrooper jumps from an aeroplahe he falls freely for a few moments. Then, the parachute opens. At this stage, the force of gravity acting downward on the paratrooper is balanced by the resistance of air on the parachute that acts upward. Consequently, the paratrooper moves down with **uniform velocity**.

#### \*20 What is acceleration? Write its SI unit.

Acceleration is defined as the time rate of change of velocity.

It is a vector quantity, meaning its direction is the same as that of the change in velocity.

If a body is moving with an initial velocity  $v_i$  and after some time t, its velocity changes to  $v_f$ , then the change in velocity is  $\Delta v = v_f - v_i$ 

The average acceleration is given by:

$$Average \ acceleration = \frac{Change \ in \ velocity}{Time \ taken}$$

$$a_{av} = \frac{v_f - v_i}{t} \cdots (i)$$
$$a_{av} = \frac{\Delta v}{t}$$

The SI unit of acceleration is meter per second square  $(ms^{-2}).$ 

If acceleration a is constant, then Eq (i) can be written as  $v_f = v_i + at$ 

### \*21. What are the types of acceleration?

Acceleration is of two types:

Positive Acceleration: If the velocity is increasing, the acceleration is positive. For example, when a car overtakes another vehicle, it accelerates to a greater velocity.

Negative Acceleration (Deceleration or Retardation): If the velocity is decreasing, the acceleration is negative. For example, when brakes are applied to slow down a bicycle or a car, the velocity decreases.

Acceleration is a **vector quantity**, and its **direction** is that of the **change in yelocity**.

### \*22. What is uniform and non-uniform acceleration?

**Uniform Acceleration:** If the time rate of change of velocity is constant, the acceleration is said to be uniform acceleration.

**Non-Uniform Acceleration**: If anyone of the magnitude or direction or both changes, the acceleration is called variable or non-uniform acceleration.

For example, a freely falling body experiences uniform acceleration due to gravity because its velocity increases by an equal amount in equal time intervals. While if a car moving in traffic experiences non-uniform acceleration as it speeds up, slows down, and changes direction frequently.

### \*23. What is a graph, and how is it drawn?

A graph is a **pictorial diagram** in the form of a straight line or a curve that shows the relationship between two physical quantities.

Usually, we draw a graph on a paper on which equally spaced horizontal and vertical lines are drawn. Generally, every 10th line is a thick line on the graph paper.

### 24. How are the axes selected, and what is meant by the origin in a graph?

To draw a graph, two mutually perpendicular thick lines, XOX' and YOY', are selected as the x-axis and y-axis.

The point where the two axes intersect each other is known as the origin (0).

Mobile: 03338114798 Prepared By: M. Tayyab, SSE(Math) Govt Christian High School, Daska. Page **3** of **7** 

### 25. How are positive and negative values placed on a graph?

Positive values along the x-axis are taken to the **right** side of the origin, and negative values are taken to the **left** side.

Positive values along the y-axis are taken **above** the origin, whereas negative values are taken **below** the origin.

### 26. How are variables assigned to the axes, and give an example?

Normally, the **independent** quantity is taken along the x-axis, and the **dependent** variable quantity along the y-axis.

For example, in a distance-time graph, t (time) is the independent variable, and S (distance) is the dependent variable. Therefore, t should be along the x-axis, and S along the y-axis.

### 27. Why is a suitable scale chosen for a graph?

To represent a **physical quantity** along any axis, a **suitable scale** is chosen by considering the **minimum and maximum values** of the quantity.

### \*\* 28. What is a distance-time graph, and what does it represent?

A distance-time graph shows the **relation between distance (S)** and **time (t)** taken by a moving body.

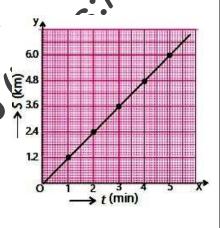
For example, suppose a car moves in a straight line on motorway. We measure its distance from the starting point after every one minute and record it in a table:

Time t (min)	0	1	2	3	4	5
Distance S (km)	0	1.2	2.4	3.6	4.8	6.0

### 29. How is a distancetime graph drawn? Write the steps.

To draw a distance-time graph on a centimetre graph paper, follow these steps:

(i) Take time (i) along the x-axis and distance (S) along the y-axis.



- (ii) Select suitable scales:  $(1 \ minute = 1 \ cm)$  on the x-axis and  $(1.2 \ km = 1 \ cm)$  on the y-axis.
- (iii) Mark values on both axes according to the chosen scale.
- (iv) Plot pairs of time and distance values from the table on the graph paper.
- (v) Join the plotted points to obtain a best straight line.

### 30. What does a straight-line distance-time graph indicate? Give an example.

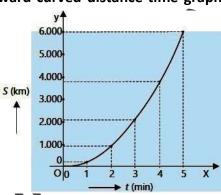
A straight-line distance-time graph indicates that the body is moving with **uniform speed**, covering equal distances in equal time intervals.

For example, in the first car journey, the graph from the table shows a **straight line**, indicating that the car moves with uniform speed.

### 31. What does an upward-curved distance-time graph

represent? Explain with an example.

An upward-curved distance-time graph indicates that the body is moving with acceleration (its speed is increasing). For example, in another journey of the car, the table should be acceleration of the car, the table should be accelerated with the car.



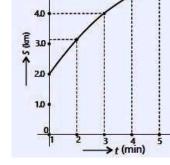
Time t (min)	0	1	2	3	4	5
Distance S (km)	0	0.240	0.960	2.160	3.840	6.000

The graph line curves upward, showing that the car's speed increases in equal intervals of time, which means the car is moving with **acceleration**.

### 32. What does a downward-curved distance-time graph

show? Explain with an example.

A downward-curved distance-time graph indicates motion with decreasing speed, which is called deceleration or negative acceleration.



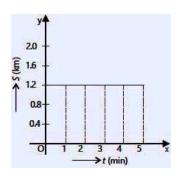
For example, in another journey, the table shows:

Time t (min)	0	1	2	3	4	5
Distance S (km)	0	2.0	3.1	4.0	4.6	5.0

The graph line curves downwards, showing that the distance traveled in the same time intervals decreases, which means the car is slowing down (decelerating).

# 33. What does a horizontal distance-time graph represent? Explain with an example.

A horizontal distance-time graph shows that the distance remains **constant with time**, meaning the object is at rest **(not moving)**.



Prepared By: M. Tayyab, SSE(Math) Govt Christian High School, Daska. Mobile: 03338114798

For example, in another case, the table shows:

Time t (min)	0	1	2	3	4	5
Distance S (km)	1.2	1.2	1.2	1.2	1.2	1.2

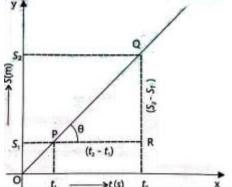
The graph line is horizontal, indicating that the car is stationary because distance does not change with time.

## \*\*34. What is meant by the gradient of a distance-time graph? How is the gradient of a distance-time graph calculated, and what is its relation to average speed?

The gradient is the measure of the slope of a line. In a distance-time graph, the gradient is equal to the average speed of the body.

To calculate the gradient:

- (i) Select any two values of time  $t_1$  and  $t_2$ .
- (ii) Draw two vertical dotted lines at  $t_1$  and  $t_2$  on the x-axis.



- (iii) These lines meet the graph at points *P* and *Q*.
- (iv) From points P and Q, draw horizontal lines to meet the y-axis at  $S_1$  and  $S_2$ , respectively.

The slope or gradient of the graph is the measure of  $tangent \ \theta$  of the triangle PQR:

$$Slope = \frac{y \ axis}{x \ axis}$$

$$= \frac{RQ}{PR}$$

$$= \frac{S_2 - S_1}{t_2 - t_1}$$

$$= \frac{S}{t}$$

From Equation  $v_{av} = \frac{s}{t}$ , S = vt where v is the average speed:

Slope =  $\tan \theta$  $= \frac{S}{t}$ = Average speed

Therefore, the gradient of the distance-time graph is equal to the average speed of the body.

### \*\* 35. What is a speed-time graph? How is it drawn?

A speed-time graph shows the relationship between **speed** (v) and **time** (t) taken by a moving body.

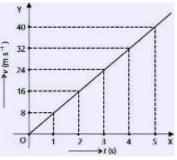
To draw a speed-time graph:

- (i) Take time (t) along the x-axis and speed (v) along the y-axis.
- (ii) Select a suitable scale.

## 36. What is the shape of the speed-time graph for uniform acceleration and constant speed? Explain with examples.

#### For Uniform Acceleration:

The speed-time graph is a straight line rising upward, showing that speed increases by the same amount in equal intervals of time.

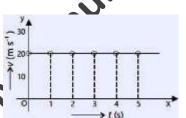


**Example:** When a car's speed is recorded every second:

Time t (s)	0	1	2	3	4	5
Speed v (m/s)	0	8	16	24	32	40

The graph is a straight line with a positive slope, indicating uniform acceleration.

For Constant Speed: The speed-time graph is a horizontal line, showing that speed remains the same over time.



**Example:** When a carn wes at a constant speed.

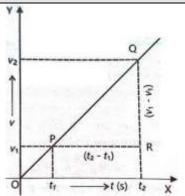
Time t (s)	0	1	2	3	4	5
Speed v (m/s)	20	20	20	20	20	20

The graph is a straight line parallel to the time axis, indicating constant speed.

## 37. What do gradients of distance-time graph and speed-time graph represent? Explain it by drawing diagrams.

The gradient (slope) of a speed-time graph is equal to the average acceleration of the body.

For Accelerating Motion: Consider the speed-time graph. The speeds at times  $t_1$  and  $t_2$  are  $v_1$  and  $v_2$  respectively. The change in speed over the time interval  $(t_2-t_1)$  is  $(v_2-v_1)$ . Therefore,



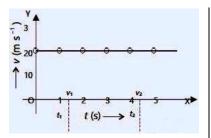
$$Slope = \frac{Change \text{ in speed}}{Time \text{ taken}}$$
$$= \frac{v_2 - v_1}{t_2 - t_1}$$
$$= \frac{\Delta v}{\Delta t}$$

Since average acceleration  $a = \frac{\Delta v}{\Delta t}$ , the slope represents:

 $\Rightarrow$  Slope = a (average acceleration)

When a car moves with constant acceleration, the velocity-time graph is a **straight line** which rises through the same height for equal intervals of time. This indicates uniform acceleration.

For Zero Acceleration (Constant Speed): When a body moves at a constant speed, the speed-time graph is a horizontal straight line parallel to the time axis.



In this case, the speed at time  $t_1$  is the same as the speed at time  $t_2$ . Therefore, the change in speed is zero:

$$v_2 - v_1 = 0$$

Hence, the slope is:

Slope = 
$$\frac{v_2 - v_1}{t_2 - t_1}$$
  
=  $\frac{0}{t_2 - t_1}$   
= 0

This shows that the acceleration of this motion is zero, meaning it is a motion without any change in speed.

### **Conclusion:**

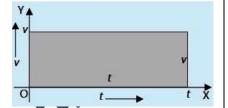
- The **slope of a speed-time graph** is equal to the body's average acceleration.
- A slanted straight line represents uniform acceleration.
- A **horizontal line** parallel to the time axis represents zero acceleration (constant speed).

### \*\* 38. Prove that the area under speed-time graph is equal to the distance covered by an object.

The distance moved by an object can be found by calculating the area under the speed-time graph.

### 1. When the Object Moves with Constant Speed: In

Figure, the object moves with a constant speed v. For a time interval t, the distance covered is:



$$Distance = v \times t$$

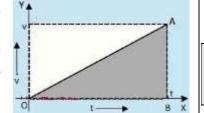
The same distance is obtained by calculating the area under the speed-time graph, which is a rectangle with sides v and t:

Area of rectangle = 
$$v \times t$$

The area under the speed-time graph up to the time axis is numerically equal to the distance covered by the object.

### 2. When the Object Moves with Uniformly Increasing

**Speed (Acceleration):** In figure, the object's speed increases uniformly from 0 to v in time t. The average speed is:



$$v_{av} = \frac{0+v}{2}$$

$$v_{av} = \frac{v}{2}$$

The distance covered is:

Distance = average speed × time  
= 
$$\frac{v}{2}$$
 × t  
=  $\frac{1}{2}vt$ 

The area under the speed-time graph is a right-angled triangle with base t and perpendicular v:

Area of triangle = 
$$\frac{1}{2} \times base \times perpendicular$$
  
=  $\frac{1}{2} \times v \times t$   
=  $\frac{1}{2}vt$ 

The area under the speed-time graph up to the time axis is numerically equal to the distance covered by the object.

Thus, whether the speed is constant or increasing uniformly, the area under the speed-time graph up to the time axis is numerically equal to the distance covered by the object.

### 39. Write the three equations of motion and state the assumptions made while applying them.

The three equations of motion are used to solve problems related to the motion of bodies. If:

- At is the initial velocity
- $v_f$  is the final velocity
  - t is the time taken
- S is the distance covered
- *a* is the acceleration

Then, the three equations of motion are:

$$v_f = v_i + at$$

$$S = v_i t + \frac{1}{2} at^2$$

$$2aS = v_f^2 - v_i^2$$

### Assumptions Made While Applying the Equations of Motion:

- (i) Motion is always considered along a straight line.
- (ii) Only the magnitudes of vector quantities are used.
- (iii) Acceleration is assumed to be uniform.
- (iv) The direction of initial velocity is taken as positive. Quantities in the same direction as the initial velocity are taken as **positive**, while those in the opposite direction are taken as **negative**.

### \*\* 40. How equations of motion can be applied to the bodies moving under the action of gravity?

When a body falls freely under the action of Earth's gravity, the acceleration acting on it is called **gravitational acceleration** and is denoted by g.

The direction of gravitational acceleration is always **downwards**. Its value is  $9.8 \ ms^{-2}$ , but for convenience, we use  $10 \ ms^{-2}$ .

Mobile: 03338114798

Since freely falling bodies move vertically downward in a straight line with uniform acceleration g, the three equations of motion can be applied to their motion by replacing a with g.

Thus, the equations of motion for freely falling bodies are:

$$v_f = v_i + gt$$

$$S = v_i t + \frac{1}{2}gt^2$$

$$2gS = v_f^2 - v_i^2$$

### **Points to Consider While Using These Equations:**

- (i) If a body is released from some height to fall freely, its initial velocity  $v_i$  is taken as zero.
- (ii) The gravitational acceleration g is taken as **positive** in the downward direction. All other quantities in the downward direction are also taken as positive, while those in the opposite direction are taken as negative.
- (iii) If a body is thrown vertically upward, the value of gis **negative**, and the final velocity is zero at the highest point.
- \*\* 41. Falling objects near the Earth have the same constant acceleration. Does this imply that a heavier object will fall faster than a lighter object?

No, a heavier object will not fall faster than a lighter object. According to the equations of motion for freely falling bodies:

- All objects experience the same gravitational acceleration ( $g = 9.8 \, ms^{-2}$ ) near Earth's surface, regardless of their mass.
- This implies that both heavy and light objects will reach the ground simultaneously in a vacual air resistance is negligible).

### 42. What is the universal speed limit and who proposed

In 1905, the famous scientist Albert Einstein proposed his revolutionary theory of special relativity, which modified many basic concepts of physics.

According to this theory

- The **speed of light** is a **universal constant** with a value of approximately  $3 \times 10^8 \ ms^{-1}$ .
- The specific light remains the same for all motions, regardless of the observer's frame of reference.
- No object with mass can achieve speeds equal to or reater than that of light.

This is known as the universal speed limit.

\*\* 43. The vector quantities are sometimes written in scalar notation (not bold face). How is the direction indicated?

When vector quantities are written in scalar notation (not boldface), their direction is indicated in the following different ways.

(i) By stating the direction in words: For example, a force of 10 N towards the east or Velocity of 5  $ms^{-1}$ northward.

- (ii) By giving the angle: For example, a displacement of 5 m at 30° from the x-axis.
- \*\* 44. A body is moving with uniform speed. Will its velocity be uniform? Give reason.

A body is moving with uniform speed may or may not have uniform velocity.

Case I: If the direction of motion of body is changing, its velocity will get changed. For example: A care moving on circular path with constant speed.

Case II: If the direction of motion of body is constant/linear then its speed as well as its velocity remain constant.

- \*\* 45. Is it possible for a body to have acceleration when moving with: (i) constant velocity (ii) constant speed?
- (i) For Constant Velocity: No, when a body moves with constant velocity its acceleration becomes equal to zero because acceleration is the rate of change of velocity over time.

For example: A car is ving in a straight line with uniform velocity.

(ii) For Constant Speed: Yes, a body can have acceleration while moving with constant speed.

For example: When a body moves with constant speed on a circular path it has acceleration because the direction of its motion changes which is along the tangent speed.

Prepared By: M. Tayyab, SSE (Math) Govt Christian High School, Daska. Mobile: 03338114798 Page **7** of **7**