

Important Formulas

- Newtons Second Law $F = ma$
- Formula of Weight $w = mg$
- Relation Between Force and Momentum $F = \frac{\Delta p}{\Delta t}$
- Centripetal Force $F_c = \frac{mv^2}{r}$
- Frictional Force $F_s = \mu mg$
- Relation Between Force and Momentum

$$F = \frac{\Delta p}{\Delta t}$$

- Impulse

$$\text{Impulse} = F \times \Delta t$$

$$\text{Impulse} = \frac{\Delta p}{\Delta t} \times \Delta t$$

$$\text{Impulse} = \Delta p$$

$$\text{Impulse} = \text{Change in momentum}$$

3.1. A 10 kg block is placed on a smooth horizontal surface. A horizontal force of 5 N is applied to the block. Find:

- (a) the acceleration produced in the block.
- (b) the velocity of block after 5 seconds.

Given Data

$$\begin{aligned}\text{Mass of block} &= m = 10 \text{ kg} \\ \text{Force} &= F = 5 \text{ N} \\ \text{Initial velocity} &= v_i = 0 \text{ ms}^{-1}\end{aligned}$$

To Find

$$\begin{aligned}\text{Acceleration} &= a = ? \\ \text{Final velocity} &= v_f = ?\end{aligned}$$

Solution

According to second law of motion

$$\begin{aligned}F &= ma \\ 5 &= (10)(a) \\ \frac{5}{10} &= a \\ 0.5 &= a \\ a &= 0.5 \text{ ms}^{-2}\end{aligned}$$

Now by using first equation of motion

$$\begin{aligned}v_f &= v_i + at \\ v_f &= 0 + (0.5)(5) \\ v_f &= 0 + 2.5 \\ v_f &= 2.5 \text{ ms}^{-1}\end{aligned}$$

3.2. The mass of a person is 80 kg. What will be his weight on the Earth? What will be his weight on the Moon? The value of acceleration due to gravity of Moon is 1.6 ms^{-2} .

Given Data

$$\begin{aligned}\text{Mass of body} &= m = 80 \text{ kg} \\ \text{Value of } g \text{ on the surface of Earth} &= g_E = 10 \text{ ms}^{-2} \\ \text{Value of } g \text{ on the surface of Moon} &= g_M = 1.6 \text{ ms}^{-2}\end{aligned}$$

To Find

$$\begin{aligned}\text{Weight on the surface of Earth} &= w_E = ? \\ \text{Weight on the surface of Moon} &= w_M = ?\end{aligned}$$

Solution

By using formula of weight $w = mg$

$$\begin{aligned}w_E &= mg_E \\ w_E &= (80)(10) \\ w_E &= 800 \text{ N}\end{aligned}$$

Now again by using formula of weight $w = mg$

$$\begin{aligned}w_M &= mg_M \\ w_M &= (80)(1.6) \\ w_M &= 128 \text{ N}\end{aligned}$$

3.3. What force is required to increase the velocity of 800 kg car from 10 ms^{-1} to 30 ms^{-1} in 10 seconds?

Given Data

$$\begin{aligned}\text{Mass of car} &= m = 800 \text{ kg} \\ \text{Initial velocity} &= v_i = 10 \text{ ms}^{-1} \\ \text{Final velocity} &= v_f = 30 \text{ ms}^{-1} \\ \text{Time} &= t = 10 \text{ s}\end{aligned}$$

To Find

$$\text{Force} = F = ?$$

Solution

According to second law of motion

$$\begin{aligned}F &= ma \\ F &= (m) \left(\frac{v_f - v_i}{t} \right) \\ F &= (800) \left(\frac{30 - 10}{10} \right) \\ F &= (800) \left(\frac{20}{10} \right) \\ F &= (800)(2) \\ F &= 1600 \text{ N}\end{aligned}$$

3.4. A 5 g bullet is fired by a gun. The bullet moves with a velocity of 300 ms^{-1} . If the mass of the gun is 10 kg, find the recoil speed of the gun.

Given Data

$$\text{Mass of bullet} = m = 5 \text{ g}$$

$$m = \frac{5}{1000} \text{ kg}$$

$$m = 0.005 \text{ kg}$$

$$\text{Velocity of bullet} = v = 300 \text{ ms}^{-1}$$

$$\text{Mass of gun} = M = 10 \text{ kg}$$

To Find

$$\text{Recoil speed of the gun} = V = ?$$

Solution

According to law of conservation of momentum

$$\begin{aligned} \text{Total momentum before firing} &= \text{Total momentum after firing} \\ 0 &= MV + mv \\ 0 &= (10)V + (0.005)(300) \\ 0 &= 10V + 1.5 \\ -1.5 &= 10V \\ \frac{-1.5}{10} &= V \\ -0.15 &= V \\ V &= -0.15 \text{ ms}^{-1} \end{aligned}$$

Negative sign indicates the gun recoils. *i. e* move in backward direction opposite to the motion of bullet.

3.5. An astronaut weighs 70 kg. He throws a wrench of mass 300 g at a speed of 3.5 ms⁻¹. Determine:

- the speed of astronaut as he recoils away from the wrench.
- the distance covered by the astronaut in 30 minutes.

Given Data

$$\begin{aligned} \text{Mass of astronaut} &= M = 70 \text{ kg} \\ \text{Mass of wrench} &= m = 300 \text{ g} \\ m &= \frac{300}{1000} \text{ kg} \\ m &= 0.3 \text{ kg} \\ \text{Speed of wrench} &= v = 3.5 \text{ ms}^{-1} \\ \text{Time} &= t = 30 \text{ min.} \\ t &= 30 \times 60 \text{ s} \\ t &= 1800 \text{ s} \end{aligned}$$

To Find

$$\text{Recoil speed of the astronaut} = V = ?$$

$$\text{Distance covered in 30 minutes} = S = ?$$

Solution

According to law of conservation of momentum

$$\begin{aligned} \text{Total momentum before throwing} &= \text{Total momentum after throwing} \\ 0 &= MV + mv \\ 0 &= (70)V + (0.3)(3.5) \\ 0 &= 70V + 1.05 \\ -1.05 &= 70V \end{aligned}$$

$$\frac{-1.05}{70} = V$$

$$-0.015 = V$$

$$V = -0.015 \text{ ms}^{-1}$$

$$V = -1.5 \times 10^{-2} \text{ ms}^{-1}$$

Negative sign indicates the astronaut recoils (moves in the opposite direction of the wrench).

Now by using formula of distance

$$\begin{aligned} S &= Vt \\ S &= (0.015)(1800) \\ S &= 27 \text{ m} \end{aligned}$$

We don't take negative speed for distance because: Distance is always positive. The negative sign shows direction, not how far something moves.

3.6. A $6.5 \times 10^3 \text{ kg}$ bogie of a goods train is moving with a velocity of 0.8 ms^{-1} . Another bogie of mass $9.2 \times 10^3 \text{ kg}$ coming from behind with a velocity of 1.2 ms^{-1} collides with the first one and couples to it. Find the common velocity of the two bogies after they become coupled.

Given Data

$$\text{Mass of first bogie} = m_1 = 6.5 \times 10^3 \text{ kg}$$

$$\text{Velocity of first bogie} = v_1 = 0.8 \text{ ms}^{-1}$$

$$\text{Mass of second bogie} = m_2 = 9.2 \times 10^3 \text{ kg}$$

$$\text{Velocity of second bogie} = v_2 = 1.2 \text{ ms}^{-1}$$

To Find

$$\text{Common velocity after coupling} = V = ?$$

Solution

According to law of conservation of momentum

$$\begin{aligned} \text{Total momentum before couple} &= \text{Total momentum after couple} \\ m_1 v_1 + m_2 v_2 &= m_1 V + m_2 V \\ m_1 v_1 + m_2 v_2 &= V(m_1 + m_2) \\ (6.5 \times 10^3)(0.8) + (9.2 \times 10^3)(1.2) &= V[(6.5 \times 10^3) + (9.2 \times 10^3)] \\ 5200 + 11040 &= V(15700) \\ \frac{16240}{15700} &= V \\ 1.03 &= V \\ V &= 1.03 \text{ ms}^{-1} \end{aligned}$$

3.7. A cyclist weighing 55 kg rides a bicycle of mass 5 kg. He starts from rest and applies a force of 90 N for 8 seconds. Then he continues at a constant speed for another 8 seconds. Calculate the total distance travelled by the cyclist.

Given Data

$$\text{Mass of cyclist} = m_1 = 55 \text{ kg}$$

$$\text{Mass of bicycle} = m_2 = 5 \text{ kg}$$

$$\text{Total mass} = m = 55 \text{ kg} + 5 \text{ kg}$$

$$m = 60 \text{ kg}$$

$$\text{Force applied} = F = 90 \text{ N}$$

$$\text{Time of acceleration} = t_1 = 8 \text{ s}$$

$$\text{Time of constant speed} = t_2 = 8 \text{ s}$$

$$\text{Initial speed} = v_i = 0 \text{ ms}^{-1}$$

To Find

$$\text{Total distance travelled} = S = ?$$

Solution

According to second law of motion

$$F = ma$$

$$90 = (60)(a)$$

$$\frac{90}{60} = a$$

$$1.5 = a$$

$$a = 1.5 \text{ ms}^{-2}$$

Now by using first equation of motion

$$v_f = v_i + at_1$$

$$v_f = 0 + (1.5)(8)$$

$$v_f = 0 + 12$$

$$v_f = 12 \text{ ms}^{-1}$$

Distance covered **during acceleration** by using second equation of motion

$$S_1 = v_i t_1 + \frac{1}{2} a t_1^2$$

$$S_1 = (0)(8) + \frac{1}{2} (1.5)(8)^2$$

$$S_1 = 0 + \frac{1}{2} (1.5)(64)$$

$$S_1 = 0 + 48$$

$$S_1 = 48 \text{ m}$$

Distance covered at **constant speed** by formula $S = vt$

$$S_2 = v_f t_2$$

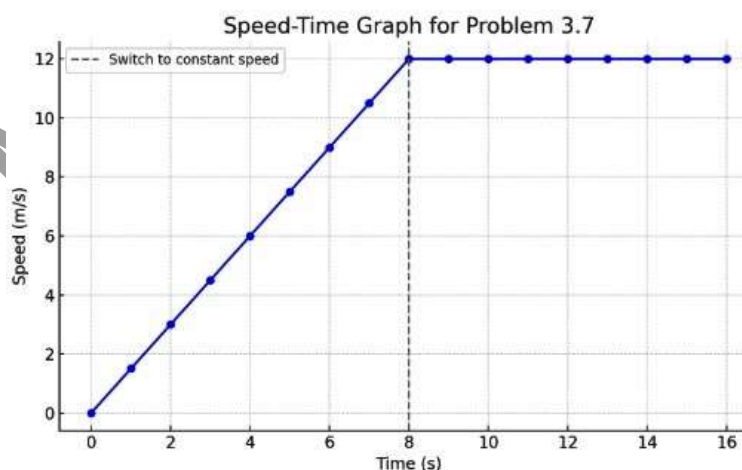
$$S_2 = (12)(8)$$

$$S_2 = 96 \text{ m}$$

$$\text{Total distance travelled} = S = S_1 + S_2$$

$$S = 48 \text{ m} + 96 \text{ m}$$

$$\mathbf{S = 144 \text{ m}}$$



3.8. A ball of mass 0.4 kg is dropped on the floor from a height of 1.8 m. The ball rebounds straight upward to a height of 0.8 m. What is the magnitude and direction of the impulse applied to the ball by the floor?

Given Data

$$\text{Mass of ball} = m = 0.4 \text{ kg}$$

$$\text{Drop height} = h_1 = 1.8 \text{ m}$$

$$\text{Rebound height} = h_2 = 0.8 \text{ m}$$

$$\text{Acceleration due to gravity} = g = 10 \text{ ms}^{-2}$$

To Find

$$\text{Impulse (magnitude and direction)} = ?$$

Solution

Since the ball is dropped so, $v_i = 0 \text{ ms}^{-1}$

$$2gh_1 = v_f^2 - v_i^2$$

$$2(10)(1.8) = v_f^2 - (0)^2$$

$$36 = v_f^2$$

$$v_f^2 = 36$$

$$\sqrt{v_f^2} = \sqrt{36}$$

$$v_f = \pm 6 \text{ ms}^{-1}$$

But since the ball is moving downward, we select the negative root. *i. e*

$$v_f = v_{\text{before}} = -6 \text{ ms}^{-1}$$

At maximum rebound height, $v_f = 0 \text{ ms}^{-1}$

$$2gh_2 = v_f^2 - v_i^2$$

$$2(-10)(0.8) = (0)^2 - v_i^2 \quad (\because \text{ball moving upward})$$

$$-16 = -v_i^2$$

$$v_i^2 = 16$$

$$\sqrt{v_i^2} = \sqrt{16}$$

$$v_i = \pm 4 \text{ ms}^{-1}$$

But since the ball is moving upward, we select the positive root. *i. e*

$$v_i = v_{\text{after}} = 4 \text{ ms}^{-1}$$

Now by using formula of impulse

$$\text{Impulse} = \text{Change in momentum}$$

$$= \Delta p$$

$$= p_f - p_i$$

$$= mv_f - mv_i$$

$$= m(v_f - v_i)$$

$$= m(v_{\text{after}} - v_{\text{before}})$$

$$= (0.4)[4 - (-6)]$$

$$= (0.4)[10]$$

$$\mathbf{Impulse = 4 \text{ Ns}}$$

The **positive result** means the impulse is **upward** (floor pushes the ball up).

Note: In physics, we always choose a reference direction to be positive.

For vertical motion:

- We choose upward as positive (by convention).
- So, any velocity in the upward direction is positive.
- And any velocity in the downward direction is negative.

3.9. Two balls of masses 0.2 kg and 0.4 kg are moving towards each other with velocities 20 ms^{-1} and 5 ms^{-1} respectively. After collision, the velocity of 0.2 kg ball becomes 6 ms^{-1} . What will be the velocity of 0.4 kg ball?

Given Data

$$\text{Mass of ball A} = m_1 = 0.2\text{ kg}$$

$$\text{Mass of ball B} = m_2 = 0.4\text{ kg}$$

$$\text{Initial velocity of ball A} = v_1 = 20\text{ ms}^{-1}$$

$$\text{Initial velocity of ball B} = v_2 = -5\text{ ms}^{-1} (\text{opposite direction})$$

$$\text{Final velocity of ball A} = v'_1 = 6\text{ ms}^{-1}$$

To Find

$$\text{Final velocity of ball B} = v'_2 = ?$$

Solution

According to law of conservation of momentum

$$\text{total momentum of the system before collision} = \text{total momentum of the system after collision}$$

$$m_1 v_1 + m_2 v_2 = m_1 v'_1 + m_2 v'_2$$

$$(0.2)(20) + (0.4)(-5) = (0.2)(6) + (0.4)(v'_2)$$

$$4 - 2 = 1.2 + (0.4)(v'_2)$$

$$2 - 1.2 = 0.4v'_2$$

$$0.8 = 0.4v'_2$$

$$\frac{0.8}{0.4} = v'_2$$

$$2 = v'_2$$

$$v'_2 = 2\text{ ms}^{-1}$$