

**DARSHAN INSTITUTE OF ENGINEERING AND TECHNOLOGY,  
RAJKOT**

GTU Mid-Sem - 1 Examination, August, 2017

B.E. Sem.- V (Computer Engineering)

Enroll. No.: \_\_\_\_\_

**Subject: Analysis and Design of Algorithms (2150703)**

**Date: 08/08/2017**

**Time : 08:00 a.m. to 10:00 a.m.**

**Total Marks : 50**

**Instructions:**

- 1. Attempt all questions**
- 2. Assume suitable data if necessary**
- 3. Figure to the right indicate full marks**

**Q - 1 Answer Following Questions.**

**06**

- (a) Define algorithm. Enlist different types of algorithm.
- (b) Write Principal of invariance.
- (c) Time complexity of \_\_\_\_\_ is in linear time.  
(a) Bubble sort (b) Radix sort (c) Shell sort (d) Selection sort
- (d) What is amortized analysis. List out the methods of amortized analysis.
- (e) Solve following recurrence using master method  $T(n) = 4T(n/2) + n^3$
- (f) Define Feasible Solution.

**Q - 2 Answer any four questions out of five.**

**16**

- (a) Why do we use asymptotic notations in the study of algorithms? Briefly describe the commonly used asymptotic notations.
- (b) Explain multiplying large integer problem for multiplying  $789 \times 3124$ .
- (c) Solve the given recurrence using recurrence tree  $T(n) = T(n/4) + T(n/2) + n^2$
- (d) Apply counting sort the following numbers to sort in ascending order. **5, 2, 0, 5, 4, 1, 3, 1, 3.**
- (e) Explain the use of Divide and Conquer Technique for Binary Search Method. What is the complexity of Binary Search Method?

**Q-3 Answer any four questions out of five.**

**28**

- (a) Write an algorithm of Quick Sort Method and sort given numbers using the algorithm. **2, 8, 7, 1, 3, 5, 6, 4.** Derive its best, average and worst case time complexity.
- (b) Sort the given elements with Heap Sort Method: **20, 50, 30, 75, 90, 60, 25, 10, 40.**
- (c) Let  $T[1.. n]$  be a sorted array of distinct integers, some of which may be negative. Give an algorithm that can find an index  $i$  such that  $1 < i < n$  and  $T[i] = i$ , provided such an index exists. Your algorithm should take a time in  $O(\log n)$  in the worst case.
- (d) Explain Selection Sort Algorithm. Derive its best case, worst case and average case time complexity.
- (e) Discuss insertion sort algorithm with its time complexity. Support your answer with suitable example.