What is a time series?

According to the wikipedia, A time series is a series of data points indexed (or listed or graphed) in time order. Most commonly, a time series is a sequence taken at successive equally spaced points in time. Thus it is a sequence of discrete-time data. For example, stock prices over a fixed period of time, hotel bookings, ecommerce sales, waether cycle reports etc.

Time series analysis comprises methods for analyzing time series data in order to extract meaningful statistics and other characteristics of the data. Time series forecasting is the use of a model to predict future values based on previously observed values.

Let's discuss a few definitions related to time series first.

Definitions

- **Level**: Level is the average of the values of the series.
- Trend: Trend shows a pattern in the data. For example, whether the stock prices are
 increasing with time(uptrend) or are they decreasing with time(downtrend) or time
 doesn't have that much effect on the prices(Horizontal trend)

Image Courtsey: Financial Hub

- **Seasonality:** When the data shows a repetative pattern for over an year, it can be termed as seasonal pattern. For example, the sale of airconditioners will increase every year during summer and the sale will decrease during winter.
- Cyclic Patterns: These are the repetative patterns shown over a longer period of time(more than one year). For example, after every five year the share market has some fluctuations due to the general elections.
- **Noise:** The variations which do not show any pattern.

Let's now take an example to see what was done before the advent of Time Series Analysis.

Let's say that we have a problem at hand where we have been asked to predict the sales of skiing products for a sports manufacturer. You can do the predictions using the following methods:

Old Methods

- Using Average: You might give the prediction as the average of all the prevous values.
- **Using Moving Average:** This is the average of the previous values over a fixed period. For example you might predict the sales in November based on the average of past 3 months. The past three months will be August, September and October. If you are predicting the sales for December, the past three months will be September, October

- and November. Although the number of months considered are same but the window moved from one set of months to another. Hence the name Moving Average.
- **Using the Naive Method:** The Naive method says that the prediction will be same as the last figure. For example, the prediction for November will be the sales for October.
- **Using the Seasonal Naive Method:** Seasonal naive method is similar to naive method. Here, the new prediction is equal to the sales for the previous season.

```
ARIMA
In [24]: import numpy as np
         from scipy import stats
         import pandas as pd
         import matplotlib.pyplot as plt
         import statsmodels.api as sm
         from statsmodels.graphics.api import qqplot
         %matplotlib inline
 In [3]: female birth data=pd.read csv("daily-total-female-births-CA.csv") # This is
 In [4]: female birth data.head()
 Out[4]:
                 date births
         0 1959-01-01
                         35
         1 1959-01-02
                         32
         2 1959-01-03
                         30
         3 1959-01-04
                         31
         4 1959-01-05
                         44
 In [6]:
         birth data=pd.read csv("daily-total-female-births-CA.csv", index col=[0], pa
 In [7]: birth_data.head()
```

Out[7]: births

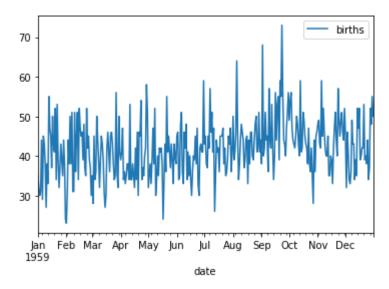
date	
1959-01-01	35
1959-01-02	32
1959-01-03	30
1959-01-04	31
1959-01-05	44

In [8]: birth_data.describe()

Out[8]:		births
	count	365.000000
	mean	41.980822
	std	7.348257
	min	23.000000
	25%	37.000000
	50%	42.000000
	75%	46.000000
	max	73.000000

In [9]: birth_data.plot() #almost a stationary series

Out[9]: <matplotlib.axes._subplots.AxesSubplot at 0x1f14fd95198>



In [21]: # also called as smoothing
moving_average_birth=birth_data.rolling(window=20).mean() # window: This is

In [22]: moving_average_birth

Out[22]: births

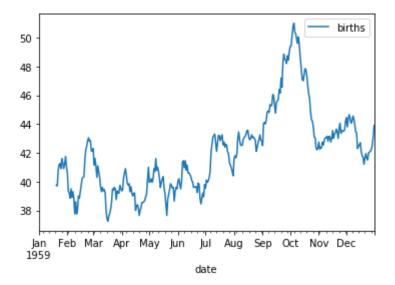
date	
1959-01-01	NaN
1959-01-02	NaN
1959-01-03	NaN
1959-01-04	NaN
1959-01-05	NaN
1959-01-06	NaN
1959-01-07	NaN
1959-01-08	NaN
1959-01-09	NaN
1959-01-10	NaN
1959-01-11	NaN
1959-01-12	NaN
1959-01-13	NaN
1959-01-14	NaN
1959-01-15	NaN
1959-01-16	NaN
1959-01-17	NaN
1959-01-18	NaN
1959-01-19	NaN
1959-01-20	39.75
1959-01-21	39.70
1959-01-22	40.75
1959-01-23	41.20
1959-01-24	41.25
1959-01-25	40.90
1959-01-26	41.60
1959-01-27	41.30
1959-01-28	40.90
1959-01-29	41.20
1959-01-30	41.75

births

date	
1959-12-03	44.35
1959-12-04	44.65
1959-12-05	44.35
1959-12-06	44.05
1959-12-07	44.20
1959-12-08	44.55
1959-12-09	44.35
1959-12-10	43.95
1959-12-11	43.45
1959-12-12	43.40
1959-12-13	42.30
1959-12-14	42.45
1959-12-15	42.55
1959-12-16	42.70
1959-12-17	42.10
1959-12-18	41.80
1959-12-19	41.70
1959-12-20	41.20
1959-12-21	41.60
1959-12-22	41.95
1959-12-23	41.65
1959-12-24	41.50
1959-12-25	42.00
1959-12-26	42.05
1959-12-27	42.10
1959-12-28	42.25
1959-12-29	42.50
1959-12-30	43.10
1959-12-31	43.90

365 rows × 1 columns

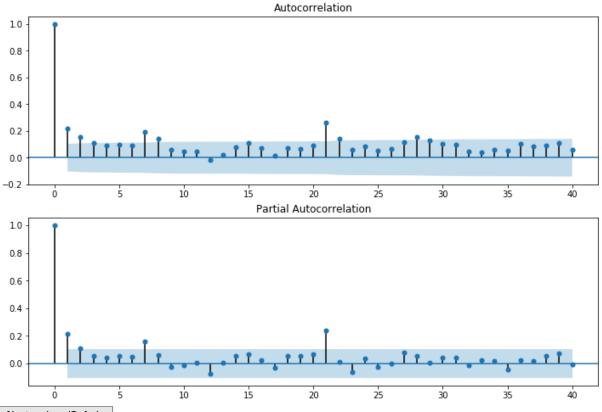
Out[23]: <matplotlib.axes. subplots.AxesSubplot at 0x1f150907b00>



In [25]: sm.stats.durbin_watson(birth_data) # very less correlation

Out[25]: array([0.04624491])

```
In [26]: # show plots in the notebook
%matplotlib inline
fig = plt.figure(figsize=(12,8))
ax1 = fig.add_subplot(211)
fig = sm.graphics.tsa.plot_acf(birth_data.values.squeeze(), lags=40, ax=ax1)
ax2 = fig.add_subplot(212)
fig = sm.graphics.tsa.plot_pacf(birth_data, lags=40, ax=ax2)
```



Loading [MathJax]/extensions/Safe.js

```
AttributeError
                                                    Traceback (most recent call last)
          Input In [1], in <cell line: 1>()
          ----> 1 from statsmodels.tsa.arima model import ARIMA
          File ~\Anaconda3\lib\site-packages\statsmodels\tsa\_init__.py:1, in <module>
          ----> 1 from statsmodels.tools._testing import PytestTester
                3 test = PytestTester()
          File ~\Anaconda3\lib\site-packages\statsmodels\tools\__init__.py:1, in <modul
          ----> 1 from .tools import add constant, categorical
                2 from statsmodels.tools._testing import PytestTester
                4 all = ['test', 'add constant', 'categorical']
          File ~\Anaconda3\lib\site-packages\statsmodels\tools\tools.py:7, in <module>
                5 import numpy.lib.recfunctions as nprf
                6 import pandas as pd
          ----> 7 import scipy.linalg
                9 from statsmodels.compat.python import lzip, lmap
               11 from statsmodels.tools.data import is using pandas, is recarray
          File ~\Anaconda3\lib\site-packages\scipy\linalg\ init .py:213, in <module>
              211 from ._procrustes import *
              212 from ._decomp_update import *
          --> 213 from ._sketches import *
              215 all = [s for s in dir() if not s.startswith(' ')]
              217 from numpy.dual import register func
          File ~\Anaconda3\lib\site-packages\scipy\linalg\ sketches.py:11, in <module>
                8 import numpy as np
               10 from scipy._lib._util import check random state
          ---> 11 from scipy.sparse import csc matrix
               13 all = ['clarkson woodruff transform']
               16 def cwt matrix(n rows, n columns, seed=None):
          File ~\Anaconda3\lib\site-packages\scipy\sparse\_init__.py:229, in <module>
              223 # Original code by Travis Oliphant.
              224 # Modified and extended by Ed Schofield, Robert Cimrman,
              225 # Nathan Bell, and Jake Vanderplas.
              227 import warnings as _warnings
          --> 229 from .base import *
              230 from .csr import *
              231 from .csc import *
          File ~\Anaconda3\lib\site-packages\scipy\sparse\base.py:8, in <module>
                6 from scipy._lib.six import xrange
                7 from scipy._lib._numpy_compat import broadcast to
          ----> 8 from .sputils import (isdense, isscalarlike, isintlike,
                                        get sum dtype, validateaxis, check reshape kwar
          gs,
                                        check shape, asmatrix)
               10
               12 all = ['spmatrix', 'isspmatrix', 'issparse',
                             'SparseWarning', 'SparseEfficiencyWarning']
               16 class SparseWarning(Warning):
Loading [MathJax]/extensions/Safe.js
```

```
File ~\Anaconda3\lib\site-packages\scipy\sparse\sputils.py:17, in <module>
            all = ['upcast', 'getdtype', 'isscalarlike', 'isintlike',
                           'isshape', 'issequence', 'isdense', 'ismatrix', 'get sum d
            12
       type']
            14 supported dtypes = ['bool', 'int8', 'uint8', 'short', 'ushort', 'int
       с',
                                    'uintc', 'longlong', 'ulonglong', 'single', 'doub
            15
        le',
                                    'longdouble', 'csingle', 'cdouble', 'clongdoubl
            16
       e' 1
        ---> 17 supported dtypes = [np.typeDict[x] for x in supported dtypes]
            19 upcast memo = {}
            22 def upcast(*args):
       File ~\Anaconda3\lib\site-packages\scipy\sparse\sputils.py:17, in <listcomp>
        (.0)
            all = ['upcast', 'getdtype', 'isscalarlike', 'isintlike',
            12
                          'isshape', 'issequence', 'isdense', 'ismatrix', 'get_sum_d
       type']
            14 supported dtypes = ['bool', 'int8', 'uint8', 'short', 'ushort', 'int
       С',
                                    'uintc', 'longlong', 'ulonglong', 'single', 'doub
            15
        le',
            16
                                    'longdouble', 'csingle', 'cdouble', 'clongdoubl
       e']
        ---> 17 supported dtypes = [np.typeDict[x] for x in supported dtypes]
            19 upcast memo = {}
            22 def upcast(*args):
       File ~\Anaconda3\lib\site-packages\numpy\_init_.py:320, in _getattr (att
        r)
                   from .testing import Tester
           317
           318
                   return Tester
        --> 320 raise AttributeError("module {!r} has no attribute "
                                    "{!r}".format( name , attr))
       AttributeError: module 'numpy' has no attribute 'typeDict'
In [ ]:
In [45]: arima= ARIMA(training data,order=(2,1,3))
       C:\Users\virat\Anaconda3\lib\site-packages\statsmodels\tsa\base\tsa model.py:
       171: ValueWarning: No frequency information was provided, so inferred frequen
       cy D will be used.
         % freq, ValueWarning)
       C:\Users\virat\Anaconda3\lib\site-packages\statsmodels\tsa\base\tsa model.py:
       191: FutureWarning: Creating a DatetimeIndex by passing range endpoints is de
       precated. Use `pandas.date range` instead.
         start=index[0], end=index[-1], freq=freq)
       C:\Users\virat\Anaconda3\lib\site-packages\statsmodels\tsa\base\tsa model.py:
       171: ValueWarning: No frequency information was provided, so inferred frequen
       cy D will be used.
         % freq, ValueWarning)
```

```
In [46]: model=arima.fit()
In [47]: model.aic
Out[47]: 2159.076974912458
In [48]: pred= model.forecast(steps=45)[0]
In [49]: pred
Out[49]: array([44.20336376, 44.64661409, 43.40243639, 43.18642407, 42.46860908,
                43.44949502, 43.80021262, 44.81159761, 44.23852903, 43.97639274,
                42.83728932, 43.04815868, 43.14699235, 44.33687764, 44.50162656,
                44.71946592, 43.69098356, 43.32064023, 42.82208716, 43.6233574 ,
                44.11878344, 44.92162375, 44.49438888, 44.08981115, 43.14260896,
                43.23608944, 43.4795044 , 44.49993718, 44.76125302, 44.83139948,
                43.94563728, 43.49084713, 43.1407838 , 43.82776885, 44.4038833 ,
                45.06229125, 44.72230914, 44.2341347 , 43.42110948, 43.44996156,
                43.78382252, 44.68646475, 44.99650633, 44.96865567, 44.17958866])
In [50]: from sklearn.metrics import mean squared error
In [51]: np.sqrt(mean squared error(test data,pred))
Out[51]: 6.419420721712673
```