

I recognise that this news will be a disappointment to you. The editors hope that you will take this feedback in the positive spirit intended, that you will undertake the additional work and revision suggested, and that we will see an improved and publishable account of this research at Geophysical Journal International in a few months' time.

Regards,

Louise

Louise Alexander
Assistant Editor
Geophysical Journal International

cc: all listed co-authors.

Reviewer: 1 Anonymous

Comments to the Author(s)

The submitted paper reports a set of numerical dynamo simulations which attempt to investigate the magnetic dipolarity with varying aspect ratio (different inner core sizes). The suite of simulations show that dipolar dominance is achieved for aspect ratios $ri/ro=0.25, 0.35$. The methods of evaluating the dipole dominance make for an impressive tool to address the title question. The authors show that dynamo action with a small aspect ratio requires a large Rayleigh number, consequently, the different aspect ratio simulations do not sample the same range of supercriticality values. This makes it difficult to separate the aspect ratio dependence from the supercriticality dependence – I suggest 2 more simulations at $ri/ro=0.25, 0.35$ with larger Ra/Rac to connect with the $ri/ro=0.15$ case. Finally, I think that the discussion needs to clarify where the authors can/cannot distinguish between the Ra/Ra_c and ri/ro dependencies on the output diagnostics.

The paper is logically structured with the results obtained appearing to contain enough novel material to make it suitable for publication in Geophysical Journal International once the major concerns discussed here are addressed. Furthermore, I think this work will be of interest to a sizeable subgroup of the journal's readership. I recommend some revisions before publication and these are listed below.

Major Comments

A1: Throughout the manuscript the authors interpret their results in terms of the aspect ratio as the title suggests. However, due to the range of Ra/Rac sampled for each ri/ro it seems difficult to separate the parameter dependence of these two quantities. The authors could address this by running two additional simulations with $ri/ro=0.25, 0.35$ at Ra/Rac values between 10 and 15 to allow a direct comparison with the $ri/ro=0.15$ case. The interpretation of the results should then be updated throughout the manuscript. See minor points listed below where I identify sentences in the manuscript for which I find the statement of an underlying ri/ro dependence unconvincing given the current results.

A2: Conclusions. The geophysical implications and interpretation need to be better described. Yes, the geometrical effect is important to determine but when considering geological time the mode of convective driving also changes (e.g. internal versus bottom heated convection, CMB heat-flow patterns, etc.). These should be highlighted explicitly to better aid the geophysical connection of how the simulations can be relevant to Earth's core.

Out of necessity the numerical simulations are ran at a rather moderate value of the Ekman number ($E=1e-3$). This does indeed allow a systematic survey, however, I suggest that this be put into the context of the parameter regimes outlined in Gastine et al. (2016) and Long et al. (2020). At $E=1e-3$ the simulations do not sample the rapidly rotating regime which suggests that they are not governed by the force balance relevant to the Earth (see also e.g. Schwaiger et al. 2019).

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(Gastine et al. (2016) use a large aspect ratio but fixed temperature boundary conditions, whereas, Long et al. (2020) use a present day Earth aspect ratio, gravity profile but use fixed heat-flux conditions)

Minor Comments

- B1. Lines 93–97: Is the observation of Heimpel et al. (2005) robust or was it only observed at fixed Ekman and Rayleigh number? It is worth explicitly stating.
- B2. Lines 134–135: Do the authors motivate the choice of these three inner core sizes? Are these geophysically motivated or arbitrarily chosen?
- B3. Equation 6: Are g_o and κ_T defined anywhere?
- B4. Line 168: “For the time steps ...” should read “For the time stepping, ...”
- B5. Line 173: Should “sectorial” be “sectoral”?
- B6. Line 182: A statement of numerical convergence should be included; how did you ensure spatial and temporal resolutions/durations were sufficient? e.g. did you check energy conservation?
- B7. Lines 204–205: Always use standard form. The 6% difference in R_{ac} value with A-Shamali et al. (2004) for $r_i/r_o=0.15$ seems quite large. This might be fine but worth checking.
- B8. Line 221–224: How was the averaging period of 0.5 diffusion times determined to be sufficient?
- B9. Lines 225–227: No need to describe markers in main text, this belongs in the figure caption and/or legend itself.
- B10. Line 237: Can the authors comment on why these two simulations are different to the other cases? Any description or observations would add to the interpretation.
- B11. Lines 254–259: The authors claim that the difference in the convective flow and the generated magnetic fields is due to the different aspect ratios. However, the contours for $r_i/r_o=0.15$ are shown for a much higher Ra/R_{ac} than the other cases – at higher Ra/R_{ac} one typically expects more chaotic and unstructured flow. I think the discussion needs to explicitly separate these two dependencies. (This difference may fit with the regimes mentioned in major comment A2.)
- B12. Lines 284–286: The value of $fdip$ looks to depend on Ra/R_{ac} so stating the tendency is different only for r_i/r_o seems inappropriate. If larger Ra/R_{ac} runs with $r_i/r_o=0.25, 0.35$ are performed they will explicitly show if this dependence depends solely on Ra/R_{ac} .
- B13. Lines 305–310: Similar to before, does the f_{mag_fit} data collapse for $Ra/R_{ac} \geq 10$, independent of aspect ratio? The two additional simulations mentioned in major comment A1 would also help to address this.
- B14. Lines 369–371: Table 4 states that none of the $r_i/r_o=0.35$ cases have an $fdip \leq 0.35$. I don’t think the authors can say their results are consistent with previous work or that they verified the dipolar–nondipolar transition. This claim needs to be reworded or removed.
- B15. Figure 2: I suggest adding a second panel showing a failed dynamo simulation.
- B16. Figure 3: I suggest making the x-axis the same for all three plots.

Additional references not in the manuscript

Gastine, T., Wicht, J. and Aubert, J., 2016. Scaling regimes in spherical shell rotating convection. *Journal of Fluid Mechanics*, 808, pp.690–732.

Long, R., Mound, J., Davies, C. and Tobias, S., 2020. Scaling behaviour in spherical shell rotating convection with fixed-flux thermal boundary conditions. *Journal of Fluid Mechanics*.

Schwaiger, T., Gastine, T. and Aubert, J., 2019. Force balance in numerical geodynamo simulations: a systematic study. *Geophysical Journal International*, 219(Supplement_1), pp.S101–S114.

Reviewer: 2 Anonymous

Comments to the Author(s)

General Comments

This paper explores the effect of spherical geometry (ratio of inner/outer boundary radius) on magnetic dipolarity in numerical dynamo simulations. The application is the nature of the geomagnetic field over the time from after inner core nucleation to the present. The radius ratios used here (namely 0.15, 0.25 along with the the present day Earth core radius ratio 0.35) were studied in previous dynamo models (Heimpel et al, 2005) and are cited in this work. The novelty of this work is a focus on bipolarity for radius ratios that are smaller than 0.35. The analysis of dipolarity has been extensively studied in previous work, some of which is appropriately cited here.

If anything can really be called new in this work it is the dipolarity analysis of the 0.15 and 0.25 radius ratio cases. This may be of some interest to the geodynamo community.

However, the parameter space of the numerical simulations has been studied previously and extensively, and unfortunately the simulations are of relatively low resolution, given modern computing capabilities. Indeed, the fixed Ekman number of 0.001 is arguably too viscous to give Earth-like behaviour (e.g. Christensen, PEPI 187, 157, 2011). Also, many studies dating from the 1990's to 2000's have used higher resolutions, and explored much larger ranges of parameter space (e.g. Kutzner and Christensen, 2002).

Specific comments

The discussion of failed dynamos at high Ra is not explained very well. Comparing with previous work, (e.g. Kutzner and Christensen, 2002), it is clear that failed dynamos occur for $Ek = 0.001$ at the boundary between dipolar and multipolar dynamos, which occur at even higher Ra . However, these failed dynamos do not occur at higher resolution (i.e. lower Ek), and it is not obvious that they should occur at lower radius ratio, even at $Ek = 0.001$.

A failed dynamo is found at radius ratio 0.25 here, but not at 0.15. Does that mean that the transition to multipolar dynamos exist only for radius ratios greater than 0.15? Why did you not do runs for higher Ra at radius ratio 0.15? This radius ratio is arguably the most interesting in terms of the relationships between Ra , dipolarity, and the transition to multipolar dynamos. It seems that more computation is necessary to make these relationships clear.

It is argued at the end of the paper that more simulations should be carried out for different boundary conditions, and for dynamos with no inner boundary. However, you fail to cite key papers on this topic. There are numerous papers on the effect of different boundary conditions (e.g. Heimpel and Evans, PEPI, 224, 124, 2013). The effect of no inner core was studied by others, including Landeau et al. (EPSL 465, 193, 2017).