## Natural Disasters, Asymmetric Exposure, and War: Why Empirical Evidence on Climate Conflict Is Mixed

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#### Abstract

Evidence on the effect of extreme weather events or natural disasters on the risk of armed conflict is mixed. I explain the pattern by arguing that disasters have heterogeneous effects on conflict risks and, consequently, systematically make empirical evidence mixed. Specifically, I develop a model of conflict that focuses on the role of political groups' asymmetric resilience/vulnerability to disasters. It presents two contrasting equilibrium strategies arising from disaster-induced power shifts. In the first case, where two groups have similar levels of resilience, one of them opportunistically attacks its rival after a disaster if the latter incurred disproportionately severe damage. Disaster events and conflicts are positively correlated. In the second case, where one of the players is inherently more vulnerable to disaster risks, she attacks the relatively resilient side preemptively before a disaster occurs. Here, disaster events negatively correlate with conflicts. Based on the theory, this paper (i) draws a new empirical implication and assesses it with the data of intrastate conflicts and droughts in African countries and (ii) formally shows that the conditional average treatment effect (CATE) of disaster events on conflict risks becomes negative in the second case, providing a novel interpretation of why the evidence on climate conflict seems ostensibly mixed.

**Keywords:** Conflict; natural disasters; climate change; formal political theory; EITM/TIEM

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## 1 Introduction

The evidence on the effect of climate anomalies and natural disasters on the risk of violent conflict is mixed. On the one hand, these events can threaten peace by generating resource scarcity, opening a window of opportunity to exploit the affected group/country that is temporarily vulnerable, and by reducing the opportunity costs of resorting to violent conflict (e.g., Hsiang et al., 2013; Jun and Sethi, 2021; Roche et al., 2020). On the other hand, because fighting an armed conflict requires belligerents to continually mobilize material resources, climate shocks can rather reduce the risk of conflict by undermining groups' mobilization and their war-fighting capabilities (Devlin and Hendrix, 2014; Salehyan and Hendrix, 2014). Moreover, some studies report little effects of climate factors on the risk of conflict and find that the positive correlation between them is sensitive to the definition of armed conflict (Buhaug, 2010; Theisen et al., 2011). Mach et al. (2019) also report divergent views among researchers. Hence, it seems plausible to state that there does not exist a wide consensus over the effect of natural disasters and climate events on the risk of armed conflict. Why is the empirical evidence mixed? If natural disasters can lead to armed conflict, when do they cause wars?

One possible root of the mixed results is that there exist problems with measurements or the methodology used in some studies in the literature. Namely, it might be possible that there exists the true mean effect of climate events on conflict and that one wing of the debate is "correct" and others are not. For example, Hsiang et al. (2013) and Hsiang and Burke (2014) report a "remarkable convergence" in the literature and suggest the presence of a general positive relationship between climate variabilities and conflict risks. On the other hand, Buhaug et al. (2014) point out the arbitrariness in their meta-analysis and find that a replication of Hsiang et al. (2013) leads to divergent results. Salehyan (2014) frames the disagreement as conceptual and empirical problems. This paper aims to conceptually and theoretically contribute to the empirical literature.

Instead of attempting to identify and measure the general effect of climate anomalies on conflicts, this paper focuses on another possibility. Namely, the empirical results in the literature may be divergent because natural disasters affect the risk of conflict in multiple ways and such heterogeneous effects systematically make the evidence mixed. That is, the theory presented in this paper allows disasters to be positively associated with conflicts in some cases and negatively associated in others. A game-theoretic model shows that two types of contrasting strategy profiles constitute the unique equilibrium in a broad set of parameter values and that these opposing results arise from a single theoretical dynamic: rapid shifts in power between rival political groups. I briefly preview the two strategic logics in the equilibrium below.

Key concepts that drive the contrasting results are realized and expected asymmetric exposure to natural disasters. It is plausible to assume that the severity of a certain disaster to different political groups varies. We focus on two sources of such variations in damage from extreme climate events. First, some groups incur disproportionately higher costs than others from a natural disaster that has just occurred. Because most natural disasters cause more severe damage to particular areas (e.g., damages from hurricanes depend on each one's course), one group that has incurred only a small cost from a disaster may happen to be temporarily advantageous over its political rival group. Consequently, the former group can commit opportunistic aggression against the latter after an extreme weather event as a result of the realized asymmetric exposure to it.<sup>1</sup>

Second, damage from a disaster is *expected* to vary along with the geographical and social resilience of a political group.<sup>2</sup> Some groups in a coastal area may expect to incur disproportionately high costs from tsunamis and hurricanes. Other groups, such as farmers

<sup>&</sup>lt;sup>1</sup>See Kikuta (2019) for an empirical discussion based on post-disaster dynamic commitment problems. Jun and Sethi (2021) also find that natural disasters increase the probability that affected groups are invaded by their rivals.

<sup>&</sup>lt;sup>2</sup>Note that this paper is not the first to point out this dynamic. It draws on and substantially extends the concept developed by Bas and McLean (2021).

or pastoralists, may also anticipate that they would be more vulnerable to droughts and floods than their rival groups. Such groups that are inherently more vulnerable than their political rivals due to the expected asymmetric exposure to an extreme weather event can have a preemptive motive to attack an opponent *before* a devastating disaster occurs because they know that they will be highly vulnerable once the damage of the event materializes.

An important implication drawn from the above two mechanisms is that (i) the actual occurrence of a disaster and armed conflict should be positively correlated in the first equilibrium (because war follows the asymmetric post-disaster balance of power) but (ii) they should be negatively associated in the second (because war erupts in the absence of a disaster). Moreover, based on assumptions drawn from the game-theoretic model, I show that the causal effect of disasters on conflict in the sense of the conditional average treatment effect (CATE) becomes negative in the second case. This observation provides a novel theoretical interpretation of why the empirical evidence on climate conflict looks mixed ostensibly. Namely, I argue that overlooking the second mechanism (i.e., war caused by expected asymmetric exposure to disasters) may lead researchers to underestimate the true conflict-inducing effect of climate anomalies and other natural disasters.

#### 1.1 Intuition

To further facilitate the intuition of the two different types of equilibrium outcomes discussed in the model section, here I present two informal illustrations.<sup>3</sup> As common assumptions, suppose that (i) a climate disaster occurs with a certain probability; (ii) the region that a disaster hits most severely is also randomly determined; (iii) disasters lower political groups' military capabilities because they can directly damage military assets and have negative impacts on power projection capabilities by destroying infrastructures; and (iv) the affected

<sup>&</sup>lt;sup>3</sup>The following cases correspond to case (R), i.e., Case 1 below, and cases  $(E_1)$  and  $(E_1)$ , i.e., Case 2 below, respectively.

political groups will eventually recover from the costs of a disaster. The two cases below differ in only one aspect: the level of (a)symmetry in expected exposure to disasters.

Case 1 (Opportunistic aggression after a disaster). Consider two rival political groups, Group 1 and Group 2. They can be two sovereign states or different groups in a single country. Assume that the groups are geographically proximate and have similar levels of economic development, military capabilities, and resilience in social infrastructures. To make a comparison with Case 2 below easier, assume that both of them are in a disaster-prone region. If a natural disaster takes place, the two groups are expected to incur similar costs because they are equally vulnerable. We say that Groups 1 and 2 face symmetric exposure to disaster risks.

Now suppose that an extreme weather event hits the area in which Groups 1 and 2 are located. Further, because the distribution of damages arising from natural disasters is random, assume that Group 2 incurred disproportionately large costs and that the disaster did not cause large damage to Group 1. Recall the assumption that a disaster negatively affects groups' military capabilities. Because the disaster happened to hit Group 2 severely, Group 1 would find itself temporarily advantaged militarily. In this case, Group 1 can have the incentive for opportunistic aggression before Group 2 recovers from the severe damage. For later use, observe that this opportunistic conflict should erupt right after a disaster occurs in this case.

Case 2 (preemptive war before a disaster). Next, consider a different pair of hostile political groups, Group 1 and Group 2'. We think of Group 1 as located in the same location as Case 1. On the other hand, unlike Case 1, Group 2' is in a distant region and inherently more resilient to climate anomalies than Group 1 is. Because Group 1 is relatively more vulnerable to extreme weather events, we say that the groups face asymmetric risks of exposure to disasters. Suppose that Group 2 in Case 1 and Group 2' have identical attributes other than resilience to disaster risks.

In contrast to Case 1, consider a period of time when there is no disaster in the area. Group 1 knows that it is disproportionately vulnerable to disaster risks compared to its political rival, Group 2'. Thus, it *anticipates* that it can incur severe disaster costs in the future. Further, Group 1 expects that Group 2' may commit opportunistic aggression when a disaster crupts and the military balance of power rapidly shifts in favor of Group 2'. Predicting this risk, Group 1 has a preemptive motive to attack Group 2' before it actually incurs severe disaster costs.

Contrasting the two cases. Figure 1 highlights the contrast between them. The squares represent the regions in which Groups 1 and 2 or 2' are located. Groups 1 and 2 are geographically proximate (Case 1) and 1 and 2' are distant (Case 2). That is, Groups 1 and 2 face similar disaster risks, whereas Group 1 is inherently more vulnerable than Group 2. The solid arrows outside the square region denote the materialized disaster costs (Case 1) and the dashed ones represent expected damages imposed by future disasters (Case 2). The line widths of the arrows indicate the asymmetry of the damages.

We can consider such (a)symmetry in exposure risks to disasters as distributions of random variables. Suppose that a random variable Z with density  $f_1(Z)$  (Case 1) and  $f_2(Z)$ (Case 2) determines the relative disaster damage on the two groups, where a smaller (larger) value represents a greater disaster cost on Group 1 (2 or 2'). As Figure 1 illustrates, the distribution is highly symmetric in Case 1, whereas it is skewed in Case 2. In Case 1, because the expected disaster costs are roughly symmetric between the two groups, they do not have the preemptive motive in the absence of a disaster. However, because Z is random, it can be the case that its particular realization happens to be extreme. War is possible only in this circumstance in Case 1.

On the other hand, the graph of  $f_2(Z)$  is skewed (Figure 1). The density being larger for smaller Z indicates that Group 1 is more likely to incur severe damage from a disaster. Note that a conflict can still erupt right after an extreme climate event in this case as well.

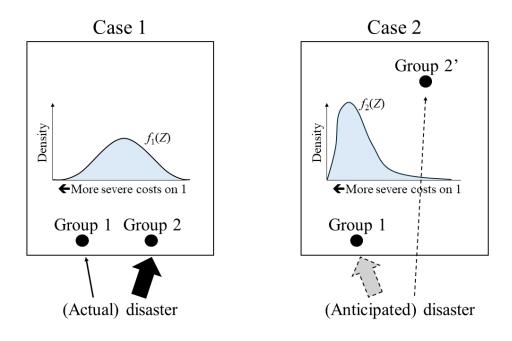


Figure 1: Conflict-prone conditions in the two illustrative cases

Nonetheless, because the relative disaster-related costs are randomly determined, a war may not ensue after it. Namely, if a particular weather event happened to impose roughly equal costs on the two rival groups, neither of them finds itself temporarily (dis)advantaged in terms of the military balance of power. In contrast, in the simple example of Case 2, Group 1 attacks Group 2' with probability one in the absence of a disaster because the former knows that  $f_2(Z)$  is skewed: in expectation, it will likely be militarily weaker in the future. Consequently, although conflict onset is possible in Case 2 both when a disaster has occurred and when it has not, war is strictly more likely in its absence.

This leads to an empirical implication. Suppose we want to estimate the effects of disasters on violent conflict with data on the timing of extreme weather events and conflict onsets. It is straightforward that the correlation between extreme climate events and conflicts should be positive in Case 1. On the other hand, it should be negative in Case 2 because the vulnerable group is strictly more likely to fight in the absence of such events. However,

as Case 2 shows, the expected asymmetric exposure to disasters is mainly responsible for conflict onset. Namely, disasters trigger conflict in *both* cases. Hence, failure to incorporate the dynamic in Case 2 might lead to underestimation of the conflict-inducing effects of natural disasters. The model presented below illustrates the core logic above in a more well-defined manner.

#### 1.2 Related Literature

This study contributes to the growing literature on extreme weather events and armed conflict.<sup>4</sup> In particular, I draw on the findings of a recent paper by Bas and McLean (2021) that the expectations of natural disasters can induce preemptive attacks and that conflicts are associated with disaster *risks*. While I draw on their notion of the expected effects of natural disasters, the model presented here differs in important ways. First, it allows recurrent disasters and recovery of the economy after them. Second, it also models the asymmetry in disaster costs as a random variable. These extensions make the disaster expectation mechanism a special case generated by a single model, which enables us to take the findings of Bas and McLean (2021) one step further and theoretically explain the source of mixed empirical results.

Both Roche et al. (2020) and this study extend Chassang and Padró i Miquel (2009). Whereas Roche et al. (2020) investigate the impact of changes in the distribution of rainfalls and economic shocks as a result of climate change, they assume that players share the same severity of those shocks. In contrast, the present model incorporates the asymmetric exposure to negative shocks to players' resources. Ide (2023) is also closely related in that he also focuses on the multiple effects of disasters on armed conflict. While he qualitatively assesses disasters' impacts on the intensity of ongoing conflicts, I develop a game-theoretic model that

<sup>&</sup>lt;sup>4</sup>For review, see Buhaug and von Uexkull (2021); Burke et al. (2015); Koubi (2019). Jun and Sethi (2021); Kikuta (2019) examine the opportunistic aggression caused by natural disasters.

explains the empirical results that might seem to contradict ostensibly.

The model is also related to the literature on costly conflicts due to dynamic shifts in power (e.g., Fearon, 2004; Krainin, 2017; Powell, 2004, 2006). A recent model by Little and Paine (2023) is of particular relevance. By assuming that, as with the present model, the probability that one group wins in war is randomly drawn each period, Little and Paine (2023) distinguish the sources of the threat of a challenger group into (i) the maximum probability of the challenger's victory in war and (ii) its mean (or the probability of the challenger being "strong"), and show that the combination of a larger maximum challenger threat and a smaller average threat is most prone to conflict. This paper departs by further distinguishing opportunistic and preemptive attacks. In the former, war occurs under a shock to the balance of power (i.e., disaster) when one player finds herself temporarily advantaged militarily. In the latter, players can also fight in the absence of a shock if one player is inherently vulnerable to it and has a preemptive motive to fight. The coexistence of the two distinct types of conflict enables us to systematically explain why some empirical studies find positive correlations between extreme weather events and conflict and others discover negative ones.

More broadly, this paper is related to the growing movement of Theoretical Implications of Empirical Models (TIEM). The TIEM approach aims to theoretically comprehend empirical findings (e.g., Bueno de Mesquita and Tyson, 2020; Slough, 2023, 2024; Wolton, 2019, 2021). One can situate the present paper in the literature in that, based on a theoretical model presented below, it proposes a new interpretation of the mixed empirical evidence on the causal effects of natural disasters and extreme weather events on violent conflict. It also points out the possibility that some empirical approaches, including the potential outcome framework that estimates the average treatment effect or the conditional average treatment

<sup>&</sup>lt;sup>5</sup>See also Benson and Smith (2023); Sawada (2024) for a similar dynamic, where the source of power shifts is external intervention. On the other hand, Smith (2019) develops a model in which such fluctuations in the balance of power are mitigated by arms transfers from an ally.

effect of natural disasters on conflict, might not always be suitable if those events generate rapid shifts in military power.

The remainder of this paper proceeds as follows. After formally presenting the two opposing cases by developing a simple infinite-horizon game, I draw a new empirical prediction from the model and assess if it explains patterns in data on armed conflicts and water scarcity in African countries. Next, I point out that the potential outcome framework might underestimate the effect of disasters on conflict risks. Then, based on this implication, I revisit the case of drought to reinterpret the seemingly contradictory results of some existing studies.

## 2 The Model

This paper develops a simple infinite horizon game that incorporates the two contrasting types of asymmetry in exposure to disasters. A key feature is that asymmetric risk in exposure is a necessary condition in the model. Thus, war on any equilibrium path is triggered by the actual occurrence or expectation of natural disasters that can impose disproportionate damage on one of the players.

## 2.1 Setup

Two players (e.g., rival political groups in the context of domestic conflict or neighboring states in the context of interstate conflict) 1 and 2 interact each period t = 1, 2, ... Both groups have a fixed amount of resources,  $\theta$ . At the beginning of each period, Nature determines the presence/absence of a natural disaster as a draw of an identically and independently distributed random variable D following a Bernoulli distribution with mean  $\pi$ : in each t, a disaster occurs (i.e.,  $D_t = 1$ ) with probability  $\pi$  and does not (i.e.,  $D_t = 0$ ) with probability  $1-\pi$ . We model asymmetric exposure to a disaster as another independently and identically

<sup>&</sup>lt;sup>6</sup>We call the period in which a natural disaster has occurred a "disaster period." Similarly, we label a period without a disaster as a "no-disaster period".

distributed random variable Z over the unit interval with mean  $\mu$ . Suppose that Z follows a distribution with a continuously differentiable cumulative distribution function F whose density is f. At a disaster period t, the materialized value of  $Z_t$ , denoted as  $z_t$ , discounts (i) the resources of Player 1 to  $z_t\theta$  and (ii) those of Player 2 to  $(1-z_t)\theta$ . Namely, after  $D_t=1$ , Nature determines the level of asymmetry in the damage imposed on each player.

After Nature's moves, players simultaneously decide whether to attack the other or not. In this model, we assume that a conflict is a unilateral act: war ensues when at least one player chooses to fight. If neither player fights, players receive a flow payoff equal to the amount of their wealth in the period ( $\theta$  when there is no disaster or  $z_t\theta$  and  $(1-z_t)$  when a disaster has erupted in the period), and the game proceeds to the next period.

When either player attacks the opponent, a game-ending war ensues. Its outcome is determined by the amount of players' resources: the probability that player i wins a war is

$$p_i^{\neg d} \equiv \frac{\theta}{2\theta}$$

$$= \frac{1}{2} \text{ (when a disaster did not occur); or}$$
 $p_1^{\mathsf{d}}(Z_t) \equiv \frac{Z_t \theta}{Z_t \theta + (1 - Z_t) \theta}$ 

$$= Z_t \text{ (when a disaster erupted in } t \text{) and}$$
 $p_2^{\mathsf{d}}(Z_t) \equiv 1 - p_1^{\mathsf{d}}(Z_t)$ 

$$= 1 - Z_t.$$

Because a war is costly, it discounts the amount of resources in the society by  $c \in (0,1)$ : the remaining resource is  $\theta(1-c)$  or  $2\theta(1-c)$  when war erupts in disaster and no-disaster periods, respectively. If a war ensues, the game ends and the winner receives all remaining resources in the society in the current period  $(\theta(1-c))$  or  $2\theta(1-c)$  and a long-term benefit from its dominance over resources. By a long-term benefit, we mean that the victor gains the entire pie  $2\theta$  that can be discounted in half with probability  $\pi$  for infinitely many periods.

Formally, the long-term payoff from dominance is:

$$\overline{\mathcal{V}} \equiv \mathbb{E}_{D,Z} \left[ \sum_{t=1}^{\infty} \delta^{t-1} \left( D_t \left( Z_t \theta + (1 - Z_t) \theta \right) + (1 - D_t) 2\theta \right) \right]$$

$$= \sum_{t=1}^{\infty} \delta^{t-1} \left[ \pi \theta + (1 - \pi) 2\theta \right]$$

$$= \frac{\theta (2 - \pi)}{1 - \delta},$$

where  $\delta \in (0,1)$  is a common discount factor.

Figure 2 summarizes the timeline of the game. We assume complete information. To focus on interesting cases in which disasters affect players' equilibrium strategies, we introduce the following assumption which excludes trivial equilibria such as one in which players attack the opponent after any history.

**Assumption 1.** Players do not attack the other one when they are indifferent between attacking and not attacking.

This assumption also enables us to focus on pure strategies. Moreover, we introduce another assumption to render the model tractable.

**Assumption 2.** Consider a pair of different distributions of  $Z_t$ . Then, we assume that they are identical except for one parameter.

For example, in numerical examples in the next section, I use  $Z_t \sim \text{Beta}(\alpha, \text{constant})$  and vary the value of  $\alpha$ , fixing the type of distribution and one of the two parameters. Our solution concept is pure-strategy (stationary) Markov perfect equilibrium (MPE).<sup>7</sup> That is, a strategy in this model is a mapping from the state space  $\{0,1\} \times [0,1]$  to the action space  $\{\text{Attack}, \text{Not}\}$ .

<sup>&</sup>lt;sup>7</sup>Whereas we focus on MPE in the analysis section, we use subgame perfect equilibrium for the preliminary results (Remarks 1 and 2) presented below.

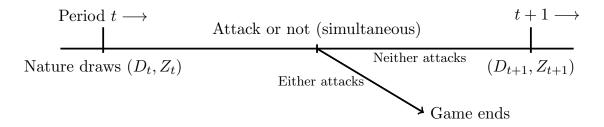


Figure 2: Timeline

#### 2.2 Comments on the Model

Before analyzing the model, it is useful to discuss the interpretations of its key features. First, the parameter  $\mu \equiv \mathbb{E}[Z]$  represents the *expected* asymmetry in players' exposure to the disaster. More specifically, it captures the region-specific vulnerabilities that amplify the costs caused by natural disasters. For example, coastal areas may be more vulnerable to hurricanes (due to storm surges) and post-earthquake tsunamis. Some mountainous regions may also face a higher risk of landslides after excessive rainfall or earthquakes. In the model,  $\mu$  close to 1/2 implies that the two groups have similar vulnerabilities to natural disasters. On the other hand, a small or large value of  $\mu$  means that one of the players is more vulnerable to climate risks. A specific draw of  $Z_t$ , i.e., denoted as  $z_t$ , represents the realized asymmetric exposure to a disaster, which varies depending on which region the disaster hits most severely.

Second, disasters matter militarily by shifting the balance of power between players. This process takes place through the following two steps. First, the realized damage of a disaster  $z_t$  discounts the players' resources. Second, the affected amounts of resources determine the outcome of conflict via the probability of victory  $p_i^{\mathbf{d}}(z_t)$ , which is either  $z_t$  or  $1 - z_t$ .

Third, in order to examine the possible causal paths from natural disasters to armed conflict, the possibility of a disaster with asymmetric negative impacts is a necessary condition for war in this model. That is, as the following two results show, the game always proceeds peacefully without (i) the risk of natural disasters and (ii) asymmetric exposure to them.

**Remark 1.** Suppose  $\pi = 0$ . Then, under Assumption 1, the unique subgame perfect equilib-

rium (SPE) is a strategy profile where both players never attack the opponent.

Remark 2. Suppose  $\pi \in (0,1)$  but  $z_t = 1/2$  for any t. That is, the damage from a disaster is always symmetric. Then, under Assumption 1, the unique SPE is a strategy profile where both players never attack the opponent.

These results are straightforward. Consider Remark 1. Because war is costly and there is no asymmetric information or a sudden power shift, a unilateral attack cannot be optimal after any history, which is in line with standard models of armed conflict (Fearon, 1995). The logic behind Remark 2 is also intuitive: the complete symmetry in exposure to a disaster prevents the temporary advantage that incentivizes aggression.<sup>8</sup> The model in which war can occur only under some risk of natural disasters with asymmetric exposure allows us to theoretically identify the effects of those extreme events on the risk of armed conflict.

Fourth, the assumption that the distribution F and, in particular, its mean  $\mu$  are common knowledge establishes a scope condition of this model. Namely, we focus on relatively foreseeable disasters because the assumption implies that players can evaluate and take into account future disaster risks. Examples include seasonal climate anomalies such as storms, floods, and droughts. On the other hand, other natural disasters that are difficult to anticipate, including earthquakes, are beyond the scope.

Fifth, the negative impact of disasters on entire social welfare is fixed. Namely, any extreme weather event always halves resources in the society composed of players 1 and 2. While the distribution of discounted resources varies according to  $Z_t$ , a disaster cannot make the total amount of resources more or less than 1/2. This simplifying assumption makes clear how asymmetric exposure to extreme weather events, rather than their magnitude itself, affects players' incentive for maintaining intergroup peace and gambling on a costly

<sup>&</sup>lt;sup>8</sup>In the model of Chassang and Padró i Miquel (2009), war erupts under symmetric economic shocks because they assume the presence of offensive advantage: if only one player launches a unilateral attack, her probability of victory is greater than 1/2, which renders the outcome more conflict-prone. The war outcome in the present model is determined by the asymmetry in resources rather than by who started the war.

war.

## 3 Analysis

This section presents two different equilibria in which realized and unrealized (expected) asymmetric costs of natural disasters cause armed conflict. The disproportionate vulnerability to natural disasters has two opposing effects depending on whether (i) the cost of a disaster has actually materialized following its outbreak or (ii) a disaster is expected in the future but has not occurred yet. In the first case, a player can attack the other to exploit the opponent's temporary vulnerability arising from the latter's disproportionate damage of a disaster in the current period. In the second case, a player has the incentive to fight in a no-disaster period when she expects she will become disproportionately vulnerable in the future.

## 3.1 War Caused by *Realized* Disproportionate Damage

First, I present an equilibrium in which a conflict erupts as a result of opportunistic aggression by a player who is temporarily advantaged in a disaster period. To derive the equilibrium, we consider the following stationary strategies:

- (R-I): In a disaster period, i.e., t such that  $D_t = 1$ , either one of the players attacks the other if the realized cost of the disaster is disproportionately incurred.
  - When  $z_t$  is larger than a threshold  $\overline{z}^{R}(\mu)$  given  $\mu$ , Player 1 attacks 2.
  - When  $z_t$  is smaller than a threshold  $\underline{z}^{\mathtt{R}}(\mu)$  given  $\mu$ , Player 2 attacks 1.
- (R-II): In a no-disaster period, i.e., t such that  $D_t = 0$ , neither player fights.

Slightly abusing notation, we often write the threshold values as  $\overline{z}^R$  and  $\underline{z}^R$  instead of  $\overline{z}^R(\mu)$  and  $\underline{z}^R(\mu)$ , which are functions of  $\mu$  as we discuss below.

When we assume the players follow the above strategies, on the equilibrium path, a war occurs if the damage inflicted by a disaster in the current period is highly asymmetric. The following result specifies the condition under which they are an equilibrium.

**Proposition 1** (Realized asymmetric exposure). Consider an interval  $M^R \equiv [\underline{\mu}^R, \overline{\mu}^R]$ , where the thresholds  $\underline{\mu}^R$  and  $\overline{\mu}^R$  are defined below. When  $\mu \in M^R$ , the strategies (R-I) and (R-II) constitute an MPE.

• Given  $\mu \in M^R$ , the thresholds above/below which one player attacks the other when  $D_t = 1$  are given as the solution to the following system of equations.

$$\begin{cases}
\overline{z}^{R}(\mu) = \delta \cdot \frac{(1-\pi) + \pi \left(\mu + \left(\int_{0}^{\underline{z}^{R}(\mu)} z dF(z) + \int_{\overline{z}^{R}(\mu)}^{1} z dF(z)\right) \left[\delta \frac{2-\pi}{1-\delta} - c\right]\right)}{(1-\delta \left(1-\pi \left(1-\Delta_{F}\left(\overline{z}^{R}(\mu), \underline{z}^{R}(\mu)\right)\right)\right)) \left[\delta \frac{2-\pi}{1-\delta} - c\right]} \\
\begin{cases}
(1-\pi) + \pi \left(1-\mu + \left[1-\Delta_{F}\left(\overline{z}^{R}(\mu), \underline{z}^{R}(\mu)\right) - \left(\int_{0}^{\underline{z}^{R}(\mu)} z dF(z) + \int_{\overline{z}^{R}(\mu)}^{1} z dF(z)\right)\right] \left[\delta \frac{2-\pi}{1-\delta} - c\right]\right)} \\
(1-\delta \left(1-\pi \left(1-\Delta_{F}\left(\overline{z}^{R}(\mu), \underline{z}^{R}(\mu)\right)\right)\right)) \left[\delta \frac{2-\pi}{1-\delta} - c\right]
\end{cases}, (1)$$

where  $\Delta_F(b, a) \equiv F(b) - F(a)$  with  $a \leq b$ .

The maximum and minimum of M<sup>R</sup> are, respectively, given as part of the solution to a
system of three equations composed of each of the following equations and two equations
in (1) with μ = μ̄<sup>R</sup> or μ = μ̄<sup>R</sup>.

$$\begin{split} \overline{\mu}^{R} &= \frac{1}{2} + \delta \frac{2-\pi}{1-\delta} \left( \int_{0}^{\underline{z}^{R}(\overline{\mu}^{R})} \frac{1}{2} - z \mathrm{d}F(z) + \int_{\overline{z}^{R}(\overline{\mu}^{R})}^{1} \frac{1}{2} - z \mathrm{d}F(z) \right) \\ &+ c \left( \int_{0}^{\underline{z}^{R}(\overline{\mu}^{R})} z \mathrm{d}F(z) + \int_{\overline{z}^{R}(\overline{\mu}^{R})}^{1} z \mathrm{d}F(z) + \frac{1-\delta}{\delta \pi} \right) \quad and \\ \underline{\mu}^{R} &= \frac{1}{2} + \delta \frac{2-\pi}{1-\delta} \left( \int_{0}^{\underline{z}^{R}(\underline{\mu}^{R})} \frac{1}{2} - z \mathrm{d}F(z) + \int_{\overline{z}^{R}(\underline{\mu}^{R})}^{1} \frac{1}{2} - z \mathrm{d}F(z) \right) \\ &- c \left( \int_{0}^{\underline{z}^{R}(\underline{\mu}^{R})} 1 - z \mathrm{d}F(z) + \int_{\overline{z}^{R}(\underline{\mu}^{R})}^{1} 1 - z \mathrm{d}F(z) + \frac{1-\delta}{\delta \pi} \right). \end{split}$$

We denote this equilibrium by (R). Note that war can erupt only in disaster periods on the equilibrium path. That is, peace sustains as long as extreme asymmetry in players' resources does not arise from a natural disaster. Conversely, war occurs when highly disproportionate exposure to an extreme weather event generates an opportunistic motive of the temporarily advantaged player. Thus, the equilibrium probability of conflict is (i) zero in a given nodisaster period and (ii) positive in a disaster period.

This result is intuitively straightforward. When  $\mu$  is in the interval  $M^{\rm R}$ , unlike the second case presented below, the players' inherent resilience to natural disasters is relatively symmetric. This means that the military parity between the players is likely to remain even if a disaster occurs. Because, on average, the military parity is not likely to fluctuate under an extreme weather event, neither player obtains a temporary military advantage (and opportunistic motive for war) unless such a balance is disturbed by a disaster that imposes disproportionately high costs on one of them. We shall come back to this point to compare this equilibrium and the one introduced below.

The key assumption sustaining the above equilibrium is that the economy of the society will recover from the negative economic shock caused by destructive disasters in the next period (Chassang and Padró i Miquel, 2009; Kikuta, 2019). If post-disaster humanitarian relief helps the players rebuild their economy and military capabilities, the one who incurred disproportionately *small* damage faces a closing window of opportunity: she has the incentive to attack the temporarily vulnerable rival before parity in players' military power is restored.<sup>9</sup>

Figure 3 provides an example. The horizontal axis and vertical axis represent the value of  $\mathbb{E}[Z_t] = \mu$  and the density of  $Z_t$ , respectively. When c = 0.55,  $\delta = 0.5$ ,  $\pi = 0.1$ , and  $Z_t \sim \text{Beta}(10, 10)$  (i.e.,  $\mu = 0.5$ ), we have  $\underline{z}^{\mathbb{R}}(\mu = 0.5) \approx 0.3$  and  $\overline{z}^{\mathbb{R}}(\mu = 0.5) \approx 0.7$ . Intuitively, on this equilibrium path, each player attacks the other in period t such that  $D_t = 1$  if she has at least a seventy percent chance of winning. To compare the results below,

<sup>&</sup>lt;sup>9</sup>Jun and Sethi (2021); Kikuta (2019) provide empirical support for this logic.

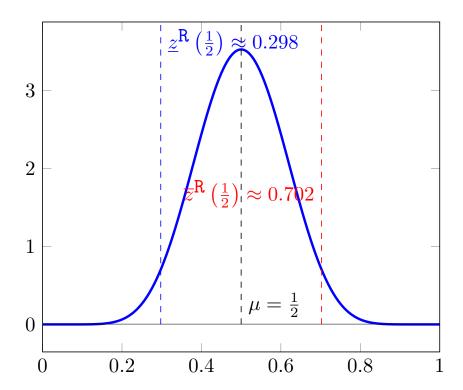


Figure 3: Thresholds in (R)  $(c = 0.55, \delta = 0.5, \pi = 0.1, Z_t \sim \text{Beta}(10, 10))$ 

note again that neither has the incentive to fight in a no-disaster period.

## 3.2 War Caused by *Expected* Disproportionate Damage

Next, we consider the conditions under which a war occurs due to an inherently vulnerable player's fear of future exploitation. To present equilibria that illustrate this case, consider the following stationary strategies.

- (E-I): In a disaster period, i.e., t such that  $D_t = 1$ , either one of the players attacks the other if the realized cost of the disaster is disproportionately incurred.
  - When  $z_t$  is larger than a threshold  $\overline{z}^{\mathtt{E}}(\mu)$ , Player 1 attacks 2.
  - When  $z_t$  is smaller than a threshold  $\underline{z}^{\mathtt{E}}(\mu)$ , Player 2 attacks 1.

(E-II): In a no-disaster period, i.e., t such that  $D_t = 0$ , the more vulnerable player attacks the other.

In the strategies above, notice that war immediately ensues if there is no disaster. The following proposition provides the conditions under which (E-I) and (E-II) constitute two equilibria with a different player who attacks at a no-disaster period.

**Proposition 2** (Expected asymmetric exposure). Consider the union of two half-open intervals  $M^E \equiv [0, \underline{\mu}^E) \cup (\overline{\mu}^E, 1]$ , where the thresholds  $\underline{\mu}^E$  and  $\overline{\mu}^E$  are defined below. When  $\mu \in M^E$ , the strategies (E-I) and (E-II) constitute an MPE.

- In no-disaster periods, Player 1 attacks Player 2 when  $\mu < \underline{\mu}^E$  and Player 2 attacks Player when  $\mu > \overline{\mu}^E$ .
- Given  $\mu \in M^E$ , the thresholds  $\overline{z}^E(\mu)$  and  $\underline{z}^E(\mu)$  are given as the solution to the following system of equations.

$$\begin{cases}
\overline{z}^{E}(\mu) = \delta \cdot \frac{\left[ (1-\pi) \left[ \frac{1-\delta\pi/2}{1-\delta} - c \right] + \left[ \frac{\pi \left( \mu + \left( \int_{0}^{\underline{z}^{E}(\mu)} z dF(z) + \int_{\overline{z}^{E}(\mu)}^{1} z dF(z) \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right) \right]}{\left( 1 - \delta\pi \Delta_{F} \left( \overline{z}^{E}(\mu), \underline{z}^{E}(\mu) \right) \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right]} \\
\begin{cases}
\left[ (1-\pi) \left[ \frac{1-\delta\pi/2}{1-\delta} - c \right] + \left[ \frac{1-\Delta_{F} \left( \overline{z}^{E}(\mu), \underline{z}^{E}(\mu) \right)}{1-\delta} \left( \frac{1-\mu}{1-\delta} - c \right] + \left[ \frac{1-\Delta_{F} \left( \overline{z}^{E}(\mu), \underline{z}^{E}(\mu) \right)}{1-\delta} \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right] \right] \\
\underline{z}^{E}(\mu) = 1 - \delta \cdot \frac{\left[ (1-\pi) \left[ \frac{1-\delta\pi/2}{1-\delta} - c \right] + \left( \frac{1-\delta\pi/2}{1-\delta} - c \right] \right]}{\left( 1 - \delta\pi\Delta_{F} \left( \overline{z}^{E}(\mu), \underline{z}^{E}(\mu) \right) \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right]} .
\end{cases} (2)$$

• The values of  $\overline{\mu}^E$  and  $\underline{\mu}^E$  are, respectively, given as part of the solution to the system of three equations composed of each of the following equations and two equations in (2)

with  $\mu = \overline{\mu}^E$  or  $\mu = \mu^E$ .

$$\overline{\mu}^{E} = \frac{1}{2} + \delta \frac{2 - \pi}{1 - \delta} \left( \int_{0}^{\underline{z}^{E}(\overline{\mu}^{E})} \frac{1}{2} - z \mathrm{d}F(z) + \int_{\overline{z}^{E}(\overline{\mu}^{E})}^{1} \frac{1}{2} - z \mathrm{d}F(z) \right)$$

$$+ c \left( \int_{0}^{\underline{z}^{E}(\overline{\mu}^{E})} z \mathrm{d}F(z) + \int_{\overline{z}^{E}(\overline{\mu}^{E})}^{1} z \mathrm{d}F(z) + \frac{1 - \delta}{\delta \pi} \right)$$

$$\underline{\mu}^{E} = \frac{1}{2} + \delta \frac{2 - \pi}{1 - \delta} \left( \int_{0}^{\underline{z}^{E}(\underline{\mu}^{E})} \frac{1}{2} - z \mathrm{d}F(z) + \int_{\overline{z}^{E}(\underline{\mu}^{E})}^{1} \frac{1}{2} - z \mathrm{d}F(z) \right)$$

$$- c \left( \int_{0}^{\underline{z}^{E}(\underline{\mu}^{E})} 1 - z \mathrm{d}F(z) + \int_{\overline{z}^{E}(\underline{\mu}^{E})}^{1} 1 - z \mathrm{d}F(z) + \frac{1 - \delta}{\delta \pi} \right).$$

Denote these equilibria by  $(E_1)$  when  $\mu < \underline{\mu}^E$  and  $(E_2)$  when  $\mu > \overline{\mu}^E$ , respectively. In contrast to the first case (R), these  $(E_1)$  and  $(E_2)$  depict how expected (or inherent) asymmetry in disaster costs leads to war. To see this, suppose  $\mu$  is geographically vulnerable to disaster risks, i.e., case  $(E_1)$ , so that Player 1 attacks 2 when  $D_t = 0$  for sure. Her incentive to fight arises in two steps. First, as in case (R) above, observe that the opportunistic motive for aggression is also at work here. Because we have assumed that  $\mu$  is small (by case  $(E_1)$ ), it is likely that Player 2 becomes temporarily advantaged if there is a disaster.

Second, anticipating this, Player 1 is facing a fear of future aggression and exploitation by the opponent (Bas and McLean, 2021). That is, Player 1 knows that Player 2 will face the temptation to fight in a disaster period if a realized  $z_t$  is very small. If Player 1 were to acquiesce to this possibility, she would not win the war because her probability of victory,  $p_i^d(z_t) = z_t$ , is also very small. As a result, the inherent vulnerability of Player 1 generates a preemptive motive: she has the incentive to attack Player 2 in order to fight under a relatively favorable balance of power.

Figure 4 shows an example when c = 0.55,  $\delta = 0.5$ ,  $\pi = 0.1$ , and  $Z_t \sim \text{Beta}(10/9, 10)$  (i.e.,  $\mu = 0.1$ ). Observe that the values of the parameters are identical to those in Figure 3 except for the first parameter of the Beta distribution. Compared to the symmetric case (R), the

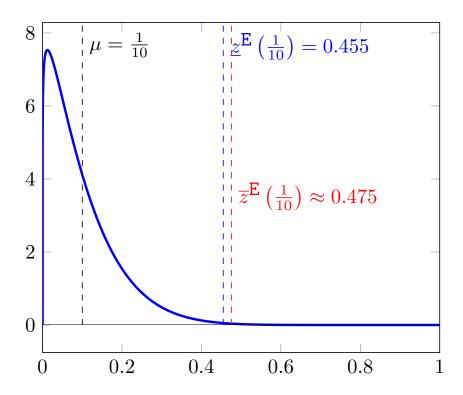


Figure 4: Thresholds in  $(E_1)$   $(c = 0.55, \delta = 0.5, \pi = 0.1, Z_t \sim \text{Beta}(10/9, 10))$ 

region of  $\mu$  under which war occurs in a disaster period is larger, i.e.,  $[0,0.455) \cup (0.475,1]$ . The strategic logic is as follows. First, the inherently vulnerable Player 1 expects that she will likely be disadvantaged and that Player 2 will have an opportunistic motive for conflict once a disaster erupts. Thus, incorporating this risk, Player 1 is willing to fight even when she does not have a military advantage in a disaster period. Second, Player 2 anticipates Player 1's preemptive motive. Therefore, although Player 2 should be militarily advantaged in a disaster period on average (i.e.,  $\mu = 0.1$ ), she is also willing to fight even when her actual advantage is not very large.

<sup>10</sup> Notice  $p_1^{\mathsf{d}}\left(\overline{z}^{\mathsf{E}}(\mu=0.1)\right) \approx 0.475 < p_1^{\neg d} = 0.5$ . In other words, Player 1 can launch opportunistic aggression when she is slightly disadvantaged militarily.

<sup>&</sup>lt;sup>11</sup>Compare  $p_2^d(\mu = 0.1) = 0.9$  and  $p_2^d(\underline{z}^E(\mu = 0.1)) = 0.545$ .

#### 3.3 Summary and Comparison

The result below shows that (R), (E<sub>1</sub>), and (E<sub>2</sub>) exhaust all possible equilibria for any value of  $\mu$ . Because we consider multiple CDFs of  $Z_t$  with different means, denote a CDF whose mean is  $\mu$  by  $F_{\mu}$ .<sup>12</sup>

**Proposition 3.** Fix all parameters other than  $\mu$ , and suppose  $\overline{\mu}^R$  and  $\underline{\mu}^R$  satisfy

$$c < \min \left\{ \begin{aligned} &\frac{\frac{1}{2} - \delta \frac{2 - \pi}{1 - \delta} \left( \int_{0}^{\underline{z}^{R}(\overline{\mu}^{R})} \frac{1}{2} - z \mathrm{d}F_{\overline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\overline{\mu}^{R})}^{1} \frac{1}{2} - z \mathrm{d}F_{\overline{\mu}^{R}}(z) \right)}{\int_{0}^{\underline{z}^{R}(\overline{\mu}^{R})} z \mathrm{d}F_{\overline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\overline{\mu}^{R})}^{1} z \mathrm{d}F_{\overline{\mu}^{R}}(z) + \frac{1 - \delta}{\delta \pi}} \\ &\frac{\frac{1}{2} + \delta \frac{2 - \pi}{1 - \delta} \left( \int_{0}^{\underline{z}^{R}(\underline{\mu}^{R})} \frac{1}{2} - z \mathrm{d}F_{\underline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\underline{\mu}^{R})}^{1} \frac{1}{2} - z \mathrm{d}F_{\underline{\mu}^{R}}(z) \right)}{\int_{0}^{\underline{z}^{R}(\underline{\mu}^{R})} z \mathrm{d}F_{\underline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\underline{\mu}^{R})}^{1} z \mathrm{d}F_{\underline{\mu}^{R}}(z) + \frac{1 - \delta}{\delta \pi}} \right\}. \end{aligned}$$

Then, there exists a unique partition  $\{0,\underline{\mu}^{\mathtt{R}},\underline{\mu}^{\mathtt{E}},\overline{\mu}^{\mathtt{E}},\overline{\mu}^{\mathtt{R}},1\}$  such that

- when  $\mu < \underline{\mu}^{\mathtt{R}},$  the unique equilibrium is  $(\mathtt{E}_{1}),$
- when  $\mu \in \left[\underline{\mu}^{\mathtt{R}},\underline{\mu}^{\mathtt{E}}\right)$ , (R) and (E\_1) constitute equilibria,
- when  $\mu \in \left[\underline{\mu}^{\mathtt{E}}, \overline{\mu}^{\mathtt{E}}\right]$ , the unique equilibrium is (R),
- when  $\mu \in (\overline{\mu}^{\mathtt{E}}, \overline{\mu}^{\mathtt{R}}]$ , (R) and (E2) constitute equilibria, and
- when  $\mu>\overline{\mu}^{\text{R}},$  the unique equilibrium is (E2),

Figure 5 illustrates the result. Parameters are fixed as c = 0.08,  $\delta = 0.5$ , and  $\pi = 0.1$ .  $Z_t$  follows Beta( $\alpha$ , 10), and  $\mu$  takes different values as  $\alpha$  varies. In this example, a unique equilibrium exists when  $\mu$  has a middling value (case (R)) and small or large (cases (E<sub>1</sub>)

<sup>&</sup>lt;sup>12</sup>By Assumption 2, recall that the functional form of each  $F_{\mu}$  is still identical.

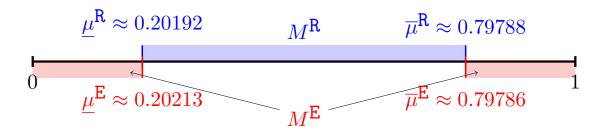


Figure 5: Intervals of  $\mu$  and equilibrium ( $c=0.08,\,\delta=0.5,\,\pi=0.1,\,Z_t\sim \mathrm{Beta}(\alpha,10)$ )

and  $(E_2)$ ). There are also small regions of equilibrium multiplicity. Approximately speaking, when  $\mu \in [0.20192, 0.20213)$ , both cases (R) and  $(E_1)$  constitute equilibria. Similarly, when  $\mu \in (0.79786, 0.79788]$ , cases (R) and  $(E_2)$  are supported as MPE.

We now compare the equilibrium outcomes of the two types of equilibria: (R) on the one hand and  $(E_1)$  and  $(E_2)$  on the other. First, observe that conflict occurs in both disaster and no-disaster periods in cases  $(E_1)$  and  $(E_2)$ . In a disaster period, because a mechanism similar to one in case (R) (i.e., opportunistic motive) is at work, conflict erupts with a positive probability. In a no-disaster period, recall that war never occurs in case (R). On the other hand, however, because the vulnerable player expects to be disadvantaged in the future in cases  $(E_1)$  and  $(E_2)$ , she preemptively attacks the other with probability one in a no-disaster period. Thus, in the cases of asymmetric inherent disaster risks, i.e.,  $(E_1)$  and  $(E_2)$ , war is strictly more likely in the absence of a disaster, whereas it can erupt in both types of periods.

For later use in the following sections, I formally summarize this comparison. Define  $Y_t^{\mathsf{game}} = \mathbb{1}\{\text{Conflict occurs at time } t \text{ on the equilibrium path}\}$  and interpret it as a random variable generated by an equilibrium of the model. Further, denote  $\mu = \mu^{\mathtt{R}}$  when  $\mu \in M^{\mathtt{R}}$  and  $\mu = \mu^{\mathtt{E}}$  when  $\mu \in M^{\mathtt{E},13}$  Then, we obtain the straightforward result below.

Corollary 1. For any t in each equilibrium, we have

$$(i) \ \Pr \left( Y_t^{\mathit{game}} = 1 | D_t = 1, \mu^{\mathit{R}} \right) > \Pr \left( Y_t^{\mathit{game}} = 1 | D_t = 0, \mu^{\mathit{R}} \right) = 0, \ and$$

<sup>&</sup>lt;sup>13</sup>For simplicity, assume equilibrium  $(E_1)$  or  $(E_2)$  will be played when  $\mu \in M^{\mathbb{R}} \cap M^{\mathbb{E}}$ .

(ii) 
$$\Pr(Y_t^{\text{game}} = 1 | D_t = 1, \mu^E) < \Pr(Y_t^{\text{game}} = 1 | D_t = 0, \mu^E) = 1.$$

We shall discuss the implications of this theoretical result in the following sections. Specifically, in the next section, I derive a novel prediction from it and present suggestive evidence to connect data and the theory. Then, given the corollary, I propose theoretical implications for empirical research to make sense of the seemingly mixed results in the literature.

# 4 Empirical Implications of the Theoretical Model: The Case of Droughts

Here, I present an empirical exercise to draw empirical implications from the asymmetric-exposure model. We focus on a specific type of climate anomaly: drought. This is because, in addition to the state that social scientists have yet to reach a consensus on the effect of droughts on conflict, we will also examine the case of drought (from a different perspective) in the next section. To begin with, I briefly discuss the datasets and connect them to the model. Next, I draw an empirical implication from Corollary 1 and offer suggestive evidence based on the data.

## 4.1 Data and Empirical Analogues to the Model Features

Before introducing data, observe that the key parameter in the model  $\mu$  is a dyadic feature. To see this, recall the hypothetical examples in the introduction. Let Group 1 be the same in Cases 1 and 2. Although Groups 1, 2, and 2' are in the same region (the same country in the context of intrastate conflict), the level of asymmetry in disaster risks between Groups 1 and 2 is different from that between Groups 1 and 2'. This implies that highly aggregated data may not be able to capture the dyadic characteristics of the model.

To incorporate the dyadic nature, we use two sources of geo-referenced data: Armed Conflict Location and Event Data (ACLED, Raleigh et al., 2023) and the Palmer Drought Severity Index (PDSI, Dai et al., 2004). The ACLED provides event-level data on political unrest that occurred in or after 1997. Because we are interested in armed conflict (as opposed to, say, nonviolent demonstrations), we also restrict our attention to observations in the ACLED whose event\_type variable is coded as "Battles". It also specifies the identity of the involved parties in a given conflict event and classifies the type of the group (e.g., state forces; a rebel group). The PDSI dataset assigns the level of water scarcity/abundance to each  $2.5^{\circ} \times 2.5^{\circ}$  grid cell. A PDSI score takes a value in [-10, 10], where a higher (lower) value indicates water abundance (scarcity). The monthly dataset covers from 1850 to 2018. I attach the corresponding PDSI score to each ACLED event.

We focus on conflict events in African countries for two reasons. First, Africa is a favorable case in Salehyan and Hendrix (2014) (in the sense that their subsample of African countries supports their argument strongly) that we critically discuss in the next section. Thus, although the goal of the empirical exercise below is not to falsify their findings, if it still supports the asymmetric-exposure theory in their "favorite" case, then it would suggest that the findings of Salehyan and Hendrix (2014) are a special case of the theory. Second, focusing on Africa mitigates the risk of biased inferences. Rosvold and Buhaug (2021) point out the possibility that cross-continent comparisons of geo-coded data might lead to biases because of different qualities in reporting by region. Because richer regions tend to have greater capabilities of reporting disaster and conflict events, focusing on a specific (though still diverse) region mitigates the risk of bias. Consequently, our empirical exercise covers conflict events and the levels of water abundance in Africa from 1997 to 2018.

Using the above data, we now define empirical analogues to variables/parameters in the game-theoretic model. Because we are interested in the implications of Corollary 1, we want to relate  $Y_t^{\text{game}}$ ,  $D_t$ , and  $\mu$  to data. First, define  $Y_{dt}^{\text{data}} \in \{0,1\}$  as a variable that takes

the value of one when dyad d of two belligerent groups had a conflict event at time t and zero otherwise. It is important to note that, whereas the ACLED dataset provides georeferenced and detailed information about political violence and the parties involved, the unit of observation in the dataset is a conflict event rather than, say, country-year. This implies that the ACLED data essentially presents the cases of  $Y_{dt}^{\text{data}} = 1$ . In other words, we are unable to directly compare the observations that take  $Y_{dt}^{\text{data}} = 1$  and those with  $Y_{dt}^{\text{data}} = 0$ . Although this nature might lead to an issue of selection when we analyze the dataset, I draw a theoretical prediction to avoid this issue below.

Second, we interpret a smaller value of PDSI as the presence of drought. Specifically, we define the PDSI score in the previous month as the severity of drought at the time of conflict in dyad d at time t.<sup>14</sup> Denote it by PDSI<sub>d,t-1</sub>. Note that this is a continuous variable, unlike  $D_t$  which represents the presence/absence of a disaster in the model. Namely, a higher value of PDSI<sub>d,t-1</sub> is an empirical analogue to  $D_t = 0$  because it implies water abundance, whereas a smaller PDSI<sub>d,t-1</sub> is analogous to  $D_t = 1$  (i.e., presence of drought) because it stands for water scarcity.

Third, we are interested in the level of asymmetry in disaster risks of dyad d. Although this is the key parameter in the theory ( $\mu$  in the model), it is at least challenging to measure the relative risks of disaster exposure for every dyad of all politically relevant groups in African countries and assign it to each dyad. I assume the following statement to derive an informative analogue to  $\mu$  from the ACLED dataset.

**Assumption 3.** An intrastate conflict involving the government as one of the belligerents tends to be between groups with asymmetric disaster risks than a conflict involving only non-state actors.

In other words, given that two groups are engaged in a conflict, we interpret that they

<sup>&</sup>lt;sup>14</sup>The one-month lag guarantees that the climate condition in a certain region proceeds the occurrence of conflict in the location.

face a symmetric risk of exposure to disasters if the types of the involved parties are similar. Conversely, they tend to have asymmetric disaster risks when one side of the parties is part of the government forces and the other is not. Though an imperfect measure, it is natural to assume that, on average, government forces tend to be more resilient to disasters than rebel groups are.<sup>15</sup>

Under this assumption, we reinterpret  $\mu$  (given parameter in the model) as a random variable. For later use, let  $\mu^{RV} \in [0, 1]$  a random variable that represents the level of asymmetry in disaster risks for two relevant groups.<sup>16</sup> As an empirical analogue of  $\mu^{RV}$  in the ACLED dataset, define a binary variable  $gov_{dt} \in \{0, 1\}$  that indicates if (i) an incident involved the government forces or (ii) both sides were non-state actors:

$$\operatorname{\mathsf{gov}}_{dt} \equiv \mathbbm{1} \left\{ egin{align*} & \text{One of the belligerents in an incident} \\ & \text{in dyad } d \text{ at time } t \text{ is state forces} \\ & \end{array} \right\}.$$

Given the definition of  $gov_{dt}$  and Assumption 3, we say dyad d that had a conflict event at time t faces asymmetric disaster risks when  $gov_{dt} = 1$  and symmetric risks when  $gov_{dt} = 0$ .<sup>17</sup> Table 1 summarizes the empirical analogues to the model features.

<sup>&</sup>lt;sup>15</sup>One possible problem is selection effect: rebel groups that have enough material capabilities to fight government forces may also be resilient. However, relatively weak rebel groups can still continue armed struggles with the (more powerful) government in some environments. For example, conflicts in locations distant from the capital tend to last longer because government control in those regions tends to be weaker (Buhaug et al., 2009). Moreover, even weaker groups may be able to endogenously render their armed struggle last longer by adopting guerrilla tactics (Qiu, 2022).

 $<sup>^{16}</sup>$ Recall that  $\mu$  is an exogenous parameter in the game. However, it is also natural to think of the asymmetry in inherent disaster risks between two rival political groups as randomly distributed among dyads. Here, we take this interpretation to show the connection between the theory and data.

<sup>&</sup>lt;sup>17</sup>To distinguish conflicts in symmetric and asymmetric dyads as clearly as possible, I exclude events between (i) two state forces (e.g., different fractions in military forces in the same country) and (ii) state forces and an external group (e.g., international conflict).

	Model	Empirical analogue	Note
Conflict	$Y_t^{\mathtt{game}}$	$Y_{dt}^{\mathtt{data}} \in \{0,1\}$	$Y_{dt}^{\mathtt{data}} = 1 \text{ for all } dt \text{ in ACLED}$
Disaster	$D_t$	$PDSI_{d,t-1} \in [-10,10]$	Smaller $PDSI_{d,t-1}$ stands for $D_t = 1$ (drought)
Asymmetry	$\mu$	$\mathtt{gov}_{dt} \in \{0,1\}$	$\mu$ reinterpreted as a random variable, $\mu^{RV}$

Table 1: Empirical analogues to the model features

#### 4.2 Prediction and Results

Given the empirical analogues defined above, we now connect the theory and data. Despite some limitations, such as  $Y_{dt}^{\text{data}}$  being one for all dt and  $\text{gov}_{dt}$  being a coarse measure of  $\mu$ , we are still able to draw an empirical implication from the model and assess it with the data. To this end, recall that we have reinterpreted  $\mu$  (which was an exogenously given parameter in the game-theoretic model) as a random variable. Let  $\Pr(\mu^{\text{RV}} \in M^{\text{E}}) \in (0,1)$ , and suppose that  $\mu^{\text{RV}}$  and  $D_t$  are independent. Then, a direct application of Bayes' rule to Corollary 1-(ii) yields the following result.

Corollary 2. 
$$\Pr\left(\mu^{\mathit{RV}} \in M^{\mathit{E}} | Y_t^{\mathit{game}} = 1, D_t = 0\right) > \Pr\left(\mu^{\mathit{RV}} \in M^{\mathit{E}} | Y_t^{\mathit{game}} = 1, D_t = 1\right)$$
.

This result is intuitively straightforward. In the game, recall that conflict erupts on the equilibrium path when  $D_t = 0$  only in the asymmetric cases. Thus, given that a conflict took place at t such that  $D_t = 0$  in the model, it must be that the players are playing an asymmetric equilibrium. As a result, the left-hand side of the above inequality is one. One can see that the inequality holds because the right-hand side is strictly smaller than one: conflict can ensue in both symmetric and asymmetric equilibria, thus  $\mu^{RV}$  may or may not be in  $M^E$  in this case.

We now translate this theoretical implication into empirical terminologies. That is, replacing  $Y_t^{\text{game}}$ ,  $D_t$ , and  $\mu^{\text{RV}}$  with  $Y_{dt}^{\text{data}}$ ,  $\text{PDSI}_{d,t-1}$ , and  $\text{gov}_{dt}$ , respectively, yields a novel prediction below:

#### Implication 1. Corollary 2 implies

$$\Pr\left(\underbrace{\underset{\text{Stands for } \mu^{\text{RV}} \in M^{\text{E}}}{\text{gov}_{dt} = 1}}_{\text{Stands for } \mu^{\text{RV}} \in M^{\text{E}}}\right| \underbrace{\underset{\text{Stands for } D_{t} = 0}{\text{Fixed} = 1 \text{ in data}}}_{\text{Stands for } D_{t} = 0}\right) > \Pr\left(\text{gov}_{dt} = 1 \middle| Y_{dt}^{\text{data}} = 1, \underbrace{\underset{\text{Stands for } D_{t} = 1}{\text{Event PDSI}_{d,t-1}}}_{\text{Stands for } D_{t} = 1}\right).$$

Note that this empirical analogue to the theoretical prediction (Corollary 2) is not a causal statement. Rather, by reinterpreting  $\mu$  in the model as a random variable, it speaks to the probability distribution of the level of asymmetry in disaster risks between belligerent groups ( $gov_{dt}$ ) given that they are engaged in political violence.

Given Implication 1, we are interested in  $\Pr(\mathsf{gov}_{dt} = 1 | Y_{dt}^{\mathtt{data}} = 1, \mathtt{PDSI}_{d,t-1})$  for each  $\mathtt{PDSI}_{d,t-1} \in [-10,10]$ . To assess it, consider the simple logistic regression below:

$$\Pr\left(\text{gov}_{dt} = 1 \middle| Y_{dt}^{\text{data}} = 1, \text{PDSI}_{d,t-1}\right) = \frac{1}{1 + e^{-\left(\tilde{\beta}_{0} + \beta_{1} \text{PDSI}_{d,t-1} + \beta_{2}} Y_{dt}^{\text{data}}\right)} = \frac{1}{1 + e^{-\left(\beta_{0} + \beta_{1} \text{PDSI}_{d,t-1}\right)}}.$$
(3)

Because we always have  $Y_{dt}^{\text{data}} = 1$  in the data, we interpret that the effect of  $Y_{dt}^{\text{data}}$  is captured in the constant  $\beta_0$  (i.e.,  $\beta_0 \equiv \tilde{\beta}_0 + \beta_2$ ). Recall that (i)  $\text{gov}_{dt} = 1$  is assumed to imply that the belligerents face asymmetric disaster risks (i.e.,  $\mu \in M^E$  in the model) and (ii) a higher value represents water abundance (i.e.,  $D_t = 0$  in the model). Thus, by Implication 1, the (estimated) probability should be an increasing function of the PDSI score (PDSI<sub>d,t-1</sub>) if the above theory is consistent with the data. In sum, our estimand is the pair of the constant and coefficient  $(\beta_0, \beta_1)$  in expression (3).

Figure 6 illustrates the result. The horizontal and vertical axes represent  $PDSI_{d,t-1}$  and  $gov_{dt}$ , respectively. Thus, it suggests that  $Pr(gov_{dt} = 1|Y_{dt}^{data} = 1, PDSI_{d,t-1})$  is increasing in  $PDSI_{d,t-1}$ . Table 4.2 presents a few additional results. First, the distance between the location of a given conflict event and the capital city might be driving the result. A possible logic is

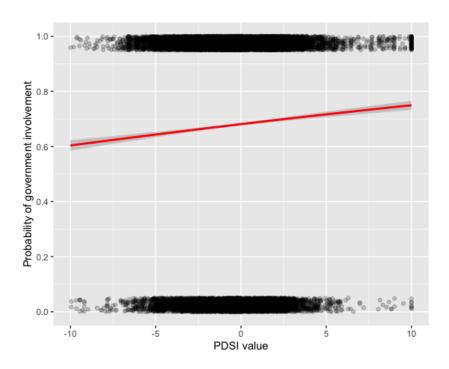


Figure 6: Asymmetry in a belligerent dyad as an increasing function of water abundance

that (i) a capital city might tend to be located in geographically resilient regions historically (possible correlation with  $PDSI_{d,t-1}$ ) and (ii) government control tends to be weaker in regions distant from the capital, leading to more conflicts between rebel groups and government forces (possible correlation with  $gov_{dt}$ ). Second, the PDSI score of the month in which the conflict event took place ( $PDSI_{dt}$ ) is also added to see if the score for the previous month seems an appropriate measure. The results remain similar.

Whereas the above result is first-cut evidence, the prediction in Implication 1 drawn from the model is, to the best of my knowledge, novel. This empirical exercise attempts to connect the theory and data as directly as possible and suggests that the model explains some parts of real-world data. Given the result, now we shall tentatively accept the theory and discuss what we can learn from it about empirical research on the climate-conflict nexus.

	Dependent variable: $gov_{dt}$					
	(1)	(2)	(3)	(4)		
$ extstyle{ t PDSI}_{d,t-1}$	0.034*** (0.004)	0.033*** (0.004)		$0.029^{***}$ $(0.005)$		
Distance to capital (standardized)		0.053*** (0.010)		0.053*** (0.010)		
$\mathtt{PDSI}_{dt}$			0.025*** (0.004)	$0.008 \\ (0.005)$		
Constant	0.758*** (0.011)	0.759*** (0.011)	0.754*** (0.010)	0.760*** (0.011)		
Observations	43,194	43,194	43,194	43,194		

Note:  $^{\dagger}p < 0.1; *p < 0.05; **p < 0.01; ***p < 0.001$ 

Table 2: Drought and government involvement in conflict events

## 5 Theoretical Implications for Empirical Research: The Case of the Potential Outcome Framework

The theoretical discussion leads to important implications for the empirical literature on climate shocks and armed conflict. The model (Corollary 1) implies that disasters have heterogeneous treatment effects on the risk of armed conflict. That is, in the asymmetric case, conflict events should be positively associated with disaster risks, rather than actual disaster events. In addition to the suggestive evidence presented above, a recent paper by Bas and McLean (2021) also supports such implication empirically. To take their findings one step further, this section provides a possible explanation for why the empirical results of climate conflict research are mixed. First, I show that overlooking the asymmetric case of the model (cases  $(E_1)$  and  $(E_2)$ ) can lead to an underestimation of the effect of natural disasters on conflict risks in the potential outcome framework. Second, based on this discussion, I

revisit the case of drought to make sense of the ostensibly mixed empirical results.

## 5.1 Heterogeneous Effects of Disaster Events

Suppose that we want to employ the potential outcomes framework to study the causal effects of natural disasters and climate anomalies on armed conflict. Let the (binary) potential outcome  $Y_{dt}^{po}(D_{dt}) \in \{0,1\}$  represent the presence  $(Y_{dt}^{po}(D_{dt}) = 1)$  and absence  $(Y_{dt}^{po}(D_{dt}) = 0)$  of armed conflict at time t in dyad of groups d given treatment  $D_{dt}$ . We define the observable treatment  $D_{dt}$  in a similar way as in the game-theoretic model. That is,  $D_{dt} \in \{0,1\}$  denotes the presence  $(D_{dt} = 1)$  and absence  $(D_{dt} = 0)$  of a natural disaster in dyad d in period t, which is independently and identically drawn.

Next, recall that  $\mu$  is also a *dyadic* concept because it stands for the (a)symmetry in inherent disaster risks *between* two players. Thus, suppose that we have data on the level of such asymmetry for dyad d, denoted by  $\mu_d \in [0,1]$ .<sup>19</sup> Further, as in the game-theoretic model, suppose that we have two sets  $M^R$ ,  $M^E \subset [0,1]$  such that (i) rival political groups in dyad d face a symmetric risk of exposure to natural disasters when  $\mu_d \in M^R$  and (ii) they face an asymmetric risk of exposure when  $\mu_d \in M^E$ .<sup>20</sup> In the potential outcomes framework, this formulation implies that  $(Y_{dt}^{PO}(D_{dt})|\mu') \neq (Y_{dt}^{PO}(D_{dt})|\mu'')$ , where  $\mu' \in M^R$ ,  $\mu'' \in M^E$ , which leads to a simple implication below.

Implication 2. Suppose we want to examine the causal effect of a disaster on armed conflict onset using the potential outcome framework. Then, a desirable estimand may be the conditional average treatment effect (CATE),  $\tau(\mu) \equiv \mathbb{E}[Y_{dt}^{po}(1) - Y_{dt}^{po}(0)|\mu_d = \mu]$ , rather than the average treatment effect (ATE),  $\tau \equiv \mathbb{E}[Y_{dt}^{po}(1) - Y_{dt}^{po}(0)]$ .

<sup>&</sup>lt;sup>18</sup>One can think of d as a pair of rival political groups or sovereign states.

<sup>&</sup>lt;sup>19</sup>In the discussion below,  $\mu_d$  does not have to be considered as a random variable, unlike the previous section

 $<sup>^{20}</sup>$  For simplicity, assume that  $M^{\tt R}$  and  $M^{\tt E}$  are mutually disjoint. The simplest example is the case where  $\mu_d$  is binary. For instance, in the previous section, I define  $M^{\tt R}=\{0\}$  and  $M^{\tt E}=\{1\}$ , and the measure that represents  $\mu_d$  (i.e.,  ${\tt gov}_{dt}$ ) only takes zero or one.

To derive more specific implications, suppose that we have country-year data of conflict events in dyad d at time t. Denote the presence and absence of conflict by  $Y_{dt}^{\mathtt{data}} = 1$  and  $Y_{dt}^{\mathtt{data}} = 0$ , respectively. Further, let us tentatively assume that the game-theoretic model captures the true data-generating process.

Assumption 4. We can interpret 
$$Y_{dt}^{\text{data}} = Y_{t}^{\text{game}}$$
 and  $D_{dt} = D_{t}$ .

In other words, we interpret real-world conflict data as products of equilibrium outcomes in the game of asymmetric exposure to extreme weather events. Then, given that  $(Y_{dt}^{\text{data}}|D_{dt}=1) = Y_{dt}^{\text{PO}}(1)$ , we obtain the following.

Corollary 3. Assumption 4 and Corollary 1 yield:

(i) 
$$\Pr(Y_{dt}^{PO}(1) = 1 | \mu_d = \mu^R) > \Pr(Y_{dt}^{PO}(0) = 1 | \mu_d = \mu^R)$$
 and

(ii) 
$$\Pr(Y_{dt}^{PO}(1) = 1 | \mu_d = \mu^E) < \Pr(Y_{dt}^{PO}(0) = 1 | \mu_d = \mu^E)$$
.

In words, the result represents the two types of equilibrium outcomes: (i) when two rival political groups face a symmetric risk of exposure to disasters, war is more likely to erupt in a given period t when a disaster has occurred in the same period (i.e.,  $D_{dt} = 1$ ); (ii) when they face an asymmetric risk of exposure, conflict is more likely when there is no disaster in period t (i.e.,  $D_{dt} = 0$ ).

This result drawn from the game-theoretic model leads to another, more specific implication. Suppose  $\mu_d = \mu^{R}$ . Rearranging Part (i) of Corollary 3 immediately yields

$$\begin{split} \Pr\left(Y_{dt}^{\text{PO}}(1) = 1 \middle| \mu^{\text{R}}\right) - \Pr\left(Y_{dt}^{\text{PO}}(0) = 1 \middle| \mu^{\text{R}}\right) &= 1 \cdot \Pr\left(Y_{dt}^{\text{PO}}(1) = 1 \middle| \mu^{\text{R}}\right) + 0 \cdot \Pr\left(Y_{dt}^{\text{PO}}(1) = 0 \middle| \mu^{\text{R}}\right) \\ &- 1 \cdot \Pr\left(Y_{dt}^{\text{PO}}(0) = 1 \middle| \mu^{\text{R}}\right) + 0 \cdot \Pr\left(Y_{dt}^{\text{PO}}(0) = 0 \middle| \mu^{\text{R}}\right) \\ &= \mathbb{E}\left[Y_{dt}^{\text{PO}}(1) \middle| \mu^{\text{R}}\right] - \mathbb{E}\left[Y_{dt}^{\text{PO}}(0) \middle| \mu^{\text{R}}\right] \\ &= \tau\left(\mu^{\text{R}}\right) > 0. \end{split}$$

Similarly, from Part (ii) of Corollary 3, we obtain  $\Pr(Y_{dt}^{PO}(1) = 1 | \mu^{E}) - \Pr(Y_{dt}^{PO}(0) = 1 | \mu^{E}) = \tau(\mu^{E}) < 0$ . Implication 3 below summarizes the results.

## **Implication 3.** Corollary 3 implies $\tau(\mu^{\mathbb{R}}) > 0 > \tau(\mu^{\mathbb{E}})$ .

It is important to note that, even if researchers rely on CATE rather than ATE, the potential outcome approach itself could be problematic in this case. To see this, suppose that belligerent groups in dyad d face an asymmetric risk of exposure to disasters (i.e.,  $\mu_d = \mu^{\rm E}$ ). Then, Implication 3 states that the effect of a disaster on conflict onset in the sense of CATE is negative,  $\tau(\mu^{\rm E}) < 0$ , under Corollary 3.

However, although the CATE is negative, asymmetric exposure to disaster risks causes a war in the game-theoretic model: Remarks 1 and 2 show that the possibility of disasters and variation in  $Z_t$  are necessary conditions for a conflict to erupt on the equilibrium path. Therefore, if asymmetric exposure to disasters and climate anomalies generates an anticipation of temporary military power shifts in the real world (as empirically tested by Bas and McLean, 2021), overlooking the strategic dynamic of the second equilibrium leads to underestimation of their true causal effect on the propensity of war.

Put differently, Implication 3 suggests that some frameworks for causal inference may sometimes not be suitable for particular phenomena. Suppose that researchers have fine data on conflicts that erupted right after a natural disaster. Despite abundant data, the model and Implication 3 show that there can exist conflict episodes that are classified as ones that erupted because of factors other than disasters but were actually triggered by asymmetric exposure to disaster risks. If such a case exists, the causal effect of disasters on conflicts in terms of CATE should not be appropriate.

#### 5.2 Making Sense of Seemingly Mixed Evidence

To reinterpret existing empirical results theoretically, let us revisit the case of drought. In particular, I discuss the results presented by Salehyan and Hendrix (2014), who find a pacifying effect of droughts, and point out that their findings could be due to the ostensible negative effect of droughts. To be clear, the discussion below is not aimed at falsifying Salehyan and Hendrix (2014). Rather, it attempts to demonstrate the possibility that some empirical findings on the negative causal effects of climate disasters on conflict might be driven by a particular form of their *positive* effect, namely, the preemptive mechanism in the asymmetric cases  $(E_1)$  and  $(E_2)$  of the model.

Salehyan and Hendrix (2014) argue that water scarcity can decrease armed conflict. Droughts harm agricultural production in affected areas and reduce economic resources. As a result, water scarcity impairs the mobilization capabilities of rival political groups, and thus organized armed conflict should decline under such conditions. Utilizing data on water scarcity (including the PDSI data) and armed conflict, Salehyan and Hendrix (2014) find that water abundance positively correlates with conflict.

Their interpretation of the correlation might be problematic. To see this, observe the implicit assumption in the logic of Salehyan and Hendrix (2014) that water scarcity affects groups' mobilization capabilities symmetrically. Namely, conflict becomes a less attractive option under water scarcity because, in their theory, both sides of a given dispute face a lower mobilization capability. However, if one drought happens to cause water scarcity in a particular region, such an (implicit) assumption does not necessarily remain plausible. Rather, if water scarcity is more severe in one region than others, then only one side of a political dispute can lose its power to mobilize. In this case, the rival group that has incurred less severe water scarcity remains its mobilization capability. As the formal model suggests, such asymmetry in power can generate an incentive for rival political groups to fight, rather than deescalate.

Given the demanding implicit assumption on the symmetry in disaster damages, the findings of Salehyan and Hendrix (2014) may be a product of preemptive motives arising from the asymmetric equilibrium (E<sub>1</sub>) or (E<sub>2</sub>). Whereas Salehyan and Hendrix (2014) argue that droughts and water scarcity decrease conflict, the equilibrium suggests that conflict is strictly more likely in periods without water scarcity due to preemptive motives. The empirical results should look similar: the former logic predicts that "more droughts in the present period make conflict less likely due to the mobilization-capability logic," whereas the latter states that "fewer droughts in the present period make conflict more likely due to the preemptive motive." However, recall that what triggers conflict in the latter logic is the asymmetric exposure to disaster risks. Hence, opposing two reasonings, i.e., pacifying effects of extreme weather events on the one hand and destabilizing effects of their risks on the other, lead to the same empirical pattern.

Figure 7 illustrates the intuition. Consider the horizontal and vertical axes as time and the risk of conflict, respectively. The green line represents the risk of conflict as a function of time and other variables than water scarcity. Then, let the shaded areas on the horizontal axis denote the periods during which the region experienced droughts. In this simplified setting, the mobilization-capability logic by Salehyan and Hendrix (2014) predicts that the value of the function should be smaller under water scarcity (blue line in Figure 7). On the other hand, the preemptive-war logic in the second equilibrium of the above model suggests that the value should be greater under relative water abundance (red line). Based on the former logic, the graph of the function consists of the blue segments (in the shaded periods) and green lines (periods without water scarcity), whereas the latter logic draws a graph composed of the red segments (periods without water scarcity) and green lines (in the shaded periods). Observe that the shapes of the two graphs should look similar, although the latter one is strictly greater than the former.

The data in Salehyan and Hendrix (2014) suggest that their findings might be driven

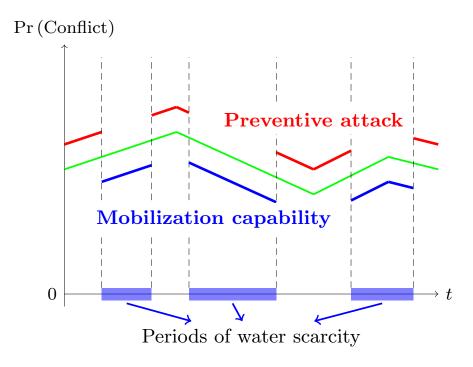


Figure 7: Opposing theories leading to similar empirical patterns

by the logic of asymmetric exposure to disaster risks. Recall that, in the game-theoretic model, the equilibrium outcomes vary across the value of  $\mu$ , which represents the level of (a)symmetric exposure to disaster risks. The second, preemptive-war equilibrium (E<sub>1</sub>) or E<sub>2</sub> emerges when  $\mu$  is close to zero or one, where one group is inherently more vulnerable to future extreme weather events. Moreover, for the second equilibrium to arise, natural disasters in question and their expected damage should be, at least to some extent, foreseeable: as Remarks 1 and 2 suggest, the preemptive war in the second equilibrium never erupts if the risk and asymmetric costs are not perceptible in the first place.

These conditions seem to be satisfied in Salehyan and Hendrix (2014). First, their unit of observation is country-year. Thus, it is more likely that relevant rival groups are geographically distant. Consequently, the level of asymmetry in disaster risks should be greater ( $\mu$  close to zero or one) in country-year data than in more geographically disaggregated ones, where relevant groups are inevitably more proximate in the geographical unit and should be

facing similar disaster risks. Second, droughts are seasonal disasters. Thus, at least, they are relatively more foreseeable than other natural disasters such as earthquakes. The relative predictability of droughts renders the preemptive motive in the second equilibrium a plausible strategic logic connecting future disaster risks to conflict in the present period.

One can also situate other studies that seem to contradict Salehyan and Hendrix (2014) in the context of the asymmetric-exposure theory. For example, Fjelde and von Uexkull (2012) find that negative rainfall anomalies are associated with more communal conflicts between non-state actors in sub-Saharan Africa. Recall the variable  $gov_{dt}$  defined in the previous section: based on the measure, the conflict data in Fjelde and von Uexkull (2012) should have  $gov_{dt} = 0$  (symmetric dyads) because they focus on non-state conflicts. If we assume  $gov_{dt} = 0$  captures  $\mu \in M^{\mathbb{R}}$ , the theory also predicts that droughts and communal conflicts are positively correlated.

Moreover, Bell and Keys (2018) argue that the effect of drought on conflict in sub-Saharan Africa is conditional on other factors related to conflict risks, such as social vulnerability (e.g., inadequate food supply), equal distribution of or access to emergency resources (e.g., ethnic exclusion), and state capacity (e.g., low urbanization). For instance, they find a significant positive association between drought and conflict contingent on low ethnic exclusion. If inclusive distribution of resources among different ethnic groups implies that those groups have relatively symmetric resilience/vulnerability to extreme weather events ( $\mu \in M^{\mathbb{R}}$  in the model), this finding exemplifies Corollary 1. Hence, it is also consistent with the asymmetric-exposure theory.

In sum, some of the seemingly contradictory empirical results can be driven by one of the two heterogeneous effects of disasters conditional on the level of (a)symmetry in disaster risks. We may be able to make sense of them by taking theory and the data-generating process behind them more seriously.

## 6 Conclusion

This paper has shown that a single process of asymmetric exposure to climate anomalies and other natural disasters generates two qualitatively distinct equilibrium strategies. The key parameter is the asymmetry in the inherent risk of exposure to extreme weather events and other natural disasters. It determines the source of conflict in the equilibrium path. In the first case, conflict erupts as a consequence of an actual disaster that causes a temporary shock to the balance of power. In the second, war is more likely before a disaster occurs because of the anticipated asymmetry of its costs. Put differently, although disasters trigger conflict in both cases either through their actual occurrence or their future risks, in the asymmetric case, the probability of conflict onset is strictly larger in the absence of a disaster than right after it.

This theoretical result yields a novel (i) empirical prediction and (ii) theoretical interpretation of why the results of empirical research on climate conflict are inconclusive. Although it does not directly dispute specific empirical results, the game-theoretic model implies that we might be underestimating the causal effect of disasters and extreme weather events on armed conflict. Specifically, in the second (asymmetric) case, the actual occurrence of a natural disaster and conflict onset should be negatively correlated, but those conflicts are also caused by disaster risks. Therefore, if extreme weather events have multiple effects, including the one studied in this paper (randomness and asymmetry in exposure), the seemingly mixed results may be mixed only ostensibly. Namely, it is possible that the conflict-inducing effects of natural disasters are larger than shown in empirical studies if they overlook the heterogeneous impacts.

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## **Appendix**

## Proofs of the Statements in the Main Text

Proof of Remark 1. We want to show that (i) a strategy profile in which both players never fight constitutes an SPE and (ii) it is the unique equilibrium. First, consider an arbitrary subgame, and suppose that one player is following a strategy in which she never attacks the opponent at any decision node. Let  $\mathcal{V}^0$  and  $\mathcal{W}^0$  denote the other player's continuation payoff and expected war payoff, respectively. Then, we have

$$\mathcal{V}^{0} = \theta + \delta \mathcal{V}^{0}$$

$$\mathcal{W}^{0} = \frac{1}{2} \left[ 2\theta (1 - c) + \delta \sum_{t=1}^{\infty} \delta^{t-1} \cdot 2\theta \right] + \frac{1}{2} \cdot 0$$

$$= \theta \left[ \frac{1}{1 - \delta} - c \right].$$

Since solving the first equation for  $\mathcal{V}^0$  yields  $\mathcal{V}^0 = \theta/(1-\delta)$ , we obtain  $\mathcal{V}^0 > \mathcal{W}^0$  for any  $c \in (0,1)$ . Because any deviation (attacking the opponent) ends the game, we do not need to check off-path strategies. Hence, the strategy profile in which neither player ever fights constitutes an SPE.

The above equilibrium is unique under Assumption 1. To see this, suppose to the contrary that there exists another SPE. If so, because such an equilibrium is different from the one shown above in which neither attacks the other at any history, it implies that war must occur in some history. Assumption 1 rules out strategy profiles in which both players attack in the same period. Thus, it leaves a strategy profile where one player unilaterally attacks the other at some history t'. Consider the attacker's incentive at such period t'. For an arbitrary continuation game, a one-step deviation of not attacking at period t' would yield a path of play on which peace is maintained for  $\tau \geq 1$  periods and war erupts in the  $(\tau + 1)$ th period

(unless  $\tau = \infty$ ). Such deviation would generate a continuation payoff  $\sum_{t=1}^{\tau} \delta^{t-1}\theta + \delta^{\tau} \mathcal{W}^0$ . In sum, the incentive of the attacker at period t' has to satisfy

$$\underbrace{\mathcal{W}^{0}}_{\text{Attack at }t'} \geq \underbrace{\frac{1 - \delta^{\tau}}{1 - \delta}\theta + \delta^{\tau}\mathcal{W}^{0}}_{\text{Deviation}}$$
$$-c \geq 0,$$

which never holds by  $c \in (0,1)$ . Therefore, any potential attacker has the incentive to deviate to sustain peace in any strategy profile where war occurs at some history t'. This result contradicts the assumption that there is another SPE, which proves that no other equilibrium is possible under Assumption 1.

*Proof of Remark 2.* As in Remark 1, we want to show that the completely peaceful strategy profile is the only SPE. To show this, first define players' continuation payoff from the strategy profile:

$$\mathcal{V}^{\text{sym}} \equiv (1 - \pi) \left( \theta + \delta \mathcal{V}^{\text{sym}} \right) + \pi \left( \frac{1}{2} \theta + \delta \mathcal{V}^{\text{sym}} \right)$$
$$\mathcal{V}^{\text{sym}} = \theta \cdot \frac{1 - \pi/2}{1 - \delta}.$$

Next, let  $\mathcal{W}^{d,sym}$  and  $\mathcal{W}^{\neg d,sym}$  be the expected war payoff when a war occurs in a disaster and no-disaster periods, respectively.

$$\begin{split} \mathcal{W}^{\rm d,\,sym} &= \frac{1}{2} \left( \theta(1-c) + \delta \overline{\mathcal{V}} \right) \\ \mathcal{W}^{\rm -d,\,sym} &= \frac{1}{2} \left( 2\theta(1-c) + \delta \overline{\mathcal{V}} \right). \end{split}$$

Not attacking is the best response in disaster and no-disaster periods if  $\frac{1}{2}\theta + \delta \mathcal{V}^{\text{sym}} > \mathcal{W}^{\text{d,sym}}$  and  $\theta + \delta \mathcal{V}^{\text{sym}} > \mathcal{W}^{\text{-d,sym}}$ , respectively. Simple computation reduces both inequalities to c > 0, which always holds. Because not attacking is the best response to the other player not

attacking in any subgame, the strategy profile in which both players never fight is an SPE.

The same logic as Remark 1 proves the equilibrium uniqueness: no other equilibrium is possible given that (i) not attacking is strictly more beneficial when the other player is following the peaceful strategy (in which she never attacks the opponent) and (ii) mutual attacks do not occur under Assumption 1.

Proof of Proposition 1. I prove the proposition in three simple steps. Before doing so, for simplicity, let us introduce the following notation. Notice that the game is symmetric except for variables related to Z. Then, for a variable/parameter  $x \in \{Z, z_t, \mu\}$ , denote its relevant value to each player by  $\tilde{x} \equiv \mathbb{1}\{i=1\} \cdot x + \mathbb{1}\{i=2\} (1-x)$ . For example,  $\tilde{z}_t\theta$  represents the remaining amount of resources for Player 1 (i.e.,  $z_t\theta$ ) and Player 2 (i.e.,  $(1-z_t)\theta$ ) in a disaster period.

Step 1 (Preliminaries). First, we identify the players' expected payoffs when they follow strategies (R-I) and (R-II). First, consider war payoffs. Suppose that Nature has determined the presence/absence of a disaster and its asymmetric exposure  $z_t$  if one occurred. Let  $\mathcal{W}_i^d$  and  $\mathcal{W}_i^{-d}$  denote player i's expected war payoff in a disaster and no-disaster periods, respectively. Then, we have

$$\begin{split} \mathcal{W}_{i}^{\mathrm{d}} &= p_{i}^{\mathrm{d}}\left(z_{t}\right)\left(\theta(1-c)+\delta\overline{\mathcal{V}}\right) \\ &= \tilde{z}_{t}\theta\left[\frac{1+\delta(1-\pi)}{1-\delta}-c\right] \\ \mathcal{W}_{i}^{-\mathrm{d}} &= p_{i}^{-\mathrm{d}}\left(2\theta(1-c)+\delta\overline{\mathcal{V}}\right) \\ &= \theta\left[\frac{1-\delta\pi/2}{1-\delta}-c\right]. \end{split}$$

Next, consider the expected peace payoffs. Let  $\mathcal{V}_i^{\mathtt{R}}$  denote player i's continuation payoff when both players follow strategies (R-I) and (R-II). We can see that  $\mathcal{V}_i^{\mathtt{R}}$  consists of four components: cases where (i) a disaster does not take place; (ii) a disaster erupts and neither player fights; (iii) a disaster takes place and  $z_t$  is small so that Player 2 attacks 1; and (iv) a

disaster occurs and  $z_t$  is large so that Player 1 attacks 2. Thus, we have

$$\mathcal{V}_{i}^{\mathrm{R}} = \overbrace{(1-\pi)\left(\theta+\delta\mathcal{V}_{i}^{\mathrm{R}}\right)}^{(i) \; \mathrm{No\text{-}disaster period}}$$

$$+ \pi \begin{bmatrix} \overbrace{\Delta_{F}\left(\overline{z}^{\mathrm{R}},\underline{z}^{\mathrm{R}}\right)}^{(ii) \; \mathrm{Pr}(\mathrm{Peace})} \left(\mathbb{E}\left[\tilde{Z}\Big|Z\in\left[\underline{z}^{\mathrm{R}},\overline{z}^{\mathrm{R}}\right]\right]\theta+\delta\mathcal{V}_{i}^{\mathrm{R}}\right) \\ + \underbrace{F\left(\underline{z}^{\mathrm{R}}\right)}_{(iii) \; \mathrm{Pr}(\mathrm{P2\; attacks})} \mathbb{E}\left[\tilde{Z}\Big|Z<\underline{z}^{\mathrm{R}}\right]\theta\left[(1-c)+\delta\frac{2-\pi}{1-\delta}\right] \\ + \underbrace{\left(1-F\left(\overline{z}^{\mathrm{R}}\right)\right)}_{(iv) \; \mathrm{Pr}(\mathrm{P1\; attacks})} \mathbb{E}\left[\tilde{Z}\Big|Z>\overline{z}^{\mathrm{R}}\right]\theta\left[(1-c)+\delta\frac{2-\pi}{1-\delta}\right] \\ \mathbb{E}\left[\mathcal{W}_{i}^{\mathrm{d}}\Big|Z>\overline{z}^{\mathrm{R}}\right]}$$

where  $\Delta_F(b,a) = F(b) - F(a)$  with  $a \leq b$ . Solving this for  $\mathcal{V}_i^{\mathbf{R}}$  yields

$$\mathcal{V}_{i}^{\mathbf{R}} \ = \ \theta \cdot \frac{ (1-\pi) + \pi \left[ \begin{array}{c} \Delta_{F} \left( \overline{z}^{\mathbf{R}}, \underline{z}^{\mathbf{R}} \right) \mathbb{E} \left[ \tilde{Z} \middle| Z \in \left[ \underline{z}^{\mathbf{R}}, \overline{z}^{\mathbf{R}} \right] \right] \\ + \left( F \left( \underline{z}^{\mathbf{R}} \right) \mathbb{E} \left[ \tilde{Z} \middle| Z < \underline{z}^{\mathbf{R}} \right] + \left( 1 - F \left( \overline{z}^{\mathbf{R}} \right) \right) \mathbb{E} \left[ \tilde{Z} \middle| Z > \overline{z}^{\mathbf{R}} \right] \right) \left[ (1-c) + \delta \frac{2-\pi}{1-\delta} \right] \right] }{ 1 - \delta \left( 1 - \pi \left( 1 - \Delta_{F} \left( \overline{z}^{\mathbf{R}}, \underline{z}^{\mathbf{R}} \right) \right) \right) }$$
 
$$= \theta \cdot \frac{ \left[ \begin{array}{c} \Delta_{F} \left( \overline{z}^{\mathbf{R}}, \underline{z}^{\mathbf{R}} \right) \mathbb{E} \left[ \tilde{Z} \middle| Z \in \left[ \underline{z}^{\mathbf{R}}, \overline{z}^{\mathbf{R}} \right] \right] \\ + F \left( \underline{z}^{\mathbf{R}} \right) \mathbb{E} \left[ \tilde{Z} \middle| Z < \underline{z}^{\mathbf{R}} \right] + \left( 1 - F \left( \overline{z}^{\mathbf{R}} \right) \right) \mathbb{E} \left[ \tilde{Z} \middle| Z > \overline{z}^{\mathbf{R}} \right] \right) \\ + \left( F \left( \underline{z}^{\mathbf{R}} \right) \mathbb{E} \left[ \tilde{Z} \middle| Z < \underline{z}^{\mathbf{R}} \right] + \left( 1 - F \left( \overline{z}^{\mathbf{R}} \right) \right) \mathbb{E} \left[ \tilde{Z} \middle| Z > \overline{z}^{\mathbf{R}} \right] \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right] }{ 1 - \delta \left( 1 - \pi \left( 1 - \Delta_{F} \left( \overline{z}^{\mathbf{R}}, \underline{z}^{\mathbf{R}} \right) \right) \right) }$$
 
$$= \theta \cdot \frac{ \left( 1 - \pi \right) + \pi \left[ \tilde{\mu} + \left( F \left( \underline{z}^{\mathbf{R}} \right) \mathbb{E} \left[ \tilde{Z} \middle| Z < \underline{z}^{\mathbf{R}} \right] + \left( 1 - F \left( \overline{z}^{\mathbf{R}} \right) \right) \mathbb{E} \left[ \tilde{Z} \middle| Z > \overline{z}^{\mathbf{R}} \right] \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right] }{ 1 - \delta \left( 1 - \pi \left( 1 - \Delta_{F} \left( \overline{z}^{\mathbf{R}}, \underline{z}^{\mathbf{R}} \right) \right) \right) } ,$$

where the last equation holds by the law of iterated expectations. By  $\mathbb{E}\left[Z|Z\in[\underline{z},\overline{z}]\right]$  =

 $\frac{\int_{\underline{z}}^{\overline{z}} z f(z) dz}{\int_{z}^{\overline{z}} f(z) dz}$ , we obtain

$$\mathcal{V}_{i}^{\mathbf{R}} = \theta \cdot \frac{(1-\pi) + \pi \left( \tilde{\mu} + \left( \int_{0}^{\underline{z}^{\mathbf{R}}} \tilde{z} dF(\tilde{z}) + \int_{\overline{z}^{\mathbf{R}}}^{1} \tilde{z} dF(\tilde{z}) \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right)}{1 - \delta \left( 1 - \pi \left( 1 - \Delta_{F}\left( \overline{z}^{\mathbf{R}}, \underline{z}^{\mathbf{R}} \right) \right) \right)}.$$

When players follow strategies (R-I) and (R-II), player i's expected peace payoff at any information set in a no-disaster period is  $\theta + \delta \mathcal{V}_i^{\text{R}}$ . On the other hand, i's expected peace payoff in a disaster period when the realized asymmetric exposure is  $z_t$  is  $\tilde{z}_t\theta + \delta \mathcal{V}_i^{\text{R}}$ .

Step 2 (R-I). Consider an arbitrary disaster period. Strategy (R-I) states that when the realized asymmetric exposure  $z_t$  is extreme, the (temporarily) advantaged side attacks the other. Given that the opponent is playing (R-I) and (R-II), if  $W_i^d > \tilde{z}_t \theta + \delta V_i^R$ , it is the best response for player i to attack the other in a disaster period t after any history. The above inequality yields

$$\tilde{z}_{t}\theta\left[\frac{1+\delta(1-\pi)}{1-\delta}-c\right] > \tilde{z}_{t}\theta+\delta\theta\cdot\frac{\left(1-\pi\right)+\pi\left(\tilde{\mu}+\left(\int_{0}^{\underline{z}^{\mathsf{R}}}\tilde{z}\mathrm{d}F(\tilde{z})+\int_{\overline{z}^{\mathsf{R}}}^{1}\tilde{z}\mathrm{d}F(\tilde{z})\right)\left[\delta\frac{2-\pi}{1-\delta}-c\right]\right)}{1-\delta\left(1-\pi\left(1-\Delta_{F}\left(\overline{z}^{\mathsf{R}},\underline{z}^{\mathsf{R}}\right)\right)\right)}$$

$$\tilde{z}_{t} > \delta\cdot\frac{\left(1-\pi\right)+\pi\left(\tilde{\mu}+\left(\int_{0}^{\underline{z}^{\mathsf{R}}}\tilde{z}\mathrm{d}F(\tilde{z})+\int_{\overline{z}^{\mathsf{R}}}^{1}\tilde{z}\mathrm{d}F(\tilde{z})\right)\left[\delta\frac{2-\pi}{1-\delta}-c\right]\right)}{\left(1-\delta\left(1-\pi\left(1-\Delta_{F}\left(\overline{z}^{\mathsf{R}},\underline{z}^{\mathsf{R}}\right)\right)\right)\right)\left[\delta\frac{2-\pi}{1-\delta}-c\right]}.$$

Recall that  $\tilde{z}_t = z_t$ ,  $\tilde{\mu} = \mu$ , and  $\tilde{Z} = Z$  for Player 1. Hence, the threshold  $\overline{z}^R$  above which Player 1 attacks 2 is given implicitly by

$$\overline{z}^{\mathrm{R}} = \delta \cdot \frac{\left(1 - \pi\right) + \pi \left(\mu + \left(\int_{0}^{\underline{z}^{\mathrm{R}}} z \mathrm{d}F(z) + \int_{\overline{z}^{\mathrm{R}}}^{1} z \mathrm{d}F(z)\right) \left[\delta \frac{2 - \pi}{1 - \delta} - c\right]\right)}{\left(1 - \delta \left(1 - \pi \left(1 - \Delta_{F}\left(\overline{z}^{\mathrm{R}}, \underline{z}^{\mathrm{R}}\right)\right)\right)\right) \left[\delta \frac{2 - \pi}{1 - \delta} - c\right]}.$$

On the other hand, by  $\tilde{z}_t = 1 - z_t$ ,  $\tilde{\mu} = 1 - \mu$ , and  $\tilde{Z} = 1 - Z$  for Player 2,  $\underline{z}^{R}$  below which Player 2 attacks 1 is implicitly characterized by,

$$\underline{z}^{\mathrm{R}} = 1 - \delta \cdot \frac{(1 - \pi) + \pi \left(1 - \mu + \left(1 - \Delta_{F}\left(\overline{z}^{\mathrm{R}}, \underline{z}^{\mathrm{R}}\right) - \left(\int_{0}^{\underline{z}^{\mathrm{R}}} z \mathrm{d}F(z) + \int_{\overline{z}^{\mathrm{R}}}^{1} z \mathrm{d}F(z)\right)\right) \left[\delta \frac{2 - \pi}{1 - \delta} - c\right]\right)}{\left(1 - \delta \left(1 - \pi \left(1 - \Delta_{F}\left(\overline{z}^{\mathrm{R}}, \underline{z}^{\mathrm{R}}\right)\right)\right)\right) \left[\delta \frac{2 - \pi}{1 - \delta} - c\right]}$$

Solving the system of the two equations for  $\overline{z}^R$  and  $\underline{z}^R$  determines the thresholds in realized asymmetric exposure above and below which either one player attacks the other, respectively.

Step 3 (R-II). Finally, consider a no-disaster period. Neither player attacks the opponent when  $W_i^{-d} \leq \theta + \delta V_i^{R}$ . This yields

$$\frac{1}{2} \left[ 2\theta(1-c) + \delta \frac{\theta(2-\pi)}{1-\delta} \right] \leq \theta + \delta \theta \frac{(1-\pi) + \pi \left( \tilde{\mu} + \left( \int_0^{\underline{z}^{\mathbb{R}}} \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathbb{R}}}^1 \tilde{z} \mathrm{d}F(\tilde{z}) \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right)}{1 - \delta \left( 1 - \pi \left( 1 - \Delta_F \left( \overline{z}^{\mathbb{R}}, \underline{z}^{\mathbb{R}} \right) \right) \right)}$$

$$\tilde{\mu} \geq \frac{1}{2} + \delta \frac{2-\pi}{1-\delta} \left( \int_0^{\underline{z}^{\mathbb{R}}} \frac{1}{2} - \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathbb{R}}}^1 \frac{1}{2} - \tilde{z} \mathrm{d}F(\tilde{z}) \right)$$

$$-c \left( \int_0^{\underline{z}^{\mathbb{R}}} 1 - \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathbb{R}}}^1 1 - \tilde{z} \mathrm{d}F(\tilde{z}) + \frac{1-\delta}{\delta \pi} \right),$$

where  $\tilde{\mu}$  for which the above expression holds with equality is the threshold value. Recall Assumption 2. The only moving part when we vary  $\mu$  or F is one parameter. This constitutes a necessary condition to solve for  $\underline{\mu}^R$  and  $\overline{\mu}^R$ : for each of these threshold values, we have a system of three equations with three unknowns (i.e.,  $\underline{z}^R(\mu)$ ,  $\overline{z}^R(\mu)$ , and the parameter that determines the value of  $\mu$ ). If we solve the system of equations, by  $\tilde{\mu} = \mathbb{1}\{i=1\} \cdot \mu + \mathbb{1}\{i=2\}(1-\mu)$  and  $\tilde{z} = \mathbb{1}\{i=1\} \cdot z + \mathbb{1}\{i=2\}(1-z)$ , we obtain the desired result.  $\square$ 

Proof of Proposition 2. We can prove this proposition in a similar manner to Proposition 1.

**Step 1** (Preliminaries). From the proof of Proposition 1, we know players' expected war payoffs, i.e.,  $W_i^d$  and  $W_i^{\neg d}$ . Let  $V_i^E$  represent player i's continuation payoff when both players

are following strategies (E-I) and (E-II):

$$\mathcal{V}_{i}^{\mathrm{E}} = \underbrace{(1-\pi) \, \mathcal{W}_{i}^{-\mathrm{d}}}_{\text{Pr(Peace)}} \\ + \underbrace{\pi \left[ \underbrace{\sum_{i=1}^{\mathrm{Pr(Peace)}} \left( \mathbb{E} \left[ \tilde{Z} \middle| Z \in \left[ \underline{z}^{\mathrm{E}}, \overline{z}^{\mathrm{E}} \right] \right] \theta + \delta \mathcal{V}_{i}^{\mathrm{E}} \right)}_{\text{Pr(P2 attacks)}} \mathbb{E} \left[ \tilde{Z} \middle| Z < \underline{z}^{\mathrm{E}} \right] \theta \left[ (1-c) + \delta \frac{2-\pi}{1-\delta} \right] \\ + \underbrace{\left( 1 - F \left( \overline{z}^{\mathrm{E}} \right) \right)}_{\text{Pr(P1 attacks)}} \mathbb{E} \left[ \tilde{Z} \middle| Z > \overline{z}^{\mathrm{E}} \right] \theta \left[ (1-c) + \delta \frac{2-\pi}{1-\delta} \right] \\ \mathbb{E} \left[ \mathcal{W}_{i}^{\mathrm{d}} \middle| Z > \overline{z}^{\mathrm{E}} \right]} \\ \underbrace{\left[ \mathcal{W}_{i}^{\mathrm{d}} \middle| Z > \overline{z}^{\mathrm{E}} \right]}_{\text{Disaster period}}$$

Solving this for  $\mathcal{V}_i^{\mathtt{E}}$ , we obtain

$$\mathcal{V}_{i}^{\mathrm{E}} = \theta \cdot \frac{(1-\pi)\left[\frac{1-\delta\pi/2}{1-\delta} - c\right] + \pi\left(\tilde{\mu} + \left(\int_{0}^{\underline{z}^{\mathrm{E}}} \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathrm{E}}}^{1} \tilde{z} \mathrm{d}F(\tilde{z})\right)\left[\delta\frac{2-\pi}{1-\delta} - c\right]\right)}{1-\delta\pi\Delta_{F}\left(\overline{z}^{\mathrm{E}}, \underline{z}^{\mathrm{E}}\right)}$$

Step 2 (E-I). Consider an arbitrary disaster period t and suppose that the opponent is playing strategies (E-I) and (E-II). Then, it is optimal for player i to attack the other when  $W_i^d > \tilde{z}_t \theta + \delta V_i^E$ . That is,

$$\begin{split} \tilde{z}_{t}\theta \left[\frac{1+\delta(1-\pi)}{1-\delta} - c\right] + & \left[\frac{1-\delta\pi/2}{1-\delta} - c\right] + \\ \frac{\pi\left(\tilde{\mu} + \left(\int_{0}^{\underline{z}^{\mathbb{E}}} \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathbb{E}}}^{1} \tilde{z} \mathrm{d}F(\tilde{z})\right) \left[\delta\frac{2-\pi}{1-\delta} - c\right]\right)}{1-\delta\pi\Delta_{F}\left(\overline{z}^{\mathbb{E}},\underline{z}^{\mathbb{E}}\right)} \\ & \frac{\left[(1-\pi)\left[\frac{1-\delta\pi/2}{1-\delta} - c\right] + \left(\frac{\pi\left(\tilde{\mu} + \left(\int_{0}^{\underline{z}^{\mathbb{E}}} \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathbb{E}}}^{1} \tilde{z} \mathrm{d}F(\tilde{z})\right) \left[\delta\frac{2-\pi}{1-\delta} - c\right]\right)\right]}{\left(1-\delta\pi\Delta_{F}\left(\overline{z}^{\mathbb{E}},\underline{z}^{\mathbb{E}}\right)\right)\left[\delta\frac{2-\pi}{1-\delta} - c\right]}. \end{split}$$

By  $\tilde{z}_t = z_t$  for player 1 and  $\tilde{z}_t = 1 - z_t$  for player 2, substituting them in the above inequality yields the thresholds  $\underline{z}^{\text{E}}$  and  $\overline{z}^{\text{E}}$ .

Step 3 (E-II). Similarly, consider an arbitrary no-disaster period. When the other player is playing strategies (E-I) and (E-II), it is optimal to attack the other when  $W_i^{\neg d} > \theta + \delta V_i^{E}$ . Namely,

$$\frac{1}{2} \left[ 2\theta(1-c) + \delta \frac{\theta(2-\pi)}{1-\delta} \right] > \theta + \delta \theta \cdot \frac{\left[ (1-\pi) \left[ \frac{1-\delta\pi/2}{1-\delta} - c \right] + \left( \frac{\tilde{\mu}}{\pi} \left( \tilde{\mu} + \left( \int_{0}^{\underline{z}^{\mathsf{E}}} \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathsf{E}}}^{1} \tilde{z} \mathrm{d}F(\tilde{z}) \right) \left[ \delta \frac{2-\pi}{1-\delta} - c \right] \right) \right]}{1 - \delta\pi\Delta_{F} \left( \overline{z}^{\mathsf{E}}, \underline{z}^{\mathsf{E}} \right)}$$

$$\tilde{\mu} < \frac{1}{2} + \delta \frac{2-\pi}{1-\delta} \left( \int_{0}^{\underline{z}^{\mathsf{E}}} \frac{1}{2} - \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathsf{E}}}^{1} \frac{1}{2} - \tilde{z} \mathrm{d}F(\tilde{z}) \right) - c \left( \int_{0}^{\underline{z}^{\mathsf{E}}} 1 - \tilde{z} \mathrm{d}F(\tilde{z}) + \int_{\overline{z}^{\mathsf{E}}}^{1} 1 - \tilde{z} \mathrm{d}F(\tilde{z}) + \frac{1-\delta}{\delta\pi} \right).$$

As in the case of Proposition 1, we obtain the desired results by  $\tilde{\mu} = \mu$  and  $\tilde{z} = z$  for Player 1 and  $\tilde{\mu} = 1 - \mu$  and  $\tilde{z} = 1 - z$  for Player 2.

To prove Proposition 3, consider the following lemmas.

**Lemma 1.** Under Assumption 1, there is no mixed-strategy equilibrium.

*Proof.* This directly stems from the fact that players are indifferent between pure strategies in the support of any mixed (equilibrium) strategy. Namely, if a player were to mix attacking and not attacking at some t, she must be indifferent between the two actions. Assumption 1 assigns "not attack" in this case, which rules out mixed-strategy equilibria.

**Lemma 2.** The set of values of  $z_t$  under which a player fights when  $D_t = 1$  constitutes a one-sided interval.

*Proof.* We know that  $W_i^d$  is monotonic in  $z_t$ : it is strictly increasing and decreasing for player 1 and player 2, respectively. Let  $V_i$  represent a continuation payoff generated by arbitrary

equilibrium strategies. Also recall we have denoted  $\tilde{z}_t = \mathbb{1}\{i=1\} \cdot z_t + \mathbb{1}\{i=2\} (1-z_t)$ . Then, player i attacks the other in this equilibrium at period t such that  $D_t = 1$  when

$$\tilde{z}_t \theta \left[ (1-c) + \delta \frac{2-\pi}{1-\delta} \right] > \tilde{z}_t \theta + \delta \mathcal{V}_i$$

$$\tilde{z}_t > \frac{\delta \mathcal{V}_i}{\theta \left[ \delta \frac{2-\pi}{1-\delta} - c \right]}.$$

Note that the continuation payoff  $\mathcal{V}_i$  is not a function of the current realized damage  $\tilde{z}_t$ . Hence, whenever  $\frac{\delta \mathcal{V}_i}{\theta \left[\delta \frac{2-\pi}{1-\delta} - c\right]} \in (0,1)$ , we can conclude that the set of values of  $\tilde{z}_t$  under which i fights is  $\left(\frac{\delta \mathcal{V}_i}{\theta \left[\delta \frac{2-\pi}{1-\delta} - c\right]}, 1\right]$ , which is a one-sided interval.

**Lemma 3.** Fix all parameters and suppose  $\mu \in M^R \cap M^E \neq \emptyset$ . Then,

$$\underline{z}^{R}(\mu) \leq \underline{z}^{E}(\mu)$$
 and  $\overline{z}^{E}(\mu) \leq \overline{z}^{R}(\mu)$ .

Proof. Suppose to the contrary that  $\underline{z}^{\mathtt{R}}(\mu) > \underline{z}^{\mathtt{E}}(\mu)$  or  $\underline{z}^{\mathtt{E}}(\mu) > \underline{z}^{\mathtt{R}}(\mu)$ . However, recall that, in cases  $(\mathtt{E}_1)$  and  $(\mathtt{E}_2)$ , the vulnerable player will fight for sure in any no-disaster period. Without loss of generality, consider case  $(\mathtt{E}_1)$ . Because Player 1 (the vulnerable one) will fight once there is no disaster in  $(\mathtt{E}_1)$ , Player 2 can profitably deviate by setting a smaller  $\overline{z}^{\mathtt{E}_1}(\mu)$  not to miss an advantage when there is a disaster, leading to a contradiction. Similarly, knowing that (i) Player 2 is at least as willing as in  $(\mathtt{R})$  to fight in a disaster period and that (ii) Player 1 will initiate a war without an advantage in any no-disaster period, Player 1 must be more willing to fight in a disaster period and has a profitable deviation by setting a larger  $\underline{z}^{\mathtt{E}_1}(\mu)$ . This contradicts the assumption that  $\underline{z}^{\mathtt{R}}(\mu) > \underline{z}^{\mathtt{E}_1}(\mu)$ . Analogous discussions apply to  $\overline{z}^{\mathtt{E}_1}(\mu) \leq \overline{z}^{\mathtt{R}}(\mu)$ .

**Lemma 4.** Fix all parameters, and suppose  $\mu \in M^R \cap M^E \neq \emptyset$  and that Player i is more vulnerable. Then, the expected probability of her victory in war at a disaster period,  $\mathbb{E}_{Z_t}[p_i^d(Z_t)]$ ,

is greater in (R) than in  $(E_1)$  or  $(E_2)$ .

*Proof.* Without loss of generality, consider case  $(E_1)$ , where Player 1 is the vulnerable one. Suppose to the contrary that  $\mathbb{E}_{Z_t}[p_1^{\mathsf{d}}(Z_t)]$  is greater for  $(E_1)$  than for (R). That is, Player 1 has a better chance of winning in a disaster period under cutoffs  $\underline{z}^{\mathsf{E}_1}$  and  $\overline{z}^{\mathsf{E}_1}$  than under  $\underline{z}^{\mathsf{R}}$  and  $\overline{z}^{\mathsf{R}}$ .

Because we have assumed  $\mu \in M^{\mathbb{R}} \cap M^{\mathbb{E}}$ , there exist multiple equilibria (in this case,  $\mu \in [\underline{\mu}^{\mathbb{R}}, \underline{\mu}^{\mathbb{E}})$ ). The assumption that strategy profile (R) constitutes an equilibrium implies that Player 1 does not have the incentive to deviate to fighting when  $D_t = 0$ , i.e.,  $W_1^{-d} \leq \theta + \delta V_1^{\mathbb{R}}$ . Because strategy profile (E<sub>1</sub>) also constitutes an equilibrium, we have  $W_1^{-d} > \theta + \delta V_1^{\mathbb{E}_1}$ .

Now consider Player 1's deviation to a stationary strategy in which she (i) never attacks Player 2 when  $D_t = 0$  but (ii) still uses cutoff  $\underline{z}^{\mathsf{E}}$  for  $D_t = 1$ . Denote her continuation value under this deviation by  $V_1^{\mathsf{dev}}$ . By the assumption (for the sake of contradiction) that Player 1 has a higher (expected) probability of victory in a disaster period under cutoffs  $\underline{z}^{\mathsf{E}_1}$  and  $\overline{z}^{\mathsf{E}_1}$ , we have  $V_1^{\mathsf{R}} < V_1^{\mathsf{dev}}$ . Consequently, we have established

$$\theta + \delta V_1^{\mathtt{E}_1} < W_1^{-\mathtt{d}} \leq \theta + \delta V_1^{\mathtt{R}} < \theta + \delta V_1^{\mathtt{dev}}.$$

By  $W_1^{\neg d} < \theta + \delta V_1^{\text{dev}}$ , Player 1 has the incentive to deviate to the above strategy profile, which contradicts the assumption that  $(E_1)$  constitutes an equilibrium. Analogous discussions apply to the case of  $(E_2)$ .

**Lemma 5.** Fix parameter values and the functional form of F. Then, we have

$$\underline{\mu}^{\mathtt{R}} < \underline{\mu}^{\mathtt{E}} \quad and \quad \overline{\mu}^{\mathtt{E}} < \overline{\mu}^{\mathtt{R}}.$$

*Proof.* Focus on  $\underline{\mu}^{\mathtt{R}} < \underline{\mu}^{\mathtt{E}}$ . Denote  $V_1^{\mathtt{R}}$  and  $V_1^{\mathtt{E}_1}$  when  $\mu = \underline{\mu}^{\mathtt{R}}$  by  $V_1^{\mathtt{R}} \left(\underline{\mu}^{\mathtt{R}}\right)$  and  $V_1^{\mathtt{E}_1} \left(\underline{\mu}^{\mathtt{R}}\right)$ . First,

we want to show  $V_1^{\mathtt{R}}\left(\underline{\mu}^{\mathtt{R}}\right) > V_1^{\mathtt{E}_1}\left(\underline{\mu}^{\mathtt{R}}\right)$ . Then, we show that it is a sufficient condition for  $\mu^{\mathtt{R}} < \mu^{\mathtt{E}}$ .

Step 1  $(V_1^{\mathbb{R}}(\underline{\mu}^{\mathbb{R}}) > V_1^{\mathbb{E}_1}(\underline{\mu}^{\mathbb{R}}))$ . By the definition of  $\underline{\mu}^{\mathbb{R}}$ , recall  $W_1^{\neg d} = \theta + \delta V_1^{\mathbb{R}}(\underline{\mu}^{\mathbb{R}})$ . Thus, we have

$$V_{1}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right) \ = \ \left(1-\pi\right)W_{1}^{\neg\mathrm{d}} + \pi \left[\begin{array}{c} \Delta_{F}\left(\overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right),\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right)\left(\mathbb{E}\left[Z|Z\in\left[\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right),\overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right]\right]\theta + \delta V_{1}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right) \\ + F\left(\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right)\mathbb{E}\left[Z|Z<\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right]\theta\left[\left(1-c\right) + \delta\frac{2-\pi}{1-\delta}\right] \\ + \left(1-F\left(\overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right)\right)\mathbb{E}\left[Z|Z>\overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right]\theta\left[\left(1-c\right) + \delta\frac{2-\pi}{1-\delta}\right] \\ V_{1}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right) \ = \ \theta \cdot \frac{\left(1-\pi\right)W_{1}^{\neg\mathrm{d}} + \pi\left(\mu + \left(\frac{F\left(\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right)\mathbb{E}\left[Z|Z<\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right]\right)\left[\delta\frac{2-\pi}{1-\delta} - c\right]\right)}{1-\delta\pi\Delta_{F}\left(\overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right),\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right)}.$$

Next, observe

$$V_{1}^{\mathsf{E}_{1}}\left(\underline{\mu}^{\mathsf{R}}\right) \ = \ \theta \cdot \frac{\left(1-\pi\right)W_{1}^{\neg\mathsf{d}}+\pi\left(\mu+\left(\frac{F\left(\underline{z}^{\mathsf{E}_{1}}\left(\underline{\mu}^{\mathsf{R}}\right)\right)\mathbb{E}\left[Z\big|Z<\underline{z}^{\mathsf{E}_{1}}\left(\underline{\mu}^{\mathsf{R}}\right)\right]\right)\left[\delta\frac{2-\pi}{1-\delta}-c\right]\right)}{1-\delta\pi\Delta_{F}\left(\overline{z}^{\mathsf{E}_{1}}\left(\underline{\mu}^{\mathsf{R}}\right),\underline{z}^{\mathsf{E}_{1}}\left(\underline{\mu}^{\mathsf{R}}\right)\right)}.$$

To compare these two quantities, observe that, by Lemma 3,  $\Delta_F\left(\overline{z}^R\left(\underline{\mu}^R\right),\underline{z}^R\left(\underline{\mu}^R\right)\right) > \Delta_F\left(\overline{z}^{E_1}\left(\underline{\mu}^R\right),\underline{z}^{E_1}\left(\underline{\mu}^R\right)\right)$ . Hence, the denominator of  $V_1^R\left(\underline{\mu}^R\right)$  is smaller than that of  $V_1^{E_1}\left(\underline{\mu}^R\right)$ . Then, the only difference in the numerators is the quantities in the inner parentheses. To compare them, write Player 1's expected probability of victory in a disaster period under

strategy profile (R) as, by the law of iterated expectations,

$$\mathbb{E}\left[p_{1}^{\mathsf{d}}(Z)\right] = \mathbb{E}\left[p_{1}^{\mathsf{d}}(Z_{t})\big|\operatorname{War}, Z < \underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right] \operatorname{Pr}\left(\operatorname{War}, Z < \underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right) \\ + \mathbb{E}\left[p_{1}^{\mathsf{d}}(Z_{t})\big|\operatorname{War}, Z \in \left[\underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right), \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right]\right] \operatorname{Pr}\left(\operatorname{War}, Z \in \left[\underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right), \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right]\right) \\ + \mathbb{E}\left[p_{1}^{\mathsf{d}}(Z_{t})\big|\operatorname{War}, Z > \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right] \operatorname{Pr}\left(\operatorname{War}, Z > \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right) \\ = \mathbb{E}\left[p_{1}^{\mathsf{d}}(Z_{t})\big|\operatorname{War}, Z < \underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right] \operatorname{Pr}\left(\operatorname{War}\big|Z < \underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right) \operatorname{Pr}\left(Z < \underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right) \\ + \mathbb{E}\left[p_{1}^{\mathsf{d}}(Z_{t})\big|\operatorname{War}, Z \in \left[\underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right), \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right]\right] \\ \times \operatorname{Pr}\left(\operatorname{War}\big|Z \in \left[\underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right), \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right]\right) \operatorname{Pr}\left(Z \in \left[\underline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right), \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right]\right) \\ + \mathbb{E}\left[p_{1}^{\mathsf{d}}(Z_{t})\big|\operatorname{War}, Z > \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right] \underbrace{\operatorname{Pr}\left(\operatorname{War}\big|Z > \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right)}_{1-F\left(\overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right)} \cdot \\ = 1 \operatorname{(Player 1 fights)} \underbrace{\operatorname{Pr}\left(Z > \overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right)}_{1-F\left(\overline{z}^{\mathsf{R}}\left(\underline{\mu}^{\mathsf{R}}\right)\right)}.$$

By  $p_1^d(Z) = Z$ , we obtain

$$\mathbb{E}\left[p_1^{\mathrm{d}}(Z)\right] = F\left(\underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right) \mathbb{E}\left[Z\middle|Z < \underline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right] + \left(1 - F\left(\overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right)\right) \mathbb{E}\left[Z\middle|Z > \overline{z}^{\mathrm{R}}\left(\underline{\mu}^{\mathrm{R}}\right)\right],$$

which coincides with the quantity in the inner parentheses in the numerator of  $V_1^{\rm R}\left(\underline{\mu}^{\rm R}\right)$ . Similarly, the analogous quantity in  $V_1^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)$  is  $F\left(\underline{z}^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)\right)\mathbb{E}\left[Z\big|Z<\underline{z}^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)\right]+\left(1-F\left(\overline{z}^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)\right)\right)$   $\mathbb{E}\left[Z\big|Z>\overline{z}^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)\right]$ , which is also Player 1's expected probability of victory in a disaster period under strategy profile (E<sub>1</sub>). By Lemma 4, because  $\mathbb{E}\left[p_1^{\rm d}(Z)\right]$  is greater under (R), we have established that the numerator of  $V_1^{\rm R}\left(\underline{\mu}^{\rm R}\right)$  is greater than that of  $V_1^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)$ . Because the numerator is greater and the denominator is smaller in  $V_1^{\rm R}\left(\underline{\mu}^{\rm R}\right)$ , we obtain  $V_1^{\rm R}\left(\underline{\mu}^{\rm R}\right)>V_1^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)$ . Step 2  $(\underline{\mu}^{\rm R}<\underline{\mu}^{\rm E})$ . Because  $V_1^{\rm R}\left(\underline{\mu}^{\rm R}\right)>V_1^{\rm E_1}\left(\underline{\mu}^{\rm R}\right)$  holds, by the definition of  $\underline{\mu}^{\rm R}$ , we have  $W_1^{\rm rd}=\theta+\delta V_1^{\rm R}\left(\underline{\mu}^{\rm R}\right)>\theta+\delta V_1^{\rm E}\left(\underline{\mu}^{\rm R}\right)$ . Also, because Player 1 strictly prefers fighting to not fighting at  $\mu=\underline{\mu}^{\rm R}$  under strategy profile (E<sub>1</sub>), there exists  $\varepsilon>0$  such that  $W_1^{\rm rd}=\theta+\delta V_1^{\rm E}\left(\underline{\mu}^{\rm R}+\varepsilon\right)$ . By the definition of  $\underline{\mu}^{\rm E}$ , we write  $\underline{\mu}^{\rm E}=\underline{\mu}^{\rm R}+\varepsilon$ . By  $\varepsilon>0$ , we obtain  $\underline{\mu}^{\rm E}>\underline{\mu}^{\rm R}$ .

Analogous discussions apply to  $\overline{\mu}^{E} < \overline{\mu}^{R}$ .

**Lemma 6.** When  $\overline{\mu}^R$  and  $\underline{\mu}^R$  satisfy

$$c < \min \left\{ \frac{\frac{1}{2} - \delta \frac{2 - \pi}{1 - \delta} \left( \int_{0}^{\underline{z}^{R}(\overline{\mu}^{R})} \frac{1}{2} - z \mathrm{d}F_{\overline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\overline{\mu}^{R})}^{1} \frac{1}{2} - z \mathrm{d}F_{\overline{\mu}^{R}}(z) \right)}{\int_{0}^{\underline{z}^{R}(\overline{\mu}^{R})} z \mathrm{d}F_{\overline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\overline{\mu}^{R})}^{1} z \mathrm{d}F_{\overline{\mu}^{R}}(z) + \frac{1 - \delta}{\delta \pi}} \right\},$$

$$\left\{ \frac{\frac{1}{2} + \delta \frac{2 - \pi}{1 - \delta} \left( \int_{0}^{\underline{z}^{R}(\underline{\mu}^{R})} \frac{1}{2} - z \mathrm{d}F_{\underline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\underline{\mu}^{R})}^{1} \frac{1}{2} - z \mathrm{d}F_{\underline{\mu}^{R}}(z) \right)}{\int_{0}^{\underline{z}^{R}(\underline{\mu}^{R})} z \mathrm{d}F_{\underline{\mu}^{R}}(z) + \int_{\overline{z}^{R}(\underline{\mu}^{R})}^{1} z \mathrm{d}F_{\underline{\mu}^{R}}(z) + \frac{1 - \delta}{\delta \pi}} \right\},$$

we have  $\underline{\mu}^{\rm R} > 0$  and  $\overline{\mu}^{\rm R} < 1$ .

*Proof.* Using expressions in Proposition 1, rearranging inequalities  $\underline{\mu}^{R} > 0$  and  $\overline{\mu}^{R} < 1$  immediately leads to the condition in the lemma.

Now we are ready to prove Proposition 3.

Proof of Proposition 3. Assumption 1 and Lemma 1 guarantee that, in stationary strategies, each player either fights for sure or never fights in no-disaster periods. This observation and Lemma 2 imply that there are only three combinations of equilibrium strategies in our equilibrium concept (stationary MPE in pure strategies): (i) Neither attacks when  $D_t = 0$ ; (ii) Player 1 attacks when  $D_t = 0$ ; and (iii) Player 2 attacks when  $D_t = 0$ , all with one-sided intervals of  $z_t$  under which players fight when  $D_t = 1$ . They correspond to strategy profiles (R) (E<sub>1</sub>), and (E<sub>2</sub>), respectively. Lemma 5 shows that there are regions of equilibrium multiplicity,  $[\underline{\mu}^{\mathtt{R}}, \underline{\mu}^{\mathtt{E}}]$  and  $(\overline{\mu}^{\mathtt{E}}, \overline{\mu}^{\mathtt{R}}]$ . Finally, Lemma 6 implicitly specifies conditions under which the partition exists in [0, 1].

Proof of Corollary 1. By Proposition 1, we have

Pr (Conflict at 
$$t$$
 such that  $D_t = 1$  in case (R)) = Pr  $(Y_t^{\text{game}} = 1 | D_t = 1, \mu^{\text{R}})$   
 $\in (0, 1)$  and  
Pr (Conflict at  $t$  such that  $D_t = 0$  in case (R)) = Pr  $(Y_t^{\text{game}} = 1 | D_t = 0, \mu^{\text{R}})$   
 $= 0.$ 

Similarly, Proposition 2 yields

Pr (Conflict at 
$$t$$
 such that  $D_t = 1$  in cases  $(E_1)$  or  $(E_2)$ ) = Pr  $(Y_t^{\text{game}} = 1 | D_t = 1, \mu^{\text{E}})$   
 $\in (0, 1)$  and  
Pr (Conflict at  $t$  such that  $D_t = 0$  in cases  $(E_1)$  or  $(E_2)$ ) = Pr  $(Y_t^{\text{game}} = 1 | D_t = 0, \mu^{\text{E}})$   
= 1.

which completes the proof.

Proof of Corollary 2. This result follows directly from Bayes' rule. First, we can rewrite the

left-hand side of the inequality (Pr  $(\mu^{RV} \in M^E | Y_t^{game} = 1, D_t = 0))$  as follows.

$$\begin{split} & \Pr\left(\mu^{\text{RV}} \in M^{\text{E}} \middle| Y_{t}^{\text{game}} = 1, D_{t} = 0\right) \\ & = \frac{\Pr\left(Y_{t}^{\text{game}} = 1, D_{t} = 0 \middle| \mu^{\text{RV}} \in M^{\text{E}}\right) \Pr\left(\mu^{\text{RV}} \in M^{\text{E}}\right)}{\Pr\left(Y_{t}^{\text{game}} = 1, D_{t} = 0 \middle| \mu^{\text{RV}} \notin M^{\text{E}}\right) \Pr\left(\mu^{\text{RV}} \in M^{\text{E}}\right) +} \\ & \Pr\left(Y_{t}^{\text{game}} = 1, D_{t} = 0 \middle| \mu^{\text{RV}} \notin M^{\text{E}}\right) \left(1 - \Pr\left(\mu^{\text{RV}} \in M^{\text{E}}\right)\right) \\ & = \frac{1}{\Pr\left(Y_{t}^{\text{game}} = 1 \middle| D_{t} = 0, \mu^{\text{RV}} \in M^{\text{E}}\right) \Pr\left(D_{t} = 0 \middle| \mu^{\text{RV}} \in M^{\text{E}}\right) \Pr\left(\mu^{\text{RV}} \in M^{\text{E}}\right)}{\Pr\left(Y_{t}^{\text{game}} = 1 \middle| D_{t} = 0, \mu^{\text{RV}} \notin M^{\text{E}}\right) \Pr\left(D_{t} = 0 \middle| \mu^{\text{RV}} \notin M^{\text{E}}\right) \Pr\left(\mu^{\text{RV}} \in M^{\text{E}}\right) +} \\ & = \frac{\Pr\left(Y_{t}^{\text{game}} = 1 \middle| D_{t} = 0, \mu^{\text{RV}} \notin M^{\text{E}}\right) \Pr\left(D_{t} = 0 \middle| \mu^{\text{RV}} \notin M^{\text{E}}\right) \Pr\left(\mu^{\text{RV}} \in M^{\text{E}}\right) +}{\mathbb{E}\left(0,1\right)} \\ & = 1. \end{split}$$

Similarly, we have

$$\begin{split} & \Pr \left( {{\mu ^{{\text{RV}}}} \in {M^{\text{E}}}{\left| {{Y_t^{\text{game}}}} \right.} = 1,{D_t} = 1} \right) } \\ & = \frac{{\Pr \left( {{Y_t^{\text{game}}} = 1,{D_t} = 1|{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)\Pr \left( {{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)}}{{\Pr \left( {{Y_t^{\text{game}}} = 1,{D_t} = 1|{\mu ^{\text{RV}}} \notin {M^{\text{E}}}} \right)\Pr \left( {{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right) + } \\ & = \frac{{\Pr \left( {{Y_t^{\text{game}}} = 1,{D_t} = 1|{\mu ^{\text{RV}}} \notin {M^{\text{E}}}} \right)\left( {1 - \Pr \left( {{\mu ^{\text{RV}}} \in {M^{\text{E}}}}} \right)} \right)}}{{\Pr \left( {{Y_t^{\text{game}}} = 1|{D_t} = 1,{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)\Pr \left( {{D_t} = 1|{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)\Pr \left( {{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)}}}{{\Pr \left( {{Y_t^{\text{game}}} = 1|{D_t} = 1,{\mu ^{\text{RV}}} \notin {M^{\text{E}}}}} \right)\Pr \left( {{D_t} = 1|{\mu ^{\text{RV}}} \notin {M^{\text{E}}}} \right)\Pr \left( {{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)}}} \\ & = \frac{{\Pr \left( {{Y_t^{\text{game}}} = 1|{D_t} = 1,{\mu ^{\text{RV}}} \notin {M^{\text{E}}}}} \right)}}}{{\Pr \left( {{Y_t^{\text{game}}} = 1|{D_t} = 1,{\mu ^{\text{RV}}} \notin {M^{\text{E}}}}} \right)\Pr \left( {{D_t} = 1|{\mu ^{\text{RV}}} \notin {M^{\text{E}}}} \right)\Pr \left( {{1 - \Pr \left( {{\mu ^{\text{RV}}} \in {M^{\text{E}}}} \right)}} \right)}}}{ \in (0,1)}} \\ & < 1, \end{split}$$

which yields the desired result.

Proof of Corollary 3. By Corollary 1 and the identity  $Y_{dt}^{\mathtt{data}} = D_{dt}Y_{dt}^{\mathtt{PO}}(1) + (1 - D_{dt})Y_{dt}^{\mathtt{PO}}(0)$ ,

direct substitutions yield part (i) of the statement:

$$\begin{split} & \operatorname{Pr}\left(Y_{t}^{\mathsf{game}} = 1 \middle| D_{t} = 1, \mu^{\mathtt{R}}\right) > \operatorname{Pr}\left(Y_{t}^{\mathsf{game}} = 1 \middle| D_{t} = 0, \mu^{\mathtt{R}}\right) \\ & \overset{\mathsf{Assumption 4}}{\Longrightarrow} & \operatorname{Pr}\left(Y_{dt}^{\mathtt{data}} = 1 \middle| D_{dt} = 1, \mu^{\mathtt{R}}\right) > \operatorname{Pr}\left(Y_{dt}^{\mathtt{data}} = 1 \middle| D_{dt} = 0, \mu^{\mathtt{R}}\right) \\ & \Longrightarrow & \operatorname{Pr}\left(Y_{dt}^{\mathtt{PO}}(1) = 1 \middle| \mu^{\mathtt{R}}\right) > \operatorname{Pr}\left(Y_{dt}^{\mathtt{PO}}(0) = 1 \middle| \mu^{\mathtt{R}}\right). \end{split}$$

Part (ii) is derived in the same manner.