## lec2\_step1

## November 30, 2022

```
[15]: ## Python basics for novice data scientists, supported by Wagatsuma Lab@Kyutech
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        →FROM, OUT OF OR IN CONNECTION WITH THE SOFTWARE OR THE USE OR OTHER DEALINGS
       → IN THE SOFTWARE. */
       # # @Time : 2022-8-10
       # # @Author : Hiroaki Wagatsuma
       # # @Site : https://qithub.com/hirowqit/2A1 python intermediate_course
                   : Python 3.9.13 (main, Aug 7 2022, 01:33:23) [Clang 13.1.6⊔
       # # @IDE
        \hookrightarrow (clang-1316.0.21.2.5)] on darwin
       # # @File
                    : lec2_step1.py
[512]: import numpy as np
       import matplotlib.pyplot as plt
[163]: allData = np.loadtxt('allData200.csv', delimiter=',', dtype='int64')
       allData
[163]: array([[ 9, 7, 3, ..., 4, 1, 10],
              [6, 4, 10, ..., 5, 1,
              [4, 3, 6, ..., 10, 1, 8],
```

```
[3, 4, 1, ..., 2, 7,
                                         8],
               [6, 7,
                         3, ..., 8,
                                     9,
                                          4],
               [9, 8, 5, ..., 10, 7,
                                          6]])
[158]: a = np.array([[1,2,4],[3,2,1]])
       np.sort(a, axis=None)
[158]: array([1, 1, 2, 2, 3, 4])
[160]: np.sort(a, axis=0)
[160]: array([[1, 2, 1],
               [3, 2, 4]])
[394]: allData_sample=allData[0:20,:]
       np.sort(allData_sample,axis=0)
[394]: array([[ 1,
                     1,
                         2,
                              1,
                                  1,
                                      1,
                                                   1,
                                                        1],
                                          1,
                                               1,
               [ 2,
                     2,
                         2,
                              1,
                                  1,
                                      1,
                                           1,
                                               2,
                                                   1,
                                                        2],
               [ 2,
                     3,
                         3,
                              2,
                                  1,
                                      2,
                                           1,
                                               2,
                                                   1,
                                                        2],
               [ 2,
                     3,
                              2,
                                  1,
                                      3,
                                               2,
                         3,
                                          1,
                                                   1,
                                                        5],
               [ 3,
                         3,
                     3,
                              3,
                                  2,
                                      3,
                                           2,
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                                                        6],
                                  3,
               [ 3,
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                                                        6],
                     4,
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               [4,
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                         4,
                              5,
                                  3,
                                      4,
                                           3,
                                               3,
                                                   3,
                                                       7],
               [4,
                     4,
                              5,
                                  5,
                                      4,
                                           3,
                                                   4,
                                                       7],
                         4,
                                               3,
               [5,
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                              5,
                                  5,
                                      4,
                                           4,
                                               4,
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                         4,
               [6,
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                                                       7],
                     4,
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                                      5,
                                          5,
                              7,
               [ 6,
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                                                       7],
               [7,
                     6,
                         6,
                             7,
                                  6,
                                      6,
                                           5,
                                               5,
                                                   6,
                                                       7],
                                      6,
               [8,
                     6,
                         6,
                             8,
                                  7,
                                           6,
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                                               5,
               [8,
                     6,
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                                  7,
                                      7,
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                                               6,
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                                                        8],
                                  9,
               [8,
                     7,
                         7,
                             8,
                                      8,
                                          8,
                                               6,
                                                   8,
                                                        9],
                                                   9,
               [ 9,
                     7,
                         7,
                             9,
                                  9,
                                      8,
                                          8,
                                               8,
                                                       9],
               [ 9,
                     8,
                             9, 10,
                                      9,
                                                   9,
                         8,
                                          8,
                                               8,
                             9, 10, 10,
               [ 9,
                    8,
                         9,
                                          8, 8, 10, 10],
               [ 9, 10,
                         9, 9, 10, 10, 9, 10, 10, 10],
               [10, 10, 10, 10, 10, 9, 10, 10, 10]])
[170]: data = np.array([[3, 0, 0, .24],
                          [4, 1, 1, .41],
                          [2, 1, 1, .63],
                          [1, 1, 3, .38]]) #imagine rows of a spreadsheet
       #now do sortrows(data,[3,-4])
       ix = np.lexsort((data[:, 3][::-1], data[:, 2]))
       #this yields [0, 2, 1, 3]
```

```
#note that lexsort sorts first from the last row, so sort keys are in reverse,
       \hookrightarrow order
      data[ix]
[170]: array([[3., 0., 0., 0.24],
             [2. , 1. , 1. , 0.63],
             [4., 1., 1., 0.41],
             [1. , 1. , 3. , 0.38]])
[177]: sample_2d = np.array([[50,4, 89], [5, 150, 20], [110, 8, 1]])
      print(sample_2d)
      print(' ')
      col id = 1
      print(sample_2d[:, col_id])
      print(' ')
      print(np.argsort(a_2d[:, col_id]))
      [[ 50
             4 89]
       Γ 5 150
                201
      Γ110
            8
                1]]
      [ 4 150
                8]
      [0 2 1]
[178]: | sorted_by_col = sample_2d[np.argsort(sample_2d[:, col_id])]
      print(sorted_by_col)
      [[ 50
             4 89]
       [110
                 1]
             8
       [ 5 150 20]]
[460]: allData_sample
                                               1, 10],
[460]: array([[ 9, 7, 3,
                           5, 6,
                                   2, 8, 4,
             [6, 4, 10,
                           7,
                                   3,
                                       8,
                               9,
                                           5,
                                               1,
                       6,
                           2,
                              7,
                                   5,
                                       9, 10,
                                               1,
                                                   8],
             [3, 6,
                       7,
                           4,
                               1,
                                   8,
                                       2,
                                           5,
                                               9, 10],
                           8,
                       4,
             [ 1, 10,
                              7,
                                   6,
                                       3,
                                           5,
                                               2,
                                                   91.
             [7, 8,
                       9,
                           2,
                               3,
                                   4,
                                       5, 10,
                                               1,
                                                   6],
             [ 9, 4,
                       2,
                           5, 10,
                                   3,
                                       1,
                                               6,
                                                 7],
                                           8,
             [5, 8, 4,
                           9,
                               3,
                                   1,
                                      7,
                                           6,
                                               2, 10],
                                   4,
             [ 9, 10, 3, 6,
                                               5, 7],
                              1,
                                      8,
                                           2,
                                  9,
             [3, 6, 2, 10,
                              1,
                                      4,
                                           8,
                                                  7],
             [2, 4, 3, 9, 6, 10, 1,
                                           8, 5, 7],
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[8,
                          7,
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                                  5, 10,
                                            2,
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                                                    3,
                                                         6],
               [4,
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                          8,
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                                       6,
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               [10,
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                                   6,
                                       4,
                                            8,
                                                3,
                                                         7],
               [6,
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                                                     7,
                              8,
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               [ 9,
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               [ 2,
                              8, 10,
                                       7,
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                          5,
                                                         9],
               [ 2,
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                                       8,
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                                                4, 10,
                                                         1],
                                  9,
                             7,
                                       4,
               [8,
                     3,
                          6,
                                           1,
                                                2, 10,
                                                         5]])
[461]: sorted_data=np.sort(allData_sample, axis=0)
       sorted_data
[461]: array([[ 1,
                                            1,
                                                         1],
                     1,
                          2,
                               1,
                                   1,
                                       1,
                                                1,
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               [ 2,
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               [ 3,
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               [4,
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               [4,
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               [5,
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               [6,
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                                       9,
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               [ 9,
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                     8,
                          9,
                              9, 10, 10,
                                            8,
                                                8, 10, 10],
               [ 9, 10, 9, 9, 10, 10, 9, 10, 10, 10],
               [10, 10, 10, 10, 10, 9, 10, 10, 10]])
[462]: diffData=np.diff(sorted_data,axis=0)
       diffData
[462]: array([[1, 1, 0, 0, 0, 0, 0, 1, 0, 1],
               [0, 1, 1, 1, 0, 1, 0, 0, 0, 0],
               [0, 0, 0, 0, 0, 1, 0, 0, 0, 3],
               [1, 0, 0, 1, 1, 0, 1, 0, 1, 1],
               [0, 1, 0, 1, 1, 1, 0, 1, 0, 0],
               [1, 0, 1, 1, 0, 0, 1, 0, 1, 1],
               [0, 0, 0, 0, 2, 0, 0, 0, 1, 0],
               [1, 0, 0, 0, 0, 0, 1, 1, 1, 0],
               [1, 0, 1, 1, 1, 0, 1, 0, 0, 0],
               [0, 1, 0, 1, 0, 1, 0, 1, 0, 0],
```

9, 2, 1,

6,

3, 10,

7],

[8,

5,

4,

```
[1, 0, 0, 1, 1, 0, 1, 0, 1, 0],
              [0, 0, 0, 0, 0, 1, 1, 1, 0, 1],
              [0, 1, 1, 0, 2, 1, 1, 0, 1, 1],
              [1, 0, 0, 1, 0, 0, 0, 2, 1, 0],
              [0, 1, 1, 0, 1, 1, 0, 0, 0, 0],
              [0, 0, 1, 0, 0, 1, 0, 0, 1, 1],
              [0, 2, 0, 0, 0, 0, 1, 2, 0, 0],
              [1, 0, 1, 1, 0, 0, 0, 0, 0, 0]])
[464]:
[464]: array([[1, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 0, 0, 1, 0, 0, 0, 1],
              [1, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 1, 0, 1, 0, 2, 0],
              [0, 1, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0, 1],
              [0, 1, 0, 1, 1, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 0, 0, 1],
              [0, 0, 0, 1, 1, 0, 2, 0, 1, 0, 0, 1, 0, 2, 0, 1, 0, 0, 0],
              [0, 1, 1, 0, 1, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 0],
              [0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0],
              [1, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1, 0, 2, 0, 0, 2, 0],
              [0, 0, 0, 1, 0, 1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0],
              [1, 0, 3, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 0, 1, 0, 0]])
[465]: key=np.where(np.transpose(diffData)>0)
      key
[465]: (array([0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2,
              2, 2, 2, 3, 3, 3, 3, 3, 3, 3, 3, 4, 4, 4, 4, 4, 4, 4, 5, 5, 5,
              5, 5, 5, 5, 5, 5, 6, 6, 6, 6, 6, 6, 6, 6, 7, 7, 7, 7, 7, 7, 7, 8,
              8, 8, 8, 8, 8, 8, 8, 9, 9, 9, 9, 9, 9, 9]),
       array([ 0, 3, 5, 7, 8, 10, 11, 14, 18, 0,
                                                      1, 4, 9, 10, 13, 15, 17,
                       8, 10, 13, 15, 16, 18,
                                                   3,
                                                       4, 5, 8, 9, 11, 14, 18,
                   5,
                                               1,
                                              2,
                                                  4,
                                                      9, 10, 12, 13, 15, 16, 3,
                       6, 8, 11, 13, 15, 1,
                                                  7, 9, 12, 14, 17, 3, 5,
               5, 7, 8, 11, 12, 13, 17, 0,
                                              4,
               7, 10, 11, 13, 14, 16, 0, 2, 3, 5, 12, 13, 16]))
[466]: kj=key[0]
      kj
[466]: array([0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2,
             2, 2, 2, 3, 3, 3, 3, 3, 3, 3, 3, 4, 4, 4, 4, 4, 4, 4, 5, 5, 5,
             5, 5, 5, 5, 5, 5, 6, 6, 6, 6, 6, 6, 6, 7, 7, 7, 7, 7, 7, 8,
             8, 8, 8, 8, 8, 8, 8, 8, 9, 9, 9, 9, 9, 9, 9])
[467]: ki=key[1]
      ki
```

[1, 1, 1, 0, 0, 1, 0, 0, 1, 0],

```
[467]: array([ 0, 3, 5, 7, 8, 10, 11, 14, 18, 0, 1, 4, 9, 10, 13, 15, 17,
              1, 5, 8, 10, 13, 15, 16, 18,
                                             1, 3, 4, 5, 8, 9, 11, 14, 18,
                                              2, 4, 9, 10, 12, 13, 15, 16,
              3, 4, 6, 8, 11, 13, 15, 1,
              5, 7, 8, 11, 12, 13, 17, 0, 4, 7, 9, 12, 14, 17, 3, 5, 6,
              7, 10, 11, 13, 14, 16, 0, 2, 3, 5, 12, 13, 16])
[468]: bodyK=np.where(np.diff(kj)>0)
      bodyK
[468]: (array([ 8, 16, 24, 33, 40, 49, 57, 64, 73]),)
[403]: sizeD=np.shape(allData_sample)
      sizeD
[403]: (20, 10)
[469]: \# n0=np.array([0], dtype=int)
      np.concatenate([bodyK, bodyK],axis=1)
[469]: array([[ 8, 16, 24, 33, 40, 49, 57, 64, 73, 8, 16, 24, 33, 40, 49, 57,
              64, 73]])
[234]: np.array([0])
[234]: array([0])
[237]: bodyK
[237]: (array([ 5, 11, 16, 21, 28, 38, 43, 50]),)
[247]: bodyK
[247]: (array([ 5, 11, 16, 21, 28, 38, 43, 50]),)
[277]: a1 = np.ones((1,3), int)
      a2 = np.ones((1,3), int)
      np.concatenate([a1, a2],axis=1)
[277]: array([[1, 1, 1, 1, 1, 1]])
[270]: a1 = np.ones((1,3), int)
[299]: [0,list(bodyK), len(kj)]
[299]: [0, [array([ 5, 11, 16, 21, 28, 38, 43, 50])], 57]
[266]: np.shape(bodyK)
```

```
[266]: (1, 8)
[281]: len(kj)
[281]: 57
        len(kj)*np.ones((1,1), int)
[284]:
[284]: array([[57]])
[285]: [[ len(kj)]]
[285]: [[57]]
[294]: bodyK
[294]: (array([ 5, 11, 16, 21, 28, 38, 43, 50]),)
[296]: list(bodyK)
[296]: [array([ 5, 11, 16, 21, 28, 38, 43, 50])]
[302]: arr_1d=list(bodyK)
       bodyK.tolist()
                                                  Traceback (most recent call last)
        /var/folders/mg/w5t8lkhc8xj79f001s7kzpfh0000gp/T/ipykernel_46672/3209845136.pyu
        →in <module>
              1 arr_1d=list(bodyK)
        ----> 2 bodyK.tolist()
        AttributeError: 'tuple' object has no attribute 'tolist'
[303]: bodyK
[303]: (array([ 5, 11, 16, 21, 28, 38, 43, 50]),)
[307]: bodyK
[307]: (array([ 5, 11, 16, 21, 28, 38, 43, 50]),)
[308]: kj
[308]: array([0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3,
              4, 4, 4, 4, 4, 4, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 6, 6, 6, 6, 6,
```

```
[313]: kj[bodyK]
[313]: array([0, 1, 2, 3, 4, 5, 6, 7])
[314]: ab=np.concatenate([[[0]], bodyK],axis=1)
[314]: array([[ 0, 5, 11, 16, 21, 28, 38, 43, 50]])
[315]: kj[ab]
       NameError
                                                Traceback (most recent call last)
       /var/folders/mg/w5t8lkhc8xj79f001s7kzpfh0000gp/T/ipykernel_46672/942133995.py i: _
        →<module>
       ----> 1 kj[ab]
       NameError: name 'ab' is not defined
[496]: bodyK2=bodyK+np.array([[1]])
      sect id=np.insert(bodyK2, 0,0)
      sect_id=np.append(sect_id, len(kj))
      sect id
[496]: array([ 0, 9, 17, 25, 34, 41, 50, 58, 65, 74, 81])
[497]: kj
[497]: array([0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2,
             2, 2, 2, 3, 3, 3, 3, 3, 3, 3, 3, 3, 4, 4, 4, 4, 4, 4, 4, 5, 5, 5,
             5, 5, 5, 5, 5, 6, 6, 6, 6, 6, 6, 6, 6, 7, 7, 7, 7, 7, 7, 7, 8,
             8, 8, 8, 8, 8, 8, 8, 8, 9, 9, 9, 9, 9, 9, 9])
[498]: ki
[498]: array([ 0, 3, 5, 7, 8, 10, 11, 14, 18, 0, 1, 4, 9, 10, 13, 15, 17,
              1, 5, 8, 10, 13, 15, 16, 18, 1, 3, 4, 5, 8, 9, 11, 14, 18,
              3, 4, 6, 8, 11, 13, 15, 1, 2, 4, 9, 10, 12, 13, 15, 16,
              5, 7, 8, 11, 12, 13, 17, 0, 4, 7, 9, 12, 14, 17, 3, 5, 6,
              7, 10, 11, 13, 14, 16, 0, 2, 3, 5, 12, 13, 16])
[339]: kj[sect_id]
[339]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 8])
```

7, 7, 7, 7, 7, 7, 8, 8, 8, 8, 8, 8])

```
[363]: kj[sect_id[0]:sect_id[1]]
[363]: array([0, 0, 0, 0, 0, 0, 1])
[368]: sect_id[1]
[368]: 6
[499]: g2=np.arange(sect_id[0],sect_id[1])
       g2
[499]: array([0, 1, 2, 3, 4, 5, 6, 7, 8])
[347]: kj[sect_id[1]:sect_id[2]]
[347]: array([1, 1, 1, 1, 1, 1])
[367]: kj[g2]
[367]: array([0, 0, 0, 0, 0, 0])
[350]: sect_id
[350]: array([ 0, 6, 12, 17, 22, 29, 39, 44, 51, 56])
[501]: setN=sizeD[0]
       NofD=sizeD[1]
[500]: sect_eg=np.vstack([sect_id[0:-1],sect_id[1:]])
       sect_eg
[500]: array([[ 0, 9, 17, 25, 34, 41, 50, 58, 65, 74],
              [ 9, 17, 25, 34, 41, 50, 58, 65, 74, 81]])
[502]: sect_egT=np.transpose(sect_eg)
       sect_egT
[502]: array([[ 0, 9],
              [9, 17],
              [17, 25],
              [25, 34],
              [34, 41],
              [41, 50],
              [50, 58],
              [58, 65],
              [65, 74],
              [74, 81]])
```

```
[492]: [sect_egT[i] for i in range(0,5)]
[492]: [array([0, 9]),
       array([ 9, 17]),
       array([17, 25]),
       array([25, 34]),
       array([34, 41])]
[439]: sect_egT[0][1]
[439]: 4
[440]: len(sect_egT)
[440]: 19
[503]: | [kj[sect_egT[i][0]:sect_egT[i][1]] for i in range(0,len(sect_egT))]
[503]: [array([0, 0, 0, 0, 0, 0, 0, 0]),
       array([1, 1, 1, 1, 1, 1, 1, 1]),
       array([2, 2, 2, 2, 2, 2, 2]),
       array([3, 3, 3, 3, 3, 3, 3, 3]),
       array([4, 4, 4, 4, 4, 4, 4]),
       array([5, 5, 5, 5, 5, 5, 5, 5]),
       array([6, 6, 6, 6, 6, 6, 6, 6]),
       array([7, 7, 7, 7, 7, 7]),
       array([8, 8, 8, 8, 8, 8, 8, 8]),
       array([9, 9, 9, 9, 9, 9])]
[518]: | sect_range=[ki[sect_egT[i][0]:sect_egT[i][1]] | for i in range(0,len(sect_egT))]
      sect_range
[518]: [array([ 0, 3, 5, 7, 8, 10, 11, 14, 18]),
       array([ 0, 1, 4, 9, 10, 13, 15, 17]),
       array([ 1, 5,
                      8, 10, 13, 15, 16, 18]),
       array([ 1, 3,
                       4, 5, 8, 9, 11, 14, 18]),
       array([ 3, 4,
                       6, 8, 11, 13, 15]),
                       4, 9, 10, 12, 13, 15, 16]),
       array([ 1, 2,
       array([ 3, 5,
                       7, 8, 11, 12, 13, 17]),
       array([ 0, 4, 7, 9, 12, 14, 17]),
       array([3, 5, 6, 7, 10, 11, 13, 14, 16]),
       array([0, 2, 3, 5, 12, 13, 16])]
[505]: [np.diff(np.hstack([-1,d,setN-1])) for d in sect_range]
[505]: [array([1, 3, 2, 2, 1, 2, 1, 3, 4, 1]),
       array([1, 1, 3, 5, 1, 3, 2, 2, 2]),
```

```
array([2, 4, 3, 2, 3, 2, 1, 2, 1]),
       array([2, 2, 1, 1, 3, 1, 2, 3, 4, 1]),
       array([4, 1, 2, 2, 3, 2, 2, 4]),
       array([2, 1, 2, 5, 1, 2, 1, 2, 1, 3]),
       array([4, 2, 2, 1, 3, 1, 1, 4, 2]),
       array([1, 4, 3, 2, 3, 2, 3, 2]),
       array([4, 2, 1, 1, 3, 1, 2, 1, 2, 3]),
       array([1, 2, 1, 2, 7, 1, 3, 3])]
[508]: | [np.diff(np.hstack([-1,d,setN-1]))/setN for d in sect_range]
[508]: [array([0.05, 0.15, 0.1, 0.1, 0.05, 0.1, 0.05, 0.15, 0.2, 0.05]),
       array([0.05, 0.05, 0.15, 0.25, 0.05, 0.15, 0.1, 0.1, 0.1]),
       array([0.1, 0.2, 0.15, 0.1, 0.15, 0.1, 0.05, 0.1, 0.05]),
       array([0.1, 0.1, 0.05, 0.05, 0.15, 0.05, 0.1, 0.15, 0.2, 0.05]),
       array([0.2, 0.05, 0.1, 0.1, 0.15, 0.1, 0.1, 0.2]),
       array([0.1, 0.05, 0.1, 0.25, 0.05, 0.1, 0.05, 0.1, 0.05, 0.15]),
       array([0.2, 0.1, 0.1, 0.05, 0.15, 0.05, 0.05, 0.2, 0.1]),
       array([0.05, 0.2, 0.15, 0.1, 0.15, 0.1, 0.15, 0.1]),
       array([0.2, 0.1, 0.05, 0.05, 0.15, 0.05, 0.1, 0.05, 0.1, 0.15]),
       array([0.05, 0.1, 0.05, 0.1, 0.35, 0.05, 0.15, 0.15])]
[519]: NofE_data=[np.diff(np.hstack([-1,ki[sect_egT[i][0]:sect_egT[i][1]]],setN-1]))
       →for i in range(0,len(sect egT))]
      NofE_data
[519]: [array([1, 3, 2, 2, 1, 2, 1, 3, 4, 1]),
       array([1, 1, 3, 5, 1, 3, 2, 2, 2]),
       array([2, 4, 3, 2, 3, 2, 1, 2, 1]),
       array([2, 2, 1, 1, 3, 1, 2, 3, 4, 1]),
       array([4, 1, 2, 2, 3, 2, 2, 4]),
       array([2, 1, 2, 5, 1, 2, 1, 2, 1, 3]),
       array([4, 2, 2, 1, 3, 1, 1, 4, 2]),
       array([1, 4, 3, 2, 3, 2, 3, 2]),
       array([4, 2, 1, 1, 3, 1, 2, 1, 2, 3]),
       array([1, 2, 1, 2, 7, 1, 3, 3])]
[520]: NofE_{data_p}=[np.diff(np.hstack([-1,ki[sect_egT[i][0]:sect_egT[i][1]]],setN-1]))/
       \rightarrowsetN
                for i in range(0,len(sect egT))]
      NofE_data_p
[520]: [array([0.05, 0.15, 0.1, 0.1, 0.05, 0.1, 0.05, 0.15, 0.2, 0.05]),
       array([0.05, 0.05, 0.15, 0.25, 0.05, 0.15, 0.1, 0.1, 0.1]),
       array([0.1, 0.2, 0.15, 0.1, 0.15, 0.1, 0.05, 0.1, 0.05]),
       array([0.1, 0.1, 0.05, 0.05, 0.15, 0.05, 0.1, 0.15, 0.2, 0.05]),
       array([0.2, 0.05, 0.1, 0.1, 0.15, 0.1, 0.1, 0.2]),
       array([0.1, 0.05, 0.1, 0.25, 0.05, 0.1, 0.05, 0.1, 0.05, 0.15]),
```

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array([0.2, 0.1, 0.1, 0.05, 0.15, 0.05, 0.05, 0.2, 0.1]),
       array([0.05, 0.2, 0.15, 0.1, 0.15, 0.1, 0.15, 0.1]),
       array([0.2, 0.1, 0.05, 0.05, 0.15, 0.05, 0.1, 0.05, 0.1, 0.15]),
        array([0.05, 0.1 , 0.05, 0.1 , 0.35, 0.05, 0.15, 0.15])]
[521]: NofE_data_p[1]
[521]: array([0.05, 0.05, 0.15, 0.25, 0.05, 0.15, 0.1 , 0.1 , 0.1])
[524]: x=np.arange(0,NofD)
       y=NofE_data_p[3]
       plt.plot(x,y)
       plt.show()
               0.20
               0.18
               0.16
               0.14
               0.12
               0.10
               0.08
               0.06
                      0
                                   2
                                              4
                                                           6
                                                                      8
 []:
[517]: np.arange(0,NofD)
[517]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
[454]: sorted_data
[454]: array([[ 1,
                    1,
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              [ 9, 8,
                        9,
                            9, 10, 10,
                                         8, 8, 10, 10],
              [ 9, 10, 9, 9, 10, 10, 9, 10, 10, 10],
              [10, 10, 10, 10, 10, 9, 10, 10, 10]])
  []: sect_range=[ki[sect_egT[i][0]:sect_egT[i][1]] for i in range(0,len(sect_egT))]
       sect_range
[373]: array([0, 6])
[325]: sect_id[0:-1]
[325]: array([ 0, 5, 11, 16, 21, 28, 38, 43, 50])
[333]: kj[sect_id[0:-1]]
[333]: array([0, 0, 1, 2, 3, 4, 5, 6, 7])
[327]: bodyK
[327]: (array([ 5, 11, 16, 21, 28, 38, 43, 50]),)
[331]: bodyK-np.array([[1]])
[331]: array([[ 4, 10, 15, 20, 27, 37, 42, 49]])
                                                   Traceback (most recent call last)
        /var/folders/mg/w5t8lkhc8xj79f001s7kzpfh0000gp/T/ipykernel_46672/466309160.py i
        →<module>
        ----> 1 setN
```

[373]: g3[0]

[388]: setN

NameError: name 'setN' is not defined

[]: