

System of Linear Equation

L1.3

eq₁ $8x + 8y + 4z = 1960 \Rightarrow$ Buyer A \rightarrow $\frac{\text{div}}{\text{by } 2}$ $4x + 4y + 2z = 980$
 $\hookrightarrow \underline{\underline{\times 3}}$
 $12x + 12y + 6z = 2940$
 \downarrow
 Subtract from,
 $7y - z = 725$
 ... (solve the rest during revision)

- $12x + 5y + 7z = 2216 \Rightarrow$ Buyer B
 - $3x + 2y + 5z = 1135 \Rightarrow$ Buyer C

- linear eqⁿ is an eqⁿ in the form,

$$a_1x_1 + a_2x_2 + \dots + a_nx_n = b$$

\hookrightarrow real no.

x_1, x_2 are the variables.

a_1, a_2 are the coefficients.

- A system of linear eqⁿ is the collection of more linear eqⁿ with same set of variables.

- The solⁿ is the group of values to the variables such that all the eqⁿ are simultaneously satisfied...

- System of linear eqⁿ is equivalent to a matrix eqⁿ of form

$$\boxed{Ax = b}$$

coefficient matrix $\begin{bmatrix} a_{11} & a_{12} & \dots \\ \vdots & \vdots & \ddots \end{bmatrix}$

column matrix $\begin{bmatrix} x_1 \\ x_2 \\ \vdots \end{bmatrix}$

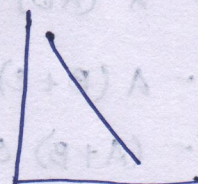
- There are 3 possibilities for the solⁿ of linear system of eqⁿ.

- ∞ solⁿ
- 1 unique solⁿ
- no solⁿ

- ∞ solⁿ \Rightarrow $2x + y = 215$
 $4x + 2y = 430$

both the eqⁿ represent the same straight line in \mathbb{R}^2

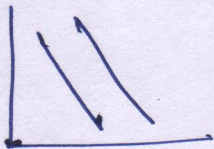
LHS = RHS ratio
 $\left(\frac{42}{42}, \frac{42}{42} \right)$



- no solⁿ $\Rightarrow (2x + y = 215) \times 2$

$$4x + 2y = 400$$

$$\underline{\underline{430 \neq 400}}$$



both the eqⁿ have parallel line

- unique solⁿ $\Rightarrow 2x + y = \text{sth} \dots$

$$3x + y = \text{sth} \dots$$

