

Matrices #L1.2

- Matrix - a rectangular array of nos, arranged in rows and columns.

ex, $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \end{bmatrix}$ $\xrightarrow{(1,2)^{\text{th}} \text{ entry}}$

2x3
matrix

(2 rows
and 3 columns)

- (m x n) matrix \Rightarrow m rows and n columns

- (i, j)th entry \Rightarrow ith row and jth column.

- ~~The diagonal of a~~ sq. matrix \Rightarrow no. of rows = no. of column

- The ith diagonal entry of the sq. matrix is the (i, i)th entry.

- The diagonal of a sq. matrix is a set of diagonal entries

- Diagonal matrix - sq. matrix in which all entries except the diagonal are 0.

- Scalar matrix - A diagonal matrix in which all the entries of the diagonal are same.

- Identity matrix (I) - Scalar matrix with all diagonal entries 1.

- A set of linear eqⁿ can be represented as matrices.

ex, $\begin{aligned} 3x + 4y &= 5 \\ 4x + 6y &= 10 \end{aligned}$

$$\left[\begin{array}{cc|c} 3 & 4 & 5 \\ 4 & 6 & 10 \end{array} \right]$$

ex, $\begin{bmatrix} 1 & 9 \\ 0.6 & 7 \\ 4 & 1.5 \end{bmatrix}_{3 \times 2} + \begin{bmatrix} 0 & 7 \\ 0.6 & 7 \\ 2.5 & 0.6 \end{bmatrix}_{3 \times 2} = \begin{bmatrix} 1 & 16 \\ 1.2 & 14 \\ 6.5 & 2.1 \end{bmatrix}_{3 \times 2}$

- $(A+B)_{ij} = A_{ij} + B_{ij}$

ex, $3 \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} = \begin{bmatrix} 3 & 6 & 9 \\ 12 & 15 & 18 \end{bmatrix}$ Scalar Multiplication

- $(cA)_{ij} = c(A_{ij})$

$$\text{ex, } \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2} \begin{bmatrix} 1 & 2 & 3 \\ 3 & 4 & 5 \end{bmatrix}_{2 \times 3} = \begin{bmatrix} 7 & 10 & 13 \\ 15 & 22 & 29 \end{bmatrix}_{2 \times 3}$$

$$\text{ex, } \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2} \times \begin{bmatrix} 5 \\ 6 \end{bmatrix}_{2 \times 1} = \begin{bmatrix} 17 \\ 39 \end{bmatrix}_{2 \times 1} \quad \text{Matrix Multiplication}$$

* The no. of columns in first matrix should be same as the no. of rows in second matrix.

$$\left. \begin{aligned} A_{m \times n} B_{n \times p} &= (AB)_{m \times p} \\ (AB)_{ij} &= \sum_{k=1}^n A_{ik} B_{kj} \end{aligned} \right\} \text{Matrix Multiplication}$$

$$- \begin{bmatrix} c & 0 & 0 \\ 0 & c & 0 \\ 0 & 0 & c \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix} = \begin{bmatrix} c & 2c \\ 3c & 4c \\ 5c & 6c \end{bmatrix} = c \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}$$

↳ multiplication of a spe (scalar/identity) matrix

$$\{ I A_{3 \times 3} = A_{3 \times 3} = A_{3 \times 3} I \} \rightarrow \text{Identity matrix acts as 1}$$

- $(A+B)+C = A+(B+C)$ Association of addⁿ
- $(AB)C = A(BC)$ Association of Multiplication
- $A+B = B+A$ Commutativity of addⁿ
- $AB \neq BA$ (both should make sense)
- $\lambda(A+B) = \lambda A + \lambda B$ λ is a scalar
- $\lambda(AB) = \lambda(A)B = \lambda A(B)$
- $A(B+C) = AB + AC$
- $(A+B)C = AC + BC$