

Homework5_hitenkothari

December 4, 2023

#ECE 4554 / ECE 5554 / Computer Vision This file contains the coding problems (Problems 3 and 4) for Homework 5. Your job is to implement/modify the sections within this notebook that are marked with “TO DO”.

##TO DO: Enter your Virginia Tech Username (PID) here: hitenkothari Do not write a student ID number. Your Username is normally part of your @vt.edu email address.

##Honor Code

Once again, please review the Honor Code statement in the syllabus. This is not a “team project”. *If you make use of code from ANY source except the instructor, you must provide comment lines in your programs to state where you obtained that code.* Failure to cite sources of code that you borrowed will be considered a violation of the Honor Code.

##Code libraries For all of these problems, you will be using the PyTorch library. The individual problems will let you know if you are not allowed to use particular PyTorch functions, and whether you are allowed to use functions from any other libraries. For example, parts of Problem 4 allow the use of cross-correlation/convolution Scipy library functions. Do not use other library functions without permission from the instructor.

You may re-use any code that *you* have written for previous assignments.

##Submission guidelines for the coding problems (Google Colab)

1. Please verify that you have entered your Virginia Tech Username in all of the appropriate places.
2. After your solutions are complete, click Runtime->“Restart and run all”; then verify that all of your solutions are visible in this notebook.
3. Click File->Save near the top of the page to save the latest version of your notebook at Google Drive.
4. Verify that the last 2 cells have executed, creating a PDF version of this notebook at Google Drive. (Note: if you face difficulty with this step, please refer to <https://pypi.org/project/notebook-as-pdf/>)
5. Look at the PDF file and check that all of your solutions are displayed correctly there.
6. Download your notebook file and the PDF version to your laptop.
7. If needed, change the file names to Homework5_USERNAME.ipynb and Homework5_Notebook_USERNAME.pdf, using your own Username. Don’t zip either of the files.
8. **Submit these 2 files along with your PDF file for Problems 1-3 SEPARATELY to Canvas.** Do not zip them all together.

##Overview

In this assignment, you will explore the use of Convolutional Neural Networks (CNNs) for object recognition.

Problem 3 provides a tutorial-type introduction to CNNs, along with a task that you need to solve using a network model that is provided to you.

Problem 4 asks you to implement part of a CNN (your own convolutional layer).

1 Problem 4: Using PyTorch to train simple CNN

This entire section is a walkthrough of how to use PyTorch for Machine Learning. After you read and run the code in this entire section, you will see what your task for Problem 4 is, but for now just go through this tutorial and take the time to learn what is going on.

PyTorch is a Machine Learning library that provides functionality for loading datasets and pre-trained neural-network models. It also provides the building blocks we need to be able to create our own convolutional neural network (CNN).

This problem will walk you through how PyTorch works through these steps: 1. Loads the CIFAR-10 dataset into a *training set* and a *test set* 2. Creates a SimpleCNN neural network 3. Trains the SimpleCNN network on the CIFAR-10 training data 4. Use the trained model to predict the classes of new images from the test set

This tutorial part of Problem 4 is adapted from PyTorch: https://pytorch.org/tutorials/beginner/blitz/cifar10_tutorial.html - Feel free to look at that tutorial's source too, but here we walk you through everything that they explain as well.

```
[ ]: %pip install torch torchvision torchsummary
```

```
Requirement already satisfied: torch in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(2.1.0)
Requirement already satisfied: torchvision in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(0.16.0)
Requirement already satisfied: torchsummary in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(1.5.1)
Requirement already satisfied: filelock in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torch) (3.13.1)
Requirement already satisfied: typing-extensions in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torch) (4.8.0)
Requirement already satisfied: sympy in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torch) (1.12)
Requirement already satisfied: networkx in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torch) (3.2.1)
```

Requirement already satisfied: jinja2 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torch) (3.1.2)

Requirement already satisfied: fsspec in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torch) (2023.10.0)

Requirement already satisfied: numpy in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torchvision) (1.25.2)

Requirement already satisfied: requests in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torchvision) (2.31.0)

Requirement already satisfied: pillow!=8.3.*,>=5.3.0 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from torchvision) (10.0.1)

Requirement already satisfied: MarkupSafe>=2.0 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from jinja2->torch) (2.1.3)

Requirement already satisfied: charset-normalizer<4,>=2 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from requests->torchvision) (3.3.2)

Requirement already satisfied: idna<4,>=2.5 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from requests->torchvision) (3.4)

Requirement already satisfied: urllib3<3,>=1.21.1 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from requests->torchvision) (2.0.7)

Requirement already satisfied: certifi>=2017.4.17 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from requests->torchvision) (2023.11.17)

Requirement already satisfied: mpmath>=0.19 in
/Library/Frameworks/Python.framework/Versions/3.10/lib/python3.10/site-packages
(from sympy->torch) (1.3.0)

Note: you may need to restart the kernel to use updated packages.

```
[1]: import numpy as np
import matplotlib.pyplot as plt
from tqdm import tqdm # For progress bar

# PyTorch imports
import torch
from torch import nn
from torch import optim
import torch.nn.functional as F
from torchvision import datasets, transforms, utils
from torch.utils.data import Dataset, Subset, DataLoader
from torchsummary import summary
```

```
[2]: # Mount your Google Drive to this notebook
# The purpose is to allow your code to access to your files
from google.colab import drive
drive.mount('/content/drive')

# Change the directory to your own working directory
# Your code will be able to read and write files in your working directory
# TO DO: enter the name of your directory
import os
os.chdir('/content/drive/My Drive/Colab Notebooks/HW5')
```

Mounted at /content/drive

1.1 Load data from CIFAR-10 Dataset

You can find more info on the CIFAR-10 dataset here: <https://www.cs.toronto.edu/~kriz/cifar.html> - 60,000 images that are 32x32, RGB - 60,000 total images have been partitioned into a training set of 50,000 and a test set of 10,000 - 10 classes: plane, car, bird, cat, deer, dog, frog, horse, ship, truck

Normalization of pixels: $\rho' = \frac{\rho - \mu}{\sigma}$ - Normalizing pixels to range [-1, 1] by using $\mu = 0.5$ and $\sigma = 0.5$ - Done in `transforms.Normalize` - Ensures all input images have same scale

Load data: - Load training data from CIFAR10 (`trainloader`) - Load test data from CIFAR10 (`testloader`) - Loads the data into a folder called `data` in your Google Drive folder

Batch: - A batch is the number of images the model will be trained on at a time before updating weights. In this case the batch size chosen was 4 (`batch_size` variable) - Batches help reduce training time, and keeping batches small will ensure the model is still accurately trained.

```
[ ]: transform = transforms.Compose(
    [transforms.ToTensor(),
     transforms.Normalize((0.5, 0.5, 0.5), (0.5, 0.5, 0.5))]
)

batch_size = 4

# This downloads the CIFAR10 dataset into Google Drive under a 'data' folder
trainset = datasets.CIFAR10(root='./data', train=True,
                             download=True, transform=transform)
trainloader = torch.utils.data.DataLoader(trainset, batch_size=batch_size,
                                           shuffle=True, num_workers=2)

testset = datasets.CIFAR10(root='./data', train=False,
                             download=True, transform=transform)
testloader = torch.utils.data.DataLoader(testset, batch_size=batch_size,
                                          shuffle=False, num_workers=2)

# The 10 classes/labels for the CIFAR10 dataset
```

```
classes = ('plane', 'car', 'bird', 'cat',
           'deer', 'dog', 'frog', 'horse', 'ship', 'truck')
```

Files already downloaded and verified

Files already downloaded and verified

1.2 Visualize images from CIFAR10

Unnormalize pixels: $\rho = \rho' \sigma + \mu$

This shows a random batch (4 images) from the training data along with their class labels

`images` variable is a tensor of shape (4, 3, 32, 32) - Tensors are the same concept as NumPy arrays; they are n-dimensional structures - First axis: 4 is the number of images in our batch - Second axis: 3 is the number of channels in each image (RGB) - Third and fourth axes: Images are 32x32

`labels` is a list of integers corresponding to the index of the label for each image in the batch (4) - So if the label for an image is `i`, we can use `classes[i]` to obtain the actual class name (plane, car, bird, ...)

```
[ ]: def imshow(img):
    # Unnormalize pixels
    img = img / 2 + 0.5
    npimg = img.numpy()
    # Put image into shape (32, 32, 3) to display
    plt.imshow(np.transpose(npimg, (1, 2, 0)))
    plt.show()

# Get random training image batch
dataiter = iter(trainloader)
images, labels = next(dataiter)

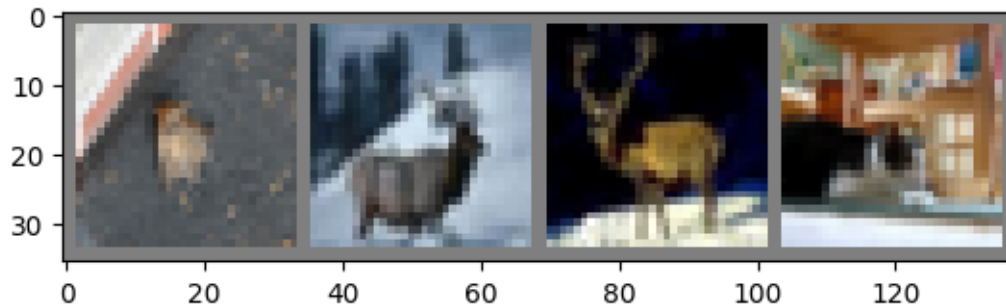
print(f'Images data shape: {images.shape}')
print(f'Label raw data: {labels}\n')

# Show images
print("Example of training set batch:")
imshow(utils.make_grid(images))
# Print labels
print('Actual Labels: ', '\t'.join(f'{classes[labels[j]]:5s}' for j in
    ↪range(batch_size)))
```

Images data shape: torch.Size([4, 3, 32, 32])

Label raw data: tensor([3, 4, 4, 3])

Example of training set batch:



Actual Labels: cat deer deer cat

1.3 SimpleCNN Neural Network

The `SimpleCNN` class is a Convolutional Neural Network that is defined in PyTorch. It inherits from the `nn.Module` class.

The `__init__` function for `SimpleCNN` defines the layers that the network is going to use. The `forward` function defines how to connect the layers, and for a particular input returns the predicted output.

Here is a graphic of what this Convolutional Neural Network looks like. (Notice that the input image shown here is not from CIFAR10).

Here is a summary of the layers (from input to output) that this CNN consists of:

Layer 1: Convolutional layer (`self.conv1`) - Input: 32x32x3 (RGB) image - Performs convolution with 6 kernels (`out_channels` parameter) of size 5x5 - Output: 28x28x6 convolution output

Layer 2: Max pooling layer (`self.pool`) - Input: 28x28x6 output from layer 1 - Subsamples each of the 6 results by taking the max element in 2x2 windows - Output: 14x14x6 subsampled output

Layer 3: Convolutional layer (`self.conv2`) - Input: 14x14x6 output from layer 2 - Performs convolution with 16 kernels (`out_channels` parameter) of size 5x5 - Output: 10x10x16 convolution output

Layer 4: Max pooling layer (`self.pool`) - Input: 10x10x16 output from layer 3 - Output: 5x5x16 subsampled output

Linear/Fully-connected layers: - The diagram above shows 2 fully connected (FC) layers (`n1` and `n2`), but the code contains 3 as described here. - `self.fc1` takes all 5x5x16 (400) pixels as input nodes and maps them to 120 output nodes - `self.fc2` takes the 120 nodes as input and maps them to 84 output nodes - Lastly, `self.fc3` takes the 84 nodes as input and outputs the final 10 nodes corresponding to each class/label for CIFAR10

```
[ ]: # Don't change the code in this block
```

```

class SimpleCNN(nn.Module):
    '''Simple CNN neural network. See above description for what each layer_
    ↪ does.'''

    def __init__(self):
        '''Defines each layer for SimpleCNN.'''
        super().__init__()
        self.conv1 = nn.Conv2d(in_channels=3, out_channels=6, kernel_size=5)
        self.pool = nn.MaxPool2d(kernel_size=2, stride=2)
        self.conv2 = nn.Conv2d(in_channels=6, out_channels=16, kernel_size=5)
        self.fc1 = nn.Linear(in_features=16 * 5 * 5, out_features=120)
        self.fc2 = nn.Linear(in_features=120, out_features=84)
        self.fc3 = nn.Linear(in_features=84, out_features=10)

    def forward(self, x):
        '''Defines graph of connections for each layer in SimpleCNN.'''
        x = self.pool(F.relu(self.conv1(x)))
        x = self.pool(F.relu(self.conv2(x)))
        x = torch.flatten(x, 1) # flatten all dimensions except batch
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x

```

1.4 Loss Function and Gradient Descent

Here is more information about the implementation details. Most if this is background, as far as these Colab problems are concerned.

First, we attempt to use our computer's GPUs if we have any available. On free Google Colab instances, they won't be available, but if you are running this locally with an NVIDIA GPU, you should be able to enable CUDA to run and train the model on your GPU (although this is not necessary).

While this is almost necessary for most larger networks, our network is fairly simple and only takes 32x32 images as input, so training won't take too long on just a CPU.

Loss Function: The cross-entropy loss will be our loss function. The loss function is a function we want to minimize. Cross-entropy is a popular loss function for multi-class classification (we have 10 classes).

$$L = -\sum_i (t_i * \log(p_i))$$

- The summation is going through each label (i) (plane, car, bird, ...).
- t_i is the actual ground truth label we want our model to predict (it is equal to 1 for the true label, 0 for the other 9).
- p_i is the predicted probability for each label from our model.
- Think of all the p_i values as representing a probability distribution. This loss function will approach 0 when the computed distribution is about the same as the given set of t_i values; and this loss function will be high when the computed distribution is wrong.
- More info on cross entropy loss can be found in section 5.1.3 of the textbook and also at this site: <https://www.v7labs.com/blog/cross-entropy-loss-guide>

Gradient Descent: This is the algorithm that updates the weights of our model, based on computing the gradient of L with respect to the weights. We are using SGD (stochastic gradient descent), which just means that we update the weights after each batch. (This example will use a batch size of 4 images).

$$\mathbf{W}_{t+1} = \mathbf{W}_t - \alpha \nabla L$$

- is the set of all of the weights in our model, which we are updating by using this equation. - is the learning rate. A higher number will update our weight more substantially each iteration, while a lower number will update them more slowly ($\text{lr} = 0.001$ in this code).

```
[ ]: device = "cuda" if torch.cuda.is_available() else "cpu" # Use GPU if possible
print(device)
simple_model = SimpleCNN().to(device)
summary(simple_model, input_size=(3, 32, 32))

criterion = nn.CrossEntropyLoss()
optimizer = optim.SGD(simple_model.parameters(), lr=0.001, momentum=0.9)
```

cpu

```
-----
              Layer (type)              Output Shape          Param #
=====
              Conv2d-1              [-1, 6, 28, 28]          456
              MaxPool2d-2            [-1, 6, 14, 14]           0
              Conv2d-3              [-1, 16, 10, 10]         2,416
              MaxPool2d-4            [-1, 16, 5, 5]           0
              Linear-5                [-1, 120]                48,120
              Linear-6                [-1, 84]                 10,164
              Linear-7                [-1, 10]                  850
=====
Total params: 62,006
Trainable params: 62,006
Non-trainable params: 0
-----
Input size (MB): 0.01
Forward/backward pass size (MB): 0.06
Params size (MB): 0.24
Estimated Total Size (MB): 0.31
-----
```

1.5 Training

This is the training loop for the network to actually learn the weights. This loop updates the weights by trying to minimize the loss function, which is eventually computed for all of the training images.

The training loop runs for a defined number of epochs, which is the number of times the model is trained on the entire set of training data (`trainloader`). The data is shuffled between each epoch.

Since we have set everything up, PyTorch does almost everything for us in this step. Here is what it does:

Steps: 1. Gets the input images and labels for the current batch (4 images at a time) 2. Gives the model the images, and it will predict the output labels 3. Calculates the loss function between ground truth and predicted labels 4. Calculates all gradients for backpropagation (`loss.backward()`) 5. Performs gradient descent to update the model weights (`optimizer.step()`) 6. Repeats on all images in the training set (50,000 images / 4 per batch = 12,500 iterations) 7. Repeats this for each epoch

```
[ ]: # Don't change the code in this block

def train(model, loader, criterion, optimizer, epochs=2):
    '''Train a model from training data.

    Args:
    - model: Neural network to train
    - epochs: Number of epochs to train the model
    - loader: Dataloader to train the model with
    '''
    print('Start Training')

    for epoch in range(epochs): # loop over the dataset multiple times

        running_loss = 0.0
        total = 0
        correct = 0
        for i, data in enumerate(tqdm(loader)):
            # get the inputs; data is a list of [inputs, labels]
            inputs, labels = data

            # zero the parameter gradients
            optimizer.zero_grad()

            # forward + backward + optimize
            outputs = model(inputs)
            loss = criterion(outputs, labels)
            loss.backward()
            optimizer.step()

            # the class with the highest energy is what we choose as prediction
            _, predicted = torch.max(outputs.data, 1)
            total += labels.size(0)
            correct += (predicted == labels).sum().item()

            # print statistics
            running_loss += loss.item()
            if i % 2000 == 1999: # print every 2000 mini-batches
```

```

        print(f'[epoch {epoch + 1}, batch {i + 1:5d}] loss: {running_loss_
↪ / 2000:.3f}')
        running_loss = 0.0

        print(f'\nAccuracy of the network on last 2000 training images:␣
↪ {100 * correct // total} %')
        total = 0
        correct = 0

    print('\nFinished Training')

```

1.5.1 This will train our SimpleCNN.

- This will take some time, so be patient.
- It will train the SimpleCNN for 2 epochs, and will print out the average loss and the training accuracy for every 2000 batches.
- Notice that every 2000 batches, the loss decreases and the training accuracy improves, this is how to tell if a model is correctly learning and improving throughout training.

```

[ ]: # Train model on training data from CIFAR10
    train(simple_model, trainloader, criterion, optimizer)

```

Start Training

```
16%|          | 2054/12500 [00:13<00:22, 469.17it/s]
```

```
[epoch 1, batch 2000] loss: 2.223
```

Accuracy of the network on last 2000 training images: 16 %

```
33%|          | 4094/12500 [00:17<00:16, 508.08it/s]
```

```
[epoch 1, batch 4000] loss: 1.901
```

Accuracy of the network on last 2000 training images: 31 %

```
49%|          | 6077/12500 [00:21<00:12, 525.56it/s]
```

```
[epoch 1, batch 6000] loss: 1.707
```

Accuracy of the network on last 2000 training images: 36 %

```
64%|          | 8015/12500 [00:30<01:00, 74.50it/s]
```

```
[epoch 1, batch 8000] loss: 1.588
```

Accuracy of the network on last 2000 training images: 41 %

```
81%|          | 10069/12500 [00:42<00:06, 356.61it/s]
```

```

[epoch 1, batch 10000] loss: 1.542

Accuracy of the network on last 2000 training images: 44 %
 96%|      | 12045/12500 [00:48<00:01, 363.92it/s]

[epoch 1, batch 12000] loss: 1.463

Accuracy of the network on last 2000 training images: 46 %
100%|      | 12500/12500 [00:59<00:00, 209.78it/s]
 16%|      | 2056/12500 [00:10<00:25, 413.85it/s]

[epoch 2, batch 2000] loss: 1.386

Accuracy of the network on last 2000 training images: 49 %
 33%|      | 4069/12500 [00:15<00:20, 416.57it/s]

[epoch 2, batch 4000] loss: 1.363

Accuracy of the network on last 2000 training images: 51 %
 49%|      | 6076/12500 [00:20<00:15, 405.80it/s]

[epoch 2, batch 6000] loss: 1.323

Accuracy of the network on last 2000 training images: 52 %
 65%|      | 8074/12500 [00:25<00:10, 413.07it/s]

[epoch 2, batch 8000] loss: 1.282

Accuracy of the network on last 2000 training images: 54 %
 80%|      | 10050/12500 [00:30<00:05, 413.20it/s]

[epoch 2, batch 10000] loss: 1.281

Accuracy of the network on last 2000 training images: 54 %
 97%|      | 12064/12500 [00:35<00:01, 418.34it/s]

[epoch 2, batch 12000] loss: 1.257

Accuracy of the network on last 2000 training images: 55 %
100%|      | 12500/12500 [00:46<00:00, 268.95it/s]

Finished Training

```

1.6 View CNN Prediction

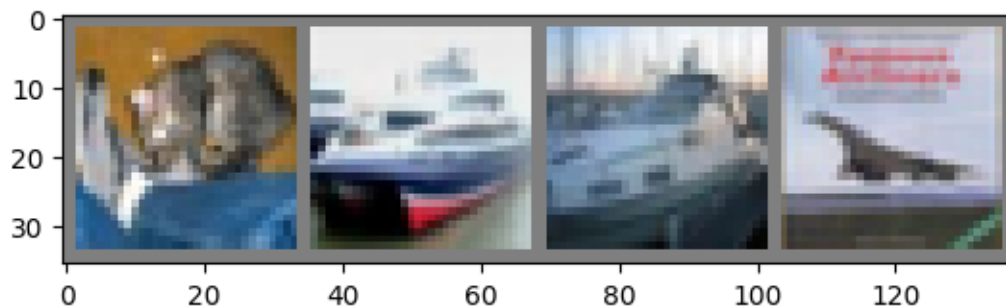
Here is an example of 4 images with their ground truth labels and with the predictions from our CNN model

```
[ ]: dataiter = iter(testloader)
      images, labels = next(dataiter)

      # print images from test set
      imshow(utils.make_grid(images))
      print('Ground Truth: ', '\t'.join(f'{classes[labels[j]]:5s}' for j in
      ↪range(4)))

      # Input images into model and see ouptut
      outputs = simple_model(images)
      _, predicted = torch.max(outputs, 1)

      print('CNN prediction: ', '\t'.join(f'{classes[predicted[j]]:5s}' for j in
      ↪range(4)))
```



Ground Truth:	cat	ship	ship	plane
CNN prediction:	ship	ship	ship	plane

1.7 Testing our SimpleCNN Model

Now we will run our model on the test dataset (`testloader`) from CIFAR10. The model was not trained on this data, so we can measure the accuracy of our model (# correct / total) on this test set. The test dataset contains 10,000 images, which will be 2500 batches for us.

```
[ ]: # Don't change the code in this block

def evaluation(model, loader):
    '''Evaluate a model and output its accuracy on a test dataset.

    Args:
        - model: Neural network to evaluate
```

```

    - loader: Dataloader containing test dataset
'''
# Evaluate accuracy on validation / test set
correct = 0
total = 0
# since we're not training, we don't need to calculate the gradients for our
↳ outputs
with torch.no_grad():
    for data in tqdm(loader):
        images, labels = data
        # calculate outputs by running images through the network
        outputs = model(images)
        # the class with the highest energy is what we choose as prediction
        _, predicted = torch.max(outputs.data, 1)
        total += labels.size(0)
        correct += (predicted == labels).sum().item()

print(f'\nAccuracy of the network on the 10000 test images: {100 * correct //
↳ total} %')
```

1.7.1 Evaluate SimpleCNN

After running below, you'll see that the accuracy is much better than a random guess (which would be 10% since there are 10 classes), but it is still not perfect. (We got around 50% when running it).

This example shows the tradeoffs that are made when doing Machine Learning. Our model is simple and the input images are only 32x32x3, so the model trains fast and does not have many weights, but the accuracy is not amazing because of these choices. Typically, more complex models with more weights require GPUs to run, so this model was kept simple to avoid that need. However, later in this problem you will improve this network and increase the accuracy.

```
[ ]: # Evaluate trained model on test dataset
evaluation(simple_model, testloader)
```

```
100%|          | 2500/2500 [00:16<00:00, 152.85it/s]
```

```
Accuracy of the network on the 10000 test images: 56 %
```

Save trained model so it can be loaded everytime you restart this Notebook, so you don't need to re-train it if you don't want to. Only run the cell below if your model was previously trained.

This step is optional, but useful if you plan to come back to this notebook and want to load your trained model without training it again.

```
[ ]: # UNCOMMENT below if you want to save your trained model after training
```

```
# (only do this after your model finished training, so you can use it later if
↳desired)
#
↳-----

# SIMPLECNN_MODEL_PATH = './simplecnn_model.pth'
# torch.save(simple_model.state_dict(), SIMPLECNN_MODEL_PATH)
```

Load saved model from before. Once again, this is optional.

```
[ ]: # UNCOMMENT below if you want to load your saved trained model from before
# (only need to do this if you come back to this notebook and don't want to
↳re-train the model again above)
#
↳-----

# simple_model = SimpleCNN().to(device)
# simple_model.load_state_dict(torch.load(SIMPLECNN_MODEL_PATH))
```

```
[ ]: <All keys matched successfully>
```

1.8 View SimpleCNN in Action

Run this cell as many times as you want to show a random batch from the test set, the model's predicted class, and the real class

```
[ ]: # Random number between 1 and size of test set (9995 + batch_size (4))
random_idx = np.random.randint(9995)

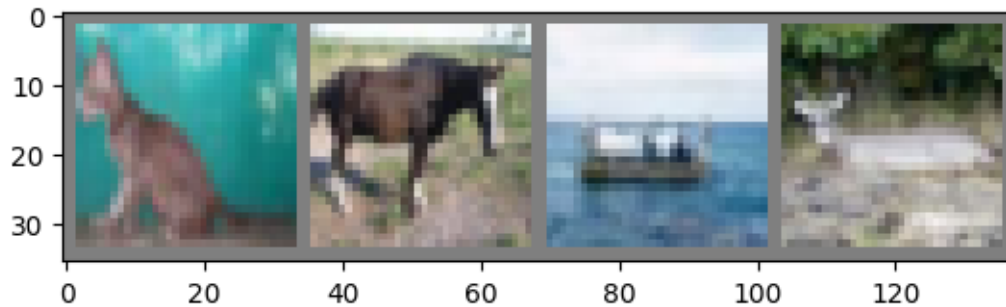
images = []
labels = []
for i in range(random_idx, random_idx + batch_size):
    image, label = testset[i]
    images.append(image)
    labels.append(label)

image_tensors = torch.stack(images)

# print images from test set
imshow(utils.make_grid(image_tensors))
print('Ground Truth: ', '\t'.join(f'{classes[labels[j]]:5s}' for j in
↳range(4)))

# Input images into model and see ouptut
outputs = simple_model(image_tensors)
_, predicted = torch.max(outputs, 1)
```

```
print('CNN prediction: ', '\t'.join(f'{classes[predicted[j]]:5s}' for j in
↪range(4)))
```



Ground Truth:	cat	horse	ship	deer
CNN prediction:	deer	horse	ship	deer

2 TO DO (Problem 3): Change hyperparameters from the preceeding code

2.1 Create ChangedSimpleCNN

Now that you've gone through a walkthrough of the code above, your goal for this problem is to change the code above to increase the accuracy of the above model to **at least 70%**. You will do this by changing anything about the SimpleCNN network model. Here are some recommendations of parameters to change: - Add layers (more layers means more parameters to learn) - Change existing Conv2d layer parameters: - Kernel size - Padding - Number of kernels (out_channels) - Increasing the number of kernels used in the Conv2d layer can also give the model more learning possibilities - Remove or replace any layers (if desired) - You are welcome to use other built-in PyTorch `nn` layers or activation functions if you are comfortable with them

Don't change the SimpleCNN model above, instead change the code below, and then re-train and re-evaluate your new network called `ChangedSimpleCNN`

`nn.Conv2d` class API: <https://pytorch.org/docs/master/generated/torch.nn.Conv2d.html#torch.nn.Conv2d>

Problem 4 will require you to understand the Conv2d layer in more detail, so if you need more context for this problem, it can be useful to learn about it for that problem and then come back to this one.

```
[ ]: # TO DO: Change below neural network to achieve expected accuracy
```

```
class ChangedSimpleCNN(nn.Module):
    '''Make any changes to achieve the expected accuracy.

    Feel free to change the CNN layers to achieve higher accuracy
    Convolutional layer: nn.Conv2d
```

```

    Max pooling layer: nn.MaxPool2d
    Linear classifier layer: nn.Linear
'''

# Changed the depth size and feature size to increase the number of hyper-
↳ parameters, trial-and-error different models, this worked best

def __init__(self):
    '''Make any changes to layers from SimpleCNN.'''
    super().__init__()
    self.conv1 = nn.Conv2d(in_channels=3, out_channels=64,
↳ kernel_size=3, padding=1)
    self.pool = nn.MaxPool2d(kernel_size=2, stride=2)
    self.conv2 = nn.Conv2d(in_channels=64, out_channels=128,
↳ kernel_size=3, padding=1)
    self.fc1 = nn.Linear(in_features=128 * 8 * 8, out_features=512)
    self.fc2 = nn.Linear(in_features=512, out_features=10)

def forward(self, x):
    '''Make any changes to layer connections from SimpleCNN.'''
    x = self.pool(F.relu(self.conv1(x)))
    x = self.pool(F.relu(self.conv2(x)))
    x = torch.flatten(x, 1) # flatten all dimensions except batch
    x = F.relu(self.fc1(x))
    x = self.fc2(x)
    return x

```

2.1.1 You may also change the marked hyperparameters below, including:

- Learning rate (lr parameter in the optimizer)
 - Lower number means more gradual steps, higher number means faster, larger steps
- Epochs (epochs variable)
 - This is the number of times the model is trained on the training data (shuffled).
 - Higher number means more training time but will take longer
 - Keep number of epochs to 10 or below

```

[ ]: changed_model = ChangedSimpleCNN().to(device)
summary(changed_model, input_size=(3, 32, 32))

# Do not change loss function
criterion = nn.CrossEntropyLoss()
# Do not change optimizer type (optim.SGD)
# You CAN change the learning rate (lr) if desired
optimizer = optim.SGD(changed_model.parameters(), lr=0.001, momentum=0.9)

```

Layer (type)	Output Shape	Param #
--------------	--------------	---------


```

=====
      Conv2d-1          [-1, 64, 32, 32]          1,792
    MaxPool2d-2        [-1, 64, 16, 16]           0
      Conv2d-3          [-1, 128, 16, 16]        73,856
    MaxPool2d-4        [-1, 128, 8, 8]           0
      Linear-5           [-1, 512]        4,194,816
      Linear-6           [-1, 10]         5,130
=====
Total params: 4,275,594
Trainable params: 4,275,594
Non-trainable params: 0
-----
Input size (MB): 0.01
Forward/backward pass size (MB): 0.94
Params size (MB): 16.31
Estimated Total Size (MB): 17.26
-----

```

2.1.2 Train ChangedSimpleCNN

```

[ ]: # Can change number of epochs, but keep it at 10 or below
epochs = 7
train(changed_model, trainloader, criterion, optimizer, epochs=epochs)

```

Start Training

```

16%|          | 2005/12500 [00:40<04:29, 38.93it/s]
[epoch 1, batch 2000] loss: 1.853

Accuracy of the network on last 2000 training images: 32 %
32%|          | 4003/12500 [01:23<04:36, 30.68it/s]
[epoch 1, batch 4000] loss: 1.479

Accuracy of the network on last 2000 training images: 46 %
48%|          | 6008/12500 [01:59<01:36, 67.51it/s]
[epoch 1, batch 6000] loss: 1.342

Accuracy of the network on last 2000 training images: 51 %
64%|          | 8011/12500 [02:29<01:07, 66.48it/s]
[epoch 1, batch 8000] loss: 1.243

Accuracy of the network on last 2000 training images: 55 %
80%|          | 10006/12500 [03:00<00:38, 64.83it/s]

```

[epoch 1, batch 10000] loss: 1.159

Accuracy of the network on last 2000 training images: 58 %
 96%| | 12008/12500 [03:30<00:07, 66.59it/s]

[epoch 1, batch 12000] loss: 1.099

Accuracy of the network on last 2000 training images: 60 %
 100%| | 12500/12500 [03:48<00:00, 54.81it/s]
 16%| | 2007/12500 [00:35<02:34, 67.95it/s]

[epoch 2, batch 2000] loss: 0.976

Accuracy of the network on last 2000 training images: 65 %
 32%| | 4007/12500 [01:05<02:09, 65.35it/s]

[epoch 2, batch 4000] loss: 0.962

Accuracy of the network on last 2000 training images: 65 %
 48%| | 6010/12500 [01:35<01:36, 66.99it/s]

[epoch 2, batch 6000] loss: 0.917

Accuracy of the network on last 2000 training images: 68 %
 64%| | 8010/12500 [02:06<01:07, 66.77it/s]

[epoch 2, batch 8000] loss: 0.901

Accuracy of the network on last 2000 training images: 68 %
 80%| | 10012/12500 [02:36<00:36, 67.33it/s]

[epoch 2, batch 10000] loss: 0.872

Accuracy of the network on last 2000 training images: 69 %
 96%| | 12010/12500 [03:09<00:08, 57.31it/s]

[epoch 2, batch 12000] loss: 0.846

Accuracy of the network on last 2000 training images: 70 %
 100%| | 12500/12500 [03:28<00:00, 60.09it/s]
 16%| | 2012/12500 [00:35<02:33, 68.35it/s]

[epoch 3, batch 2000] loss: 0.705

Accuracy of the network on last 2000 training images: 75 %
 32%| | 4006/12500 [01:12<02:18, 61.35it/s]

[epoch 3, batch 4000] loss: 0.684

Accuracy of the network on last 2000 training images: 75 %
 48%| | 6013/12500 [01:42<01:35, 68.21it/s]

[epoch 3, batch 6000] loss: 0.699

Accuracy of the network on last 2000 training images: 75 %
 64%| | 8007/12500 [02:11<01:06, 67.74it/s]

[epoch 3, batch 8000] loss: 0.684

Accuracy of the network on last 2000 training images: 76 %
 80%| | 10007/12500 [02:41<00:36, 68.33it/s]

[epoch 3, batch 10000] loss: 0.704

Accuracy of the network on last 2000 training images: 75 %
 96%| | 12012/12500 [03:11<00:07, 68.34it/s]

[epoch 3, batch 12000] loss: 0.688

Accuracy of the network on last 2000 training images: 76 %
 100%| | 12500/12500 [03:28<00:00, 59.94it/s]
 16%| | 2008/12500 [00:42<02:34, 67.76it/s]

[epoch 4, batch 2000] loss: 0.490

Accuracy of the network on last 2000 training images: 82 %
 32%| | 4011/12500 [01:16<02:27, 57.46it/s]

[epoch 4, batch 4000] loss: 0.502

Accuracy of the network on last 2000 training images: 82 %
 48%| | 6007/12500 [01:52<01:34, 68.64it/s]

[epoch 4, batch 6000] loss: 0.483

Accuracy of the network on last 2000 training images: 83 %
 64%| | 8008/12500 [02:22<01:05, 68.21it/s]

[epoch 4, batch 8000] loss: 0.507

Accuracy of the network on last 2000 training images: 81 %
 80%| | 10013/12500 [02:53<00:39, 63.25it/s]

[epoch 4, batch 10000] loss: 0.516

Accuracy of the network on last 2000 training images: 82 %
 96%| | 12009/12500 [03:33<00:08, 55.13it/s]

[epoch 4, batch 12000] loss: 0.508

Accuracy of the network on last 2000 training images: 82 %
 100%| | 12500/12500 [03:50<00:00, 54.15it/s]
 16%| | 2006/12500 [00:36<02:43, 64.33it/s]

[epoch 5, batch 2000] loss: 0.292

Accuracy of the network on last 2000 training images: 89 %
 32%| | 4008/12500 [01:07<02:11, 64.60it/s]

[epoch 5, batch 4000] loss: 0.304

Accuracy of the network on last 2000 training images: 89 %
 48%| | 6010/12500 [01:37<01:40, 64.45it/s]

[epoch 5, batch 6000] loss: 0.324

Accuracy of the network on last 2000 training images: 88 %
 64%| | 8009/12500 [02:08<01:09, 65.04it/s]

[epoch 5, batch 8000] loss: 0.347

Accuracy of the network on last 2000 training images: 87 %
 80%| | 10011/12500 [02:38<00:38, 64.48it/s]

[epoch 5, batch 10000] loss: 0.331

Accuracy of the network on last 2000 training images: 88 %
 96%| | 12013/12500 [03:09<00:07, 66.02it/s]

[epoch 5, batch 12000] loss: 0.371

Accuracy of the network on last 2000 training images: 87 %
 100%| | 12500/12500 [03:26<00:00, 60.52it/s]
 16%| | 2009/12500 [00:35<02:37, 66.57it/s]

[epoch 6, batch 2000] loss: 0.157

Accuracy of the network on last 2000 training images: 95 %
 32%| | 4010/12500 [01:08<02:05, 67.55it/s]

[epoch 6, batch 4000] loss: 0.159

Accuracy of the network on last 2000 training images: 94 %
48%| | 6011/12500 [01:40<01:35, 68.12it/s]

[epoch 6, batch 6000] loss: 0.175

Accuracy of the network on last 2000 training images: 94 %
64%| | 8007/12500 [02:10<01:06, 67.71it/s]

[epoch 6, batch 8000] loss: 0.185

Accuracy of the network on last 2000 training images: 93 %
80%| | 10007/12500 [02:40<00:41, 60.40it/s]

[epoch 6, batch 10000] loss: 0.199

Accuracy of the network on last 2000 training images: 93 %
96%| | 12011/12500 [03:09<00:07, 67.46it/s]

[epoch 6, batch 12000] loss: 0.216

Accuracy of the network on last 2000 training images: 92 %
100%| | 12500/12500 [03:27<00:00, 60.27it/s]
16%| | 2011/12500 [00:35<02:33, 68.15it/s]

[epoch 7, batch 2000] loss: 0.073

Accuracy of the network on last 2000 training images: 98 %
32%| | 4007/12500 [01:04<02:02, 69.25it/s]

[epoch 7, batch 4000] loss: 0.078

Accuracy of the network on last 2000 training images: 97 %
48%| | 6008/12500 [01:34<01:37, 66.40it/s]

[epoch 7, batch 6000] loss: 0.102

Accuracy of the network on last 2000 training images: 96 %
64%| | 8011/12500 [02:05<01:07, 66.87it/s]

[epoch 7, batch 8000] loss: 0.115

Accuracy of the network on last 2000 training images: 96 %
80%| | 10013/12500 [02:35<00:37, 66.91it/s]

```
[epoch 7, batch 10000] loss: 0.107
```

Accuracy of the network on last 2000 training images: 96 %

```
96%|      | 12008/12500 [03:05<00:07, 66.73it/s]
```

```
[epoch 7, batch 12000] loss: 0.131
```

Accuracy of the network on last 2000 training images: 95 %

```
100%|     | 12500/12500 [03:22<00:00, 61.65it/s]
```

Finished Training

2.1.3 Evaluate ChangedSimpleCNN

```
[ ]: # Try to achieve accuracy >=70% for this problem on the test set
     evaluation(changed_model, testloader)
```

```
100%|     | 2500/2500 [00:26<00:00, 95.61it/s]
```

Accuracy of the network on the 10000 test images: 75 %

Changes Made: Epoch = 7 and Layers

Time to train this model ~ 24 min 52s on Macbook M1 Air

Accuracy on Training Set: 95%

Accuracy on Testing Set: 75%

3 Problem 4: Implement Convolutional Layer Yourself

3.1 Implement Custom Conv2d Layer

In the previous problem, we used PyTorch's built-in `nn.Conv2d` layer, which is called the Convolutional Layer (Conv2d layer), and is the backbone of a CNN.

In this problem, you will make the Conv2d layer yourself.

###Conv2d Quick Overview: - In short, the Conv2d layer performs convolution as you have learned in this course, but with several sets of kernels. - As we train the network, it will learn what values to use in each kernel to correctly classify the images. - Thus, the network essentially learns which filters work best (such as edge detectors) instead of us having to hand-pick them.

In order to implement the Conv2d layer yourself, you will need to understand how this layer works in-depth, and familiarize yourself with the size of the inputs and outputs of the layer.

For an in-depth breakdown of CNNs, see section 5.4 of the textbook, or skip to the Convolutional Layer section at this site: <https://cs231n.github.io/convolutional-networks/> - This resource

mentions padding (P) and stride (S), but we will simplify our layer and not worry about these parameters.

To simplify parts of it, your Conv2d layer will only use stride 1 ($S = 1$, normal convolution) and no padding ($P = 0$).

###Conv2d Breakdown: Note: *The rest of this notebook uses this notation, so you will most likely reference this a lot.* - Input (shape $B * N * H_1 * W_1$): - B : Batch size (number of images in this input) - N : Number of channels (depth) in input - W_1 : Width of input image - H_1 : Height of input image - Kernels: - F : Kernel size, such that kernel width and height is $F * F$ - Output (shape $B * D * H_2 * W_2$): - B : Batch size (need an output for each image in the batch) - D : Number of channels (depth) for output - This is equal to the number of kernels that will be convolved with the inputs - $W_2 = (W_1 - F) + 1$ - Width of output image - Since we have square images, $H_2 = W_2$

3.1.1 In the code below, you will implement the forward function for a Conv2d layer.

Read how Conv2d layer does forward pass: <https://pytorch.org/docs/master/generated/torch.nn.Conv2d.html#torch.nn.Conv2d>

Forward pass for convolutional layer:

$$Y_i = B_i + \sum_{j=1}^N X_j \star K_{ij} \text{ for } i = 1 \dots D \quad (1)$$

In above equation: - Y_i : Output image at output depth i - X_j : Input image at input depth j - K_{ij} : Kernel for output depth i and input depth j - B_i : Bias for output depth i - \star operator: Valid cross-correlation - See ‘valid’ mode: <https://docs.scipy.org/doc/scipy/reference/generated/scipy.signal.correlate2d.html>

Hints: - You are allowed use cross-correlation library functions such as `scipy.signal.correlate2d`, which are optimized, instead of doing it by hand, but do NOT use any PyTorch built-in convolution functions, such as `Conv2d`. If you implement the convolutions by hand, we recommend not to use loops as the training time will take too long. - It can be useful to look at the cell after this to see what inputs will be given to this function for testing.

- Your implementation here will heavily determine the **speed** of training this model. If you want to implement convolution by hand it can be done with linear algebra techniques to vectorize and use no loops in this function, which is ideal but can be tricky (this is not required). Our **forward** implementation did use some for loops, and the model took about 1 hour to fully train. - You will be working with PyTorch tensors to implement this problem. Treat these as you treat NumPy ndarray, as they are largely the same with the same functions - For example, to create a PyTorch tensor of all zeros with shape (2, 2, 3): `torch.zeros(2, 2, 3)` - For functions that output NumPy arrays, you can use `torch.from_numpy(...)` to convert it to a PyTorch tensor.

```
[ ]: # TO DO: implement the 'forward' function

from scipy import signal

class MyConv2dForward(torch.autograd.Function):
    '''Convolutional Layer from Scratch to replace nn.Conv2d.'''

    @staticmethod
```

```
def forward(x, kernels, bias):
    '''Forward pass of convolutional layer.

    Convolves each input image (along depth dimension) with a different kernel.

    (Most of this information is also in text cells above)
    Args:
        - x: Input tensor (of shape B*N*H1*W1)
          - B: batch size
          - N: depth of input (from `self.in_channels`)
          - H1: height of each image
          - W1: width of each image

        - kernels: Kernels (of shape F*F*N*D)
          - F: kernel size
          - N (same as above, depth of input)
          - D (same as below, depth of output)

        - bias: Bias (of shape D*H2*W2)
          - D (same as below, depth of output)
          - H2 (same as below, height of output)
          - W2 (same as below, width of output)

    Output:
        - Tensor (of shape B*D*H2*W2)
          - B: batch size
          - D: depth of input (from `self.out_channels`)
          - H2: height of output
          - W2: width of output

        - W2 and H2 are calculated using:  $(W - F) + 1$ 
          - Where  $W$  = width of input image;  $F$  = kernel size (from `self.
↪kernel_size`)
          - Assuming width ( $W$ ) and height ( $H$ ) of input images are the same
            (they are in this notebook)

        - For example:
          - For a 32x32x3 input ( $W = 32$ ,  $H = 32$ ,  $N = 3$ ), and  $F = 5$  (5x5 kernels):
             $W2$  and  $H2$  will be size  $(32 - 5) + 1 = 28$ 
          - Thus, the output images will be 28x28
          - Then, if  $D = 6$  (`out_channels` is 6), there will be 6 sets of kernels
            - Then the output will be 28x28x6
    '''
    # Placeholder, replace with your code

    #shape assignment
    B,N,H1,W1 = x.shape
```



```

F,D = kernels.shape[0],kernels.shape[3]
H2,W2 = H1-F+1,W1-F+1

#tensor creation
Y = torch.zeros([B,D,H2,W2])

#output calculation for forward pass
for batch_num in range(B):
    for i in range(D):
        sum =torch.zeros([H2,W2])
        for j in range(N):
            conv = signal.correlate2d(x[batch_num,j],kernels[:,,:
↵,j,i],mode='valid')
            sum = sum + conv
        Y[batch_num,i]=sum+bias[i]

return Y

```

3.1.2 Test your Conv2d forward pass:

```

[ ]: # Get random training image batch
dataiter = iter(trainloader)
images, labels = next(dataiter)
print(f'Input shape: {images.shape}')

# Sanity check of convolutional layer
kernels = torch.randn(5, 5, 3, 6)
bias = torch.randn(6, 28, 28)
out = MyConv2dForward.forward(images, kernels, bias)
print(f'Output shape: {out.shape}')

# CHECK: Output shape should be [4, 6, 28, 28]

```

Input shape: torch.Size([4, 3, 32, 32])
Output shape: torch.Size([4, 6, 28, 28])

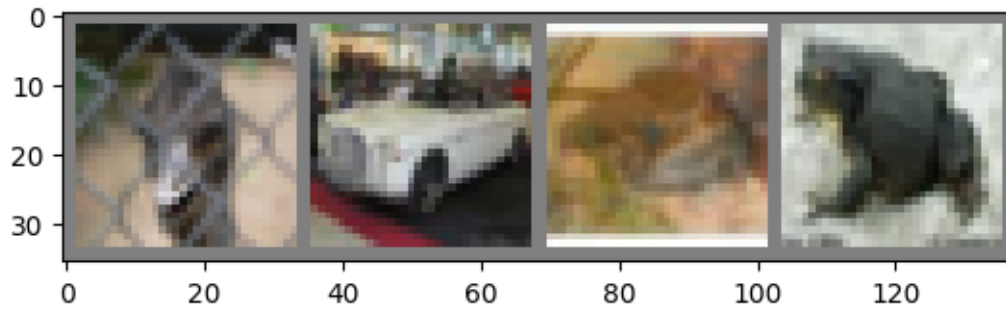
```

[ ]: imshow(utils.make_grid(images))

# Visualize output images after filtering (in grayscale)
print('Images after filtering:')
out = out.reshape(out.shape[0]*out.shape[1], 1, out.shape[2], out.shape[3])
imshow(utils.make_grid(out, nrow=6))

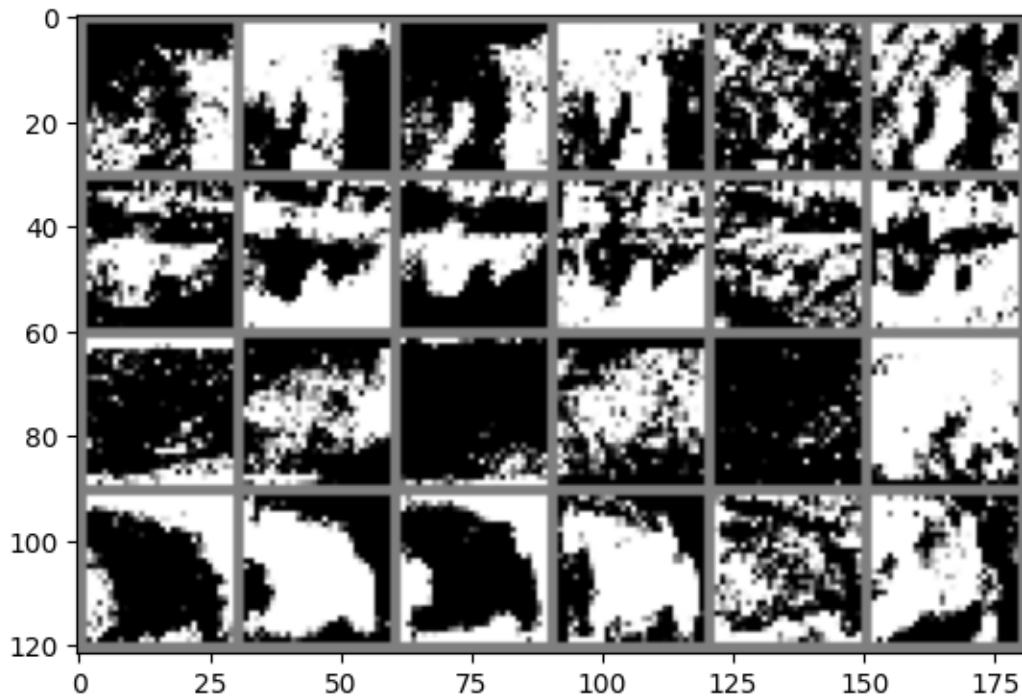
# CHECK: The images after filtering should look as such if correct:
# - Each row corresponds to a different image
# - Each column is that image filtered with a different kernel

```



Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).

Images after filtering:



3.1.3 In the code below, you will now implement the backward function for your Conv2d layer

To implement backpropagation for a neural network, the network needs the gradient of the loss function with respect to each input passed to the **forward** function. In the case of the Conv2d layer, we will be calculating this gradient for the kernels, input images, and bias.

Loss gradients you need to find with respect to each input variable:

$$\frac{\partial L}{\partial X_i}, \frac{\partial L}{\partial B_i}, \frac{\partial L}{\partial K_{ij}} \text{ known: } \frac{\partial L}{\partial Y_i} \quad (2)$$

In the above partial derivatives: - L : loss function (error) - Y_i : Output image from forward pass - X_i : Input image to layer - B_i : Bias parameters - K_{ij} : Kernel parameters

The derivative of the loss function with respect to the output image (Y_i) is given by PyTorch as an input parameter to **backward** called **grad_output**, so we don't need to worry about finding this, treat it as an input. - **grad_output** has shape $(B * D * H_2 * W_2)$

It is possible to derive these backpropagation partial derivatives (gradients) using the forward pass equation. The derivations are shown here (optional read): https://deeplearning.cs.cmu.edu/F21/document/recitation/Recitation5/CNN_Backprop_Recitation_5_F21.pdf

You will use these equations to calculate the gradients: 1. Gradient w.r.t. input image:

$$\frac{\partial L}{\partial X_j} = \sum_{i=1}^D \frac{\partial L}{\partial Y_i} * K_{ij} \text{ for } j = 1 \dots N \quad (3)$$

- $*$ operator: Full convolution - see 'full' mode: <https://docs.scipy.org/doc/scipy/reference/generated/scipy.signal.c>

2. Gradient w.r.t. kernel

$$\frac{\partial L}{\partial K_{ij}} = X_j \star \frac{\partial L}{\partial Y_i} \text{ for } i = 1 \dots D, j = 1 \dots N \quad (4)$$

- \star operator: Valid cross-correlation (see link in **forward** section)

3. Gradient w.r.t. bias

$$\frac{\partial L}{\partial B_i} = \frac{\partial L}{\partial Y_i} \text{ for } i = 1 \dots D \quad (5)$$

Hints: - You can use library functions to perform convolution and cross-correlation, such as `scipy.signal.correlate2d` and `scipy.signal.convolve2d`

```
[ ]: # TO DO: implement the 'backward' function

class MyConv2d(MyConv2dForward):
    '''Full custom Conv2d functions with backpropagation.'''

    @staticmethod
    def setup_context(ctx, inputs, output):
        '''Save tensors for backward. Don't change this function.'''
        x, kernels, bias = inputs
        ctx.save_for_backward(x, kernels, bias)

    @staticmethod
    def backward(ctx, grad_output):
        '''Backpropagation for convolutional layer.

        Args:
```

- ctx: Used to get input variables, no need to use this after the first line provided to you.

- grad_output: Partial derivative of loss function with respect to the output from the last layer in backpropagation. PyTorch provides us with this.

Outputs:

- 3 Tensors (calculated using backpropagation formulas in above text cell)
- grad_x: Partial derivative of loss function with respect to the input image
- grad_kernels: Partial derivative of loss function with respect to the kernels
- grad_bias: Partial derivative of loss function with respect to bias
- MUST return the above tensors in that order (grad_x, grad_kernels, grad_bias) for PyTorch

```
'''
# Don't delete this line. You should use x, kernels, and bias
x, kernels, bias = ctx.saved_tensors

#shape assignment
B,D,H2,W2 = grad_output.shape
F = kernels.shape[0]
N = x.shape[1]
H1,W1 = H2+F-1,W2+F-1

#tensor creation
grad_x = torch.zeros([B,N,H1,W1])

#grad_input calculation

for b in range(B):
    for j in range(N):
        sum =torch.zeros([H1,W1])
        for i in range(D):
            conv = signal.convolve2d(grad_output[b,i],kernels[:, :,
↪,j,i],mode='full')
            sum = sum+conv
        grad_x[b,j]=sum

#tensor creation
grad_kernels_b = torch.zeros([B,F,F,N,D])
grad_kernels = torch.zeros([F,F,N,D])

#grad_kernel calculation
for b in range(B):
    for j in range(N):
```

```

        for i in range(D):
            conv = torch.from_numpy(signal.
↪correlate2d(x[b,j],grad_output[b,i],mode='valid'))
            grad_kernels_b[b,:,:j,i] = conv

        grad_kernels = torch.sum(grad_kernels_b,0)

        #grad_bias calculation
        grad_bias = torch.sum(grad_output,0)

        #I am adding the gradients for batches as suggested by Danny on Piazza

    return grad_x,grad_kernels,grad_bias

```

3.1.4 Test backward function

- PyTorch has a function called `gradcheck` which will numerically check if your **backward** function has the correct gradient for your **forward** function.
- If done correctly, this cell should output `True`

```

[ ]: # Check that gradients calculated in `backward` are correct
images.requires_grad = True
kernels.requires_grad = True
bias.requires_grad = True
image = images[0, 0, :16, :16]

bias = torch.randn(2, 15, 15)
kernels = torch.randn(2, 2, 1, 2)

test = torch.autograd.gradcheck(MyConv2d.apply, (image.reshape(1, 1, 16, 16),
↪kernels, bias), eps=1e-3, atol=1e-2)
print(test)
# CHECK: should output True if forward and backward passes are correct

```

True

3.1.5 In the code below, you will now implement the actual Conv2d custom layer.

- This `MyConv2dLayer` class will use the `MyConv2d` forward and backward functions you implemented above.
- In the constructor of this class, you will initialize the kernels and biases as the model parameters.

We will initialize our parameters the same way that the PyTorch `nn.Conv2d` layer does. See the ‘Variables:’ section at the bottom for information: <https://pytorch.org/docs/master/generated/torch.nn.Conv2d.html#torch.nn.Conv2d>

From the above reference, - Initialize the kernels with a Uniform Distribution (look into `np.random.uniform`) where the bounds are $(-\sqrt{k}, \sqrt{k})$. - where $k = \frac{1}{N*F*F}$

Hints: - Since we want the kernels and biases to be learnable parameters for the model, they should be set as such:

- `self.kernels = nn.Parameter(...)` - `self.bias = nn.Parameter(...)` - You are welcome to change the parameters to this `MyConv2dLayer` or which ones you use if you please. Just note you will have to change them in following code sections if you do.

```
[ ]: class MyConv2dLayer(nn.Module):
    '''Custom Conv2d Layer, which calls MyConv2d in forward function with defined
    ↪ parameters to learn.'''

    def __init__(self, in_channels, out_channels, kernel_size, image_size):
        '''
        Args:
            - in_channels: Depth of input tensor (N)
            - out_channels: Depth of output tensor (number of kernels for
            ↪ convolution) (D)
            - kernel_size: Size of kernels (width and height) (F)
            - image_size: Shape of input images to this layer (H1, W1)
            - For example, 32x32 images would be (32, 32)

        Should define self.kernels and self.bias parameters
        '''
        super().__init__()
        # TO DO: initialize self.kernels and self.bias

        #initializing as per documentation of Conv2d
        k = np.sqrt(1/(in_channels*kernel_size*kernel_size))
        self.kernels = nn.Parameter(torch.from_numpy(np.random.
        ↪ uniform(-k,k,[kernel_size,kernel_size,in_channels,out_channels])))
        self.bias = nn.Parameter(torch.from_numpy(np.random.
        ↪ uniform(-k,k,[out_channels,image_size[0]-kernel_size+1,image_size[1]-kernel_size+1])))

    def forward(self, x):
        '''Forward for layer.

        Args:
            - x: Input to layer

        Output:
            - Output from layer after forward pass to pass to next layer
        '''
        # Do not make changes to this function
        return MyConv2d(x, self.kernels, self.bias)
```

3.1.6 Test MyConv2dLayer

```
[ ]: # Test convolutional layer with N=3, D=6, F=5, with 32x32 input images
ConvTest = MyConv2dLayer(in_channels=3, out_channels=6, kernel_size=5,
    ↪image_size=(32, 32))

# Get random training image batch
dataiter = iter(trainloader)
images, labels = next(dataiter)
print(f'Input shape: {images.shape}')

# Sanity check of convolutional layer
out = ConvTest(images)
kernels = torch.randn(5, 5, 3, 6)
print(f'Output shape: {out.shape}')

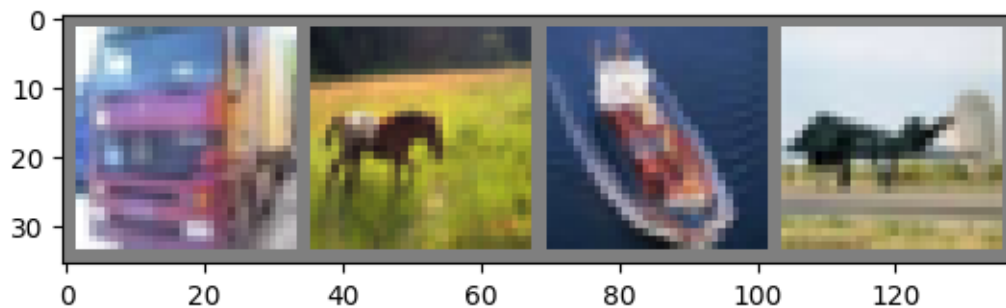
# CHECK: Output shape should be [4, 6, 28, 28]
```

Input shape: torch.Size([4, 3, 32, 32])
Output shape: torch.Size([4, 6, 28, 28])

```
[ ]: imshow(utils.make_grid(images))

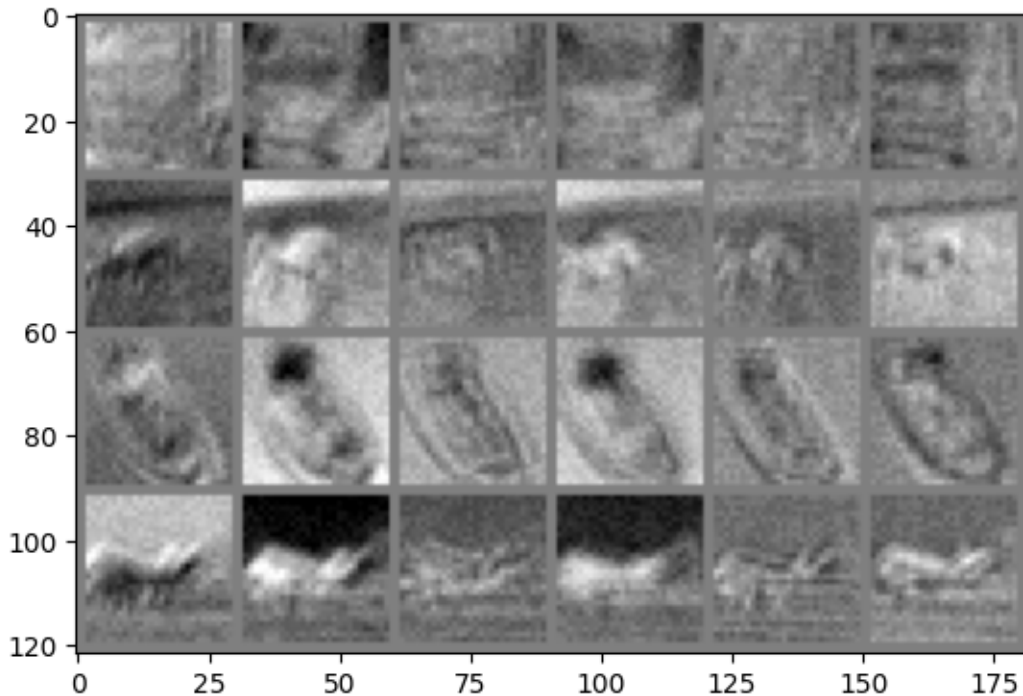
# Visualize output images after filtering (in grayscale)
print('Images after filtering:')
out = out.reshape(out.shape[0]*out.shape[1], 1, out.shape[2], out.shape[3])
imshow(utils.make_grid(out, nrow=6))

# CHECK: The images after filtering should look as such if correct
#   - Each row corresponds to a different image
#   - Each column is that image filtered with a different kernel
```



Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).

Images after filtering:



PyTorch keeps a dictionary of all parameters that will be learned for the layer, so this code makes sure that your **kernels** and **bias** tensors were registered as model parameters.

```
[ ]: print([p for p in ConvTest.named_parameters()])
      # Ensure that 'kernels' and 'bias' are listed as parameters for this layer
```

```
[('kernels', Parameter containing:
tensor([[[[ 0.0602,  0.0943, -0.0355,  0.0330,  0.0440,  0.0959],
           [ 0.0284,  0.1004, -0.0076,  0.0617, -0.1006,  0.0935],
           [ 0.0860, -0.0053,  0.0316,  0.0705,  0.0766,  0.0005]],

          [[-0.0233, -0.0519, -0.0966, -0.0237,  0.0565,  0.0859],
           [ 0.0388, -0.1137,  0.0668, -0.0986, -0.0851, -0.0410],
           [ 0.0999,  0.0955,  0.0273,  0.0348, -0.1048,  0.0676]],

          [[-0.0593, -0.0054, -0.0646,  0.0762, -0.1051,  0.0371],
           [-0.0602, -0.0558, -0.0968, -0.1154,  0.1028, -0.0590],
           [-0.0924, -0.0231, -0.0284,  0.1067,  0.0393,  0.0395]],

          [[ 0.0781, -0.1079, -0.0617, -0.0443,  0.0209, -0.0744],
           [ 0.0760,  0.0327, -0.0573, -0.0823, -0.0389,  0.0103],
           [-0.0799, -0.0843,  0.0242, -0.0538, -0.0239, -0.0651]],

          [[ 0.0235, -0.0409,  0.0147,  0.0286, -0.0308,  0.0100],
```



```

[ 0.0679, -0.0398, -0.0256, 0.0547, 0.0220, -0.0237],
[ 0.0966, -0.0821, -0.0709, 0.0130, 0.0007, -0.0232]]],

[[[-0.0466, -0.0075, -0.1089, -0.0268, 0.0146, -0.0337],
[-0.0452, 0.0896, 0.0362, -0.0915, 0.1077, 0.0942],
[ 0.0857, 0.0268, -0.0562, -0.0774, 0.0059, -0.0853]],

[[ 0.0513, -0.0449, 0.0886, -0.0807, 0.0973, -0.0336],
[ 0.0512, 0.1133, -0.0263, -0.0164, -0.0234, -0.0353],
[-0.0190, -0.0843, -0.0366, 0.1064, 0.0776, -0.0867]],

[[ 0.0196, 0.0193, 0.0432, 0.0891, 0.0068, -0.0489],
[-0.0133, 0.0648, 0.0805, -0.0660, -0.1151, 0.0868],
[-0.0044, -0.1076, -0.1117, -0.0446, -0.0717, -0.0222]],

[[ 0.0619, -0.1033, 0.0023, -0.0604, -0.0489, 0.0455],
[ 0.0537, -0.0229, -0.0424, -0.0457, -0.0642, 0.1097],
[ 0.1051, -0.0911, -0.0716, -0.0801, -0.0798, -0.0080]],

[[[-0.0451, 0.1133, 0.0870, 0.0002, -0.0665, 0.0761],
[-0.0728, -0.0410, 0.0831, -0.0641, -0.0572, 0.0966],
[-0.0266, 0.0957, 0.0951, -0.0435, 0.0882, 0.0865]]],

[[[ 0.1030, 0.0955, -0.0266, 0.0039, -0.0203, 0.0327],
[ 0.0282, -0.0582, -0.0452, 0.0708, 0.0310, -0.0009],
[ 0.0380, -0.0430, 0.1076, -0.0734, 0.0289, -0.0545]],

[[ 0.0068, -0.0724, -0.0260, 0.0837, 0.0795, -0.0600],
[ 0.0718, -0.0188, 0.0550, -0.0378, 0.0504, -0.0183],
[-0.0647, -0.0166, 0.0099, -0.1106, 0.0557, 0.0225]],

[[[-0.0466, -0.0366, -0.0395, -0.0360, -0.0480, -0.0541],
[ 0.0915, 0.0487, 0.0098, 0.0190, 0.0423, 0.0889],
[ 0.0188, -0.0387, 0.1074, -0.0583, 0.0282, 0.0129]],

[[ 0.0401, -0.1029, -0.0166, -0.0129, -0.0479, -0.0037],
[ 0.0997, 0.0461, -0.0733, 0.1128, -0.0609, 0.0949],
[ 0.1021, 0.0955, 0.0528, 0.0862, 0.0141, -0.0795]],

[[[-0.0975, -0.0994, -0.1078, -0.0315, -0.0029, -0.1081],
[-0.1109, 0.0750, -0.0056, -0.1130, 0.0948, 0.0064],
[ 0.0542, 0.0033, 0.1058, -0.0406, 0.0909, -0.0030]]],

[[[ 0.0900, -0.0752, 0.0236, -0.0715, 0.0174, -0.0253],
[-0.0906, -0.0515, -0.0135, 0.0867, -0.0337, -0.0832],

```

```

        [-0.0111, -0.0047, 0.0460, 0.0715, -0.1137, -0.0399]],

        [[-0.0348, -0.0843, 0.0386, 0.0950, -0.0140, -0.0850],
         [ 0.0176, -0.0701, 0.0998, 0.0104, -0.0452, 0.0610],
         [ 0.0118, -0.1076, -0.0752, -0.0979, -0.0446, -0.0233]],

        [[-0.1037, -0.0797, 0.0865, -0.1113, -0.0943, -0.0816],
         [-0.0242, 0.0968, -0.0519, 0.0966, -0.1000, -0.0766],
         [ 0.0390, -0.1105, 0.0813, -0.1051, -0.0082, -0.0997]],

        [[-0.0283, -0.0190, 0.0035, -0.0411, -0.0387, 0.0865],
         [ 0.1124, -0.0103, 0.1097, -0.0989, 0.0791, 0.0037],
         [-0.0693, 0.0873, 0.0013, 0.0115, -0.0667, -0.1145]],

        [[-0.1012, 0.0892, -0.0805, -0.0007, -0.0711, 0.0448],
         [-0.0820, -0.0420, -0.0238, -0.0543, 0.0087, 0.0432],
         [ 0.0512, -0.0944, -0.1092, -0.1080, 0.0046, -0.1013]]],

        [[[-0.0115, -0.0668, -0.1020, -0.0949, 0.0561, 0.0726],
          [-0.0055, 0.0160, -0.1090, 0.0062, 0.1021, -0.0007],
          [ 0.0608, -0.1015, 0.0444, -0.0782, -0.0246, -0.0024]],

          [[ 0.0594, -0.0542, -0.0605, -0.0804, 0.0742, -0.1042],
           [-0.0157, -0.0795, -0.0714, 0.0523, -0.1089, -0.0709],
           [ 0.0909, 0.0839, -0.0791, 0.0446, 0.0398, 0.0103]],

          [[-0.0251, 0.0392, -0.0197, 0.0506, 0.0376, -0.0007],
           [-0.0685, 0.0178, 0.1138, -0.0551, -0.0830, 0.0334],
           [ 0.1092, -0.0905, 0.0212, -0.0275, 0.0796, -0.0711]],

          [[-0.0734, -0.1044, 0.0369, -0.1037, 0.0160, 0.0753],
           [-0.1118, -0.0846, -0.0791, 0.0356, 0.0776, -0.0183],
           [-0.1040, 0.0532, -0.0942, 0.0739, 0.0611, -0.0019]],

          [[ 0.0985, -0.0180, -0.0728, -0.0671, -0.0406, -0.0412],
           [-0.0178, -0.0528, 0.0304, 0.1035, -0.0255, 0.0422],
           [-0.0180, 0.0802, 0.0415, 0.0820, -0.0030, 0.0930]]]],
        dtype=torch.float64, requires_grad=True)), ('bias', Parameter containing:
tensor([[[[ 0.0226, -0.0427, -0.0758, ..., 0.0449, 0.0443, 0.0295],
          [-0.0349, -0.0075, 0.1020, ..., -0.0364, -0.0917, -0.0089],
          [ 0.0771, -0.0762, -0.0946, ..., 0.0746, 0.0646, 0.0700],
          ...,
          [ 0.0341, -0.0772, -0.0540, ..., -0.0356, 0.0788, 0.0896],
          [ 0.0122, 0.0479, 0.1056, ..., -0.0223, 0.0896, 0.0099],
          [-0.0965, -0.0482, 0.0612, ..., -0.0791, -0.0973, 0.0376]]],

          [[-0.0001, -0.0238, -0.0156, ..., 0.0037, 0.0594, 0.0861],

```

```

[ 0.0206, -0.0584, -0.0700, ..., -0.0073, 0.0432, -0.1137],
[-0.1028, 0.0936, -0.0949, ..., 0.1136, -0.0983, -0.0997],
...,
[ 0.0107, -0.0338, 0.0236, ..., 0.0168, 0.1006, -0.0803],
[-0.1047, -0.0194, -0.0452, ..., -0.0301, -0.0410, 0.0971],
[ 0.0173, 0.0410, -0.0684, ..., -0.0169, -0.1026, 0.0321]],

[[-0.0295, -0.0910, -0.0295, ..., -0.0341, -0.0512, -0.0078],
[-0.0743, -0.0945, 0.0271, ..., -0.0886, 0.0669, -0.1114],
[-0.0318, 0.0515, -0.0409, ..., -0.0035, 0.0482, -0.0815],
...,
[ 0.0300, 0.0662, -0.0562, ..., 0.0223, 0.0468, -0.1147],
[-0.0394, -0.0433, 0.1008, ..., -0.0447, 0.0629, 0.0309],
[ 0.1087, 0.0454, 0.0349, ..., -0.0391, 0.0800, -0.1036]],

[[ 0.0803, 0.0367, 0.0848, ..., 0.0989, -0.0128, 0.1108],
[ 0.0903, 0.1105, -0.0608, ..., 0.0668, -0.0746, -0.0917],
[ 0.0010, 0.0469, -0.0695, ..., -0.0376, -0.0856, -0.0396],
...,
[-0.0829, -0.0441, 0.0322, ..., 0.0468, 0.0187, 0.0012],
[ 0.0710, 0.0137, 0.0609, ..., -0.0324, -0.0287, 0.0846],
[ 0.1012, 0.0806, -0.0385, ..., 0.0032, -0.0881, 0.0678]],

[[-0.0868, 0.0302, 0.0827, ..., 0.0720, -0.0161, 0.0814],
[-0.0035, -0.0695, 0.1040, ..., -0.0982, -0.0880, 0.0497],
[-0.0510, -0.0236, -0.0841, ..., -0.0659, -0.0727, -0.0007],
...,
[ 0.0779, -0.0748, 0.0894, ..., 0.0578, 0.0251, 0.0944],
[-0.0775, -0.0847, 0.0693, ..., -0.0474, 0.0889, -0.0646],
[ 0.0382, -0.0892, 0.0093, ..., -0.0256, 0.0745, 0.1146]],

[[-0.0404, -0.0037, -0.0970, ..., 0.0441, -0.0684, 0.0857],
[-0.0636, -0.0203, -0.0612, ..., 0.0106, -0.0193, -0.0618],
[-0.0736, -0.0523, 0.0435, ..., 0.0588, -0.0709, -0.0300],
...,
[-0.0021, 0.0716, 0.0323, ..., 0.0993, 0.0382, 0.0667],
[-0.0295, 0.0530, -0.0523, ..., 0.0160, -0.0827, -0.0623],
[ 0.0845, -0.1034, 0.0061, ..., 0.0617, -0.0229, 0.0486]]],
dtype=torch.float64, requires_grad=True)))

```

3.2 Training your CustomSimpleCNN network

- Now, your MyConv2dLayer can replace PyTorch's nn.Conv2d layer in the SimpleCNN network, which is done for you below
- We will train this network, and should see similar accuracy results for the trained SimpleCNN architecture

```
[ ]: # No need to change anything here, unless you changed your MyConv2dLayer
      ↪ constructor parameters

class CustomSimpleCNN(nn.Module):
    '''CustomSimpleCNN uses your own custom Conv2d layer from this problem.'''

    def __init__(self):
        '''Defines layers for this network.'''
        super().__init__()

        self.conv1 = MyConv2dLayer(in_channels=3, out_channels=6,
        ↪kernel_size=5, image_size=(32, 32))
        self.pool = nn.MaxPool2d(kernel_size=2, stride=2)
        self.conv2 = MyConv2dLayer(in_channels=6, out_channels=16,
        ↪kernel_size=5, image_size=(14, 14))
        self.fc1 = nn.Linear(in_features=16 * 5 * 5, out_features=120)
        self.fc2 = nn.Linear(in_features=120, out_features=84)
        self.fc3 = nn.Linear(in_features=84, out_features=10)

    def forward(self, x):
        '''Defines graph connections for layers of this network.'''

        x = self.pool(F.relu(self.conv1(x)))
        x = self.pool(F.relu(self.conv2(x)))
        x = torch.flatten(x, 1) # flatten all dimensions except batch
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x
```

```
[ ]: custom_model = CustomSimpleCNN().to(device)
      summary(custom_model, input_size=(3, 32, 32))

      criterion = nn.CrossEntropyLoss()
      optimizer = optim.SGD(custom_model.parameters(), lr=0.001, momentum=0.9)
```

Layer (type)	Output Shape	Param #
MyConv2dLayer-1	[-1, 6, 28, 28]	4,704
MaxPool2d-2	[-1, 6, 14, 14]	0
MyConv2dLayer-3	[-1, 16, 10, 10]	1,600
MaxPool2d-4	[-1, 16, 5, 5]	0
Linear-5	[-1, 120]	48,120
Linear-6	[-1, 84]	10,164
Linear-7	[-1, 10]	850

Total params: 65,438
Trainable params: 59,134
Non-trainable params: 6,304

Input size (MB): 0.01
Forward/backward pass size (MB): 0.06
Params size (MB): 0.25
Estimated Total Size (MB): 0.32

3.2.1 Optional Debug Loop

- The code below is commented out and not necessary to run, but will run training for 3 batches and allow you to print out some sample gradients being calculated for your model parameters (kernels and bias).
 - To verify the gradients, ensure that they are valid and change between loop iterations.
- You can uncomment this and use it to print anything during training to help debug your model if necessary.

```
[ ]: # UNCOMMENT if wanting to debug anything for a couple training iterations

# print('Training Debug Loop')

# for i, data in enumerate(tqdm(trainloader)):
#     # get the inputs; data is a list of [inputs, labels]
#     inputs, labels = data

#     # zero the parameter gradients
#     optimizer.zero_grad()

#     # forward + backward + optimize
#     outputs = custom_model(inputs)
#     loss = criterion(outputs, labels)
#     loss.backward()
#     optimizer.step()

#     if i == 3:
#         break

#     print('\n')
#     ↵
#     ↵ print(f'-----{i}-----')
#     print('KERNEL GRADIENTS:\n')
#     print(custom_model.conv1.kernels.grad[0, 0, :, :])
#     print('BIAS GRADIENTS:\n')
#     print(custom_model.conv1.bias.grad[0, :5, :5])
```

3.2.2 Training CustomSimpleCNN

- This might take a while depending on your implementation's speed
- To debug quicker, check if the model accuracy increases between the first and second accuracy prints (batches 2000 and 4000).
 - If correct, your accuracy should improve between the first two outputs
- Without a fast, vectorized solution, this can take about 5 minutes per benchmark print (2000 batches)

```
[ ]: # Don't change the number of epochs for this problem  
train(custom_model, trainloader, criterion, optimizer)
```

Start Training

```
16%|          | 2001/12500 [03:02<15:14, 11.48it/s]  
[epoch 1, batch 2000] loss: 2.154  
  
Accuracy of the network on last 2000 training images: 19 %  
32%|          | 4002/12500 [06:01<12:28, 11.35it/s]  
[epoch 1, batch 4000] loss: 1.827  
  
Accuracy of the network on last 2000 training images: 33 %  
48%|          | 6002/12500 [08:58<09:25, 11.48it/s]  
[epoch 1, batch 6000] loss: 1.677  
  
Accuracy of the network on last 2000 training images: 38 %  
64%|          | 8001/12500 [11:53<06:33, 11.44it/s]  
[epoch 1, batch 8000] loss: 1.588  
  
Accuracy of the network on last 2000 training images: 41 %  
80%|          | 10001/12500 [14:48<03:37, 11.47it/s]  
[epoch 1, batch 10000] loss: 1.528  
  
Accuracy of the network on last 2000 training images: 44 %  
96%|          | 12001/12500 [17:42<00:43, 11.53it/s]  
[epoch 1, batch 12000] loss: 1.479  
  
Accuracy of the network on last 2000 training images: 46 %  
100%|         | 12500/12500 [18:36<00:00, 11.20it/s]  
16%|          | 2001/12500 [02:59<15:09, 11.55it/s]  
[epoch 2, batch 2000] loss: 1.395
```

Accuracy of the network on last 2000 training images: 48 %

32%| | 4001/12500 [05:53<12:15, 11.55it/s]

[epoch 2, batch 4000] loss: 1.396

Accuracy of the network on last 2000 training images: 49 %

48%| | 6002/12500 [08:47<09:22, 11.55it/s]

[epoch 2, batch 6000] loss: 1.390

Accuracy of the network on last 2000 training images: 51 %

64%| | 8002/12500 [11:40<06:28, 11.57it/s]

[epoch 2, batch 8000] loss: 1.319

Accuracy of the network on last 2000 training images: 52 %

80%| | 10001/12500 [14:34<03:36, 11.56it/s]

[epoch 2, batch 10000] loss: 1.301

Accuracy of the network on last 2000 training images: 53 %

96%| | 12001/12500 [17:35<00:43, 11.57it/s]

[epoch 2, batch 12000] loss: 1.304

Accuracy of the network on last 2000 training images: 53 %

100%| | 12500/12500 [18:28<00:00, 11.27it/s]

Finished Training

3.2.3 Evaluating CustomSimpleCNN

- If your Conv2d layer is correct, you should get an accuracy similar to that from the trained SimpleCNN provided in Problem 3, which was around 50% for us.

```
[ ]: # Accuracy should be similar to the trained SimpleCNN in problem 3 (around 50%)  
     evaluation(custom_model, testloader)
```

100%| | 2500/2500 [01:39<00:00, 25.17it/s]

Accuracy of the network on the 10000 test images: 54 %

Time to train custom CNN model ~ 37min 4s on Macbook Air M1
Training Accuracy: 53%
Testing Accuracy: 54%

4 Creating a PDF version of your current notebook

```
[3]: #The following two installation steps are needed to generate a PDF version of
    ↪the notebook
    #(These lines are needed within Google Colab, but are not needed within a local
    ↪version of Jupyter notebook)
    !apt-get -qq install texlive texlive-xetex texlive-latex-extra pandoc
    %pip install --quiet py pandoc
```

```
Extracting templates from packages: 100%
Preconfiguring packages ...
Selecting previously unselected package fonts-droid-fallback.
(Reading database ... 120882 files and directories currently installed.)
Preparing to unpack .../00-fonts-droid-fallback_1%3a6.0.1r16-1.1build1_all.deb
...
Unpacking fonts-droid-fallback (1:6.0.1r16-1.1build1) ...
Selecting previously unselected package fonts-lato.
Preparing to unpack .../01-fonts-lato_2.0-2.1_all.deb ...
Unpacking fonts-lato (2.0-2.1) ...
Selecting previously unselected package poppler-data.
Preparing to unpack .../02-poppler-data_0.4.11-1_all.deb ...
Unpacking poppler-data (0.4.11-1) ...
Selecting previously unselected package tex-common.
Preparing to unpack .../03-tex-common_6.17_all.deb ...
Unpacking tex-common (6.17) ...
Selecting previously unselected package fonts-urw-base35.
Preparing to unpack .../04-fonts-urw-base35_20200910-1_all.deb ...
Unpacking fonts-urw-base35 (20200910-1) ...
Selecting previously unselected package libgs9-common.
Preparing to unpack .../05-libgs9-common_9.55.0~dfsg1-0ubuntu5.5_all.deb ...
Unpacking libgs9-common (9.55.0~dfsg1-0ubuntu5.5) ...
Selecting previously unselected package libidn12:amd64.
Preparing to unpack .../06-libidn12_1.38-4ubuntu1_amd64.deb ...
Unpacking libidn12:amd64 (1.38-4ubuntu1) ...
Selecting previously unselected package libijs-0.35:amd64.
Preparing to unpack .../07-libijs-0.35_0.35-15build2_amd64.deb ...
Unpacking libijs-0.35:amd64 (0.35-15build2) ...
Selecting previously unselected package libjbig2dec0:amd64.
Preparing to unpack .../08-libjbig2dec0_0.19-3build2_amd64.deb ...
Unpacking libjbig2dec0:amd64 (0.19-3build2) ...
Selecting previously unselected package libgs9:amd64.
```



```

Preparing to unpack .../09-libgs9_9.55.0~dfsg1-0ubuntu5.5_amd64.deb ...
Unpacking libgs9:amd64 (9.55.0~dfsg1-0ubuntu5.5) ...
Selecting previously unselected package libkpathsea6:amd64.
Preparing to unpack .../10-libkpathsea6_2021.20210626.59705-1ubuntu0.1_amd64.deb
...
Unpacking libkpathsea6:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Selecting previously unselected package libwoff1:amd64.
Preparing to unpack .../11-libwoff1_1.0.2-1build4_amd64.deb ...
Unpacking libwoff1:amd64 (1.0.2-1build4) ...
Selecting previously unselected package dvisvgm.
Preparing to unpack .../12-dvisvgm_2.13.1-1_amd64.deb ...
Unpacking dvisvgm (2.13.1-1) ...
Selecting previously unselected package fonts-lmodern.
Preparing to unpack .../13-fonts-lmodern_2.004.5-6.1_all.deb ...
Unpacking fonts-lmodern (2.004.5-6.1) ...
Selecting previously unselected package fonts-noto-mono.
Preparing to unpack .../14-fonts-noto-mono_20201225-1build1_all.deb ...
Unpacking fonts-noto-mono (20201225-1build1) ...
Selecting previously unselected package fonts-texgyre.
Preparing to unpack .../15-fonts-texgyre_20180621-3.1_all.deb ...
Unpacking fonts-texgyre (20180621-3.1) ...
Selecting previously unselected package libapache-pom-java.
Preparing to unpack .../16-libapache-pom-java_18-1_all.deb ...
Unpacking libapache-pom-java (18-1) ...
Selecting previously unselected package libcommons-parent-java.
Preparing to unpack .../17-libcommons-parent-java_43-1_all.deb ...
Unpacking libcommons-parent-java (43-1) ...
Selecting previously unselected package libcommons-logging-java.
Preparing to unpack .../18-libcommons-logging-java_1.2-2_all.deb ...
Unpacking libcommons-logging-java (1.2-2) ...
Selecting previously unselected package libfontenc1:amd64.
Preparing to unpack .../19-libfontenc1_1%3a1.1.4-1build3_amd64.deb ...
Unpacking libfontenc1:amd64 (1:1.1.4-1build3) ...
Selecting previously unselected package libptexenc1:amd64.
Preparing to unpack .../20-libptexenc1_2021.20210626.59705-1ubuntu0.1_amd64.deb
...
Unpacking libptexenc1:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Selecting previously unselected package rubygems-integration.
Preparing to unpack .../21-rubygems-integration_1.18_all.deb ...
Unpacking rubygems-integration (1.18) ...
Selecting previously unselected package ruby3.0.
Preparing to unpack .../22-ruby3.0_3.0.2-7ubuntu2.4_amd64.deb ...
Unpacking ruby3.0 (3.0.2-7ubuntu2.4) ...
Selecting previously unselected package ruby-rubygems.
Preparing to unpack .../23-ruby-rubygems_3.3.5-2_all.deb ...
Unpacking ruby-rubygems (3.3.5-2) ...
Selecting previously unselected package ruby.
Preparing to unpack .../24-ruby_1%3a3.0~exp1_amd64.deb ...

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```

Unpacking ruby (1:3.0~exp1) ...
Selecting previously unselected package rake.
Preparing to unpack .../25-rake_13.0.6-2_all.deb ...
Unpacking rake (13.0.6-2) ...
Selecting previously unselected package ruby-net-telnet.
Preparing to unpack .../26-ruby-net-telnet_0.1.1-2_all.deb ...
Unpacking ruby-net-telnet (0.1.1-2) ...
Selecting previously unselected package ruby-webrick.
Preparing to unpack .../27-ruby-webrick_1.7.0-3_all.deb ...
Unpacking ruby-webrick (1.7.0-3) ...
Selecting previously unselected package ruby-xmlrpc.
Preparing to unpack .../28-ruby-xmlrpc_0.3.2-1ubuntu0.1_all.deb ...
Unpacking ruby-xmlrpc (0.3.2-1ubuntu0.1) ...
Selecting previously unselected package libruby3.0:amd64.
Preparing to unpack .../29-libruby3.0_3.0.2-7ubuntu2.4_amd64.deb ...
Unpacking libruby3.0:amd64 (3.0.2-7ubuntu2.4) ...
Selecting previously unselected package libsyntax2:amd64.
Preparing to unpack .../30-libsyntax2_2021.20210626.59705-1ubuntu0.1_amd64.deb
...
Unpacking libsyntax2:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Selecting previously unselected package libteckit0:amd64.
Preparing to unpack .../31-libteckit0_2.5.11+ds1-1_amd64.deb ...
Unpacking libteckit0:amd64 (2.5.11+ds1-1) ...
Selecting previously unselected package libtexlua53:amd64.
Preparing to unpack .../32-libtexlua53_2021.20210626.59705-1ubuntu0.1_amd64.deb
...
Unpacking libtexlua53:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Selecting previously unselected package libtexluajit2:amd64.
Preparing to unpack
.../33-libtexluajit2_2021.20210626.59705-1ubuntu0.1_amd64.deb ...
Unpacking libtexluajit2:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Selecting previously unselected package libzip-0-13:amd64.
Preparing to unpack .../34-libzip-0-13_0.13.72+dfsg.1-1.1_amd64.deb ...
Unpacking libzip-0-13:amd64 (0.13.72+dfsg.1-1.1) ...
Selecting previously unselected package xfonts-encodings.
Preparing to unpack .../35-xfonts-encodings_1%3a1.0.5-0ubuntu2_all.deb ...
Unpacking xfonts-encodings (1:1.0.5-0ubuntu2) ...
Selecting previously unselected package xfonts-utils.
Preparing to unpack .../36-xfonts-utils_1%3a7.7+6build2_amd64.deb ...
Unpacking xfonts-utils (1:7.7+6build2) ...
Selecting previously unselected package lmodern.
Preparing to unpack .../37-lmodern_2.004.5-6.1_all.deb ...
Unpacking lmodern (2.004.5-6.1) ...
Selecting previously unselected package preview-latex-style.
Preparing to unpack .../38-preview-latex-style_12.2-1ubuntu1_all.deb ...
Unpacking preview-latex-style (12.2-1ubuntu1) ...
Selecting previously unselected package t1utils.
Preparing to unpack .../39-t1utils_1.41-4build2_amd64.deb ...

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Unpacking t1utils (1.41-4build2) ...
Selecting previously unselected package teckit.
Preparing to unpack .../40-teckit_2.5.11+ds1-1_amd64.deb ...
Unpacking teckit (2.5.11+ds1-1) ...
Selecting previously unselected package tex-gyre.
Preparing to unpack .../41-tex-gyre_20180621-3.1_all.deb ...
Unpacking tex-gyre (20180621-3.1) ...
Selecting previously unselected package texlive-binaries.
Preparing to unpack .../42-texlive-
binaries_2021.20210626.59705-1ubuntu0.1_amd64.deb ...
Unpacking texlive-binaries (2021.20210626.59705-1ubuntu0.1) ...
Selecting previously unselected package texlive-base.
Preparing to unpack .../43-texlive-base_2021.20220204-1_all.deb ...
Unpacking texlive-base (2021.20220204-1) ...
Selecting previously unselected package texlive-fonts-recommended.
Preparing to unpack .../44-texlive-fonts-recommended_2021.20220204-1_all.deb ...
Unpacking texlive-fonts-recommended (2021.20220204-1) ...
Selecting previously unselected package texlive-latex-base.
Preparing to unpack .../45-texlive-latex-base_2021.20220204-1_all.deb ...
Unpacking texlive-latex-base (2021.20220204-1) ...
Selecting previously unselected package texlive-latex-recommended.
Preparing to unpack .../46-texlive-latex-recommended_2021.20220204-1_all.deb ...
Unpacking texlive-latex-recommended (2021.20220204-1) ...
Selecting previously unselected package texlive.
Preparing to unpack .../47-texlive_2021.20220204-1_all.deb ...
Unpacking texlive (2021.20220204-1) ...
Selecting previously unselected package libfontbox-java.
Preparing to unpack .../48-libfontbox-java_1%3a1.8.16-2_all.deb ...
Unpacking libfontbox-java (1:1.8.16-2) ...
Selecting previously unselected package libpdfbox-java.
Preparing to unpack .../49-libpdfbox-java_1%3a1.8.16-2_all.deb ...
Unpacking libpdfbox-java (1:1.8.16-2) ...
Selecting previously unselected package texlive-pictures.
Preparing to unpack .../50-texlive-pictures_2021.20220204-1_all.deb ...
Unpacking texlive-pictures (2021.20220204-1) ...
Selecting previously unselected package texlive-latex-extra.
Preparing to unpack .../51-texlive-latex-extra_2021.20220204-1_all.deb ...
Unpacking texlive-latex-extra (2021.20220204-1) ...
Selecting previously unselected package texlive-plain-generic.
Preparing to unpack .../52-texlive-plain-generic_2021.20220204-1_all.deb ...
Unpacking texlive-plain-generic (2021.20220204-1) ...
Selecting previously unselected package tipa.
Preparing to unpack .../53-tipa_2%3a1.3-21_all.deb ...
Unpacking tipa (2:1.3-21) ...
Selecting previously unselected package texlive-xetex.
Preparing to unpack .../54-texlive-xetex_2021.20220204-1_all.deb ...
Unpacking texlive-xetex (2021.20220204-1) ...
Setting up fonts-lato (2.0-2.1) ...

```

```

Setting up fonts-noto-mono (20201225-1build1) ...
Setting up libwoff1:amd64 (1.0.2-1build4) ...
Setting up libtexlua53:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Setting up libijs-0.35:amd64 (0.35-15build2) ...
Setting up libtexluajit2:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Setting up libfontbox-java (1:1.8.16-2) ...
Setting up rubygems-integration (1.18) ...
Setting up libzip-0-13:amd64 (0.13.72+dfsg.1-1.1) ...
Setting up fonts-urw-base35 (20200910-1) ...
Setting up poppler-data (0.4.11-1) ...
Setting up tex-common (6.17) ...
update-language: texlive-base not installed and configured, doing nothing!
Setting up libfontenc1:amd64 (1:1.1.4-1build3) ...
Setting up libjbig2dec0:amd64 (0.19-3build2) ...
Setting up libteckit0:amd64 (2.5.11+ds1-1) ...
Setting up libapache-pom-java (18-1) ...
Setting up ruby-net-telnet (0.1.1-2) ...
Setting up xfonts-encodings (1:1.0.5-0ubuntu2) ...
Setting up t1utils (1.41-4build2) ...
Setting up libidn12:amd64 (1.38-4ubuntu1) ...
Setting up fonts-texgyre (20180621-3.1) ...
Setting up libkpathsea6:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Setting up ruby-webrick (1.7.0-3) ...
Setting up fonts-lmodern (2.004.5-6.1) ...
Setting up fonts-droid-fallback (1:6.0.1r16-1.1build1) ...
Setting up ruby-xmlrpc (0.3.2-1ubuntu0.1) ...
Setting up libsynchronet2:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Setting up libgs9-common (9.55.0~dfsg1-0ubuntu5.5) ...
Setting up teckit (2.5.11+ds1-1) ...
Setting up libpdfbox-java (1:1.8.16-2) ...
Setting up libgs9:amd64 (9.55.0~dfsg1-0ubuntu5.5) ...
Setting up preview-latex-style (12.2-1ubuntu1) ...
Setting up libcommons-parent-java (43-1) ...
Setting up dvisvgm (2.13.1-1) ...
Setting up libcommons-logging-java (1.2-2) ...
Setting up xfonts-utils (1:7.7+6build2) ...
Setting up libptexenc1:amd64 (2021.20210626.59705-1ubuntu0.1) ...
Setting up texlive-binaries (2021.20210626.59705-1ubuntu0.1) ...
update-alternatives: using /usr/bin/xdvi-xaw to provide /usr/bin/xdvi.bin
(xdvi.bin) in auto mode
update-alternatives: using /usr/bin/bibtex.original to provide /usr/bin/bibtex
(bibtex) in auto mode
Setting up lmodern (2.004.5-6.1) ...
Setting up texlive-base (2021.20220204-1) ...
/usr/bin/ucfr
/usr/bin/ucfr
/usr/bin/ucfr
/usr/bin/ucfr

```

```

mktexlsr: Updating /var/lib/texmf/ls-R-TEXLIVEDIST...
mktexlsr: Updating /var/lib/texmf/ls-R-TEXMFMAIN...
mktexlsr: Updating /var/lib/texmf/ls-R...
mktexlsr: Done.
tl-paper: setting paper size for dvips to a4:
/var/lib/texmf/dvips/config/config-paper.ps
tl-paper: setting paper size for dvipdfmx to a4:
/var/lib/texmf/dvipdfmx/dvipdfmx-paper.cfg
tl-paper: setting paper size for xdvi to a4: /var/lib/texmf/xdvi/XDvi-paper
tl-paper: setting paper size for pdftex to a4: /var/lib/texmf/tex/generic/tex-
ini-files/pdftexconfig.tex
Setting up tex-gyre (20180621-3.1) ...
Setting up texlive-plain-generic (2021.20220204-1) ...
Setting up texlive-latex-base (2021.20220204-1) ...
Setting up texlive-latex-recommended (2021.20220204-1) ...
Setting up texlive-pictures (2021.20220204-1) ...
Setting up texlive-fonts-recommended (2021.20220204-1) ...
Setting up tipa (2:1.3-21) ...
Setting up texlive (2021.20220204-1) ...
Setting up texlive-latex-extra (2021.20220204-1) ...
Setting up texlive-xetex (2021.20220204-1) ...
Setting up rake (13.0.6-2) ...
Setting up libruby3.0:amd64 (3.0.2-7ubuntu2.4) ...
Setting up ruby3.0 (3.0.2-7ubuntu2.4) ...
Setting up ruby (1:3.0~exp1) ...
Setting up ruby-rubygems (3.3.5-2) ...
Processing triggers for man-db (2.10.2-1) ...
Processing triggers for fontconfig (2.13.1-4.2ubuntu5) ...
Processing triggers for libc-bin (2.35-0ubuntu3.4) ...
/sbin/ldconfig.real: /usr/local/lib/libtbbmalloc.so.2 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbbind_2_5.so.3 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbb.so.12 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbmalloc_proxy.so.2 is not a symbolic
link

/sbin/ldconfig.real: /usr/local/lib/libtbbbind.so.3 is not a symbolic link

/sbin/ldconfig.real: /usr/local/lib/libtbbbind_2_0.so.3 is not a symbolic link

Processing triggers for tex-common (6.17) ...
Running updmap-sys. This may take some time... done.
Running mktexlsr /var/lib/texmf ... done.
Building format(s) --all.
    This may take some time... done.

```

```
[ ]: # TO DO: Provide the full path to your Jupyter notebook file
!jupyter nbconvert --to PDF "/content/drive/MyDrive/Colab Notebooks/HW5/
↪Homework5_USERNAME.ipynb"
```