Naive Solution (Sorting)

- Sort the array and check
  if (arr[i] == arr[i+1])
  arr[i] is the repeated element

T.C → O(nlogn) S.C → O(1)

Optimised Solution. (Frequency map)

- Create a map and store the frequencies of elements of array
- Traverse the map and find the key with value 2
- That key is the repeated element

T.C → O(n) S.C → O(n)

Best Solution (Turtle-hare approach)

(Commonly used to find cycles in a linked list)

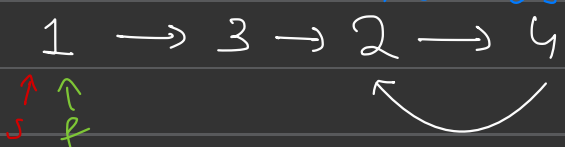
Approach: $a = [1, 3, 4, 2, 2]$ (indices 0, 1, 2, 3, 4)

Initialise 2 pointers slow & fast to a[0]

Suppose ptr is at i, ptr moves to a[i]

For above array, the ptrs follow

Step I: Initialise s = a[0] ; f = a[0]

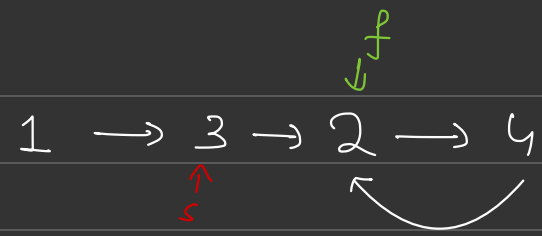


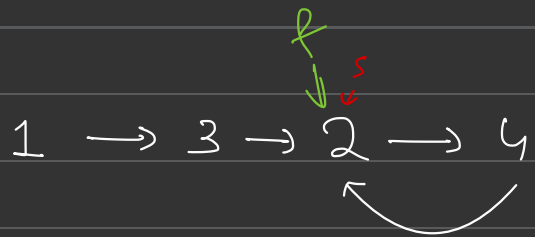
To find the cycle,

Step II: slow pointer travels 1 step (s = a[s])

fast pointer travels 2 steps (f = a[a[f]])

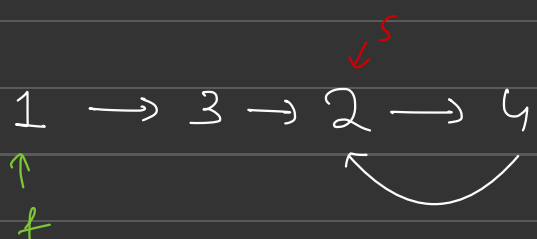
till they meet at a same point

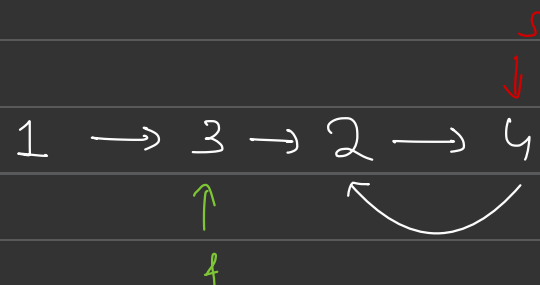


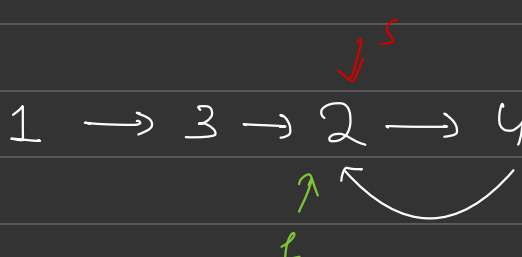


Step III : Take fast ptr to start 1 now both ptrs move 1 step till collision

[s = a[s] , f = a[f]]







∴ 2 is the repeated element

Algorithm

Step I: Initialisation

```
slow = a[0]; fast = a[0];
```

Step II: fast → 2x speed

```
do {
    slow = a[slow];
    fast = a[a[fast]];
} while (slow != fast);
```

Step III: fast → 1x speed.

```
fast = a[0]

while (slow != fast) {
    slow = a[slow];
    fast = a[fast];
}
return slow;
```

T.C → O(n) ; S.C → O(1)