Title :- constructing an optimal Binary search tree using

of n sorted object / Keys, with a search probability Pi for each key ki, Build the Binary search tree that has the least search cost given the acress probability for each key?

objectives: To build a bingry search tree that has the least search cost given the access probability for each keys?

Software Regulement:

Theory: An optimal binary search free is binary search free

For which the nodes are arranged on level such that the

tree cost is minimum for the purpose of a better

presentation of optimal binary search frees, we will consider

"extended binarry search free" which have the keys

Stored at their internal nodes suppose (n' keys k, kg

Kn are Stored at the Internal nodes of a binarry

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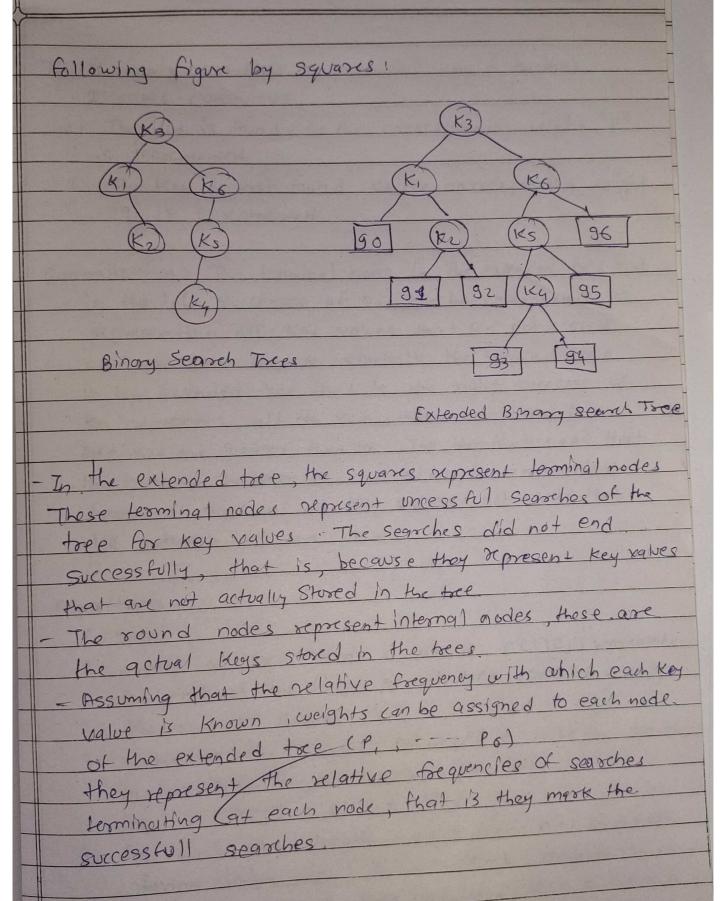
Search tree It is assumed that the keys are given in

Sosted to corder, so that kickie - - ckn

An extended binary tree is obtained from the binary

Search tree by adding successor nodes to each of its

Ferning I nodes as Indiegted in the



- If the use & searbhes a particular key in the tree. 2 cases can occur,
  - 1. The key is found, so the corresponding weight 'p? is Inoxemented.
  - 2. The Key is not found, so the corresponding weight ng' is increamented.

Generalization: The terminal node in the extended fore that is the left successor of k, can be interpreted 93 sepresenting all Key values that are not stored and are less than ke similarly the terminal noide in the extended free that is the right successor of kn sepresents all the key values not stored in the tole that are greater than kn. The terminal node that is success between Ki and Ki-i in an inorder traversal represent all they values not stored that He between Ki and KI-1

## Algorithms ?

- 1. Stort
- 2. create an nxn matrix c, where ccijejj represents the cost of the bingry search tole containing only the Keys Ki through Kj.
- 3. Initialize the diagonal enthies of c to be the search Probabilities for the corresponding Koys,

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4. for each chain length L=1,2, --- n-1 and each sharing index 1=1,2, -- n-L, compute the cost of the binary segret free containing Keys Ki mooigh. KI+L

5. The minimum cost of the binary segret tree
containing all keys is ([1]cn]

6. Stop.

The function of turns the root node of the binory search tree and the minimum cost of the tree. The minimum cost may be minimum cost may be unique, as there may be multiple binary search trees with the same minimum cost.

Conclusion: By using dynamic programming, we can
construct on optimal binary search tree that has the
least search cost given the access probability for
each key. This algorithm has a time complexity
of o(n3) and space complexity o(n2)

