

The Diffie-Hellman algorithm is being used to establish a shared secret that can be used for secret communications while exchanging data over a public network using the elliptic curve to generate points and get the secret key using the parameters.

For the sake of simplicity and practical implementation of the algorithm, we will consider only 4 variables, one prime P and G (a primitive root of P) and two private values a and b.

P and G are both publicly available numbers. Users (say Alice and Bob) pick private values a and b and they generate a key and exchange it publicly. The opposite person receives the key and that generates a secret key, after which they have the same secret key to encrypt.

Step by Step Explanation

Alice Bob

Public Keys available = P,G Public Keys available = P,G Private Key Selected

= a Private Key Selected = b Key generated = Key generated =

$x = G^a \text{ mod } P$ $y = G^b \text{ mod } P$

Exchange of generated keys takes place

Key received = y key received = x

Generated Secret Key = Generated Secret Key =

$k_a = y^a \text{ mod } P$ $k_b = x^b \text{ mod } P$

Algebraically, it can be shown that

$k_a = k_b$

Users now have a symmetric secret key to encrypt

Example:

Step 1: Alice and Bob get public numbers $P = 23$, $G = 9$ Step 2: Alice selected a private key $a = 4$ and

Bob selected a private key $b = 3$

Step 3: Alice and Bob compute public values Alice:

$$x = (9^4 \text{ mod } 23) = (6561 \text{ mod } 23) = 6$$

$$\text{Bob: } y = (9^3 \text{ mod } 23) = (729 \text{ mod } 23) = 16$$

Step 4: Alice and Bob exchange public numbers
Step 5: Alice receives public key $y = 16$ and

Bob receives public key $x = 6$

Step 6: Alice and Bob compute symmetric

keys Alice: $k_a = y^a \bmod p = 65536$

$\bmod 23 = 9$ Bob: $k_b =$

$x^b \bmod p = 216 \bmod 23 = 9$

Step 7: 9 is the shared secret.