

**modal**

## 目录

线段树合并 . . . . .	3
线段树分裂 . . . . .	5
全子序列最小值之和 . . . . .	7

## 线段树合并

```
#include <bits/stdc++.h>
using i64 = long long;
struct data {
    int u, cnt;
    friend bool operator < (data a, data b) {
        return (a.cnt == b.cnt) ? a.u > b.u : a.cnt < b.cnt;
    }
    friend data operator + (data a, data b) {
        return (data){a.u, a.cnt + b.cnt};
    }
};
const int N = 1e5;
void solve() {
    int n, m;
    std::cin >> n >> m;
    std::vector<std::vector<int>> > e(n + 1);
    for (int i = 1; i < n; i++) {
        int u, v;
        std::cin >> u >> v;
        e[u].push_back(v);
        e[v].push_back(u);
    }
    std::vector<std::vector<data>> > on(n + 1);
    int cnt = n; // 已经有 n 个节点
    std::vector<std::array<int, 2>> > c(n * 128 + 1);
    std::vector<data> t(n * 128 + 1);
    auto insert = [&](auto self, int u, int l, int r, data x) -> void {
        if (l == r) { t[u] = x + t[u]; return; }
        int mid = l + r >> 1;
        if (x.u <= mid) self(self, c[u][0] = c[u][0] ? c[u][0] : ++ cnt, l, mid, x);
        else self(self, c[u][1] = c[u][1] ? c[u][1] : ++ cnt, mid + 1, r, x);
        t[u] = std::max(t[c[u][0]], t[c[u][1]]);
    };
    auto merge = [&](auto self, int u1, int u2, int l, int r) -> void {
        if (l == r) { t[u1] = t[u1] + t[u2]; return; }
        int mid = l + r >> 1;
        if (c[u1][0] && c[u2][0]) { self(self, c[u1][0], c[u2][0], l, mid); }
        else if (c[u2][0]) { c[u1][0] = c[u2][0]; }
        if (c[u1][1] && c[u2][1]) { self(self, c[u1][1], c[u2][1], mid + 1, r); }
        else if (c[u2][1]) { c[u1][1] = c[u2][1]; }
        t[u1] = std::max(t[c[u1][0]], t[c[u1][1]]);
    };

    std::vector<std::vector<int>> > fa(19, std::vector<int>(n + 1));
```

```

std::vector<int> dep(n + 1);
auto dfs1 = [&](auto self, int u, int p) -> void {
    fa[0][u] = p;
    dep[u] = dep[p] + 1;
    for (auto v : e[u]) {
        if (v == p) continue;
        self(self, v, u);
    }
};
dfs1(dfs1, 1, 0);
for (int j = 1; j <= 18; j++) {
    for (int i = 1; i <= n; i++) {
        fa[j][i] = fa[j - 1][fa[j - 1][i]];
    }
}
auto lca = [&](int u, int v) -> int {
    if (dep[u] < dep[v]) std::swap(u, v);
    for (int d = dep[u] - dep[v], i = 18; i >= 0; i--) {
        if (d >> i & 1) u = fa[i][u];
    }
    if (u == v) return u;
    for (int i = 18; i >= 0; i--) {
        if (fa[i][u] != fa[i][v]) {
            u = fa[i][u], v = fa[i][v];
        }
    }
    return fa[0][u];
};
for (int i = 1; i <= m; i++) {
    int u, v, w;
    std::cin >> u >> v >> w;
    int o = lca(u, v);
    on[u].push_back((data){w, 1});
    on[v].push_back((data){w, 1});
    on[o].push_back((data){w, -1});
    on[fa[0][o]].push_back((data){w, -1});
}
std::vector<int> ans(n + 1);
auto dfs2 = [&](auto self, int u) -> void {
    for (auto v : e[u]) {
        if (v == fa[0][u]) continue;
        self(self, v);
        merge(merge, u, v, 0, N);
    }
    for (auto it : on[u]) {
        insert(insert, u, 0, N, it);
    }
}

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        ans[u] = t[u].u;
    };
    dfs2(dfs2, 1);
    for (int i = 1; i <= n; i++) {
        std::cout << ans[i] << '\n';
    }
}

int main() {
    std::ios::sync_with_stdio(false);
    std::cin.tie(nullptr);
    int t = 1;
    //std::cin >> t;
    while (t--) {
        solve();
    }
}

```

## 线段树分裂

```

#include <bits/stdc++.h>
#define ll long long
using namespace std;
const int MAXN=200010;
int n,m,tot,cnt,seq=1,op,x,y,z,bac[MAXN<<5],ch[MAXN<<5][2],rt[MAXN];
ll val[MAXN<<5];
int newnod () {return (cnt?bac[cnt--]:++tot);}
void del (int p) {
    bac[++cnt]=p,ch[p][0]=ch[p][1]=val[p]=0;
    return;
}
void modify (int &p,int l,int r,int pos,int v) {
    if (!p) {p=newnod();}
    val[p]+=v;
    if (l==r) {return;}
    int mid=(l+r)>>1;
    if (pos<=mid) {modify(ch[p][0],l,mid,pos,v);}
    else {modify(ch[p][1],mid+1,r,pos,v);}
    return;
}
ll query (int p,int l,int r,int xl,int xr) {
    if (xr<l||r<xl) {return 0;}
    if (xl<=l&&r<=xr) {return val[p];}
    int mid=(l+r)>>1;
    return query(ch[p][0],l,mid,xl,xr)+query(ch[p][1],mid+1,r,xl,xr);
}

```

```

int kth (int p,int l,int r,int k) {
    if (l==r) {return l;}
    int mid=(l+r)>>1;
    if (val[ch[p][0]]>=k) {return kth(ch[p][0],l,mid,k);}
    else {return kth(ch[p][1],mid+1,r,k-val[ch[p][0]]);}
}

int merge (int x,int y) {
    if (!x||!y) {return x+y;}
    val[x]+=val[y];
    ch[x][0]=merge(ch[x][0],ch[y][0]);
    ch[x][1]=merge(ch[x][1],ch[y][1]);
    del(y);
    return x;
}

void split (int x,int &y,ll k) { // 分裂出 x 为原 x 的前 k 个
    if (x==0) {return;}
    y=newnod();
    ll v=val[ch[x][0]];
    if (k>v) {split(ch[x][1],ch[y][1],k-v);}
    else {swap(ch[x][1],ch[y][1]);}
    if (k<v) {split(ch[x][0],ch[y][0],k);}
    val[y]=val[x]-k;
    val[x]=k;
    return;
}

int main () {
    scanf("%d%d",&n,&m);
    for (int i=1;i<=n;i++) {
        scanf("%d",&x);
        modify(rt[1],1,n,i,x);
    }
    for (int i=1;i<=m;i++) {
        scanf("%d",&op);
        if (op==0) {
            scanf("%d%d%d",&x,&y,&z);
            ll k1=query(rt[x],1,n,1,z),k2=query(rt[x],1,n,y,z);
            int tmp=0;
            split(rt[x],rt[++seq],k1-k2);
            split(rt[seq],tmp,k2);
            rt[x]=merge(rt[x],tmp);
        } else if (op==1) {
            scanf("%d%d",&x,&y);
            rt[x]=merge(rt[x],rt[y]);
        } else if (op==2) {
            scanf("%d%d%d",&x,&y,&z);
            modify(rt[x],1,n,z,y);
        } else if (op==3) {

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        scanf("%d%d%d",&x,&y,&z);
        printf("%lld\n",query(rt[x],1,n,y,z));
    } else if (op==4) {
        scanf("%d",&x,&y);
        if (val[rt[x]]<y) {printf("-1\n");continue;}
        printf("%d\n",kth(rt[x],1,n,y));
    }
}
return 0;
}

```

## 全子序列最小值之和

```

#include <bits/stdc++.h>
using i64 = long long;
const int inf = 1e9 + 7;
void solve() {
    int n, m;
    std::cin >> n >> m;
    std::vector<int> a(n + 2, inf);
    std::vector<std::vector<int>> > f(17, std::vector<int>(n + 1));
    for (int i = 1; i <= n; i++) {
        std::cin >> a[i];
        f[0][i] = i;
    }
    auto cmp = [&](int x, int y) -> int {
        return a[x] > a[y] ? y : x;
    };
    for (int j = 1; j <= std::__lg(n); j++) {
        for (int i = 1; i <= n; i++) {
            if (i + (1 << j) - 1 > n) break;
            f[j][i] = cmp(f[j - 1][i], f[j - 1][i + (1 << j - 1)]);
        }
    }
    auto rmq = [&](int l, int r) -> int {
        int x = std::__lg(r - l + 1);
        return cmp(f[x][l], f[x][r - (1 << x) + 1]);
    };

    std::vector<int> st, pre(n + 2), suf(n + 2);
    st.push_back(0);
    for (int i = 1; i <= n; i++) {
        while (st.size() > 1 && a[st.back()] > a[i]) {
            suf[st.back()] = i;
            st.pop_back();
        }
    }
}

```

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    }
    pre[i] = st.back();
    st.push_back(i);
}
while (st.size() > 1) {
    int u = st.back();
    st.pop_back();
    pre[u] = st.back();
    if (st.size() > 1) suf[st.back()] = n + 1;
}
std::vector<i64> fr(n + 2), fl(n + 2), gr(n + 2), gl(n + 2);
for (int i = 1; i <= n; i++) {
    fr[i] = fr[pre[i]] + 1ll * a[i] * (i - pre[i]);
    gr[i] = gr[i - 1] + fr[i];
}
for (int i = n; i >= 1; i--) {
    fl[i] = fl[suf[i]] + 1ll * a[i] * (suf[i] - i);
    gl[i] = gl[i + 1] + fl[i];
}
for (int i = 1; i <= m; i++) {
    int l, r;
    std::cin >> l >> r;
    int p = rmq(l, r);
    i64 ans = 1ll * a[p] * (p - l + 1) * (r - p + 1) +
        gr[r] - gr[p] - fr[p] * (r - p) +
        gl[l] - gl[p] - fl[p] * (p - l);
    std::cout << ans << '\n';
}
}
int main() {
    std::ios::sync_with_stdio(false);
    std::cin.tie(nullptr);
    int t = 1;
    //std::cin >> t;
    while (t--) {
        solve();
    }
}

```