modal

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bitset

```
#include <bits/stdc++.h>
using i64 = long long;
const int N = 1030;
//std::bitset<10000> s;
//std::bitset<1000005> f[110];
std::bitset<N> f[2][N];
int main() {
  std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  std::bitset<4> s(std::string("1001"));//填充字符串
  //std::cout << s << '\n';
  int t = 5;
  std::bitset<10> k(t); //不足补零
  //std::cout << k << "\n";
  //std::bitset<1000>f[100]; //支持多维, 代表有100个长度为1000的01串(默认为0)
  //s.count() 返回有多少个1
  //s.any() 至少有一个1返回true, 反之false
  //s.none() 全为0返回true, 反之false
  //s.set() 将每位全部赋值为1
  //s.set(u, v) 将第u位赋值为v, v只能取值0或者1
  //s.reset() 将每位全部赋值为0
  //s.reset(k) 将第k位赋值为0
  //example: 有n个数, x可以取值li-ri, 问sumXi可能的值有多少。(背包问题)
  // f[i] = f[i - 1] << (x * x)
  int n;
  int 1[110], r[110];
  std::cin >> n;
  for (int i = 1; i <= n; i ++) {
    std::cin >> 1[i] >> r[i];
  }
  f[0].set(0);
  for (int i = 1; i <= n; i ++) {
    for (int j = 1[i]; j <= r[i]; j ++) {
      f[i] \mid = (f[i - 1] \iff (j * j));
    }
  }
  std::cout << f[n].count() << "\n";
```

```
//example2: 优化DP时空复杂度;
      n个数,背包容量m,问装满背包时候,背包里面异或值最大可能是多少?
  //朴素方程 f[i][j][k] 前i个数,异或值为j,体积为k的方案是否存在 , 滚动只能优化掉 一维 i,
  int T;
  std::cin >> T;
  while (T --) {
    int n, m;
     std::cin >> n >> m;
     for (int i = 0; i < 1024; i ++) f[0][i] = f[1][i] = 0;</pre>
    f[0][0][0] = 1;
    for (int i = 1, x = 1; i <= n; i ++, x ^= 1) {</pre>
       int v, w;
       std::cin >> v >> w;
       for (int j = 0; j < 1024; j ++) {</pre>
         f[x][j] = f[x ^ 1][j ^ w] << v | f[x ^ 1][j];
       }
    }
    int ok = -1;
    for (int i = 0; i < 1024; i ++)</pre>
    if (f[n & 1][i][m]) ok = i;
    std::cout << ok << "\n";
  }
  return 0;
}
```

最大流

```
e[etot] = {u, head[v], 0}; head[v] = etot ++;
}
bool bfs() {
  for (int i = 1; i <= vtot; i ++) {</pre>
     dis[i] = 0;
     cur[i] = head[i];
  }
  std::queue<int> q;
  q.push(s); dis[s] = 1;
  while (! q.empty()) {
     int u = q.front(); q.pop();
     for (int i = head[u]; ~i; i = e[i].nxt) {
       if (e[i].f && ! dis[e[i].v]) {
          int v = e[i].v;
          dis[v] = dis[u] + 1;
          if (v == t) return true;
          q.push(v);
       }
     }
  }
  return false;
}
T dfs(int u, T m) {
  if (u == t) return m;
  T flow = 0;
  for (int i = cur[u]; ~i; cur[u] = i = e[i].nxt) {
     if (e[i].f && dis[e[i].v] == dis[u] + 1) {
       T f = dfs(e[i].v, std::min(m, e[i].f));
       e[i].f -= f;
       e[i ^ 1].f += f;
       m -= f;
       flow += f;
       if (! m) break;
     }
  }
  if (! flow) dis[u] = -1;
  return flow;
T dicnic() {
  T flow = 0;
  while (bfs()) {
     flow += dfs(s, std::numeric_limits<T>::max());
  return flow;
```

```
void init(int _s, int _t, int _vtot) {
     s = _s;
    t = _t;
     vtot = _vtot;
    for (int i = 1; i <= vtot; i ++) {</pre>
       head[i] = -1;
     }
  }
};
void solve() {
  int n, m, s, t;
  std::cin >> n >> m >> s >> t;
  FlowGraph<i64> g;
  g.init(s, t, n);
  for (int i = 1; i <= m; i ++) {</pre>
     int u, v, w;
    std::cin >> u >> v >> w;
     g.addedge(u, v, w);
  }
  std::cout << g.dicnic() << '\n';</pre>
}
int main(){
  std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  int t = 1;
  //std::cin >> t;
  while (t --) {
     solve();
  }
  return 0;
}
```

最流费用流

```
#include<bits/stdc++.h>
using i64 = long long;
//最小费用最大流 - 最大费用最大流
// MCMF: minimum cost maximum flow

const int V = 2010;
const int E = 20100;
template<typename T>
```

```
struct MinCostGraph {
  int s, t, vtot, etot, cur[V], head[V], pre[V];
  T dis[V], flow, cost;
  bool vis[V];
  struct edge {
     int v, nxt;
     T f, c;
  } e[E * 2];
  void addedge(int u, int v, T f, T c, T f2 = 0) {
     e[etot] = {v, head[u], f, c}; head[u] = etot ++;
     e[etot] = \{u, head[v], f2, -c\}; head[v] = etot ++;
  bool spfa() {
     T inf = std::numeric_limits<T>::max() / 2;
     for (int i = 1; i <= vtot; i ++) {</pre>
       dis[i] = inf;
       vis[i] = false;
       pre[i] = -1;
     }
     dis[s] = 0, vis[s] = true;
     std::queue<int> q; q.push(s);
     while (! q.empty()) {
       int u = q.front();
       for (int i = head[u]; ~i; i = e[i].nxt) {
          int v = e[i].v;
          if (e[i].f && dis[v] > dis[u] + e[i].c) {
             dis[v] = dis[u] + e[i].c;
             pre[v] = i;
             if (! vis[v]) {
               vis[v] = 1;
               q.push(v);
             }
          }
       }
        q.pop();
        vis[u] = false;
     }
     return dis[t] != inf;
  void augment() {
     int u = t;
     T f = std::numeric_limits<T>::max();
     while (~ pre[u]) {
       f = std::min(f, e[pre[u]].f);
       u = e[pre[u] ^ 1].v;
```

```
flow += f;
     cost += f * dis[t];
     u = t;
     while (~ pre[u]) {
       e[pre[u]].f -= f;
       e[pre[u] ^ 1].f += f;
       u = e[pre[u] ^ 1].v;
     }
  }
  std::array<T, 2> solve() {
    flow = 0;
    cost = 0;
    while (spfa()) augment();
    return {flow, cost};
  }
  void init(int _s, int _t, int _vtot) {
     s = _s;
    t = _t;
     vtot = _vtot;
     etot = 0;
     for (int i = 1; i <= vtot; i ++) {</pre>
       head[i] = -1;
     }
  }
};
void solve() {
  int n, m, s, t;
  std::cin >> n >> m >> s >> t;
  MinCostGraph<int> g;
  g.init(s, t, n);
  for (int i = 1; i <= m; i ++) {</pre>
     int u, v, f, c;
     std::cin >> u >> v >> f >> c;
     g.addedge(u, v, f, c);
  auto it = g.solve();
  std::cout << it[0] << ' ' << it[1] << '\n';
int main() {
  std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  int t = 1;
  //std::cin >> t;
```

```
while (t --) {
    solve();
}
return 0;
}
```

Fenwick

```
struct Fenwick {
  int n;
  std::vector<int> a;
  Fenwick(int n = 0) {
    init(n);
  void init(int n) {
    this \rightarrow n = n;
    a.resize(n + 1);
    a.assign(n + 1, 0);
  void add(int x, int v) {
    for (; x <= n; x += x & -x) {</pre>
       a[x] += v;
     }
  void add(int x, int y, int v) {
    add(x, v), add(y + 1, -v);
  int sum(int x) {
    int ans = 0;
    for (; x; x -= x & -x) {
       ans += a[x];
    }
    return ans;
  }
  int rangeSum(int 1, int r) {
    return sum(r) - sum(l - 1);
  int kth(int k) { // kth value
    int ans = 0;
    for (int i = std::__lg(n); i >= 0; i--) {
       int val = ans + (1 << i);</pre>
       if (val < n && a[val] < k) {</pre>
          k -= a[val];
          ans = val;
```

```
}
    return ans + 1;
}
```

线段树 tag

```
struct SegmentTree {
  int n;
  struct node {
     int 1, r, x;
     int sum, add, max;
  };
  std::vector<node> t;
  std::vector<int> a;
  SegmentTree() {}
  void init(int n) {
     this \rightarrow n = n;
     t.assign(4 * n + 1, (node){0, 0, 0, 0, 0, 0});
     a.assign(n + 1, 0);
     build(1, 1, n);
  void init(int n, std::vector<int> v) {
     this \rightarrow n = n;
     t.assign(4 * n + 1, (node){0, 0, 0, 0, 0, 0});
     a.assign(v.begin(), v.end());
     build(1, 1, n);
  }
  void pushup(int u) {
     t[u].sum = t[u << 1].sum + t[u << 1 | 1].sum;
     t[u].max = std::max(t[u << 1].max, t[u << 1 | 1].max);
  void pushdown(int u) {
     if (! t[u].add) return ;
     t[u << 1].sum += (t[u << 1].r - t[u << 1].l + 1) * t[u].add;
     t[u \ll 1 \mid 1].sum += (t[u \ll 1 \mid 1].r - t[u \ll 1 \mid 1].1 + 1) * t[u].add;
     t[u << 1].add += t[u].add, t[u << 1 | 1].add += t[u].add;
     t[u << 1].max += t[u].add, t[u << 1 | 1].max += t[u].add;
     t[u].add = 0;
  void build(int u, int l, int r) {
     t[u] = \{1, r, 0, 0, 0, 0\};
     if (1 == r) {
        t[u] = {1, r, a[1], a[1], 0, a[1]};
```

```
return ;
  }
  int mid = 1 + r >> 1;
  build(u << 1, 1, mid);</pre>
  build(u << 1 | 1, mid + 1, r);
  pushup(u);
}
void add(int u, int 1, int r, int val) {
   if (t[u].1 >= 1 && t[u].r <= r) {</pre>
     t[u].sum += (t[u].r - t[u].l + 1) * val;
     t[u].max += val;
     t[u].add += val;
     return ;
  }
  pushdown(u);
  int mid = t[u].1 + t[u].r >> 1;
  if (1 <= mid) add(u << 1, 1, r, val);</pre>
  if (mid < r) add(u << 1 | 1, 1, r, val);</pre>
  pushup(u);
int query(int u, int 1, int r) {
   if (t[u].1 >= 1 && t[u].r <= r) {</pre>
     return t[u].sum;
  pushdown(u);
  int res = 0;
  int mid = t[u].1 + t[u].r >> 1;
  if (1 <= mid) res += query(u << 1, 1, r);</pre>
  if (mid < r) res += query(u << 1 | 1, 1, r);</pre>
  return res;
int query_max(int u, int 1, int r) {
  if (t[u].1 >= 1 && t[u].r <= r) {</pre>
     return t[u].max;
  }
  pushdown(u);
  int res = -1e9;
  int mid = t[u].l + t[u].r >> 1;
  if (1 <= mid) res = std::max(res, query_max(u << 1, 1, r));</pre>
  if (mid < r) res = std::max(res, query_max(u << 1 | 1, 1, r));</pre>
  return res;
void add(int 1, int r, int val) {
  add(1, 1, r, val);
int query(int 1, int r) {
 return query(1, 1, r);
```

```
}
int Max(int 1, int r) {
    return query_max(1, 1, r);
}
```

分块

```
void resort(int x,int n){
   v[x].clear();
  for(int i=(x-1)*b+1;i<=min(x*b,n);i++)v[x].push_back(a[i]);</pre>
   sort(v[x].begin(),v[x].end());
}
void change2(int 1,int r,int c,int n){
   int p=blo[1],q=blo[r];
  for(int i=1;i<=min(r,p*b);i++)a[i]+=c;</pre>
  resort(p,n);
  if(p==q)return ;
  for(int i=(q-1)*b+1;i<=r;i++)a[i]+=c;</pre>
  resort(q,n);
  for(int i=p+1;i<q;i++)add[i]+=c;</pre>
}
void ask2(int 1,int r,int c){
   int res=-1,p=blo[1],q=blo[r];
   for(int i=1;i<=min(r,p*b);i++)</pre>
   if(a[i]+add[p]<c)res=max(res,a[i]+add[p]);</pre>
   if(p==q){cout<<res<<end1;return ;}</pre>
   for(int i=(q-1)*b+1;i<=r;i++)</pre>
   if(a[i]+add[q]<c)res=max(res,a[i]+add[q]);</pre>
  for(int i=p+1;i<q;i++){</pre>
     int pos=lower_bound(v[i].begin(),v[i].end(),c-add[i])-v[i].begin();
     if(pos&&v[i][pos-1]+add[i]<c)res=max(res,v[i][pos-1]+add[i]);</pre>
   }
   cout<<res<<endl;</pre>
}
void Sblk2(){
   int n,op,l,r,c; cin>>n; b=sqrt(n);
   for(int i=1;i<=n;i++){</pre>
      cin > a[i]; blo[i] = (i-1)/b+1;
     v[blo[i]].push_back(a[i]);
   for(int i=1;i<=blo[n];i++)sort(v[i].begin(),v[i].end());</pre>
  for(int i=1;i<=n;i++){</pre>
     cin>>op>>l>>r>>c;
     if(!op)change2(1,r,c,n);
```

```
else ask2(l,r,c);
}
```

area 扫描线

```
#include <bits/stdc++.h>
using i64 = long long;
#define int i64
struct SegmentTree {
  int n;
  struct node {
    int 1, r, len;
    int sum, add, max; // x = len, sum = times, add = delt
  };
  // 考虑改变线段树存值的方式, 因为 a[3] - a[1] -->
  //
  std::vector<node> t;
  std::vector<int> a;
  SegmentTree() {}
  void init(int n) {
    this \rightarrow n = n;
    t.assign(4 * n + 1, (node){0, 0, 0, 0, 0, 0});
    a.assign(n + 1, 0);
    build(1, 1, n);
  void init(int n, std::vector<int> v) {
    this \rightarrow n = n;
    t.assign(4 * n + 1, (node){0, 0, 0, 0, 0, 0});
    a.assign(v.begin(), v.end());
    build(1, 1, n);
  void pushup(int u) { // ub大集合!
    if (t[u].sum) {
       t[u].len = a[t[u].r] - a[t[u].1 - 1];
    } else {
       if (t[u].1 != t[u].r)
       t[u].len = t[u << 1].len + t[u << 1 | 1].len;
       else t[u].len = 0;
    }
  void build(int u, int 1, int r) {
    t[u] = \{1, r, 0, 0, 0, 0\};
    if (1 == r) {
```

```
return ;
     }
     int mid = 1 + r >> 1;
     build(u << 1, 1, mid);</pre>
     build(u << 1 | 1, mid + 1, r);
  void add(int u, int l, int r, int val) {
     if (t[u].1 >= 1 && t[u].r <= r) {</pre>
        t[u].sum += val;
        pushup(u);
        return ;
     }
     int mid = t[u].1 + t[u].r >> 1;
     if (1 <= mid) add(u << 1, 1, r, val);</pre>
     if (mid < r) add(u << 1 | 1, 1, r, val);</pre>
     pushup(u);
  }
  void add(int 1, int r, int val) {
     add(1, 1, r, val);
  }
};
signed main() {
   std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  // 扫描线.
  int n;
  std::cin >> n;
  std::vector<int> X;
  std::vector<std::array<int, 4> > e(n * 2);
  for (int i = 0; i < n; i ++) {</pre>
     int x1, y1, x2, y2;
     std::cin >> x1 >> y1 >> x2 >> y2;
     X.push_back(x1);
     X.push_back(x2);
     e[i * 2] = \{x1, x2, y1, 1\};
     e[i * 2 + 1] = \{x1, x2, y2, -1\};
  }
  std::sort(X.begin(), X.end());
  X.erase(std::unique(X.begin(), X.end()), X.end());
  int m = X.size();
  std::vector<int> a(m);
  for (int i = 1; i < m; i ++) {</pre>
     a[i] = X[i] - X[i - 1];
  }
  m --;
  for (int i = 1; i <= m; i ++) {</pre>
```

```
a[i] += a[i - 1];
}
std::sort(e.begin(), e.end(), [&](auto a, auto b) {
    return a[2] < b[2];
});

SegmentTree t;
t.init(m, a);
int ans = 0;
for (int i = 0; i < 2 * n; i ++) {
    int 1 = std::lower_bound(X.begin(), X.end(), e[i][0]) - X.begin() + 1;
    int r = std::lower_bound(X.begin(), X.end(), e[i][1]) - X.begin() + 1;
    t.add(1, r - 1, e[i][3]);
    if (i + 1 < 2 * n) ans += t.t[1].len * (e[i + 1][2] - e[i][2]);
}
std::cout << ans << '\n';
return 0;
}</pre>
```

DSU

```
struct DSU {
  std::vector<int> f, siz;
  DSU() {}
  DSU(int n) {
     init(n);
  }
  void init(int n) {
    f.resize(n + 1);
     std::iota(f.begin(), f.end(), 0);
     siz.assign(n + 1, 1);
  }
  int find(int x) {
     while (x != f[x]) {
       x = f[x] = f[f[x]];
     }
    return x;
  }
  bool same(int x, int y) {
    return find(x) == find(y);
```

```
bool merge(int x, int y) {
    x = find(x);
    y = find(y);
    if (x == y) {
        return false;
    }
    siz[x] += siz[y];
    f[y] = x;
    return true;
}

int size(int x) {
    return siz[find(x)];
    }
};
```

HLD

```
#include<bits/stdc++.h>
using i64 = long long;
const int N = 1e5 + 10, M = 2e5 + 10;
int a[N];
int tot, head[M], nxt[M], to[M];
void addedge(int u, int v) {
  nxt[++ tot] = head[u];
 head[u] = tot;
  to[tot] = v;
}
int lowbit(int x) {return x & (- x);}
struct Fenwick {
  int n;
  i64 t1[N], t2[N];
  void add(int x, i64 val) {
    for (int i = x; i <= n; i += lowbit(i)) {</pre>
       t1[i] = t1[i] + val, t2[i] = t2[i] + val * x;
     }
  i64 sum(int x) {
     i64 ans = 0;
    for (int i = x; i; i -= lowbit(i)) {
       ans = ans + (x + 1) * t1[i] - t2[i];
     }
```

```
return ans;
  }
  void update(int 1, int r, i64 val) {
     add(1, val), add(r + 1, -val);
  i64 query(int 1, int r) {
    return sum(r) - sum(l - 1);
  }
} arr;
struct TreeList {
  int cnt = 0;
  int dep[N], top[N], son[N], siz[N], fa[N], dfn[N];
  void dfs1(int cur) {
     dep[cur] = dep[fa[cur]] + (siz[cur] = 1);
     for (int i = head[cur]; i; i = nxt[i]) {
        if (to[i] == fa[cur]) continue;
       fa[to[i]] = cur;
       dfs1(to[i]);
       siz[cur] += siz[to[i]];
       if (! son[cur] || siz[son[cur]] < siz[to[i]]) {</pre>
          son[cur] = to[i];
       }
     }
  }
  void dfs2(int cur, int t) {
     dfn[cur] = ++ cnt;
     top[cur] = t;
     if (son[cur]) {
       dfs2(son[cur], t);
     for (int i = head[cur]; i; i = nxt[i]) {
       if (to[i] != fa[cur] && to[i] != son[cur]) {
          dfs2(to[i], to[i]);
       }
     }
  }
  void update(int x, int y, i64 v) {
     while (top[x] != top[y]) {
        if (dep[top[x]] < dep[top[y]]) std::swap(x, y);</pre>
        arr.update(dfn[top[x]], dfn[x], v);
       x = fa[top[x]];
     if (dfn[x] > dfn[y]) std::swap(x, y);
     arr.update(dfn[x], dfn[y], v);
```

```
i64 query(int x, int y) {
     i64 ans = 0;
     while (top[x] != top[y]) {
        if (dep[top[x]] < dep[top[y]]) std::swap(x, y);</pre>
        ans += arr.query(dfn[top[x]], dfn[x]);
        x = fa[top[x]];
     }
     if (dfn[x] > dfn[y]) std::swap(x, y);
     return ans + arr.query(dfn[x], dfn[y]);
  void update_subtree(int x, i64 v) {
     arr.update(dfn[x], dfn[x] + siz[x] - 1, v);
  i64 query_subtree(int x) {
     return arr.query(dfn[x], dfn[x] + siz[x] - 1);
  }
} tr;
void solve() {
  int n, m, r, p;
  std::cin >> n >> m >> r >> p;
  for (int i = 1; i <= n; i ++) {</pre>
     std::cin >> a[i];
  }
  for (int i = 1; i < n; i ++) {</pre>
     int u, v;
    std::cin >> u >> v;
    addedge(u, v);
     addedge(v, u);
  }
  11
  tr.dfs1(r);
  tr.dfs2(r, r);
  arr.n = n;
  for (int i = 1; i <= n; i ++) {</pre>
     tr.update(i, i, a[i]);
  while (m --) {
     int s, x, y, v;
     std::cin >> s >> x;
     if (s == 1) {
        std::cin >> y >> v;
       tr.update(x, y, v);
     } else if (s == 2) {
        std::cin >> y;
```

```
std::cout << (tr.query(x, y) \% p) << '\n';
     } else if (s == 3) {
       std::cin >> v;
        tr.update_subtree(x, v);
     } else if (s == 4) {
        std::cout << (tr.query_subtree(x) \% p) << '\n';
     }
  }
}
int main(){
  std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  int t = 1;
  //std::cin >> t;
  while (t --) {
     solve();
  }
  return 0;
}
```

LCA

```
struct LCA { // 倍增
  int n, rt = 1, deep[N], ff[16][N];
  std::vector<int> e[N];
  LCA(int n) : n(n) {}
  void dfs(int u, int p) {
    ff[0][u] = p;
    for (auto v : e[u]) {
       if (v == p) continue;
       deep[v] = deep[u] + 1;
       dfs(v, u);
     }
  void work() {
     dfs(rt, 0);
    for (int i = 1; i <= 15; i ++) {</pre>
       for (int j = 1; j <= n; j ++) {</pre>
          ff[i][j] = ff[i - 1][ff[i - 1][j]];
       }
    }
  int lca(int u, int v) {
     if (deep[u] < deep[v]) std::swap(u, v);</pre>
     for (int i = 15; i >= 0; i --) {
```

```
if (deep[u] - deep[v] >= (1 << i)) {
        u = ff[i][u];
    }

if (u == v) {
    return u;
}

for (int i = 15; i >= 0; i --) {
    if (ff[i][u] != ff[i][v]) {
        u = ff[i][u], v = ff[i][v];
    }
}

u = ff[0][u];

return u;
}
```

虚树

```
struct Xushu {
  int n, rt = 1, dn, res = 0, num = 0;
  int ff[20][N];
  struct node {
     int to, nxt;
  };
  std::vector<std::vector<int> > H;
  std::vector<int> dp, col, dfn, h;
  std::vector<node> e;
  Xushu(int n, std::vector<int> a) {
    H.assign(n + 1, {});
    this \rightarrow n = n;
    h.assign(n + 1, 0);
     col.assign(a.begin(), a.end());
     dp.assign(n + 1, 0);
     dfn.assign(n + 1, 0);
     e.assign(2 * (n + 1), (node){0, 0});
  void addEdge(int a, int b) {
     e[++ num] = {b, h[a]}; h[a] = num;
     e[++ num] = {a, h[b]}; h[b] = num;
  }
  void dfs(int u, int p) {
     ff[0][dfn[u] = ++ dn] = p;
```

```
for (int i = h[u]; i; i = e[i].nxt) {
     if (e[i].to == p) continue;
     dfs(e[i].to, u);
  }
}
int get(int x, int y) {
  if (dfn[x] < dfn[y]) return x;</pre>
  else return y;
void work() {
  dfs(rt, 0);
  for (int i = 1; i <= std::__lg(n); i ++) { //RMQ deep less</pre>
     for (int j = 1; j + (1 << i) - 1 <= n; j ++) {
        ff[i][j] = get(ff[i - 1][j], ff[i - 1][j + (1 << i - 1)]);
     }
  }
}
int lca(int u, int v) {
  if (u == v) {
     return u;
  if ((u = dfn[u]) > (v = dfn[v])) std::swap(u, v);
  int d = std::__lg(v - u);
  return get(ff[d][++ u], ff[d][v - (1 << d) + 1]);</pre>
void build(std::vector<int> a) {
  //H.assign(n + 1, {});
  int nn = a.size();
  std::sort(a.begin(), a.end(), [&](int x, int y) {
     return dfn[x] < dfn[y];</pre>
  });
  for (int i = 0; i + 1 < nn; i ++) {</pre>
     a.push_back(lca(a[i], a[i + 1]));
  a.push_back(1);
  std::sort(a.begin(), a.end(), [&](int x, int y) {
     return dfn[x] < dfn[y];</pre>
  });
  a.erase(std::unique(a.begin(), a.end()), a.end());
  int o = a.size();
  for (int i = 0; i + 1 < 0; i ++) {</pre>
     H[lca(a[i], a[i + 1])].push_back(a[i + 1]);
  }
```

```
void DFS(int u, int color) {
     int r = 1, sum = 1;
     for (auto v : H[u]) {
       DFS(v, color);
       r = r * (dp[v] + 1) \% mod;
       sum = (sum + dp[v]) \% mod;
    res = (res + r) \% mod;
     if (col[u] != color) {
       r --;
       res = (res - sum + mod) % mod;
     dp[u] = r;
     //std::cout << dp[u] << '\n';
  void solve(int cl) {
     DFS(1, cl);
     auto CLEAR = [&](auto self, int u) -> void {
       for (auto v : H[u]) self(self, v);
       H[u].clear();
    };
     CLEAR(CLEAR, 1);
  }
};
```

强连通分量 SCC

```
struct SCC {
   int n;
   std::vector<std::vector<int>> adj;
   std::vector<int> stk;
   std::vector<int> dfn, low, bel;
   int cur, cnt;

SCC() {}
SCC(int n) {
    init(n);
}

void init(int n) {
   this->n = n;
   adj.assign(n + 1, {});
   dfn.assign(n + 1, -1);
```

```
low.resize(n + 1);
     bel.assign(n + 1, -1);
     stk.clear();
     cur = cnt = 0;
  }
  void addEdge(int u, int v) {
     adj[u].push_back(v);
  }
  void dfs(int x) {
     dfn[x] = low[x] = ++ cur;
     stk.push_back(x);
     for (auto y : adj[x]) {
       if (dfn[y] == -1) {
          dfs(y);
          low[x] = std::min(low[x], low[y]);
       } else if (bel[y] == -1) {
          low[x] = std::min(low[x], dfn[y]);
       }
     }
     if (dfn[x] == low[x]) {
       int y;
       do {
         y = stk.back();
         bel[y] = cnt;
         stk.pop_back();
       } while (y != x);
       cnt ++;
     }
  }
  std::vector<int> work() {
     for (int i = 1; i <= n; i ++) {</pre>
       if (dfn[i] == -1) {
          dfs(i);
       }
     }
    return bel;
  }
};
```

SCC 缩点

```
struct SCC {
  int n;
  std::vector<std::vector<int>> adj;
  std::vector<int> stk;
  std::vector<int> dfn, low, bel;
  int cur, cnt;
  SCC() {}
  SCC(int n) {
     init(n);
  }
  void init(int n) {
     this \rightarrow n = n;
     adj.assign(n + 1, {});
    dfn.assign(n + 1, -1);
    low.resize(n + 1);
     bel.assign(n + 1, -1);
     stk.clear();
     cur = cnt = 0;
  void addEdge(int u, int v) {
     adj[u].push_back(v);
  }
  void dfs(int x) {
     dfn[x] = low[x] = ++ cur;
     stk.push_back(x);
     for (auto y : adj[x]) {
       if (dfn[y] == -1) {
          dfs(y);
          low[x] = std::min(low[x], low[y]);
       } else if (bel[y] == -1) {
          low[x] = std::min(low[x], dfn[y]);
       }
     if (dfn[x] == low[x]) {
        int y;
       do {
          y = stk.back();
          bel[y] = cnt;
```

```
stk.pop_back();
} while (y != x);
cnt ++;
}

std::vector<int> work() {
  for (int i = 1; i <= n; i ++) {
     if (dfn[i] == -1) {
       dfs(i);
     }
  }
  return bel;
}</pre>
```

无向图割点

```
struct GeDian {
  int n, root;
  std::vector<std::vector<int>> adj;
  std::vector<int> dfn, low;
  std::vector<bool> bel;
  int cur;
  GeDian() {}
  GeDian(int n) {
     init(n);
  void init(int n) {
    this \rightarrow n = n;
    adj.assign(n + 1, {});
    dfn.assign(n + 1, -1);
    low.resize(n + 1);
     bel.assign(n + 1, 0);
     cur = 0;
  }
  void addEdge(int u, int v) {
     adj[u].push_back(v);
     adj[v].push_back(u);
  }
  void dfs(int x) {
```

```
dfn[x] = low[x] = ++ cur;
     int ch = 0;
     for (auto y : adj[x]) {
       if (dfn[y] == -1) {
          ch ++;
          dfs(y);
          low[x] = std::min(low[x], low[y]);
          if (x != root && low[y] >= dfn[x] ) {
            bel[x] = 1;
          }
       } else {
          low[x] = std::min(low[x], dfn[y]);
       }
     }
     if (x == root && ch >= 2) {
       bel[x] = 1;
    }
  }
  std::vector<bool> work() {
    for (int i = 1; i <= n; i ++) {</pre>
       if (dfn[i] == -1) {
         root = i;
          dfs(i);
       }
     }
    return bel;
  }
};
```

二分图

```
struct BipartGraph {
  int n, cnt, ans, nx, ny;
  std::vector<std::vector<int>> adj;
  std::vector<int> col;
  //------
  std::vector<int> link;
  std::vector<bool> vis;

BipartGraph() {}

void init1(int n) {
```

```
this \rightarrow n = n;
  adj.assign(n + 1, {});
  col.assign(n + 1, 0);
  cnt = 0;
}
void addEdge1(int u, int v) {
  adj[u].push_back(v);
  adj[v].push_back(u);
bool bipart(int u) {
  for (auto v : adj[u]) {
     if (col[v] == col[u]) {
       return false;
     if (col[v] == 0) {
      col[v] = 3 - col[u];
       if (! bipart(v)) return false;
     }
  }
  return true;
}
bool check_bipart() {
  bool f = 1;
  for (int i = 1; i <= n; i ++) {</pre>
     if (col[i] == 0) {
       cnt ++;
       col[i] = 1;
       if (! bipart(i)) {
         f = 0;
     }
  }
  return f;
void init2(int nx, int ny) {
  this -> nx = nx;
  this -> ny = ny;
  adj.assign(nx + 1, {});
  link.assign(ny + 1, -1);
  vis.assign(nx + 1, false);
  ans = 0;
```

```
void addEdge2(int u, int v) {
     adj[u].push_back(v);
     adj[v].push_back(u);
  }
  bool dfs(int u) {
     for (auto v : adj[u]) {
       if (vis[v]) continue;
       vis[v] = true;
        if (link[v] == 0 || dfs(link[v])) {
          link[v] = u;
          return true;
       }
     }
     return false;
  }
  int Maxans() {
     for (int i = 1; i <= nx; i ++) {</pre>
        std::fill(vis.begin(), vis.end(), false);
        if (dfs(i)) ans ++;
     }
     return ans;
  }
};
```

TwoSat

```
struct TwoSat {
  int n;
  std::vector<std::vector<int>> e;
  std::vector<bool> ans;
  TwoSat(int n) : n(n), e(2 * n), ans(n) {}
  void addClause(int u, bool f, int v, bool g) {
    e[2 * u + !f].push_back(2 * v + g);
    e[2 * v + !g].push_back(2 * u + f);
  }
  bool satisfiable() {
     std::vector<int> id(2 * n, -1), dfn(2 * n, -1), low(2 * n, -1);
    std::vector<int> stk;
    int now = 0, cnt = 0;
     std::function<void(int)> tarjan = [&](int u) {
       stk.push_back(u);
       dfn[u] = low[u] = now++;
       for (auto v : e[u]) {
```

```
if (dfn[v] == -1) {
             tarjan(v);
             low[u] = std::min(low[u], low[v]);
          } else if (id[v] == -1) {
             low[u] = std::min(low[u], dfn[v]);
          }
        }
        if (dfn[u] == low[u]) {
          int v;
          do {
            v = stk.back();
            stk.pop_back();
            id[v] = cnt;
          } while (v != u);
          ++cnt;
        }
     };
     for (int i = 0; i < 2 * n; ++i) if (dfn[i] == -1) tarjan(i);</pre>
     for (int i = 0; i < n; ++i) {</pre>
        if (id[2 * i] == id[2 * i + 1]) return false;
        ans[i] = id[2 * i] > id[2 * i + 1];
     }
     return true;
  std::vector<bool> answer() { return ans; }
}; // start from 0
```

线筛

```
std::vector<int> minp, primes;
void sieve(int n) {
    minp.assign(n + 1, 0);
    primes.clear();

for (int i = 2; i <= n; i++) {
    if (minp[i] == 0) {
        minp[i] = i;
        primes.push_back(i);
    }

    for (auto p : primes) {
        if (i * p > n) {
            break;
        }
        minp[i * p] = p;
    }
}
```

```
if (p == minp[i]) {
    break;
}
}
}
```

扩展欧拉定理

```
int main() {
    scanf("%d%d", &a, &m);
    bool flag = false;
    int phi_m = getphi(m);
    cin >> s;
    for(int i = 0; i < s.length(); ++ i) {
        b = (b * 10 + s[i] - '0');
        if(b >= phi_m)
        flag = 1, b %= phi_m;
    }
    if(flag)
    b += phi_m;
    int ans = qpow(a, b, m);
    printf("%d\n", ans);
    return 0;
}
```

欧拉函数

```
int phi(int n) {
   int res = n;
   for (int i = 2; i * i <= n; i++) {
      if (n % i == 0) {
        while (n % i == 0) {
            n /= i;
        }
        res = res / i * (i - 1);
      }
   if (n > 1) {
      res = res / n * (n - 1);
   }
   return res;
}
```

```
// 线性

void get_phi(int n){
    phi[1]=1;
    vis[1]=true;
    for(int i=2;i<=n;i++){
        if(!vis[i])p[++cnt]=i,phi[i]=i-1;
        for(int j=1;i*p[j]<=n;j++){
            vis[i*p[j]]=true;
            if(i%p[j]==0){phi[p[j]*i]=phi[i]*p[j];break;}
            phi[p[j]*i]=phi[i]*(p[j]-1);
        }
    }
}
</pre>
```

Exgcd

```
int exgcd(int a, int b, int& x, int& y) {
  if (b == 0) {
    x = 1, y = 0;
    return a;
  int d = exgcd(b, a % b, x, y);
  int z = x;
  x = y;
  y = z - (a / b) * y;
  return d;
}
void solve() {
  int a, b, c;
  std::cin >> a >> b >> c;
  int x, y;
  int d = exgcd(a, b, x, y);
  if (c % d) { // not exist.
     std::cout << "-1\n";
    return ;
  int t = c / d, aa = a / d, bb = b / d;
  x *= t, y *= t;
  // xx = x + k * bb, yy = y - k * aa
  int minx = (x % bb + bb - 1) % bb + 1;
  int miny = (y % aa + aa - 1) % aa + 1;
  int maxx = (c - b * miny) / a;
  int maxy = (c - a * minx) / b;
```

```
int cnt = (maxx - minx) / bb + 1; // (maxy - miny) / aa + 1
if (maxx <= 0 && maxy <= 0); // no positive ans
}</pre>
```

静态凸包

```
struct Point {
  i64 x;
  i64 y;
  Point(i64 x = 0, i64 y = 0) : x(x), y(y) {}
};
bool operator==(const Point &a, const Point &b) {
  return a.x == b.x && a.y == b.y;
}
Point operator+(const Point &a, const Point &b) {
  return Point(a.x + b.x, a.y + b.y);
}
Point operator-(const Point &a, const Point &b) {
  return Point(a.x - b.x, a.y - b.y);
}
i64 dot(const Point &a, const Point &b) {
  return a.x * b.x + a.y * b.y;
}
i64 cross(const Point &a, const Point &b) {
  return a.x * b.y - a.y * b.x;
}
void norm(std::vector<Point> &h) {
  int i = 0;
  for (int j = 0; j < int(h.size()); j++) {</pre>
    i = j;
    }
  }
  std::rotate(h.begin(), h.begin() + i, h.end());
}
int sgn(const Point &a) {
  return a.y > 0 || (a.y == 0 && a.x > 0) ? 0 : 1;
}
```

```
std::vector<Point> getHull(std::vector<Point> p) {
   std::vector<Point> h, 1;
   std::sort(p.begin(), p.end(), [&](auto a, auto b) {
     if (a.x != b.x) {
        return a.x < b.x;</pre>
     } else {
        return a.y < b.y;</pre>
     }
  });
  p.erase(std::unique(p.begin(), p.end()), p.end());
   if (p.size() <= 1) {</pre>
     return p;
  }
  for (auto a : p) {
     while (h.size() > 1 && cross(a - h.back(), a - h[h.size() - 2]) <= 0) {</pre>
        h.pop_back();
     while (1.size() > 1 && cross(a - 1.back(), a - 1[1.size() - 2]) >= 0) {
        1.pop_back();
     1.push_back(a);
     h.push_back(a);
  1.pop_back();
   std::reverse(h.begin(), h.end());
  h.pop_back();
  1.insert(1.end(), h.begin(), h.end());
  return 1;
}
```

线性基

```
struct Basis {
   std::vector<int> a, map;
   int n, basecnt;
   int sizofarr; // must set.
   bool zero;
   Basis() {}
   void init(int n) {
      this -> n = n;
      a.assign(n, 0);
      map.clear();
```

```
bool insert(int x) {
  for (int i = n - 1; i >= 0; i --) {
     if (! (x >> i & 1)) continue;
     if (a[i]) x ^= a[i];
     else {
       for (int j = 0; j < i; j ++) {</pre>
          if (a[j] && (x >> j & 1)) {
           x ^= a[j];
          }
        }
       for (int j = i + 1; j < n; j ++) {
          if (a[j] >> i & 1) {
            a[j] ^= x;
          }
        }
        a[i] = x;
       basecnt ++;
       return true;
     }
  }
  return false;
}
void build(std::vector<int> b, int siz) {
  sizofarr = siz;
  basecnt = 0, zero = 0;
  for (int i = 1; i <= siz; i ++) {</pre>
     insert(b[i]);
  zero = (basecnt != sizofarr); // 是否有零行
  for (int i = 0; i < n; i ++) {</pre>
    if (a[i]) map.push_back(i);
  }// 对应下标,方便
int query_max() {
  int res = 0;
  for (int i = 0; i < n; i ++) {</pre>
     res ^= a[i];
  }
  return res;
}
int query_min() {
  zero = (basecnt != sizofarr);
  if (zero) return 0;
  if (! map.size()) return -1;
```

```
return a[map[0]];
}
int query_kth(int k) { // kth_small
  zero = (basecnt != sizofarr);
  int res = 0;
  if (zero) k --;
  int siz = map.size();
  if (k >= (111 << siz)) return -1;</pre>
  for (int i = 0; i < siz; i ++) {</pre>
     if (k >> i & 1) {
       res ^= a[map[i]];
  }
  return res;
int query_rank(int x) {
  zero = (basecnt != n);
  int siz = map.size(), res = zero;
  res = 0; // 本题,空为0
  for (int i = 0; i < siz; i ++) {</pre>
     if (x >> map[i] & 1) {
       res += 111 << i;
     }
  }
  return res;
bool check_in(int x) {
  for (int i = n - 1; i >= 0; i --) {
     if (x >> i & 1) x ^= a[i];
  return x == 0;
}
void mergeFrom(const Basis &other) {
  for (int i = 0; i < n; i ++) {</pre>
    int it = other.a[i];
    if (it) insert(it);
  }
friend Basis operator +(const Basis &a, const Basis &b) {
  Basis res = a;
  int X = res.n;
  for (int i = 0; i < X; i ++) {</pre>
    int it = b.a[i];
```

```
if (it) res.insert(it);
}
return res;
} // 用于线段树维护线性基
};
```

组合数

```
int qmi(int a, int b){
  if (a == 0) return 0;
  int res = 1;
  while (b) {
    if (b & 1) {
       res = 111 * res * a % mod;
    a = 111 * a * a % mod;
     b >>= 1;
  return res;
}
struct Comb {
  int n;
  std::vector<int> _fac, _invfac, _inv;
  Comb() : n{0}, _fac{1}, _invfac{1}, _inv{0} {}
  void init(int m) {
     _fac.resize(m + 1);
     _invfac.resize(m + 1);
     _inv.resize(m + 1);
    for (int i = n + 1; i <= m; i ++) {</pre>
        _fac[i] = 1ll * _fac[i - 1] * i % mod;
     _invfac[m] = qmi(_fac[m], mod - 2);
    for (int i = m; i > n; i --) {
        _invfac[i - 1] = 111 * _invfac[i] * i % mod;
       _inv[i] = 1ll * _invfac[i] * _fac[i - 1] % mod;
    }
    n = m;
  int fac(int m) {
    return _fac[m];
  int invfac(int m) {
    return _invfac[m];
```

```
int inv(int m) {
    return _inv[m];
}
int binom(int n, int m) {
    if (n < m || m < 0) return 0;
    return 1ll * fac(n) * invfac(m) % mod * invfac(n - m) % mod;
}
comb;</pre>
```

Lucas

```
//需要用到逆元处理的模板。
11 C(int a,int b,int mod){
  if(b>a)return 0;//重要
  return fact[a]*infact[b]%mod*infact[a-b]%mod;
}
11 Lucas(ll a,ll b,ll p){
  if(b==0)return 1;
  //if(a<p&&b<p)return C(a,b,p);</pre>
  return C(a%p,b%p,p)*Lucas(a/p,b/p,p)%p;
}
//----扩展Lucas
#include<algorithm>
#include<iostream>
using namespace std;
typedef long long 11;
long long n,m,p,cnt,pr[1010],al[1010];
void exgcd(ll a,ll b,ll& x,ll& y){
  if(b==0){x=1,y=0;return;}
  exgcd(b,a%b,x,y);
  ll z=x;x=y;y=z-y*(a/b);
}
ll ny(ll a,ll p){//逆元
  11 x,y;exgcd(a,p,x,y);
  return (x+p)%p;
}
11 qmi(ll a,ll k,ll p){ ll res=1;
  while(k){if(k&1)res=res*a%p;a=a*a%p;k>>=1;}
  return res;
}
ll fac(ll n,ll p,ll ppa){//计算n!
  if (n==0) return 1; ll cir=1/*循环节*/,rem=1/*余数*/;
  for(ll i=1;i<=ppa;i++)if(i%p)cir=cir*i%ppa;</pre>
  cir=qmi(cir,n/ppa,ppa);
```

```
for(ll i=ppa*(n/ppa);i<=n;i++)if(i%p)rem=rem*(i%ppa)%ppa;</pre>
  return fac(n/p,p,ppa)*cir%ppa*rem%ppa;
}
11 sum_fac(ll n, ll p){    ll count = 0;
  do {n /= p;count += n;}while(n);
  return count;
}
ll C(ll n,ll m,ll p,ll ppa){//计算Cnm%pi^ai
  11 fz=fac(n,p,ppa),fm1=ny(fac(m,p,ppa),ppa),fm2=ny(fac(n-m,p,ppa),ppa);
  11 mi=qmi(p,sum_fac(n,p)-sum_fac(m,p)-sum_fac(n-m,p),ppa);
  return fz*fm1%ppa*fm2%ppa*mi%ppa;
void pfd(ll n, ll m) {//分解p
  11 P = p;
  for (11 i = 2; i * i <= p; i ++) {</pre>
     if (! (P % i)) {
       11 ppa = 1;
       while (! (P % i)) ppa *= i, P /= i;
       pr[++ cnt] = ppa;
       al[cnt] = C(n, m, i, ppa);
     }
  }
  if(P != 1) pr[++cnt]=P,al[cnt]=C(n,m,P,P);
11 crt(){//中国剩余定理
  ll ans=0;
  for(ll i=1;i<=cnt;i++){</pre>
     11 M=p/pr[i],T=ny(M,pr[i]);
     ans=(ans+al[i]*M%p*T%p)%p;
  }return ans;
}
ll exlucas(ll n, ll m) {//扩展卢卡斯
  pfd(n, m);
  return crt();
}
int main() { // 模数不一定为质数
  cin >> n >> m >> p;
  cout << exlucas(n, m);</pre>
}
```

Manacher

```
std::vector<int> manacher(std::string s) {
   std::string t = "#";
   for (auto c : s) {
```

```
t += c;
     t += '#';
  int n = t.size();
  std::vector<int> r(n);
  for (int i = 0, j = 0; i < n; i ++) {</pre>
     if (2 * j - i >= 0 && j + r[j] > i) {
       r[i] = std::min(r[2 * j - i], j + r[j] - i);
     while (i - r[i] \ge 0 \&\& i + r[i] < n \&\& t[i - r[i]] == t[i + r[i]]) {
       r[i] += 1;
    if (i + r[i] > j + r[j]) {
       j = i;
     }
  }
  return r; // radius
  // 结论 rad[1 + r] 是区间 [1, r) 的中间位置的回文长度。
}
```

最小表示法

```
void get_min() {
  int n;
  std::cin >> n;
  for (int i = 1; i <= n; i ++) {</pre>
     std::cin >> a[i];
    a[i + n] = a[i];
  int i = 1, j = 2, k = 0;
  while (i <= n \&\& j <= n \&\& k < n) {
    if (a[i + k] == a[j + k]) k ++;
     else {
        a[i + k] > a[j + k] ? (i = i + k + 1) : (j = j + k + 1);
       if (i == j) j++;
       k=0;
     }
  }
  k = std::min(i, j);
  for (int i = k; i < k + n; i ++) {</pre>
     std::cout << a[i] << " ";
  }
}
```

KMP

```
std::vector<int> kmp(std::string s) {
  int n = s.size();
  std::vector<int> f(n + 1);
  for (int i = 1, j = 0; i < n; i ++) {</pre>
     while (j && s[i] != s[j]) {
       j = f[j];
    j += (s[i] == s[j]);
    f[i + 1] = j;
  return f;
}
void solve() {
  std::string s, t;
  std::cin >> s >> t;
  auto p = kmp(t);
  int n = s.size(), m = t.size();
  std::string a = " " + s, b = " " + t;
  for (int i = 1, j = 0; i <= n; i ++) {</pre>
     while (j && a[i] != b[j + 1]) {
        j = p[j];
     }
     j += (a[i] == b[j + 1]);
     if (j == m) {
       std::cout << i - m + 1 << '\n';
       j = p[j];
  }
  for (int i = 1; i <= m; i ++) {</pre>
     std::cout << p[i] << ' ';
  }
  std::cout << '\n';</pre>
}
```

Matrix

```
struct Matrix {
  int n;
  std::vector<std::vector<int>> M;
  Matrix() {}
```

```
void init(int n) {
     this \rightarrow n = n;
     M.assign(n + 1, std::vector < int > (n + 1, 0));
  void norm() {
     for (int i = 1; i <= n; i ++) {</pre>
       M[i][i] = 1;
     }
  }
  Matrix friend operator * (const Matrix &a, const Matrix &b) {
     Matrix ans;
     int n = a.n;
     ans.init(n);
     for (int i = 1; i <= n; i ++) {</pre>
       for (int j = 1; j <= n; j ++) {</pre>
           for (int k = 1; k <= n; k ++) {</pre>
             ans.M[i][j] = (ans.M[i][j] + 111 * a.M[i][k] * b.M[k][j]) \% mod;
           }
        }
     }
     return ans;
  }
};
Matrix qmi(Matrix a, i64 b) {
  Matrix ans;
  int n = a.n;
  ans.init(n);
  ans.norm();
  while (b) {
    if (b & 1) ans = ans * a;
     a = a * a;
     b >>= 1;
  }
  return ans;
}
```

高斯消元

```
const db eps = 1e-5;
struct guess {
  int n;
  std::vector<std::vector<db>> a;
  std::vector<db> b;
guess() {}
```

```
void init(int n, std::vector<std::vector<db>> x, std::vector<db>> y) {
  this \rightarrow n = n;
  a.assign(n + 1, {});
  b.assign(y.begin(), y.end());
  for (int i = 1; i <= n; i ++) {</pre>
     a[i].assign(x[i].begin(), x[i].end());
  }
}
int work() {
  int 1 = 1;
  for (int i = 1; i <= n; i ++) {</pre>
     int fg = 1;
     for (int j = 1; j <= n; j ++) {</pre>
        if (std::fabs(a[j][i]) > std::fabs(a[l][i])) {
          1 = j;
       }
     }
     for (int k = i; k <= n; k ++) {</pre>
        std::swap(a[1][k], a[fg][k]);
     }
     std::swap(b[1], b[fg]);
     1 = fg;
     if (std::fabs(a[l][i]) < eps) {</pre>
        continue;
     }
     for (int j = 1; j <= n; j ++) {</pre>
        if (j != 1 && std::fabs(a[j][i]) > eps) {
          db delta = a[j][i] / a[l][i];
          for (int k = i; k <= n; k ++) {</pre>
             a[j][k] -= delta * a[l][k];
          b[j] -= delta * b[1];
       }
     }
     1 ++;
  int f = 0;
  for (int i = 1; i <= n; i ++) { // 无解
     if (std::fabs(b[i]) > eps) {
        f = -1;
        break;
     }
  if (f != -1 && 1 <= n) { // 无穷多解
     f = -2;
```

```
if (f == 0) {
    for (int i = 1; i <= n; i ++) {
        b[i] /= a[i][i]; // b[i] is the ans
        a[i][i] = 1.0;
    }
}
return f;
}
</pre>
```

矩阵求逆

```
#include<bits/stdc++.h>
using namespace std;
namespace X{
  #define int long long
  constexpr int mod(1e9+7);
  int qmi(int x,int y){int ret=1;
     for(;y;y&1&&(ret=ret*x%mod),x=x*x%mod,y>>=1);return ret;}
  int ny(int x){return qmi(x,mod-2);}
  constexpr int maxn(405);
  int mt[maxn][maxn*2],N;
  void inv(){
     for(int i=1;i<=N;i++){int pos=0;</pre>
        for(int j=i;j<=N;j++)</pre>
        if(mt[j][i]){pos=j;break;}
        if(!pos){cout<<"No Solution"<<endl;exit(0);}</pre>
        if(pos^i)swap(mt[i],mt[pos]);int v=ny(mt[i][i]);
        for(int j=i;j<=N*2;j++)mt[i][j]=mt[i][j]*v%mod;</pre>
        for(int j=1;j<=N;j++){</pre>
           if(j==i)continue;int v=mt[j][i];
           for(int k=i;k<=N*2;k++)</pre>
           mt[j][k]=(mt[j][k]-v*mt[i][k])%mod;
        }
     }
  int MAIN(){cin>>N;
     for(int i=1;i<=N;i++){</pre>
        for(int j=1;j<=N;j++)scanf("%lld",&mt[i][j]);mt[i][N+i]=1;</pre>
     }inv();
     for(int i=1;i<=N;i++){</pre>
        for(int j=1;j<=N;j++)printf("%lld ",(mt[i][j+N]%mod+mod)%mod);</pre>
        puts("");
     }return 0;
```

```
};
# undef int
using namespace X;
int main(){
   return MAIN();
}
```

第二类斯特林

```
// n 不同, m 相同集合
int S(int n, int m) {
    i64 res = 0;
    for (int i = 0; i <= m; i ++) {
        res += ((m - i) % 2 ? -1 : 1) * comb.binom(m, i) % mod * qmi(i, n) % mod;
        res %= mod;
    }
    res = res * comb.invfac(m) % mod;
    return res;
}</pre>
```

ntt

```
using Poly = std::vector<int>;
//4179340454199820289
const int G = 3, mod = 998244353, Maxn = 2e6 + 10;
int qmi(int a, int b = mod - 2) {
  int res = 1;
  while (b) {
    if (b & 1) {
       res = 111 * res * a % mod;
    }
    a = 111 * a * a % mod;
    b >>= 1;
  }
  return res;
}
const int invG = qmi(G);
int tr[Maxn << 1], tf;</pre>
void tpre(int n) {
  if (tf == n) return ;
tf = n;
```

```
for (int i = 0; i < n; i ++) {</pre>
     tr[i] = (tr[i >> 1] >> 1) | ((i & 1) ? n >> 1 : 0);
  }
}
void NTT(int n, int *g, bool op) {
  tpre(n);
   static u64 f[Maxn << 1], w[Maxn << 1];</pre>
  for (int i = 0; i < n; i ++) {</pre>
     f[i] = (((i64) mod << 5) + g[tr[i]]) % mod;
  }
  for (int 1 = 1; 1 < n; 1 <<= 1) {</pre>
     u64 tG = qmi(op ? G : invG, (mod - 1) / (1 + 1));
     for (int i = 1; i < 1; i ++) w[i] = w[i - 1] * tG % mod;</pre>
     for (int k = 0; k < n; k += 1 + 1)
     for (int p = 0; p < 1; p ++) {</pre>
        int tt = w[p] * f[k | 1 | p] % mod;
        f[k | 1 | p] = f[k | p] + mod - tt;
        f[k | p] += tt;
     if (1 == (1 << 10))</pre>
     for (int i = 0; i < n; i ++) f[i] %= mod;</pre>
  }
  if (! op) {
     u64 invn = qmi(n);
     for(int i = 0; i < n; ++ i) {</pre>
        g[i] = f[i] % mod * invn % mod;
     }
  } else {
     for (int i = 0; i < n; ++ i) {</pre>
        g[i] = f[i] % mod;
     }
  }
}
void px(int n, int *f, int *g) {
  for (int i = 0; i < n; ++ i) {</pre>
     f[i] = 111 * f[i] * g[i] % mod;
  }
}
Poly operator +(const Poly &A, const Poly &B) {
  Poly C = A;
  C.resize(std::max(A.size(), B.size()));
  for (int i = 0; i < B.size(); i ++) {</pre>
    C[i] = (C[i] + B[i]) \% mod;
```

```
return C;
Poly operator -(const Poly &A, const Poly &B) {
  Poly C = A;
  C.resize(std::max(A.size(),B.size()));
  for (int i = 0; i < B.size(); i ++) {</pre>
     C[i] = (C[i] + mod - B[i]) \% mod;
  }
  return C;
}
Poly operator *(const int c, const Poly &A) {
  Poly C;
  C.resize(A.size());
  for (int i = 0; i < A.size(); i ++) {</pre>
     C[i] = 111 * c * A[i] % mod;
  }
  return C;
}
int lim; // set.
Poly operator *(const Poly &A, const Poly &B) {
   static int a[Maxn << 1], b[Maxn << 1];</pre>
  for (int i = 0; i < A.size(); i ++) a[i] = A[i];</pre>
  for (int i = 0; i < B.size(); i ++) b[i] = B[i];</pre>
  Poly C;
  C.resize(std::min(lim, (int)(A.size() + B.size() - 1)));
  int n = 1;
  for(n; n < A.size() + B.size() - 1; n <<= 1);</pre>
  NTT(n, a, 1);
  NTT(n, b, 1);
  px(n, a, b);
  NTT(n, a, 0);
  for (int i = 0; i < C.size(); i ++) {</pre>
     C[i] = a[i];
  for (int i = 0; i <= n; i ++) {</pre>
     a[i] = 0;
     b[i] = 0;
  return C;
}
void pinv(int n, const Poly &A, Poly &B) {
  if (n == 1) B.push_back(qmi(A[0]));
  else if (n & 1){
     pinv(-- n, A, B);
     int sav = 0;
     for (int i = 0; i < n; i ++) {</pre>
```

```
sav = (sav + 111 * B[i] * A[n - i] % mod) % mod;
     }
     B.push_back(111 * sav * qmi(mod - A[0]) % mod);
  } else {
     pinv(n / 2, A, B);
     Poly sA;
     sA.resize(n);
     for (int i = 0; i < n; i ++) {</pre>
       sA[i] = A[i];
     B = 2 * B - B * B * sA;
     B.resize(n);
  }
Poly pinv(const Poly &A) { // P-inv
  Poly C;
  pinv(A.size(), A, C);
  return C;
int inv[Maxn];
void Init() {
  inv[1] = 1;
  for (int i = 2; i <= lim; i ++) {</pre>
     inv[i] = 1ll * inv[mod % i] * (mod - mod / i) % mod;
  }
Poly dao(const Poly &A) { // P-qiu-dao
  Poly C = A;
  for (int i = 1; i < C.size(); i ++) {</pre>
     C[i - 1] = 111 * C[i] * i % mod;
  C.pop_back();
  return C;
}
Poly ints(const Poly &A) { // P-ji-fen
  Poly C = A;
  for (int i = C.size() - 1; i; i --)
  C[i] = 111 * C[i - 1] * inv[i] % mod;
  C[0] = 0;
  return C;
}
Poly ln(const Poly &A) { // P-ln
  return ints(dao(A) * pinv(A));
void pexp(int n, const Poly &A, Poly &B) {
  if (n == 1) B.push_back(1);
else if (n & 1) {
```

```
pexp(n - 1, A, B);
     n = 2;
     int sav = 0;
     for (int i = 0; i <= n; i ++) {</pre>
        sav = (sav + 111 * (i + 1) * A[i + 1] % mod * B[n - i] % mod) % mod;
     B.push_back(111 * sav * inv[n + 1] % mod);
  } else {
     pexp(n / 2, A, B);
     Poly lnB = B;
     lnB.resize(n);
     lnB = ln(lnB);
     for (int i = 0; i < lnB.size(); i ++) {</pre>
        lnB[i] = (mod + A[i] - lnB[i]) % mod;
     }
     lnB[0] ++;
     B = B * lnB;
     B.resize(n);
  }
Poly pexp(const Poly &A) { // P-exp
  Poly C;
  pexp(A.size(), A, C);
  return C;
}
void solve() {
  int n;
  std::cin >> n;
  lim = n + n;
  Init();
  Poly F;
  F.resize(n);
  for (int i = 0; i < n; i ++) {</pre>
     std::cin >> F[i];
  Poly ans = pexp(F);
  for (int i = 0; i < n; i ++) {</pre>
     std::cout << ans[i] << ' ';
  }
  std::cout << '\n';</pre>
}
```