## modal

# 目录

MTT.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	3
单流 EK				•	•	•							•	•	•						•	•							•	•	•		•	5
树哈希	•		•	•	•	•	•						•	•	•						•	•								•			•	7
dfs 树.				•	•		•							•	•																			9

#### **MTT**

```
#include <algorithm>
#include <iostream>
#include <cstdio>
#include <cstring>
// #define int long long
const int mod = 1e9 + 7;
namespace Math {
  inline int pw(int base, int p, const int mod) {
     static int res;
     for (res = 1; p; p >>= 1, base = static_cast<long long> (base) * base % mod) if (p & 1)
         res = static_cast<long long> (res) * base % mod;
     return res;
  }
  inline int inv(int x, const int mod) { return pw(x, mod - 2, mod); }
const int mod1 = 469762049, mod2 = 998244353, mod3 = 1004535809, G = 3;
const long long mod_1_2 = static_cast<long long> (mod1) * mod2;
const int inv_1 = Math::inv(mod1, mod2), inv_2 = Math::inv(mod_1_2 % mod3, mod3);
struct Int {
  int A, B, C;
  explicit inline Int() { }
  explicit inline Int(int __num) : A(__num), B(__num), C(__num) { }
  explicit inline Int(int \_A, int \_B, int \_C) : A(\_A), B(\_B), C(\_C) { }
  static inline Int reduce(const Int &x) {
     return Int(x.A + (x.A >> 31 \& mod1), x.B + (x.B >> 31 \& mod2), x.C + (x.C >> 31 \& mod3));
  inline friend Int operator + (const Int &lhs, const Int &rhs) {
     return reduce(Int(lhs.A + rhs.A - mod1, lhs.B + rhs.B - mod2, lhs.C + rhs.C - mod3));
  inline friend Int operator - (const Int &lhs, const Int &rhs) {
     return reduce(Int(lhs.A - rhs.A, lhs.B - rhs.B, lhs.C - rhs.C));
  inline friend Int operator * (const Int &lhs, const Int &rhs) {
     return Int(
     static_cast<long long> (lhs.A) * rhs.A % mod1,
     static_cast<long long> (lhs.B) * rhs.B % mod2,
     static_cast<long long> (lhs.C) * rhs.C % mod3);
  inline int get() {
     long long x = static_cast<long long> (B - A + mod2) % mod2 * inv_1 % mod2 * mod1 + A;
     return (static_cast<long long> (C - x % mod3 + mod3) % mod3 * inv_2 % mod3 * (mod_1_2 %
         mod) % mod + x) % mod;
```

```
};
#define maxn 131072
namespace Poly {
  #define N (maxn << 1)</pre>
  int lim, s, rev[N];
  Int Wn[N | 1];
  inline void init(int n) {
     s = -1, lim = 1; while (lim < n) lim <<= 1, ++s;
     for (register int i = 1; i < lim; ++i) rev[i] = rev[i >> 1] >> 1 | (i & 1) << s;
     const Int t(Math::pw(G, (mod1 - 1) / lim, mod1), Math::pw(G, (mod2 - 1) / lim, mod2),
          Math::pw(G, (mod3 - 1) / lim, mod3));
     *Wn = Int(1); for (register Int *i = Wn; i != Wn + lim; ++i) *(i + 1) = *i * t;
  }
  inline void NTT(Int *A, const int op = 1) {
     for (register int i = 1; i < lim; ++i) if (i < rev[i]) std::swap(A[i], A[rev[i]]);</pre>
     for (register int mid = 1; mid < lim; mid <<= 1) {</pre>
        const int t = lim / mid >> 1;
        for (register int i = 0; i < lim; i += mid << 1) {</pre>
          for (register int j = 0; j < mid; ++j) {
             const Int W = op ? Wn[t * j] : Wn[lim - t * j];
             const Int X = A[i + j], Y = A[i + j + mid] * W;
             A[i + j] = X + Y, A[i + j + mid] = X - Y;
          }
        }
     }
     if (!op) {
        const Int ilim(Math::inv(lim, mod1), Math::inv(lim, mod2), Math::inv(lim, mod3));
        for (register Int *i = A; i != A + lim; ++i) *i = (*i) * ilim;
     }
  }
  #undef N
Int A[maxn << 1], B[maxn << 1], C[maxn << 1], D[maxn << 1], res[maxn << 1];</pre>
signed main() {
  int n, m;
  std::cin >> n >> m;
  Poly::init(n + n);
  for (int i = 0; i < Poly::lim; i ++) {</pre>
     A[i] = Int(0);
     B[i] = Int(0);
  A[1] = Int(1), A[n - 1] = Int(1);
  B[0] = Int(1);
  while (m) {
     if (m & 1) {
        for (int i = 0; i < n; i ++) {</pre>
```

```
C[i] = B[i];
          D[i] = A[i];
       for (int i = n; i < Poly::lim; i ++) {</pre>
          C[i] = Int(0);
          D[i] = Int(0);
       }
       Poly::NTT(C), Poly::NTT(D);
       for (int i = 0; i < Poly::lim; i ++) {</pre>
          res[i] = C[i] * D[i];
       }
       Poly::NTT(res, 0);
       for (int i = 0; i < n + n; i ++) {</pre>
          B[i] = Int(((res[i].get() + res[i + n].get()) % mod + mod) % mod);
       }
     }
     for (int i = 0; i < n; i ++) {</pre>
       C[i] = A[i];
     for (int i = n; i < Poly::lim; i ++) {</pre>
       C[i] = Int(0);
     }
     Poly::NTT(C);
     for (int i = 0; i < Poly::lim; i ++) {</pre>
       res[i] = C[i] * C[i];
     Poly::NTT(res, 0);
     for (int i = 0; i < n + n; i ++) {</pre>
       A[i] = Int(((res[i].get() + res[i + n].get()) % mod + mod) % mod);
     }
     m >>= 1;
  std::cout << B[0].get() << '\n';
  return 0;
// 10 100 the last time
```

### 单流 EK

```
struct FlowGraph {
  int s, t, vtot, etot, head[V], dis[V], cur[V], pre[V], pre_edge[V];
  struct edge {
    int v, nxt;
    T f;
```

```
} e[E * 2];
void addedge(int u, int v, T f) {
  e[etot] = {v, head[u], f}; head[u] = etot ++;
  e[etot] = \{u, head[v], 0\}; head[v] = etot ++;
}
bool bfs() {
  for (int i = 1; i <= vtot; i ++) {</pre>
     dis[i] = 0;
     cur[i] = head[i];
  std::queue<int> q;
  q.push(s); dis[s] = 1;
  while (! q.empty()) {
     int u = q.front(); q.pop();
    for (int i = head[u]; ~i; i = e[i].nxt) {
       if (e[i].f && ! dis[e[i].v]) {
          int v = e[i].v;
          dis[v] = dis[u] + 1;
          pre[v] = u;
          pre_edge[v] = i;
          if (v == t) return true;
          q.push(v);
       }
     }
  }
  return false;
}
T dicnic() {
  T flow = 0;
  while (bfs()) {
    flow ++;
    int x = t;
     while (x != s) {
       int i = pre_edge[x];
       e[i].f -= 1;
       e[i ^ 1].f += 1;
       x = pre[x];
     }
  return flow;
void init(int _s, int _t, int _vtot) {
  s = _s;
  t = _t;
  vtot = _vtot;
  for (int i = 1; i <= vtot; i ++) {</pre>
   head[i] = -1;
```

```
}
};
```

### 树哈希

```
#include<bits/stdc++.h>
using i64 = long long;
#define u64 unsigned long long
#define int u64
const u64 b = 1331;
u64 h(u64 x) {
  return x * x * x * 1237123 + 19260817;
u64 f(u64 x) {
  u64 cur = h(x & ((111 << 31) - 1)) + h(x >> 31);
  return cur;
void solve() {
  int n, m;
  std::cin >> n >> m;
  std::vector<std::vector<int> > e(n + 1);
  for (int i = 1; i <= m; i ++) {</pre>
    int x, y;
     std::cin >> x >> y;
     e[x].push_back(y);
     e[y].push_back(x);
  }
  if (m == n - 1) {
     std::cout << "YES\n";</pre>
     return ;
  }
  if (m > n) {
     std::cout << "NO\n";
     return ;
  }
  i64 ans = 0;
  std::vector\leq int > dfn(n + 1), onloop(n + 1), loop(n * 2 + 1), fa(n + 1);
  int timer = 0, cnt;
  auto dfs = [&](auto self, int u, int p) -> void {
     dfn[u] = ++ timer;
   for (auto v : e[u]) {
```

```
if (v == p) continue;
       if (dfn[v]) {
          if (dfn[v] < dfn[u]) continue;</pre>
          loop[++ cnt] = v;
          onloop[v] = 1;
          while (v != u) {
             loop[++ cnt] = fa[v];
             onloop[fa[v]] = 1;
             v = fa[v];
       } else {
          fa[v] = u;
          self(self, v, u);
       }
     }
  };
  std::vector<u64> ff(n + 1);
  auto getsubTree = [&](auto self, int u, int p) -> void {
     ff[u] = 1;
     for (auto v : e[u]) {
       if (v == p || onloop[v]) continue;
       self(self, v, u);
       ff[u] = ff[u] + f(ff[v]);
     }
  };
  cnt = 0;
  dfs(dfs, 1, 0);
  std::vector<u64> LOOP(cnt * 2 + 1);
  for (int i = 1; i <= cnt; i ++) {</pre>
     getsubTree(getsubTree, loop[i], 0);
     LOOP[i] = ff[loop[i]];
     LOOP[i + cnt] = LOOP[i];
  for (int i = 1; i <= cnt; i ++) {</pre>
     if (LOOP[i] != LOOP[i + 2]) {
       std::cout << "NO\n";
       return ;
    }
  std::cout << "YES\n";</pre>
signed main() {
  std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  int t = 1;
  std::cin >> t;
  while (t --) {
```

```
solve();
}
return 0;
}
```

#### dfs 树

```
#include<bits/stdc++.h>
using i64 = long long;
using pii = std::array<int, 2>;
void solve() {
  int n, m;
  std::cin >> n >> m;
  std::vector<bool> vis_U(n + 1), vis_E(m + 1);
  std::vector<pii> ans(m + 1); // 0/1, 0/1
  std::vector<std::vector<pii> > e(n + 1);
  std::vector<int> fornow(n + 1);
  std::vector<pii> E(m + 1);
  for (int i = 1; i <= m; i ++) {</pre>
     int u, v;
     std::cin >> u >> v;
     E[i] = \{u, v\};
     e[u].push_back({v, i});
     e[v].push_back({u, i});
  }
  auto check = [&](int y, int id1, int id2) {
     ans[id1] = \{(E[id1][0] == y ? 0 : 1), (id1 > id2)\};
     ans[id2] = \{(E[id2][0] == y ? 0 : 1), (id1 < id2)\};
  };
  auto dfs = [&](auto&& self, int u) -> pii { // I konw i konw...
     vis_U[u] = 1;
     pii now = \{0, 0\};
     // for (int i = fornow[u]; i < e[u].size(); i = fornow[u] +) {</pre>
       // int v = e[u][i][0], id = e[u][i][1];
       // for (auto it ; e[u]) {
          // int v = it[0], id = it[1];
     while (fornow[u] < e[u].size()) {</pre>
       int v = e[u][fornow[u]][0], id = e[u][fornow[u]][1];
       fornow[u] ++;
       if (vis_E[id]) continue;
       vis_E[id] = 1;
       pii down = self(self, v); // w, id
       if (down[0]) {
          // u, v, w
          check(v, id, down[1]);
```

```
} else {
          if (now[0]) {
            check(u, now[1], id);
            now = \{0, 0\};
          } else {
            now = \{v, id\};
          }
       }
     }
    return now;
  };
  for (int i = 1; i <= n; i ++) {</pre>
    if (! vis_U[i]) {
       pii it = dfs(dfs, i); // 不需要去特判它的,
    }
  }
  for (int i = 1; i <= m; i ++) {</pre>
     std::cout << (ans[i][0] ? 'y' : 'x') << (ans[i][1] ? '-' : '+') << ' \n';
  }
}
signed main() {
  std::ios::sync_with_stdio(false);
  std::cin.tie(nullptr);
  int t = 1;
  // std::cin >> t;
  while (t --) {
     solve();
  }
  return 0;
}
```