



- **Linear Activation**

- The linear activation function, also known as "no activation," or "identity function" (multiplied x1.0), is where the activation is proportional to the input. **The function doesn't do anything to the weighted sum of the input, it simply spits out the value it was given.**

- **Generalized Delta Rule for updating weights**

$$\Delta w_{ij} = -c (\partial \text{Error} / \partial w_{ij}) = -c [-(d_j - O_j) \cdot f'(\text{act}_j) \cdot x_i]$$

- C is the learning rate
- F' is the derivative of the activation function

Delta Rule

Dataset: $\begin{bmatrix} x_1 & x_2 & x_3 \\ 1 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$ $\begin{bmatrix} b \\ w_0 \\ 2 \end{bmatrix}$ $\begin{bmatrix} \text{wheel} \\ 0 \\ 1 \end{bmatrix}$ unit step func

weight $\begin{bmatrix} w_1 & w_2 & w_3 \\ -2 & 2 & 1 \end{bmatrix}$

2nd sample

$$= b_0 w_0 + x_1 w_1 + x_2 w_2 + x_3 w_3$$

$$b_0 w_0 + x_1 w_1 + x_2 w_2 + x_3 w_3$$

$$= 1(2) + 1(-2) + 0(2) + 1(1)$$

$$1(2) + 0(-2) + 0(2) + 0(1)$$

$$= 2$$

$$= 2 - 2 + 2 + 1$$

$$\text{act}(2) = 1$$

$$\hat{y}_2 = 1$$

$$= 3$$

$$\alpha = 0.2$$

$$\hat{y}_1 = \text{act}(3) = 1$$

$y_i - \hat{y}_i$	$(y_i - \hat{y}_i) \cdot b$	$(y_i - \hat{y}_i) \cdot x_1$	$(y_i - \hat{y}_i) \cdot x_2$	$(y_i - \hat{y}_i) \cdot x_3$
$0 - 1 = -1$	$1 \times (-1) = -1$	$-1 \times 1 = -1$	$0 \times -1 = 0$	$-1 \times 1 = -1$
$1 - 1 = 0$	$1 \times 0 = 0$	$0 \times 0 = 0$	$0 \times 0 = 0$	$0 \times 0 = 0$

$$0 - 1 = -1 \quad 1 \times (-1) = -1 \quad -1 \times 1 = -1 \quad 0 \times -1 = 0 \quad -1 \times 1 = -1$$

$$1 - 1 = 0 \quad 1 \times 0 = 0 \quad 0 \times 0 = 0 \quad 0 \times 0 = 0 \quad 0 \times 0 = 0$$

$$\sum = -1 \quad \sum = -1 \quad \sum = -1 \quad \sum = 0 \quad \sum = -1$$

$$w_{0_{\text{new}}} = w_0 + \sum \alpha (y_i - \hat{y}_i) \cdot b = -2 + 0.2(-1) = -2.2$$

$$w_{1_{\text{new}}} = w_1 + \sum \alpha (y_i - \hat{y}_i) \cdot x_1 = -2 + 0.2(-1) = -2.2$$

$$w_{2_{\text{new}}} = w_2 + \sum \alpha (y_i - \hat{y}_i) \cdot x_2 = 2 + 0.2(0) = 2$$

$$w_{3_{\text{new}}} = w_3 + \sum \alpha (y_i - \hat{y}_i) \cdot x_3 = 1 + 0.2(-1) = 0.8$$

$$\begin{bmatrix} w_0 \\ w_1 \\ w_2 \\ w_3 \end{bmatrix} = \begin{bmatrix} -2.2 \\ -2.2 \\ 2 \\ 0.8 \end{bmatrix}$$