

Assignment 3

Due Date: April 22, 2025
(50 points)

Exercise 1: Compute $\text{MaxDistance}(\text{Data}, \text{Centers})$ for *Data* shown in the figure 1 and *Centers* $(2, 4)$, $(6, 7)$, and $(7, 3)$. (5 points)

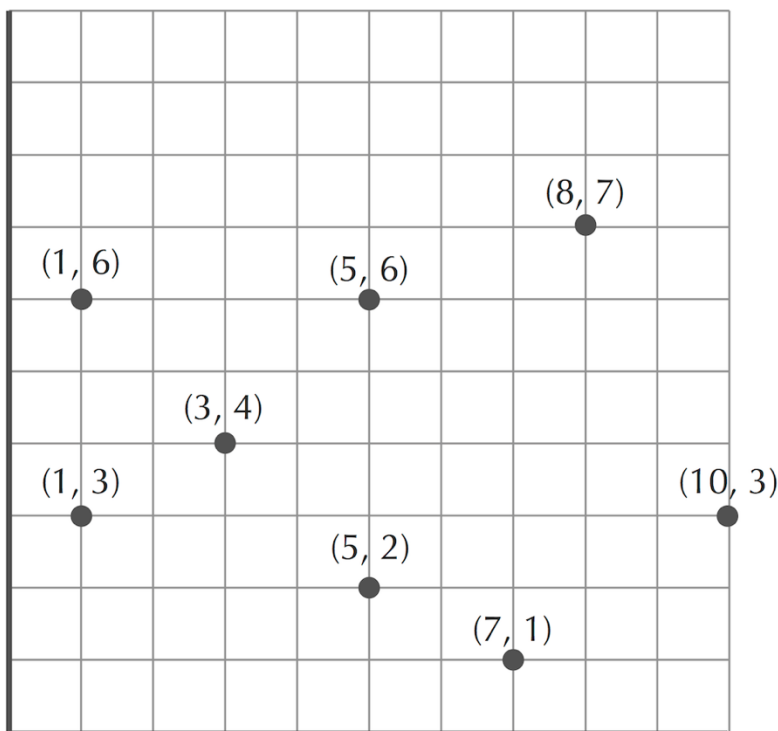


Figure 1

Exercise 2: Compute the values of $\text{MaxDistance}(\text{Data}, \text{Centers})$ and $\text{Distortion}(\text{Data}, \text{Centers})$ for the eight data points in the figure 1 and the three centers $(3, 4.5)$, $(6, 1.5)$, and $(9, 5)$. How do these values differ if the centers are instead $(5/3, 13/3)$, $(6.5, 6.5)$, and $(22/3, 2)$? (10 points)

Exercise 3: Run the Lloyd algorithm for the set of four one-dimensional data points $\{0, 1, 1.9, 3\}$ with the two initial centers $\{1, 3\}$. (5 points)

Exercise 4: Apply Hierarchical Clustering to the distance matrix using D_{\min} and D_{avg} . (30 points)

$$D_{\text{avg}}(C_1, C_2) = \frac{\sum_{\text{all points } i \text{ in cluster } C_1} \sum_{\text{all points } j \text{ in cluster } C_2} D_{i,j}}{|C_1| \cdot |C_2|}$$

$$D_{\min}(C_1, C_2) = \min_{\text{all points } i \text{ in cluster } C_1, \text{ all points } j \text{ in cluster } C_2} D_{i,j} .$$

	g_1	g_2	g_3	g_4	g_5	g_6	g_7	g_8	g_9	g_{10}
g_1	0.0	8.1	9.2	7.7	9.3	2.3	5.1	10.2	6.1	7.0
g_2	8.1	0.0	12.0	0.9	12.0	9.5	10.1	12.8	2.0	1.0
g_3	9.2	12.0	0.0	11.2	0.7	11.1	8.1	1.1	10.5	11.5
g_4	7.7	0.9	11.2	0.0	11.2	9.2	9.5	12.0	1.6	1.1
g_5	9.3	12.0	0.7	11.2	0.0	11.2	8.5	1.0	10.6	11.6
g_6	2.3	9.5	11.1	9.2	11.2	0.0	5.6	12.1	7.7	8.5
g_7	5.1	10.1	8.1	9.5	8.5	5.6	0.0	9.1	8.3	9.3
g_8	10.2	12.8	1.1	12.0	1.0	12.1	9.1	0.0	11.4	12.4
g_9	6.1	2.0	10.5	1.6	10.6	7.7	8.3	11.4	0.0	1.1
g_{10}	7.0	1.0	11.5	1.1	11.6	8.5	9.3	12.4	1.1	0.0