class09_mini_project

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1. Exploratory data analysis

```
# Save your input data file into your Project directory
fna.data <- "WisconsinCancer.csv"

# Complete the following code to input the data and store as wisc.df
wisc.df <- read.csv(fna.data, row.names=1)

# We can use -1 here to remove the first column
wisc.data <- wisc.df[,-1]

# Create diagnosis vector for later
diagnosis <- as.factor(wisc.df$diagnosis)</pre>
```

Q1. How many observations are in this dataset?

```
nrow(wisc.data)
```

[1] 569

There are 569 observations in the dataset.

Q2. How many of the observations have a malignant diagnosis?

table(diagnosis)

```
## diagnosis
## B M
## 357 212
```

212 observations have a malignant diagnosis.

Q3. How many variables/features in the data are suffixed with _mean?

```
length(grep("_mean", colnames(wisc.df)))
```

[1] 10

There are 10 variables in the data with the 'mean' suffix.

2. Principal Component Analysis Performing PCA

```
# Check column means and standard deviations
colMeans(wisc.data)
```

```
##
               radius_mean
                                        texture_mean
                                                               perimeter_mean
##
              1.412729e+01
                                        1.928965e+01
                                                                 9.196903e+01
##
                 area_mean
                                     {\tt smoothness\_mean}
                                                             compactness_mean
##
              6.548891e+02
                                        9.636028e-02
                                                                 1.043410e-01
##
            concavity_mean
                                concave.points_mean
                                                                symmetry_mean
                                        4.891915e-02
##
              8.879932e-02
                                                                 1.811619e-01
    fractal_dimension_mean
##
                                           radius_se
                                                                   texture_se
##
              6.279761e-02
                                        4.051721e-01
                                                                 1.216853e+00
##
              perimeter_se
                                             area se
                                                                smoothness se
##
              2.866059e+00
                                        4.033708e+01
                                                                 7.040979e-03
##
            compactness_se
                                        concavity_se
                                                            concave.points_se
                                        3.189372e-02
                                                                 1.179614e-02
##
              2.547814e-02
##
               symmetry_se
                               fractal_dimension_se
                                                                 radius_worst
              2.054230e-02
##
                                        3.794904e-03
                                                                 1.626919e+01
##
             texture_worst
                                    perimeter_worst
                                                                   area_worst
                                                                 8.805831e+02
##
              2.567722e+01
                                        1.072612e+02
##
          smoothness_worst
                                   compactness_worst
                                                              concavity_worst
##
              1.323686e-01
                                        2.542650e-01
                                                                 2.721885e-01
##
      concave.points_worst
                                      symmetry_worst fractal_dimension_worst
##
              1.146062e-01
                                        2.900756e-01
                                                                 8.394582e-02
```

apply(wisc.data,2,sd)

##	radius_mean	texture_mean	perimeter_mean
##	3.524049e+00	4.301036e+00	2.429898e+01
##	area_mean	${\tt smoothness_mean}$	compactness_mean
##	3.519141e+02	1.406413e-02	5.281276e-02
##	concavity_mean	concave.points_mean	symmetry_mean
##	7.971981e-02	3.880284e-02	2.741428e-02
##	fractal_dimension_mean	radius_se	texture_se
##	7.060363e-03	2.773127e-01	5.516484e-01
##	perimeter_se	area_se	smoothness_se
##	2.021855e+00	4.549101e+01	3.002518e-03
##	compactness_se	concavity_se	concave.points_se
##	1.790818e-02	3.018606e-02	6.170285e-03
##	symmetry_se	fractal_dimension_se	radius_worst
##	8.266372e-03	2.646071e-03	4.833242e+00
##	texture_worst	perimeter_worst	area_worst
##	6.146258e+00	3.360254e+01	5.693570e+02

```
## smoothness_worst compactness_worst concavity_worst
## 2.283243e-02 1.573365e-01 2.086243e-01
## concave.points_worst symmetry_worst fractal_dimension_worst
## 6.573234e-02 6.186747e-02 1.806127e-02
```

```
# Perform PCA on wisc.data by completing the following code
wisc.pr <- prcomp(wisc.data, scale=TRUE)</pre>
```

```
# Look at summary of results
summary(wisc.pr)
```

```
## Importance of components:
                                                     PC4
                                                             PC5
                                                                     PC6
##
                             PC1
                                    PC2
                                             PC3
                                                                             PC7
## Standard deviation
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
## Cumulative Proportion
                          0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
##
                              PC8
                                     PC9
                                             PC10
                                                    PC11
                                                            PC12
                                                                    PC13
## Standard deviation
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion
                          0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
                             PC15
                                     PC16
                                              PC17
                                                      PC18
                                                              PC19
## Standard deviation
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion
                          0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                             PC22
                                     PC23
                                            PC24
                                                     PC25
                                                             PC26
                                                                     PC27
                                                                             PC28
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Standard deviation
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
                          0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
## Cumulative Proportion
##
                             PC29
                                     PC30
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

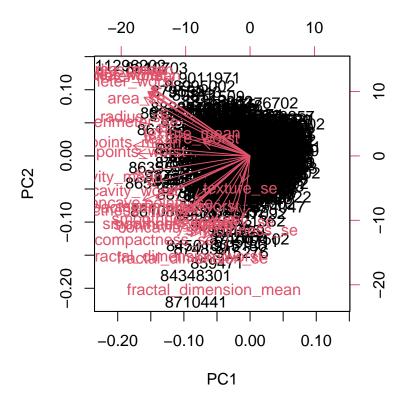
- Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?
- 44.27% of the original variance is captured by the PC1.
 - Q5. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

Three PCs

Q6. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

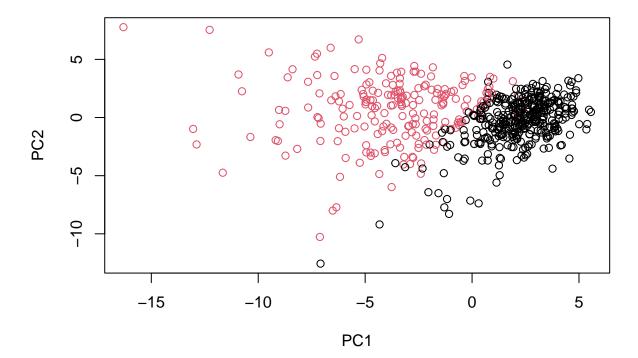
seven PCs

Q7. What stands out to you about this plot? Is it easy or difficult to understand? Why?



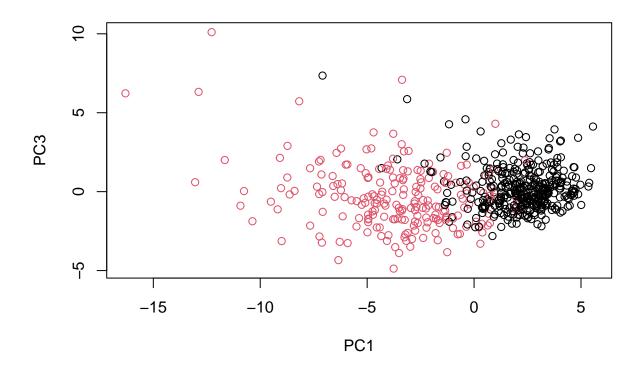
Rownames are used as the plotting character for biplots like this one which can make trends rather hard to see.

```
# Scatter plot observations by components 1 and 2
plot(wisc.pr$x[,1:2], col = diagnosis, xlab = "PC1", ylab = "PC2")
```



Q8. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?

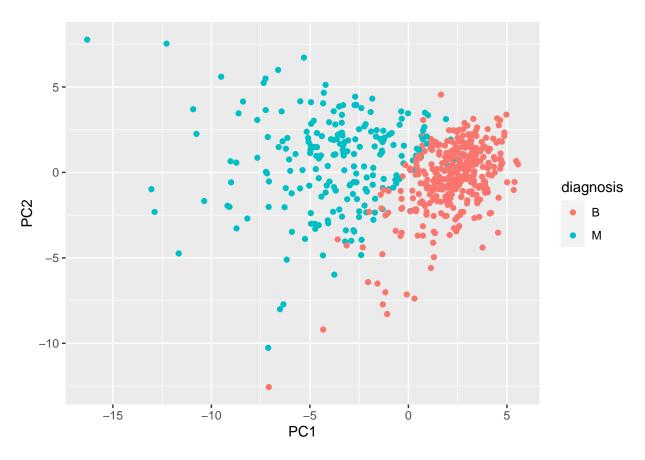
```
plot(wisc.pr$x[,c(1, 3)], col = diagnosis, xlab = "PC1", ylab = "PC3")
```



```
# Create a data.frame for ggplot
df <- as.data.frame(wisc.pr$x)
df$diagnosis <- diagnosis

# Load the ggplot2 package
library(ggplot2)

# Make a scatter plot colored by diagnosis
ggplot(df) +
   aes(PC1, PC2, col=diagnosis) +
   geom_point()</pre>
```



```
# Calculate variance of each component
pr.var <- wisc.pr$sdev^2
head(pr.var)</pre>
```

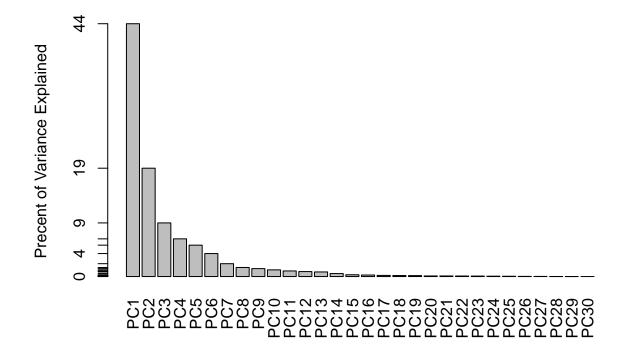
[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357

```
# Variance explained by each principal component: pue
pve <- pr.var/sum(pr.var)

# Plot variance explained for each principal component
plot(pve, xlab = "Principal Component", ylab = "Proportion of Variance Explained", ylim = c(0, 1), type</pre>
```



```
# Alternative scree plot of the same data, note data driven y-axis
barplot(pve, ylab = "Precent of Variance Explained", names.arg=paste0("PC",1:length(pve)), las=2, axes
axis(2, at=pve, labels=round(pve,2)*100)
```



Q9. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean?

```
wisc.pr$rotation[,1]["concave.points_mean"]
```

```
## concave.points_mean
## -0.2608538
```

Q10. What is the minimum number of principal components required to explain 80% of the variance of the data?

summary(wisc.pr)

```
## Importance of components:
##
                             PC1
                                     PC2
                                             PC3
                                                     PC4
                                                             PC5
                                                                      PC6
                                                                              PC7
## Standard deviation
                          3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
  Cumulative Proportion
                          0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
##
                              PC8
                                      PC9
                                             PC10
                                                    PC11
                                                            PC12
                                                                     PC13
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Standard deviation
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
                          0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
##
  Cumulative Proportion
##
                             PC15
                                      PC16
                                              PC17
                                                      PC18
                                                              PC19
                                                                       PC20
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Standard deviation
```

```
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                                     PC23
                                                            PC26
##
                             PC22
                                            PC24
                                                    PC25
                                                                    PC27
## Standard deviation
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
## Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                             PC29
                                     PC30
                          0.02736 0.01153
## Standard deviation
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

We need at least 5 of principal components to explain 80% of the variance of the data.

3. Hierarchical clustering

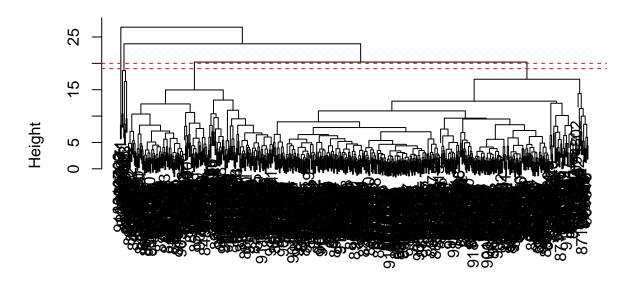
```
# Scale the wisc.data data using the "scale()" function
data.scaled <- scale(wisc.data)

data.dist <- dist(data.scaled)

wisc.hclust <- hclust(data.dist, method="complete")</pre>
```

Q11. Using the plot() and abline() functions, what is the height at which the clustering model has 4 clusters?

```
plot(wisc.hclust)
abline(h=c(19, 20), col="red", lty=2)
```



data.dist hclust (*, "complete")

The clustering model has 4 clusters at the heights of 19 and 20.

```
wisc.hclust.clusters <- cutree(wisc.hclust, k=4)
table(wisc.hclust.clusters, diagnosis)</pre>
```

```
## diagnosis
## wisc.hclust.clusters B M
## 1 12 165
## 2 2 5 5
## 3 343 40
## 4 0 2
```

Q12. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

```
for (i in 2:10) {
  clusters <- cutree(wisc.hclust, k=i)
  print(table(clusters, diagnosis))
}</pre>
```

```
## diagnosis
## clusters B M
## 1 357 210
## 2 0 2
```

```
## diagnosis
## clusters B M
  1 355 205
##
##
       2 2 5
       3 0 2
##
##
      diagnosis
## clusters B M
       1 12 165
##
       2 2 5
##
##
       3 343 40
##
       4 0 2
##
       diagnosis
## clusters B M
     1 12 165
##
##
       2 0 5
       3 343 40
##
##
       4 2 0
       5 0 2
##
       diagnosis
##
## clusters B M
       1 12 165
##
##
       2 0 5
##
       3 331 39
       4 2 0
##
##
       5 12 1
##
       6 0 2
##
       diagnosis
## clusters B M
##
       1 12 165
##
       2 0 3
       3 331 39
##
##
       4 2 0
##
       5 12 1
##
       6 0
              2
       7 0
              2
##
##
        diagnosis
## clusters B M
       1 12 86
##
       2 0 79
##
       3 0 3
##
       4 331 39
##
##
       5 2 0
       6 12
##
             1
##
       7 0
              2
       8 0
              2
##
##
       diagnosis
## clusters B M
##
       1 12 86
##
       2 0 79
       3 0 3
##
##
       4 331 39
       5 2 0
##
##
       6 12 0
##
       7 0 2
```

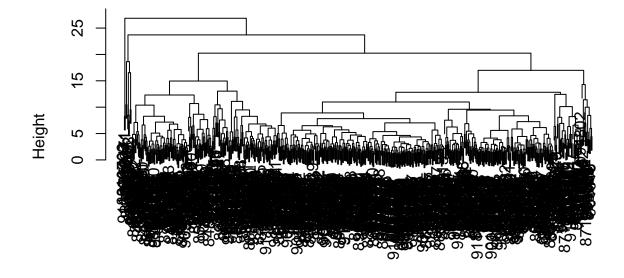
```
##
##
                      1
##
                 В
                     М
##
   clusters
##
          1
                    86
##
          2
                    59
##
          3
                     3
              331
                    39
##
##
          5
                 0
                    20
##
          6
                 2
                     0
##
               12
                     0
                     2
##
##
                     2
          10
##
```

I think that cutting into 4 clusters is the best in regard to diagnosis.

Q13. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

```
wisc.hclust.complete <- hclust(data.dist, method="complete")
plot(wisc.hclust.complete)</pre>
```

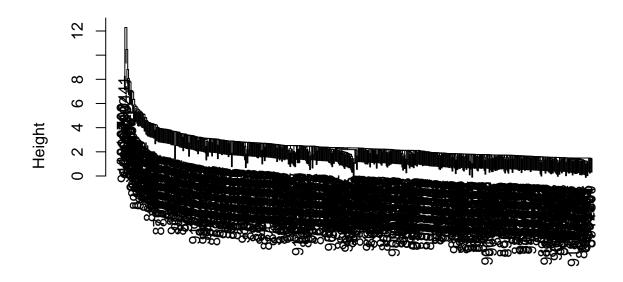
Cluster Dendrogram



data.dist hclust (*, "complete")

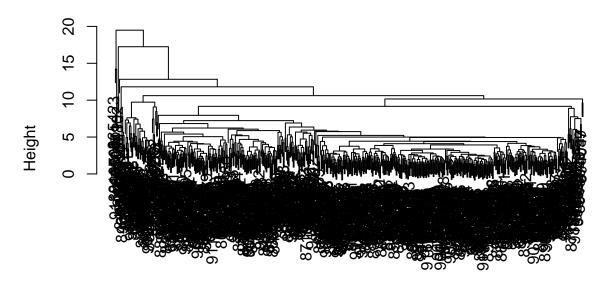
wisc.hclust.single <- hclust(data.dist, method="single")
plot(wisc.hclust.single)</pre>

Cluster Dendrogram



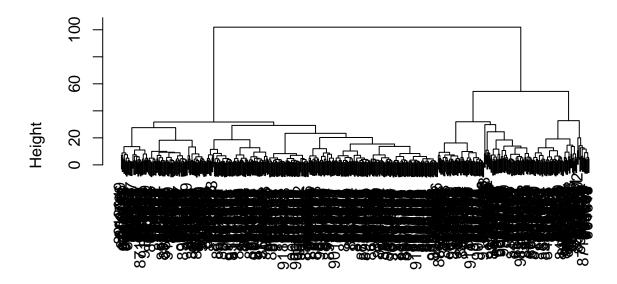
data.dist hclust (*, "single")

wisc.hclust.average <- hclust(data.dist, method="average")
plot(wisc.hclust.average)</pre>



data.dist hclust (*, "average")

wisc.hclust.ward.D2 <- hclust(data.dist, method="ward.D2")
plot(wisc.hclust.ward.D2)</pre>



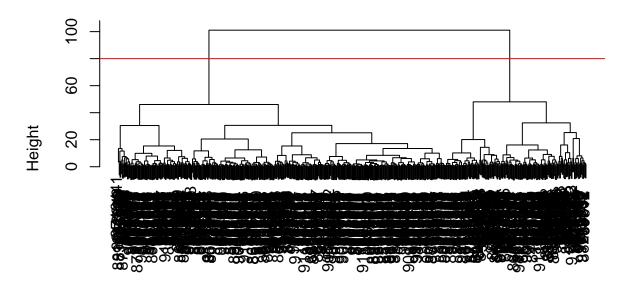
data.dist hclust (*, "ward.D2")

I think that "ward.D2" method gives me favorite results compared with others. I can get a good cluster vs diagnoses match only with the 2 clusters using this method.

4. OPTIONAL: K-means clustering

5. Combining methods

```
wisc.pr.hclust <- hclust(dist(wisc.pr$x[,1:4]), method="ward.D2")
plot(wisc.pr.hclust)
abline(h=80, col="red")</pre>
```



dist(wisc.pr\$x[, 1:4]) hclust (*, "ward.D2")

Let's find out cluster membership vector by cutting this tree into k=2 group.

```
grps <- cutree(wisc.pr.hclust, k=2)
table(grps)

## grps
## 1 2
## 171 398</pre>
```

Now let's compare to the expert M and B vector.

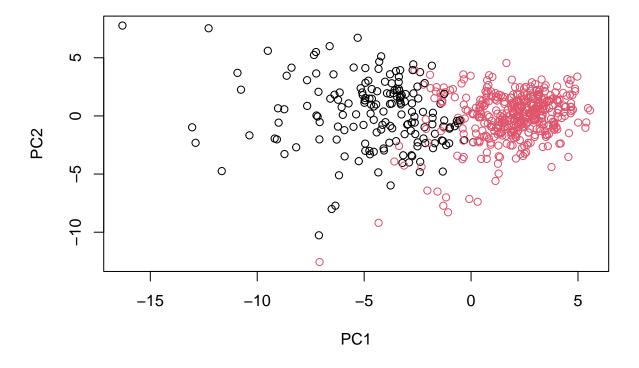
table(diagnosis)

```
## diagnosis
## B M
## 357 212
```

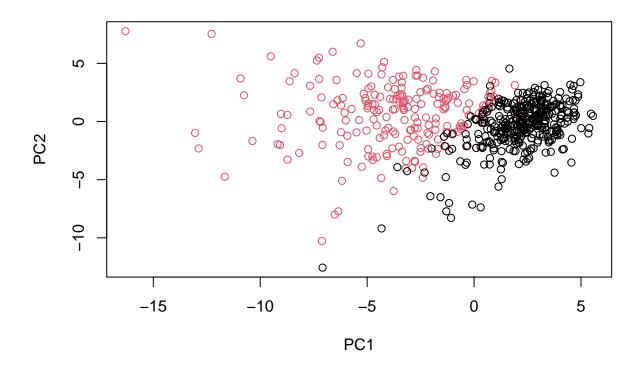
We can do a cross-table by giving the 'table()' function two inputs.

table(grps, diagnosis)

```
## diagnosis
## grps B M
## 1 6 165
## 2 351 47
```



plot(wisc.pr\$x[,1:2], col=diagnosis)



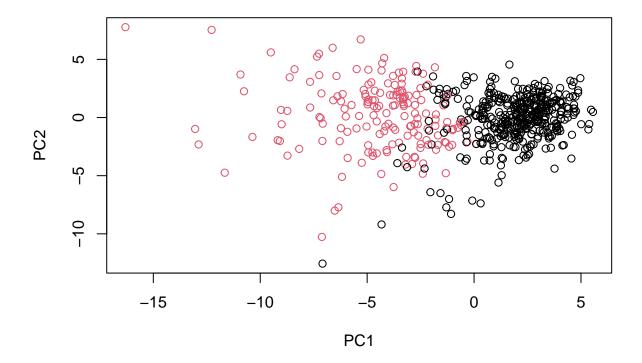
```
g <- as.factor(grps)
levels(g)

## [1] "1" "2"

g <- relevel(g,2)
levels(g)

## [1] "2" "1"

plot(wisc.pr$x[,1:2], col=g)</pre>
```



Q15. How well does the newly created model with four clusters separate out the two diagnoses?

table(grps, diagnosis)

```
## diagnosis
## grps B M
## 1 6 165
## 2 351 47
```

Q16. How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table() function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

table(wisc.hclust.clusters, diagnosis)

```
##
                          diagnosis
##
                             В
   wisc.hclust.clusters
                                  М
##
                            12 165
                         2
                                  5
##
                              2
                         3
##
                           343
                                 40
##
                              0
                                  2
```

(As section 4 is optional, I do not have the output of the k-means model)

6. Sensitivity/Specificity

Accuracy, essentially how many did we get correct?

```
(165+351)/nrow(wisc.data)
```

```
## [1] 0.9068541
```

Q17. Which of your analysis procedures resulted in a clustering model with the best specificity? How about sensitivity?

Sensitivity

```
(165)/(165+47)
```

```
## [1] 0.7783019
```

Specificity

```
(351)/(351+47)
```

```
## [1] 0.8819095
```

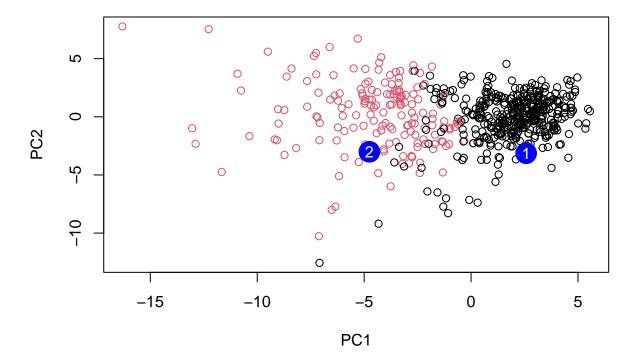
I just calculated the specificity and the sensitivity of the model with the "ward.D2" method.

7. Prediction

```
#url <- "new_samples.csv"
url <- "https://tinyurl.com/new-samples-CSV"
new <- read.csv(url)
npc <- predict(wisc.pr, newdata=new)
npc</pre>
```

```
##
              PC1
                        PC2
                                   PC3
                                              PC4
                                                         PC5
                                                                    PC6
                                                                               PC7
## [1,] 2.576616 -3.135913 1.3990492 -0.7631950 2.781648 -0.8150185 -0.3959098
  [2,] -4.754928 -3.009033 -0.1660946 -0.6052952 -1.140698 -1.2189945
               PC8
                         PC9
                                   PC10
                                             PC11
                                                       PC12
                                                                  PC13
## [1,] -0.2307350 0.1029569 -0.9272861 0.3411457
                                                   0.375921 0.1610764 1.187882
## [2,] -0.3307423 0.5281896 -0.4855301 0.7173233 -1.185917 0.5893856 0.303029
##
             PC15
                        PC16
                                    PC17
                                                PC18
                                                             PC19
## [1,] 0.3216974 -0.1743616 -0.07875393 -0.11207028 -0.08802955 -0.2495216
  [2,] 0.1299153 0.1448061 -0.40509706
                                                      0.25591230 -0.4289500
                                         0.06565549
                         PC22
                                    PC23
                                               PC24
                                                           PC25
## [1,] 0.1228233 0.09358453 0.08347651 0.1223396
                                                     0.02124121
                                                                 0.078884581
## [2,] -0.1224776 0.01732146 0.06316631 -0.2338618 -0.20755948 -0.009833238
##
                PC27
                            PC28
                                         PC29
                                                      PC30
## [1,] 0.220199544 -0.02946023 -0.015620933 0.005269029
## [2,] -0.001134152  0.09638361  0.002795349 -0.019015820
```

```
plot(wisc.pr$x[,1:2], col=g)
points(npc[,1], npc[,2], col="blue", pch=16, cex=3)
text(npc[,1], npc[,2], c(1,2), col="white")
```



Q18. Which of these new patients should we prioritize for follow up based on your results?

Based on the results, the patients in the group 2 should be prioritized for follow up.