CS 11 Haskell track: lecture 2

- This week:
 - More basics
 - Algebraic datatypes
 - Polymorphism
 - List functions
 - List comprehensions
 - Type synonyms
 - Introduction to input/output (I/O)
 - Compiling standalone programs

let and where (1)

```
let:
factorial :: Int -> Int
factorial n =
  let iter n r =
       if n == 0 then r
       else iter (n-1) (n*r)
  in
       iter n 1
```

let and where (2)

```
where:
factorial :: Int -> Int
factorial n = iter n 1
  where
   iter n r =
    if n == 0 then r
   else iter (n-1) (n*r)
```

let and where (3)

```
where (nicer):
factorial :: Int -> Int
factorial n = iter n 1
  where
  iter 0 r = r
  iter n r = iter (n-1) (n*r)
```

Lambda (λ) expressions

Used to create anonymous functions

```
\<pattern> -> <expr>
```

Usually just e.g.

```
\x -> 2*x
\x y -> x + y
```

Pattern example:

```
map (\(x, y) -> x + y)

[(1, 2), (4, 1), (-3, 20)]

\rightarrow [3, 5, 17]
```

Operator slices

Instead of writing

```
\x \rightarrow x + 1
```

you can just write:

```
(+1)
```

Similarly, instead of writing

```
\x \rightarrow 2 * x
```

you can write:

```
(2*)
```

Example:

```
map (2*) [1..5] \rightarrow [2,4,6,8,10]
```

case expressions (1)

- Used for pattern matches within expressions
- Syntax:

```
case <expr> of
  <pattern1> -> <expr1>
  <pattern2> -> <expr2>
...
```

- If want a default, use _ (wildcard) as last pattern
- matches anything and throws the value away

case expressions (2)

Example:

```
zeros :: [Int] -> [Int]
zeros lst =
  case lst of
  (_ : rest) -> 0 : zeros rest
  [] -> []
```

- (Not terribly useful)
- Could also use pattern matching on function itself

Algebraic datatypes (1)

- Often want to define own data types to express the structure of some kind of data
- Often the data can be in one of several alternative forms
- Create an algebraic datatype for this
- Many already provided in standard library
 - AKA the Prelude

Algebraic datatypes (2)

Example:

```
data MaybeInt = NoInt | AnInt Int
let (x, y, z) = (NoInt, AnInt 2, AnInt 5)
```

- N.B. type names and data constructor names must start with capital letter!
- Type of (x, y, z)?
- (MaybeInt, MaybeInt, MaybeInt)

Algebraic datatypes (3)

- N.B. Can't define new datatypes in ghci
- Best to put into file and load using :1 file.hs
- Might want to have a more general type than MaybeInt
 - the Maybe concept works just as well for any type
 - expresses concept of "not sure if will have anything, but if we do it'll be of this type"
- Don't want to have to define MaybeInt, MaybeFloat, MaybeString...
- All have same structure

Polymorphism (1)

- Data types can be parameterized over other types
- So for Maybe example we have (built-in):

```
data Maybe a = Nothing | Just a
```

- Here a is a type variable
- Written with an initial lower-case letter

Polymorphism (2)

- Types:
 - Nothing :: Maybe a
 - Just 10 :: Maybe Int
 - Just "hi there!" :: Maybe String
 - Just :: a -> Maybe a
- Parameterized type constructors are also functions!

```
map Just [1..5]

→ [Just 1, Just 2, ..., Just 5]
```

Example

```
length :: [a] \rightarrow Int
length [] = 0
length (x:xs) = 1 + length xs
```

Works for any list

More pattern matching

Pattern matching on algebraic data types:

```
foo :: Maybe Int -> Int
foo Nothing = 0
foo (Just x) = 1 + x
bar :: Maybe (Maybe String) -> String
bar Nothing = "None"
bar (Just Nothing) = "Sorta"
bar (Just (Just x)) = "Yes: " ++ x
-- N.B. ++ concatenates lists
```

Lists

Lists behave as if they were defined like this:

```
-- WARNING: Bogus pseudo-Haskell: data [a] = [] | a : [a]
```

- Note that (:) is a data constructor just like Just
- Pattern matching on lists:

```
head :: [a] -> Maybe a
head (x : _) = Just x
head [] = Nothing
```

N.B. the parentheses are important!

As-patterns (@-patterns)

- You can assign a name to a pattern while also matching its parts
- Example:

```
foo :: Maybe Int -> Maybe Int
foo x@(Just y) = x
foo Nothing = Nothing
```

 This looks useless now, but becomes useful when patterns get more complicated

List functions and the Prelude

- The Haskell Prelude is where the most basic functions are defined
- Always available to the programmer
- Includes many useful list functions
- Often fairly obvious what they do from the type signature

Useful list functions

Examples:

```
(++) :: [a] -> [a] -> [a] -- list concat
map :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
head :: [a] -> a -- not like one we defined
foldr :: (a -> b -> b) -> b -> [a] -> b
repeat :: a -> [a]
cycle :: [a] -> [a]
```

map

map f lst applies f to each element of lst, returning the results

```
map :: (a \rightarrow b) \rightarrow [a] \rightarrow [b]

map f (x:xs) = f x : map f xs

map _ [] = []

map (/2) [1...3] \rightarrow [0.5, 1.0, 1.5]
```

foldr ("fold right")

foldr op z [x1,x2, ... xn] reduces the list by computing

```
x1 `op` (x2 `op` ... (xn `op` z))
```

Definition left as "exercise for student"

```
sum :: [Int] -> Int
sum = foldr (+) 0
```

Pop quiz: what is foldr (:) [] ?

More list functions (1)

```
concat :: [[a]] -> [a]
take :: Int -> [a] -> [a]
drop :: Int -> [a] -> [a]
■ elem :: a -> [a] -> Bool
-- usually written as
-- 5 `elem` [1..10]
zip :: [a] -> [b] -> [(a, b)]
```

More list functions (2)

- Many more list functions in Prelude
- Use Prelude functions instead of reimplementing them yourself
 - read Prelude docs (linked from web pages)

List comprehensions (1)

 List comprehensions are a convenient way to create lists with particular properties

```
fibs :: [Integer]
fibs = 0:1:[x+y|(x,y) <- zip fibs (tail fibs)]</pre>
```

- Infinite list of fibonacci numbers
- To get first 20, do

```
take 20 fibs
```

List comprehensions (2)

General structure:

```
[<expr> | pattern <- source ...,
filter ...]</pre>
```

Examples:

```
[x \mid x < - [1..1000], x \mod 2 == 1]
[(x, y) \mid x < - [1..10], y < - [1..10],
x + y == 10]
```

Type synonyms

- Can create a synonym for a type
- Compiler can't always figure out the right name to use (e.g. in ghci), but it tries
- Examples:

```
type String = [Char] -- in the Prelude
type Label = String
type Point = (Double, Double)
```

Introduction to I/O (1)

- Input/output is odd in Haskell
- Can't have side effects!
- Input/output actions are values of type
 io a, where a is the type of the action's result
- Actions with no useful result have type IO ()
 - () is the sole instance of the unit type

Introduction to I/O (2)

Examples:

```
putStr :: String -> IO ()
putStrLn :: String -> IO ()
getLine :: IO String
print :: a -> IO ()
```

- Our first encounter with dreaded Monads
 - Much more to say about this in future
- Entire program is a computation of type IO ()

Compiling standalone programs

- Create a main function with type IO ()
- Compile the program with
- % ghc -o progname filename.hs
- Run the program:
- % progname
- Hit ctrl-C if the program doesn't terminate

Next week

- Much more on I/O
- Type classes