A* Shortest Path Search

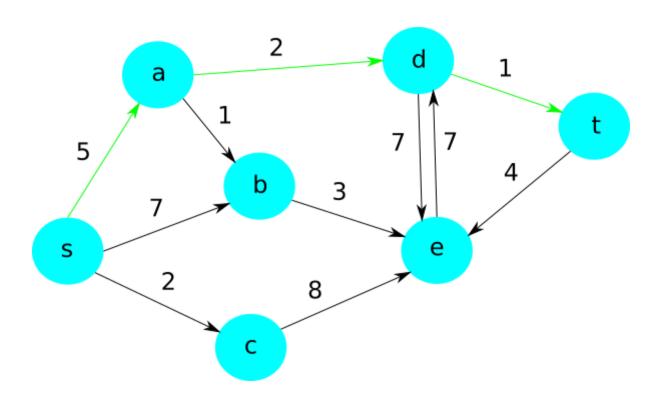
Course 4, Module 3, Lesson 3



Learning Objectives

- Understand what admissible heuristics are in the context of graph search
- Understand how to use the Euclidean heuristic to improve our mission planning speed in practice
- Implement the A* search algorithm, leveraging the Euclidean heuristic
- Understand how to apply A* search to variants on the mission planning problem involving time instead of distance

Recall: Dijkstra's for Weighted Graph



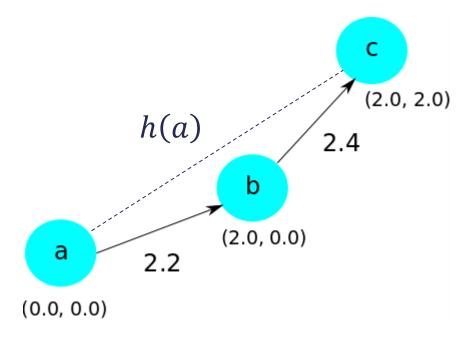
Euclidean Heuristic

- Exploits structure of the problem
- Fast to calculate
- Straight-line distance between two vertices is a useful estimate of true distance along the graph

$$h(v) = ||t - v||$$

Euclidean Heuristic - Example

$$h(a) = \sqrt{2^2 + 2^2} = 2.828$$



A* Algorithm

A* Algorithm

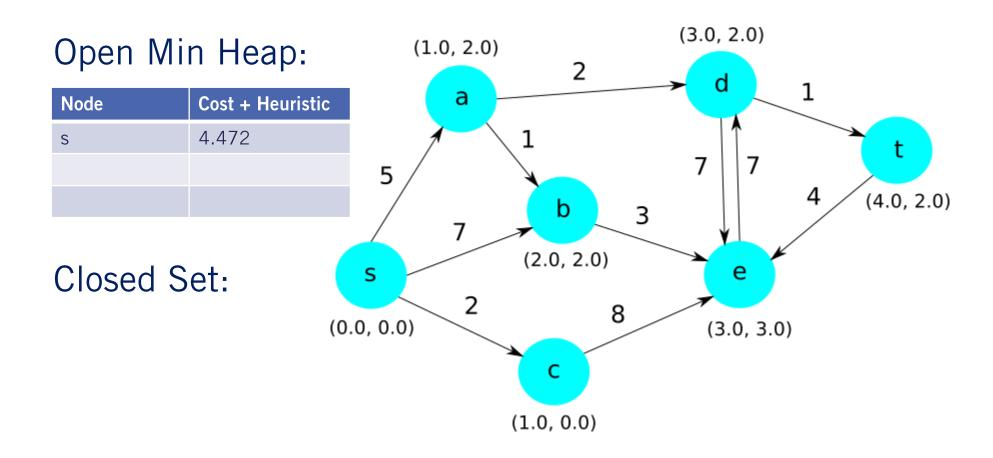
Algorithm A*(G,s,t)

```
open ← MinHeap()
       closed \leftarrow Set()
       predecessors ← Dict()
       open. push(s, 0)
5.
       while ! open. isEmpty() do
6.
          u, uCost \leftarrow open.pop()
         if isGoal(u) then
8.
            return extractPath(u, predecessors)
9.
         for all v \in u. successors()
10.
             if v \in \text{closed then}
11.
                continue
12.
            uvCost \leftarrow edgeCost(G, u, v)
13.
            if v \in \text{open then}
14.
                if uCost + uvCost + h(v) < open[v] then
15.
                    open[v] \leftarrow uCost + uvCost + h(v)
16.
                    costs[v] \leftarrow uCost + uvCost
17.
                    predecessors [v] \leftarrow u
18.
            else
19.
                open. push(v, uCost + uvCost)
20.
                costs[v] \leftarrow uCost + uvCost
21.
                predecessors [v] \leftarrow u
22.
          closed. add(u)
```

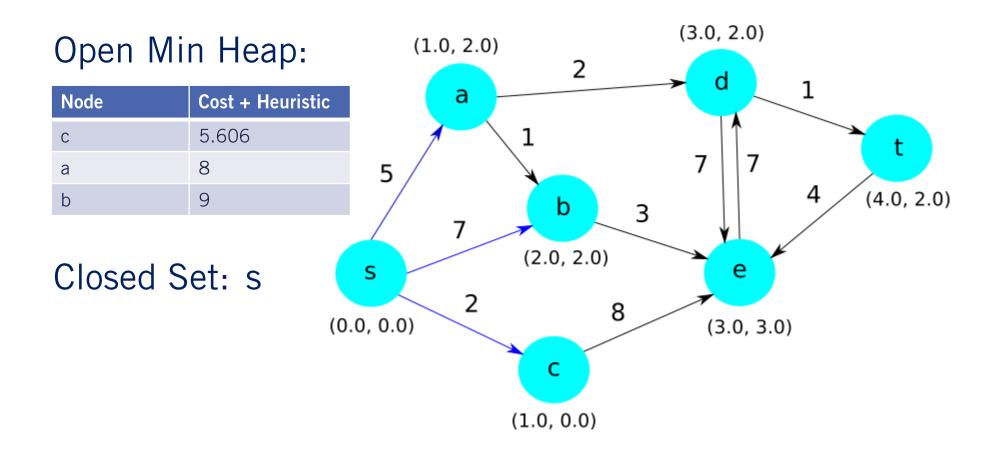
A* Algorithm

```
if v \in \text{open then}
              if uCost + uvCost + h(v) < open [v] then
                  open[v] \leftarrow uCost + uvCost + h(v)
3.
4.
                  costs[v] \leftarrow uCost + uvCost
5.
                  predecessors[v] \leftarrow u
6.
          else
              open. push(v, uCost + uvCost)
8.
              costs[v] \leftarrow uCost + uvCost
              predecessors [v] \leftarrow u
```

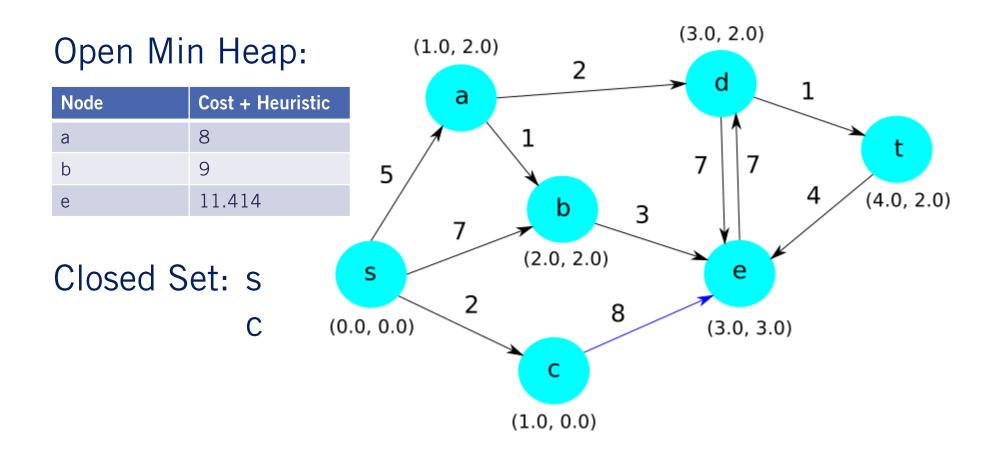
Example - Origin Node



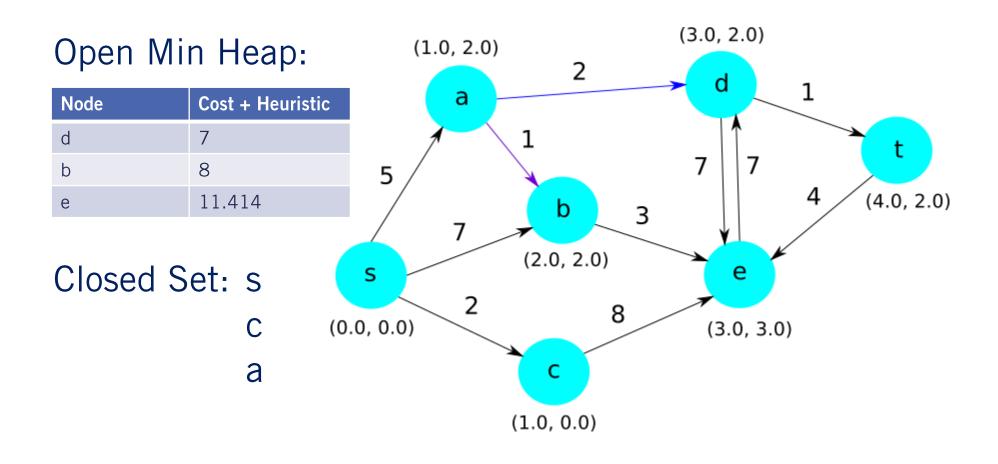
Example - Processing s



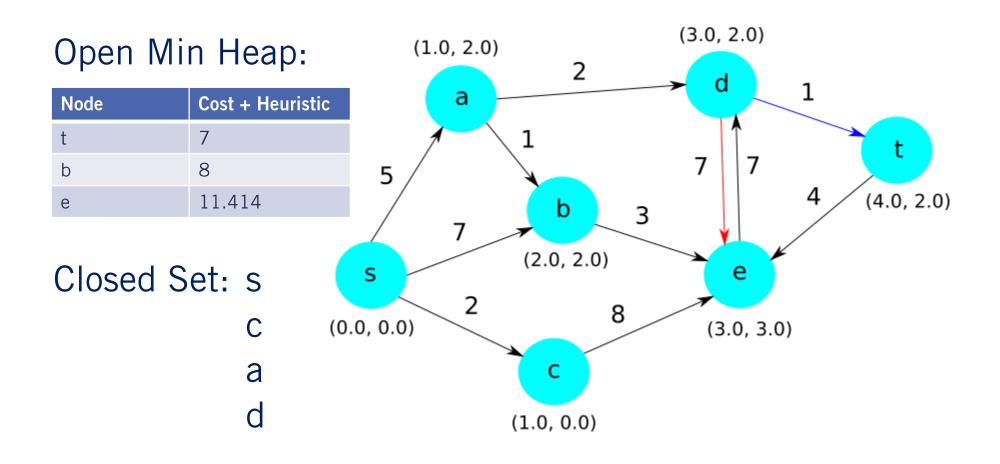
Example - Processing c



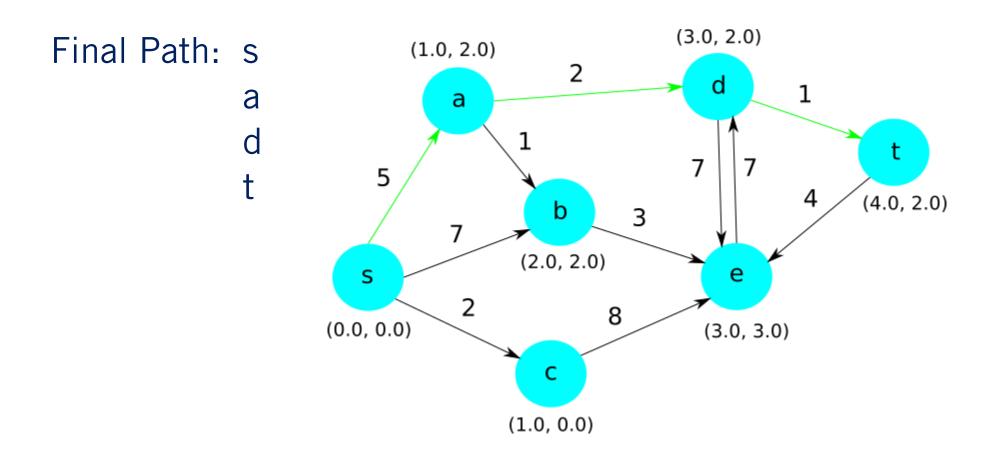
Example - Processing a



Example - Processing d



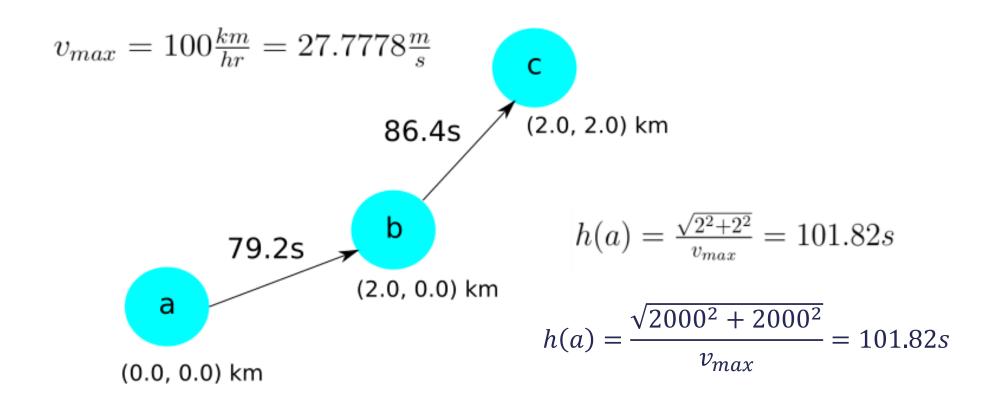
Example - Final Path



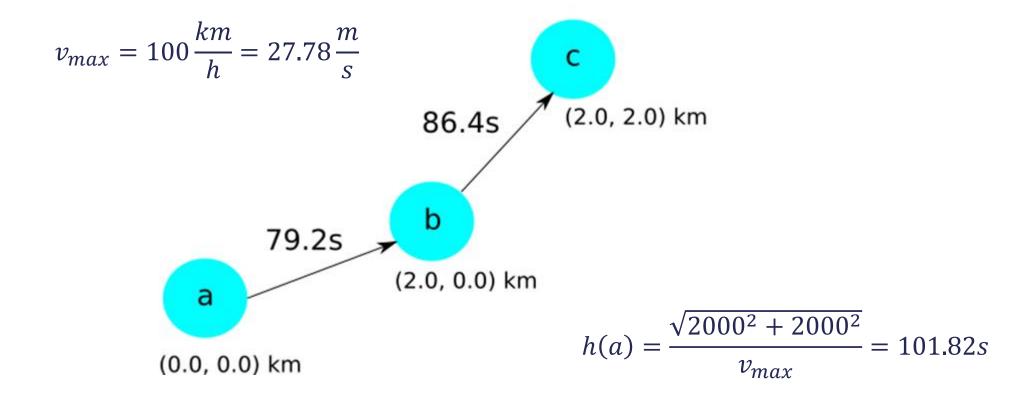
Extensions to Other Factors

- Traffic, speed limits, and weather affect mission planning
- Time rather than distance is better at capturing these factors
- Replace distance edge weights with time estimates

Example



Example



Summary

- Introduced Euclidean heuristic, showed it was admissible to our mission planning problem
- Walked through the A* search algorithm
- Discussed how to modify the heuristic to handle travel time rather than distance in our search



