Longitudinal Vehicle Model

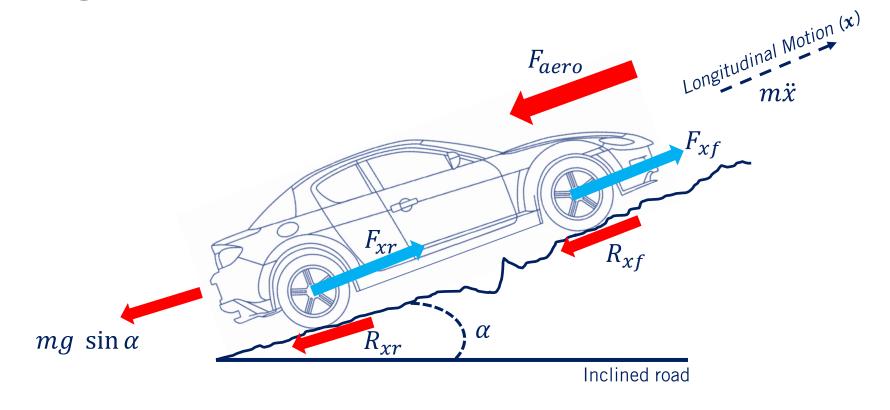
Course 1, Module 4, Lesson 4



Learning Objectives

- Define dynamic force balance on a vehicle
- Describe powertrain component models
- Connect models to create a full longitudinal motion model

Longitudinal Vehicle Model



Vehicle acceleration Front & rear tire forces forces Front & rear road rolling acceleration Front & rear road rolling to the road inclination $m \ddot{x} = F_{\chi f} + F_{\chi \gamma} - F_{ae\gamma o} - R_{\chi f} - R_{\chi \gamma} - mg \sin \alpha$

Simplified Longitudinal Dynamics

The full longitudinal dynamics

$$m\ddot{x} = F_{xf} + F_{xr} - F_{aero} - R_{xf} - R_{xr} - mg \sin \alpha$$

- Let F_x total longitudinal force: $F_x = F_{xf} + F_{xr}$
- Let R_x total rolling resistance: $R_x = R_{xf} + R_{xr}$
- Assume α is a small angle: $\sin \alpha = \alpha$
- Then the simplified longitudinal dynamics become

$$m\ddot{x} = F_x - F_{aero} - R_x - mg lpha$$
 Inertial Term Traction Force Total Resistant Forces (F_{Load})

Simple Resistance Force Models

Total resistance load:

$$F_{load} = F_{aero} + R_x + mg\alpha$$

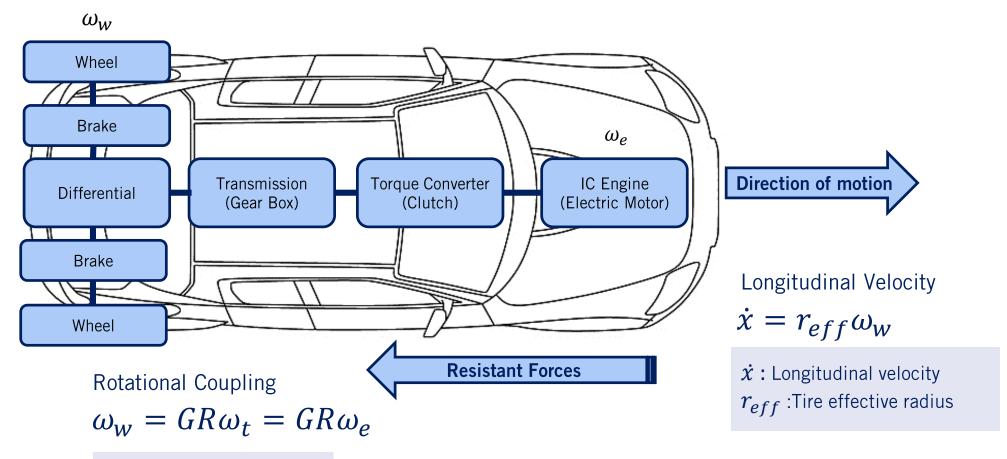
 The aerodynamic force can depend on air density, frontal area, on the speed of the vehicle

$$F_{aero} = \frac{1}{2} C_a \rho A \dot{x}^2 = C_a \dot{x}^2$$

 The rolling resistance can depend on the tire normal force, tire pressures and vehicle speed

$$R_x = N(\hat{c}_{r,0} + \hat{c}_{r,1}|\dot{x}| + \hat{c}_{r,2}\dot{x}^2) \approx c_{r,1}|\dot{x}|$$

Powertrain Modeling

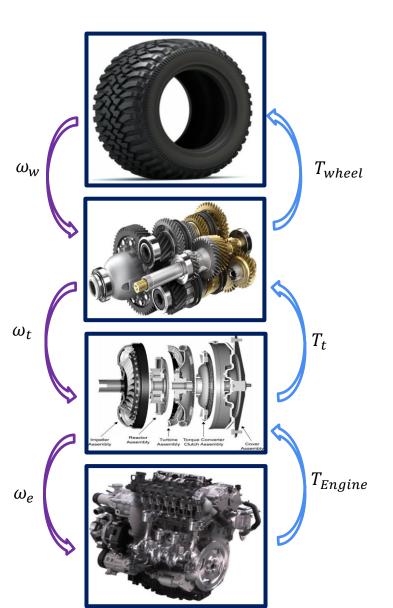


 ω_{w} : wheel angular speed ω_{t} : turbine angular speed ω_{e} : engine angular speed GR: Combined gear ratios

Longitudinal acceleration

$$\ddot{x} = r_{eff} GR \dot{\omega}_e$$

Power Flow in Powertrain



Wheel

$$I_w \dot{\omega}_w = T_{wheel} - r_{eff} F_x$$
$$T_{wheel} = I_w \dot{\omega}_w + r_{eff} F_x$$

Transmission

$$I_t \dot{\omega}_t = T_t - (GR)T_{wheel}$$

$$I_t \dot{\omega}_t = T_t - GR(I_w \dot{\omega}_w + r_{eff}F_x)$$

Torque Converter

$$\omega_t = \omega_e$$

$$T_t = (I_t + I_w GR^2) \dot{\omega}_e + GRr_{eff} F_x$$

Engine

$$I_e \dot{\omega}_e = T_{Engine} - T_t$$

$$I_e \dot{\omega}_e = T_{Engine} - (I_t + I_w GR^2) \dot{\omega}_e - GRr_{eff} F_x$$

Engine Dynamics

Tire force in terms of inertia and load force:

$$F_x = m\ddot{x} + F_{load} = mr_{eff}GR\dot{\omega}_e + F_{load}$$

Combining with our engine dynamics model yields:

$$(I_e + I_t + I_w GR^2 + m(GR^2)r_{eff}^2)\dot{\omega}_e = T_{Engine} - (GR)(r_{eff}F_{Load})$$

$$J_e$$

Finally, the engine dynamic model simplifies to

$$J_e \dot{\omega}_e = T_{Engine} - (GR)(r_{eff}F_{Load})$$

Total Load Torque (T_{Load})

Summary

What we have learned from this lesson?

- Vehicle longitudinal dynamics, resistance forces
- Powertrain components and component models
- Unified longitudinal dynamic model for speed control

What is next?

The lateral dynamics of a vehicle