# **Geometric Steering Control I – Pure Pursuit**

Course 1, Module 6, Lesson 2

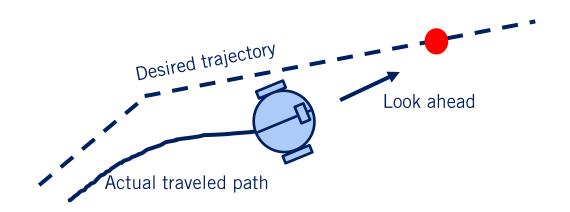


## **Learning Objectives**

- In this video, you'll
  - Define the concept of a geometric path tracking controller
  - Develop a pure pursuit controller for path tracking

# **Geometric path tracking**

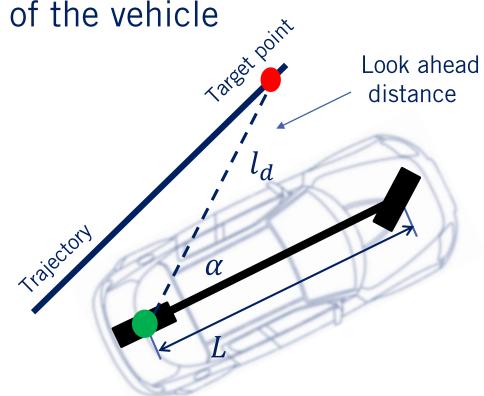
- One of the most popular classes of path tracking in robotics and autonomous vehicle
  - Exploits geometric relationship between the vehicle and the path resulting in compact control law solutions to the path tracking problem
  - Use of reference point on path to measure error of the vehicle, can be ahead of the vehicle



# **Pure pursuit**

 Pure pursuit method consists of geometrically calculating the trajectory curvature

• Connect the centre of rear axle location to a target point on the path ahead of the vehicle



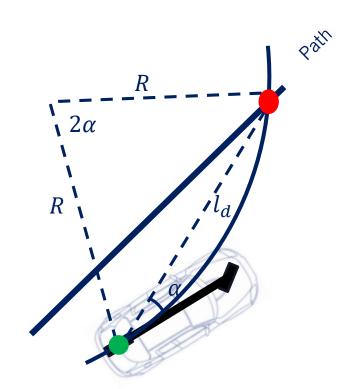
- Steering angle determined by target point location and angle between the vehicle's heading direction and lookahead direction.
- From the *law of sines*:

$$\frac{l_d}{\sin 2\alpha} = \frac{R}{\sin\left(\frac{\pi}{2} - \alpha\right)}$$

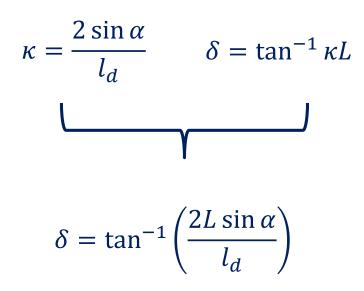
$$\frac{l_d}{2\sin\alpha\cos\alpha} = \frac{R}{\cos(\alpha)}$$

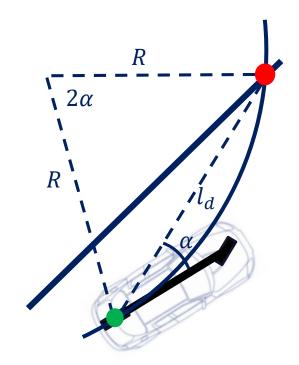
$$\frac{l_d}{\sin \alpha} = 2R$$

$$\kappa = \frac{1}{R} = \frac{2 \sin \alpha}{l_d}$$
 Path curvature



• Using the bicycle model the steering angle is calculated as:



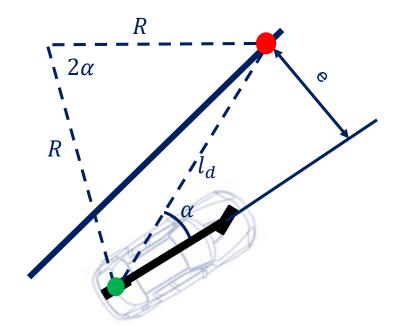


• Crosstrack error (e) is defined here as the lateral distance between the heading vector and the target point so:

$$\sin \alpha = \frac{e}{l_d}$$

$$\kappa = \frac{2 \sin \alpha}{l_d}$$

$$\kappa = \frac{2}{l_d^2} e$$



- Pure pursuit is a proportional controller of the steering angle operating on a crosstrack error some look ahead distance in front of the vehicle
- The proportional gain  $^2/_{l_d^2}$  can be tuned at different speeds (the  $l_d$  being assigned as a function of vehicle speed)

• Lookahead  $l_d$  is assigned as a linear function of vehicle speed:  $l_d = K_{dd}v_f$ 

$$\delta = \tan^{-1} \left( \frac{2L \sin \alpha}{l_d} \right) \qquad \kappa = \frac{2}{l_d^2} e$$

$$\delta = \tan^{-1} \left( \frac{2L \sin \alpha}{K_{dd} v_f} \right)$$
Forward velocity

# **Summary**

What we have learned from this lesson:

 The concept of geometrical path tracking and the pure pursuit method

#### What is next?

 A second geometrical path tracking method, the Stanley control approach