svm

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0.1 This is the svm workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement a linear support vector machine.

Please print out the workbook entirely when completed.

We thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu). These are the functions in the cs231n folders and includes code to preprocess and show the images. The classifiers used are based off of code prepared for CS 231n as well.

The goal of this workbook is to give you experience with training an SVM classifier via gradient descent.

0.2 Importing libraries and data setup

```
[511]: # Set the path to the CIFAR-10 data
cifar10_dir = 'cifar-10-batches-py' # You need to update this line
X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test data.
print('Training data shape: ', X_train.shape)
print('Training labels shape: ', y_train.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

```
Training data shape: (50000, 32, 32, 3)
      Training labels shape: (50000,)
      Test data shape: (10000, 32, 32, 3)
      Test labels shape: (10000,)
[512]: # Visualize some examples from the dataset.
      # We show a few examples of training images from each class.
      classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', _
       num_classes = len(classes)
      samples_per_class = 7
      for y, cls in enumerate(classes):
          idxs = np.flatnonzero(y_train == y)
          idxs = np.random.choice(idxs, samples_per_class, replace=False)
          for i, idx in enumerate(idxs):
              plt_idx = i * num_classes + y + 1
              plt.subplot(samples_per_class, num_classes, plt_idx)
              plt.imshow(X_train[idx].astype('uint8'))
              plt.axis('off')
              if i == 0:
                  plt.title(cls)
      plt.show()
```



```
[513]: | # Split the data into train, val, and test sets. In addition we will
       # create a small development set as a subset of the training data;
       # we can use this for development so our code runs faster.
       num_training = 49000
       num validation = 1000
       num_test = 1000
       num dev = 500
       # Our validation set will be num validation points from the original
       # training set.
       mask = range(num training, num training + num validation)
       X_val = X_train[mask]
       y_val = y_train[mask]
       # Our training set will be the first num train points from the original
       # training set.
       mask = range(num_training)
       X_train = X_train[mask]
       y_train = y_train[mask]
       # We will also make a development set, which is a small subset of
       # the training set.
       mask = np.random.choice(num_training, num_dev, replace=False)
       X dev = X train[mask]
       y_dev = y_train[mask]
       # We use the first num_test points of the original test set as our
       # test set.
       mask = range(num_test)
       X_test = X_test[mask]
       y_test = y_test[mask]
       print('Train data shape: ', X_train.shape)
       print('Train labels shape: ', y_train.shape)
       print('Validation data shape: ', X_val.shape)
       print('Validation labels shape: ', y_val.shape)
       print('Test data shape: ', X_test.shape)
       print('Test labels shape: ', y_test.shape)
       print('Dev data shape: ', X_dev.shape)
       print('Dev labels shape: ', y_dev.shape)
      Train data shape: (49000, 32, 32, 3)
      Train labels shape: (49000,)
      Validation data shape: (1000, 32, 32, 3)
      Validation labels shape: (1000,)
      Test data shape: (1000, 32, 32, 3)
      Test labels shape: (1000,)
      Dev data shape: (500, 32, 32, 3)
```

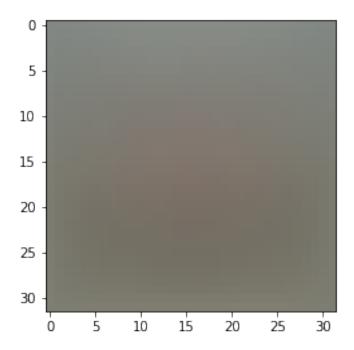
Dev labels shape: (500,)

```
[514]: # Preprocessing: reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
X_val = np.reshape(X_val, (X_val.shape[0], -1))
X_test = np.reshape(X_test, (X_test.shape[0], -1))
X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))

# As a sanity check, print out the shapes of the data
print('Training data shape: ', X_train.shape)
print('Validation data shape: ', X_val.shape)
print('Test data shape: ', X_test.shape)
print('dev data shape: ', X_dev.shape)
```

Training data shape: (49000, 3072) Validation data shape: (1000, 3072) Test data shape: (1000, 3072) dev data shape: (500, 3072)

[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082 131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]



```
[516]: # second: subtract the mean image from train and test data
X_train -= mean_image
X_val -= mean_image
X_test -= mean_image
X_dev -= mean_image

[517]: # third: append the bias dimension of ones (i.e. bias trick) so that our SVM
# only has to worry about optimizing a single weight matrix W.
X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])
print(X_train.shape, X_val.shape, X_test.shape, X_dev.shape)
```

(49000, 3073) (1000, 3073) (1000, 3073) (500, 3073)

0.3 Question:

(1) For the SVM, we perform mean-subtraction on the data. However, for the KNN notebook, we did not. Why?

0.4 Answer:

(1) For SVM mean-subtraction is performed because we want to "center" the data while in KNN we measure distances between points in order to distinguish classes so mean-subtraction would not do anything.

0.5 Training an SVM

The following cells will take you through building an SVM. You will implement its loss function, then subsequently train it with gradient descent. Finally, you will choose the learning rate of gradient descent to optimize its classification performance.

SVM loss

```
[520]: ## Implement the loss function for in the SVM class(nndl/svm.py), svm.loss()
loss = svm.loss(X_train, y_train)
print('The training set loss is {}.'.format(loss))
# If you implemented the loss correctly, it should be 15569.98
```

The training set loss is 15569.977915410187.

[]:

SVM gradient

```
[521]: ## Calculate the gradient of the SVM class.

# For convenience, we'll write one function that computes the loss

# and gradient together. Please modify sum.loss_and_grad(X, y).

# You may copy and paste your loss code from sum.loss() here, and then

# use the appropriate intermediate values to calculate the gradient.

loss, grad = svm.loss_and_grad(X_dev,y_dev)

# Compare your gradient to a numerical gradient check.

# You should see relative gradient errors on the order of 1e-07 or less if you_______

→ implemented the gradient correctly.

svm.grad_check_sparse(X_dev, y_dev, grad)
```

numerical: -3.681664 analytic: -3.681663, relative error: 2.542594e-08 numerical: 4.343144 analytic: 4.343143, relative error: 1.075819e-07 numerical: -3.260883 analytic: -3.260883, relative error: 9.346886e-09

```
numerical: 18.110456 analytic: 18.110456, relative error: 4.575248e-09 numerical: 10.624520 analytic: 10.624521, relative error: 2.793705e-08 numerical: 5.241199 analytic: 5.241198, relative error: 3.918448e-08 numerical: 5.384190 analytic: 5.384190, relative error: 5.281280e-08 numerical: -3.250758 analytic: -3.250758, relative error: 2.035146e-09 numerical: -6.618687 analytic: -6.618686, relative error: 3.693142e-08 numerical: -17.852199 analytic: -17.852198, relative error: 5.444536e-09
```

0.6 A vectorized version of SVM

To speed things up, we will vectorize the loss and gradient calculations. This will be helpful for stochastic gradient descent.

```
[522]: import time
[523]: | ## Implement sum.fast_loss_and_grad_which calculates the loss and gradient
            WITHOUT using any for loops.
       # Standard loss and gradient
       tic = time.time()
       loss, grad = svm.loss_and_grad(X_dev, y_dev)
       toc = time.time()
       print('Normal loss / grad_norm: {} / {} computed in {}s'.format(loss, np.linalg.
        →norm(grad, 'fro'), toc - tic))
       tic = time.time()
       loss_vectorized, grad_vectorized = svm.fast_loss_and_grad(X_dev, y_dev)
       toc = time.time()
       print('Vectorized loss / grad: {} / {} computed in {}s'.format(loss_vectorized,
        →np.linalg.norm(grad_vectorized, 'fro'), toc - tic))
       # The losses should match but your vectorized implementation should be much
        \hookrightarrow faster.
       print('difference in loss / grad: {} / {}'.format(loss - loss_vectorized, np.
        →linalg.norm(grad - grad_vectorized)))
       # You should notice a speedup with the same output, i.e., differences on the
        \rightarrow order of 1e-12
```

Normal loss / grad_norm: 15816.57339070797 / 2205.1819144473743 computed in 0.10318613052368164s

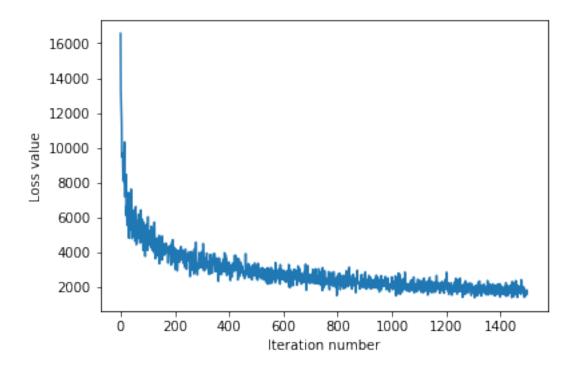
Vectorized loss / grad: 15816.573390707988 / 2205.1819144473743 computed in 0.0050106048583984375s

difference in loss / grad: -1.8189894035458565e-11 / 2.6413939701336207e-12

0.7 Stochastic gradient descent

We now implement stochastic gradient descent. This uses the same principles of gradient descent we discussed in class, however, it calculates the gradient by only using examples from a subset of the training set (so each gradient calculation is faster).

```
iteration 0 / 1500: loss 16557.38000190916
iteration 100 / 1500: loss 4701.089451272714
iteration 200 / 1500: loss 4017.333137942788
iteration 300 / 1500: loss 3681.9226471953625
iteration 400 / 1500: loss 2732.6164373988995
iteration 500 / 1500: loss 2786.6378424645045
iteration 600 / 1500: loss 2837.035784278268
iteration 700 / 1500: loss 2206.234868739933
iteration 800 / 1500: loss 2269.038824116981
iteration 900 / 1500: loss 2543.23781538592
iteration 1000 / 1500: loss 2566.6921357268257
iteration 1100 / 1500: loss 2182.0689059051633
iteration 1200 / 1500: loss 1861.1182244250447
iteration 1300 / 1500: loss 1982.9013858528256
iteration 1400 / 1500: loss 1927.5204158582117
That took 4.7113938331604s
```



0.7.1 Evaluate the performance of the trained SVM on the validation data.

```
[525]: ## Implement sum.predict() and use it to compute the training and testing error.

y_train_pred = svm.predict(X_train)
print('training accuracy: {}'.format(np.mean(np.equal(y_train,y_train_pred), )))
y_val_pred = svm.predict(X_val)
print('validation accuracy: {}'.format(np.mean(np.equal(y_val, y_val_pred)), ))
```

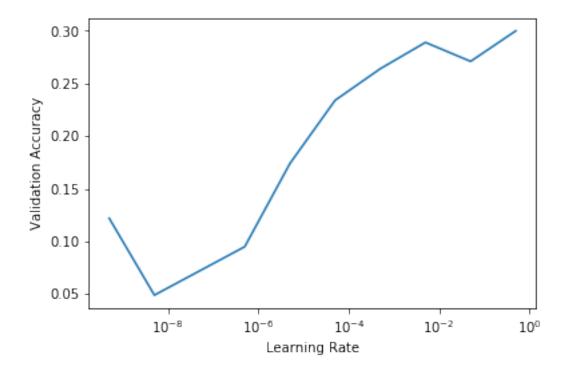
training accuracy: 0.28530612244897957 validation accuracy: 0.3

0.8 Optimize the SVM

Note, to make things faster and simpler, we won't do k-fold cross-validation, but will only optimize the hyperparameters on the validation dataset (X_val, y_val).

```
Select the SVM that achieved the best validation error and report
    its error rate on the test set.
# Note: You do not need to modify SVM class for this section
epsilon = 5*np.logspace(-10,-1,num = 10)
val_acc = np.zeros_like(epsilon)
ep_opt = 0
val_opt = 0
for i in np.arange(len(epsilon)):
   svm.train(X_train, y_train, learning_rate=epsilon[i],num_iters=1500,_
→verbose=False)
   y_val_pred = svm.predict(X_val)
   val_acc[i] = np.mean(np.equal(y_val, y_val_pred))
   if val_acc[i]> val_opt:
      val_opt = val_acc[i]
      ep_opt = epsilon[i]
print('Optimal epsilon = %4.3e with validation accuracy %4.3f'
→%(ep_opt,val_opt))
plt.semilogx(epsilon,val_acc)
plt.xlabel('Learning Rate')
plt.ylabel('Validation Accuracy')
plt.show()
svm.train(X_train, y_train, learning_rate=ep_opt,num_iters=1500, verbose=False)
y_test_pred = svm.predict(X_test)
test_err = 1-np.mean(np.equal(y_test, y_test_pred))
print('Optimal epsilon = %4.3e with test error %4.3f' %(ep_opt,test_err))
# ----- #
# END YOUR CODE HERE
# ----- #
```

Optimal epsilon = 5.000e-01 with validation accuracy 0.300



Optimal epsilon = 5.000e-01 with test error 0.741

[]: