# Homework 3

# 1 Problem 1

# 1.1 Problem Statement

(15 points) Backpropagation for autoencoders. In an autoencoder, we seek to reconstruct the original data after some operation that reduces the data's dimensionality. We maybe interested in reducing the data's dimensionality to gain a more compact representation of the data.

For example, consider  $\mathbf{x} \in \mathbb{R}^n$ . Further, consider  $\mathbf{W} \in \mathbb{R}^{m \times n}$  where m < n. Then  $\mathbf{W}\mathbf{x}$  is of lower dimensionality than  $\mathbf{x}$ . One way to design  $\mathbf{W}$  so that  $\mathbf{W}\mathbf{x}$  still contains key features of  $\mathbf{x}$  is to minimize the following expression

$$\mathcal{L} = \frac{1}{2} \left\| \mathbf{W}^T \mathbf{W} \mathbf{x} - \mathbf{x} \right\|^2$$

with respect to  $\mathbf{W}$  (To be complete, autoencoders also have a nonlinearity in each layer, i.e., the loss is  $\frac{1}{2} \| f(\mathbf{W}^T f(\mathbf{W} \mathbf{x})) - \mathbf{x} \|^2$ . However, we'll work with the linear example.)

- (a) (3 points) In words, describe why this minimization finds a  $\mathbf{W}$  that ought to preserve information about  $\mathbf{x}$ .
- (b) (3 points) Draw the computational graph for  $\mathcal{L}$ .
- (c) (3 points) In the computational graph, there should be two paths to  $\mathbf{W}$ . How do we account for these two paths when calculating  $\nabla_W \mathcal{L}$ ? Your answer should include a mathematical argument.
- (d) (6 points) Calculate the gradient:  $\nabla_W \mathcal{L}$

# 1.2 Solutions

1. Backprop for autoencoders

→ mant to reconstruct x after w reduces dimensionally

×em

$$d = \frac{1}{2} \| \mathbf{W}^{\mathsf{T}} \mathbf{W} \mathbf{x} - \mathbf{x} \|^2$$

$$\mathbf{W} \in \mathbb{R}^n$$

$$\mathbf{W} \in \mathbb{R}^n$$

minimize this wrt W

a) WTW x - x

T t t lnxi

Using example where m=1, n=2  $WX = \begin{bmatrix} w_1 & w_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ 

$$W^{T}WX = \begin{bmatrix} w_{1} \\ w_{2} \end{bmatrix} \begin{bmatrix} w_{1}x_{1} + w_{2}x_{2} \end{bmatrix}$$

$$= \begin{bmatrix} w_{1} (w_{1}x_{1} + w_{2}x_{2}) \\ w_{2} (w_{1}x_{1} + w_{2}x_{2}) \end{bmatrix} = \begin{bmatrix} w_{1}^{2}x_{1} + w_{1}w_{2}x_{2} \\ w_{1}w_{2}x_{1} + w_{2}^{2}x_{2} \end{bmatrix}$$

$$W^{T}WX - X =$$

$$\left[ (W_{1}^{2}-1)x_{1} + W_{1}W_{2}x_{1} \\ W_{1}W_{2}x_{1} + (W_{2}^{2}-1)x_{2} \right]$$

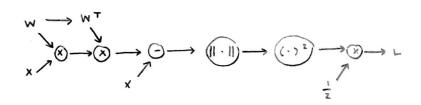
$$Want b = 0.5$$

want to minimize difference between wTNX and x:

$$\begin{bmatrix}
W_1^2 - 1 & W_1 W_2 \\
W_1 W_2 & W_2^2 - 1
\end{bmatrix}
\begin{bmatrix}
x_1 \\
x_2
\end{bmatrix}$$

can see that in order to find this mimization. Wx will preserve information about x

1. b)



c) Because there are two paths to w, must use the total law of derivatives

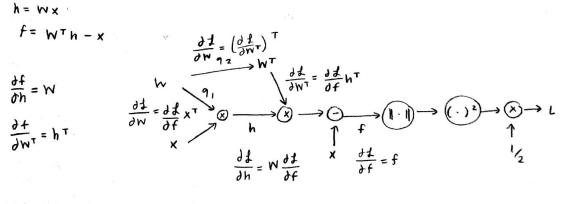
d) Vn L

$$f = W^T W X - X$$
  $f = \frac{1}{2} ||f||^2$ 

$$\frac{\partial \mathcal{L}}{\partial f} = \frac{1}{2} \cdot 2 \| f \| = f$$

h = Wx

$$\frac{d+}{dW^T} = h^T$$



back prop from q, branch
$$\frac{dl}{dN} = Wfx^{T} + (fh^{T})^{T}$$

$$\nabla_{W}f = W(W^{T}Wx - x)x^{T} + (Wx)(W^{T}Wx - x)^{T}$$

# 2 Problem 3

# 2.1 Problem Statement

(40 points) **2-layer neural network.** Compete the two-layer neural network Jupyter notebook. Print out the entire workbook and relevant code and submit it as a pdf to gradescope. Download the CIFAR-10 dataset, as you did in HW 2

# 2.2 Solution

two\_layer\_nn\_pfuncs

February 4, 2021

### 0.1 This is the 2-layer neural network workbook for ECE 247 Assignment #3

Please follow the notebook linearly to implement a two layer neural network.

Please print out the workbook entirely when completed.

We thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu). These are the functions in the cs231n folders and code in the jupyer notebook to preprocess and show the images. The classifiers used are based off of code prepared for CS 231n as well.

The goal of this workbook is to give you experience with training a two layer neural network.

## 0.2 Toy example

Before loading CIFAR-10, there will be a toy example to test your implementation of the forward and backward pass

```
[2]: from nndl.neural_net import TwoLayerNet

[3]: # Create a small net and some toy data to check your implementations.
```

```
# Note that we set the random seed for repeatable experiments.

input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5
```

```
def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=1e-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y

net = init_toy_model()
X, y = init_toy_data()
```

### 0.2.1 Compute forward pass scores

```
[4]: ## Implement the forward pass of the neural network.
     # Note, there is a statement if y is None: return scores, which is why
     # the following call will calculate the scores.
     scores = net.loss(X)
     print('Your scores:')
     print(scores)
     print()
     print('correct scores:')
     correct_scores = np.asarray([
         [-1.07260209, 0.05083871, -0.87253915],
         [-2.02778743, -0.10832494, -1.52641362],
         [-0.74225908, 0.15259725, -0.39578548],
         [-0.38172726, 0.10835902, -0.17328274],
         [-0.64417314, -0.18886813, -0.41106892]])
     print(correct_scores)
     print()
     # The difference should be very small. We get < 1e-7
     print('Difference between your scores and correct scores:')
     print(np.sum(np.abs(scores - correct_scores)))
    Your scores:
    [[-1.07260209 0.05083871 -0.87253915]
     [-2.02778743 -0.10832494 -1.52641362]
     [-0.74225908 0.15259725 -0.39578548]
     [-0.38172726 0.10835902 -0.17328274]
     [-0.64417314 -0.18886813 -0.41106892]]
    correct scores:
    [[-1.07260209 0.05083871 -0.87253915]
     [-2.02778743 -0.10832494 -1.52641362]
```

#### 0.2.2 Forward pass loss

```
[5]: loss, _ = net.loss(X, y, reg=0.05)
    correct_loss = 1.071696123862817

# should be very small, we get < 1e-12
    print('Difference between your loss and correct loss:')
    print(np.sum(np.abs(loss - correct_loss)))</pre>
```

Difference between your loss and correct loss: 0.0

```
[6]: print(loss)
```

1.071696123862817

### 0.2.3 Backward pass

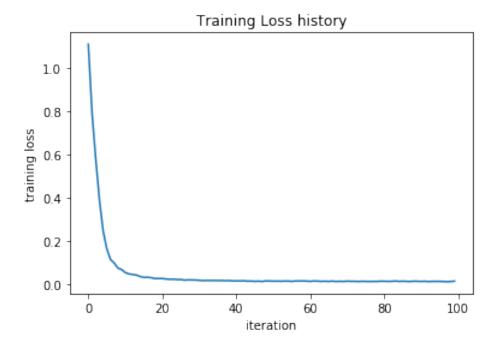
Implements the backwards pass of the neural network. Check your gradients with the gradient check utilities provided.

W2 max relative error: 2.9632245016399034e-10 b2 max relative error: 1.2482624742512528e-09 b1 max relative error: 3.172680285697327e-09 W1 max relative error: 1.2832892417669998e-09

## 0.2.4 Training the network

Implement neural\_net.train() to train the network via stochastic gradient descent, much like the softmax and SVM.

Final training loss: 0.014497864587765906



## 0.3 Classify CIFAR-10

Do classification on the CIFAR-10 dataset.

```
[9]: from cs231n.data utils import load CIFAR10
     def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
         Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
         it for the two-layer neural net classifier. These are the same steps as
         we used for the SVM, but condensed to a single function.
         # Load the raw CIFAR-10 data
         cifar10 dir = 'cifar-10-batches-py'
         X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
         # Subsample the data
         mask = list(range(num_training, num_training + num_validation))
         X_val = X_train[mask]
         y_val = y_train[mask]
         mask = list(range(num_training))
         X_train = X_train[mask]
         y_train = y_train[mask]
         mask = list(range(num_test))
         X_test = X_test[mask]
         y_test = y_test[mask]
         # Normalize the data: subtract the mean image
         mean_image = np.mean(X_train, axis=0)
         X_train -= mean_image
         X_val -= mean_image
         X_test -= mean_image
         # Reshape data to rows
         X train = X train.reshape(num training, -1)
         X_val = X_val.reshape(num_validation, -1)
         X_test = X_test.reshape(num_test, -1)
         return X_train, y_train, X_val, y_val, X_test, y_test
     # Invoke the above function to get our data.
     X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
     print('Train data shape: ', X_train.shape)
     print('Train labels shape: ', y_train.shape)
     print('Validation data shape: ', X_val.shape)
     print('Validation labels shape: ', y_val.shape)
     print('Test data shape: ', X_test.shape)
     print('Test labels shape: ', y_test.shape)
    Train data shape: (49000, 3072)
```

Train labels shape: (49000,)

```
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

### 0.3.1 Running SGD

If your implementation is correct, you should see a validation accuracy of around 28-29%.

```
iteration 0 / 1000: loss 2.302757518613176
iteration 100 / 1000: loss 2.302120159207236
iteration 200 / 1000: loss 2.2956136007408703
iteration 300 / 1000: loss 2.2518259043164135
iteration 400 / 1000: loss 2.188995235046776
iteration 500 / 1000: loss 2.1162527791897747
iteration 600 / 1000: loss 2.064670827698217
iteration 700 / 1000: loss 1.9901688623083942
iteration 800 / 1000: loss 2.0028276401246856
iteration 900 / 1000: loss 1.9465176817856498
Validation accuracy: 0.283
```

## 0.4 Questions:

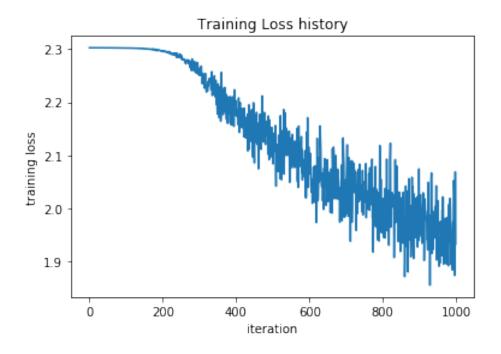
The training accuracy isn't great.

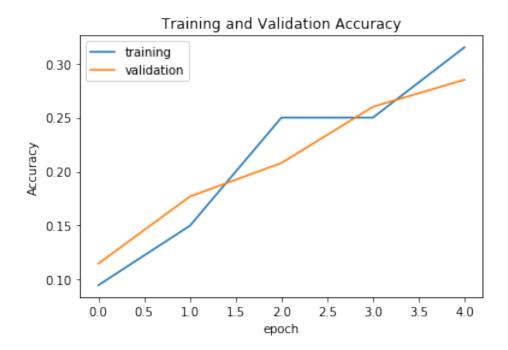
- (1) What are some of the reasons why this is the case? Take the following cell to do some analyses and then report your answers in the cell following the one below.
- (2) How should you fix the problems you identified in (1)?

```
[11]: stats['train_acc_history']
```

```
[11]: [0.095, 0.15, 0.25, 0.25, 0.315]
```

```
[12]: # ----- #
    # YOUR CODE HERE:
    # Do some debugging to gain some insight into why the optimization
    # isn't great.
    # Plot the loss function and train / validation accuracies
    # plot the loss history
    plt.plot(stats['loss_history'])
    plt.xlabel('iteration')
    plt.ylabel('training loss')
    plt.title('Training Loss history')
    plt.show()
    plt.plot(stats['train_acc_history'])
    plt.plot(stats['val_acc_history'])
    plt.xlabel('epoch')
    plt.ylabel('Accuracy')
    plt.title('Training and Validation Accuracy')
    plt.legend(['training','validation'])
    plt.show()
    # END YOUR CODE HERE
    # ============= #
```





# 0.5 Answers:

- (1) It looks like there may not be enough iterations for the loss to continue decaying over. Also, the step size may be too small because the loss function decays slowly at first
- (2) Can change hyperparameters learning\_rate, and num\_iters.

# 0.6 Optimize the neural network

Use the following part of the Jupyter notebook to optimize your hyperparameters on the validation set. Store your nets as best\_net.

```
[13]: best_net = None # store the best model into this
     # YOUR CODE HERE:
        Optimize over your hyperparameters to arrive at the best neural
        network. You should be able to get over 50% validation accuracy.
       For this part of the notebook, we will give credit based on the
        accuracy you get. Your score on this question will be multiplied by:
          min(floor((X - 28\%)) / \%22, 1)
       where if you get 50% or higher validation accuracy, you get full
        points.
        Note, you need to use the same network structure (keep hidden_size = 50)!
     iteration = np.linspace(1000,4000,num=7)
     # print(iteration)
     learning = np.logspace(-4,-3,num=5)
     val_opt = 0.5
     acc_found = False
     for num_i in iteration:
        for num_lr in learning:
            # create network
            net = TwoLayerNet(input size, hidden size, num classes)
            # Train the network
            stats = net.train(X_train, y_train, X_val, y_val,
                       num_iters=num_i, batch_size=200,
                       learning_rate=num_lr, learning_rate_decay=0.95,
                       reg=0.25, verbose=False)
            # Predict on the validation set
            val_acc = (net.predict(X_val) == y_val).mean()
            if val_acc >= val_opt:
                acc_found = True
                val_opt = val_acc
                it_opt = num_i
```

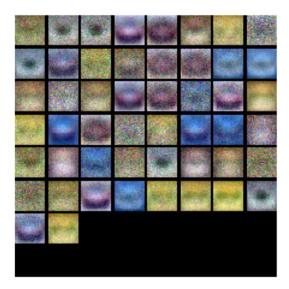
Validation accuracy: 0.500, for 1500 iterations and learning rate = 1.000e-03

```
[14]: from cs231n.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(net):
    W1 = net.params['W1']
    W1 = W1.T.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
    plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
    plt.gca().axis('off')
    plt.show()

show_net_weights(subopt_net)
show_net_weights(best_net)
```





# 0.7 Question:

(1) What differences do you see in the weights between the suboptimal net and the best net you arrived at?

### 0.8 Answer:

(1) The colors are brighter in the best net and shapes are more distinguishable

#### 0.9 Evaluate on test set

```
[15]: test_acc = (best_net.predict(X_test) == y_test).mean()
print('Test accuracy: ', test_acc)
```

Test accuracy: 0.497

```
0.10 neural net.py
[]: import numpy as np
    import matplotlib.pyplot as plt
     This code was originally written for CS 231n at Stanford University
     (cs231n.stanford.edu). It has been modified in various areas for use in the
     ECE 239AS class at UCLA. This includes the descriptions of what code to
     implement as well as some slight potential changes in variable names to be
     consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
    permission to use this code. To see the original version, please visit
     cs231n.stanford.edu.
     HHHH
    class TwoLayerNet(object):
       11 11 11
      A two-layer fully-connected neural network. The net has an input dimension of
      N, a hidden layer dimension of H, and performs classification over C classes.
      We train the network with a softmax loss function and L2 regularization on the
      weight matrices. The network uses a ReLU nonlinearity after the first fully
      connected layer.
      In other words, the network has the following architecture:
       input - fully connected layer - ReLU - fully connected layer - softmax
       The outputs of the second fully-connected layer are the scores for each class.
      def __init__(self, input_size, hidden_size, output_size, std=1e-4):
        Initialize the model. Weights are initialized to small random values and
        biases are initialized to zero. Weights and biases are stored in the
        variable self.params, which is a dictionary with the following keys:
         W1: First layer weights; has shape (H, D)
```

```
b1: First layer biases; has shape (H,)
  W2: Second layer weights; has shape (C, H)
  b2: Second layer biases; has shape (C,)
  Inputs:
  - input_size: The dimension D of the input data.
  - hidden_size: The number of neurons H in the hidden layer.
  - output_size: The number of classes C.
  self.params = {}
  self.params['W1'] = std * np.random.randn(hidden_size, input_size)
  self.params['b1'] = np.zeros(hidden_size)
  self.params['W2'] = std * np.random.randn(output_size, hidden_size)
  self.params['b2'] = np.zeros(output_size)
def loss(self, X, y=None, reg=0.0):
  Compute the loss and gradients for a two layer fully connected neural
  network.
  Inputs:
  - X: Input data of shape (N, D). Each X[i] is a training sample.
  - y: Vector of training labels. y[i] is the label for X[i], and each y[i] is
   an integer in the range 0 \le y[i] \le C. This parameter is optional; if it
    is not passed then we only return scores, and if it is passed then we
   instead return the loss and gradients.
  - reg: Regularization strength.
  Returns:
  If y is None, return a matrix scores of shape (N, C) where scores[i, c] is
  the score for class c on input X[i].
  If y is not None, instead return a tuple of:
  - loss: Loss (data loss and regularization loss) for this batch of training
   samples.
  - grads: Dictionary mapping parameter names to gradients of those parameters
    with respect to the loss function; has the same keys as self.params.
  11 11 11
  # Unpack variables from the params dictionary
  W1, b1 = self.params['W1'], self.params['b1']
  W2, b2 = self.params['W2'], self.params['b2']
  N, D = X.shape
  # Compute the forward pass
  scores = None
```

```
# ----- #
# YOUR CODE HERE:
  Calculate the output scores of the neural network. The result
 should be (N, C). As stated in the description for this class,
       there should not be a ReLU layer after the second FC layer.
       The output of the second FC layer is the output scores. Do not
       use a for loop in your implementation.
# ----- #
# defining ReLU function
f = lambda x: x*(x>0)
h = f(X.dot(W1.T)+b1)
# dont apply ReLU to output z
scores = h.dot(W2.T)+b2
# ----- #
# END YOUR CODE HERE
# If the targets are not given then jump out, we're done
if y is None:
 return scores
# Compute the loss
loss = None
# YOUR CODE HERE:
 Calculate the loss of the neural network. This includes the
      softmax loss and the L2 regularization for W1 and W2. Store the
       total loss in the variable loss. Multiply the regularization
      loss by 0.5 (in addition to the factor reg).
# ----- #
# scores is num_examples by num_classes
# defining softmax function
smax = np.exp(scores)/np.sum(np.exp(scores), axis =1, keepdims = True)
# creating indices [1,y1], [2,y2]...[N,yN]
a_ind = [np.arange(N),y]
loss = np.sum(-np.log(smax[a_ind]))
loss = 1/N*loss
# adding regularization term
loss = loss+0.5*reg*(np.sum(W1**2)+np.sum(W2**2))
# ----- #
```

```
# END YOUR CODE HERE
 grads = {}
 # YOUR CODE HERE:
         Implement the backward pass. Compute the derivatives of the
         weights and the biases. Store the results in the grads
          dictionary. e.g., grads['W1'] should store the gradient for
        W1, and be of the same size as W1.
 # creating indicator function
 ind = np.zeros_like(smax)
 ind[a_ind] = 1
 # recall for smax yi equal to j dg/df*df/dz = (smax-1) otherwise just smax
 \# dLdz = softmax_loss
 dLdz = smax - ind \#N, C
 grads['W2'] = dLdz.T.dot(h)/N + reg*W2
 grads['b2'] = 1/N*np.sum(dLdz,axis=0)
 dLdh = dLdz.dot(W2)
 a = X.dot(W1.T)+b1
 # for relu backprop I(a>0)*dLdh
 dLda = (a>0)*dLdh
 grads['b1'] = 1/N*(np.sum(dLda,axis =0))
 grads['W1'] = 1/N*dLda.T.dot(X) + reg*W1
 # ----- #
 # END YOUR CODE HERE
 # ------ #
 return loss, grads
def train(self, X, y, X_val, y_val,
        learning_rate=1e-3, learning_rate_decay=0.95,
        reg=1e-5, num_iters=100,
       batch_size=200, verbose=False):
 Train this neural network using stochastic gradient descent.
 Inputs:
 - X: A numpy array of shape (N, D) giving training data.
 - y: A numpy array f shape (N,) giving training labels; y[i] = c means that
   X[i] has label c, where 0 \le c \le C.
 - X_val: A numpy array of shape (N_val, D) giving validation data.
```

```
- y_val: A numpy array of shape (N_val,) giving validation labels.
  - learning_rate: Scalar giving learning rate for optimization.
  - learning_rate_decay: Scalar giving factor used to decay the learning rate
   after each epoch.
  - reg: Scalar giving regularization strength.
  - num_iters: Number of steps to take when optimizing.
  - batch_size: Number of training examples to use per step.
  - verbose: boolean; if true print progress during optimization.
  num_train = X.shape[0]
  iterations_per_epoch = max(int(num_train / batch_size), 1)
  # Use SGD to optimize the parameters in self.model
  loss history = []
  train_acc_history = []
  val_acc_history = []
  for it in np.arange(num_iters):
   X_batch = None
   y_batch = None
    # ----- #
    # YOUR CODE HERE:
       # Create a minibatch by sampling batch size samples
\hookrightarrow randomly.
        index = np.random.choice(num train,batch size)
   X_batch = X[index]
   y_batch = y[index]
    # END YOUR CODE HERE
    # Compute loss and gradients using the current minibatch
   loss, grads = self.loss(X_batch, y=y_batch, reg=reg)
   loss_history.append(loss)
    # YOUR CODE HERE:
        # Perform a gradient descent step using the minibatch to \Box
\hookrightarrowupdate
        # all parameters (i.e., W1, W2, b1, and b2).
        # ----- #
   self.params['W1'] = self.params['W1'] - learning_rate*grads['W1']
   self.params['W2'] = self.params['W2'] - learning_rate*grads['W2']
    self.params['b1'] = self.params['b1'] - learning_rate*grads['b1']
```

```
self.params['b2'] = self.params['b2'] - learning_rate*grads['b2']
   # END YOUR CODE HERE
   # ------ #
   if verbose and it % 100 == 0:
     print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
   # Every epoch, check train and val accuracy and decay learning rate.
   if it % iterations_per_epoch == 0:
     # Check accuracy
     train_acc = (self.predict(X_batch) == y_batch).mean()
     val_acc = (self.predict(X_val) == y_val).mean()
     train_acc_history.append(train_acc)
     val_acc_history.append(val_acc)
     # Decay learning rate
     learning_rate *= learning_rate_decay
 return {
   'loss_history': loss_history,
   'train_acc_history': train_acc_history,
   'val_acc_history': val_acc_history,
 }
def predict(self, X):
 Use the trained weights of this two-layer network to predict labels for
 data points. For each data point we predict scores for each of the C
 classes, and assign each data point to the class with the highest score.
 Inputs:
 - X: A numpy array of shape (N, D) giving N D-dimensional data points to
   classify.
 Returns:
 - y_pred: A numpy array of shape (N,) qiving predicted labels for each of
   the elements of X. For all i, y_pred[i] = c means that X[i] is predicted
   to have class c, where 0 \le c \le C.
 y_pred = None
 # ------ #
 # YOUR CODE HERE:
         Predict the class given the input data.
 # ------ #
 W1, b1 = self.params['W1'], self.params['b1']
```

# 3 Problem 4

# 3.1 Problem Statement

(25 points) **General FC neural network.** Compete the FC Net Jupyter notebook. Print out the entire workbook and relevant code and submit it as a pdf to gradescope.

# 3.2 Solutions

# 3.3 Solution

# FC nets pfuncs

February 4, 2021

# 1 Fully connected networks

In the previous notebook, you implemented a simple two-layer neural network class. However, this class is not modular. If you wanted to change the number of layers, you would need to write a new loss and gradient function. If you wanted to optimize the network with different optimizers, you'd need to write new training functions. If you wanted to incorporate regularizations, you'd have to modify the loss and gradient function.

Instead of having to modify functions each time, for the rest of the class, we'll work in a more modular framework where we define forward and backward layers that calculate losses and gradients respectively. Since the forward and backward layers share intermediate values that are useful for calculating both the loss and the gradient, we'll also have these function return "caches" which store useful intermediate values.

The goal is that through this modular design, we can build different sized neural networks for various applications.

In this HW #3, we'll define the basic architecture, and in HW #4, we'll build on this framework to implement different optimizers and regularizations (like BatchNorm and Dropout).

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

### 1.1 Modular layers

This notebook will build modular layers in the following manner. First, there will be a forward pass for a given layer with inputs (x) and return the output of that layer (out) as well as cached variables (cache) that will be used to calculate the gradient in the backward pass.

```
def layer_forward(x, w):
    """ Receive inputs x and weights w """
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output
```

cache = (x, w, z, out) # Values we need to compute gradients

```
return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
       Receive derivative of loss with respect to outputs and cache,
       and compute derivative with respect to inputs.
       # Unpack cache values
       x, w, z, out = cache
       # Use values in cache to compute derivatives
       dx = # Derivative of loss with respect to x
       dw = # Derivative of loss with respect to w
       return dx, dw
[85]: ## Import and setups
      import time
      import numpy as np
      import matplotlib.pyplot as plt
     from nndl.fc_net import *
     from cs231n.data_utils import get_CIFAR10_data
     from cs231n.gradient_check import eval_numerical_gradient,_
      →eval_numerical_gradient_array
      from cs231n.solver import Solver
     import os
     %alias kk os. exit(0)
     %matplotlib inline
     plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
     plt.rcParams['image.interpolation'] = 'nearest'
     plt.rcParams['image.cmap'] = 'gray'
      # for auto-reloading external modules
      # see http://stackoverflow.com/questions/1907993/
      \rightarrow autoreload-of-modules-in-ipython
     %load ext autoreload
     %autoreload 2
     def rel_error(x, y):
        """ returns relative error """
        return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

```
[86]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y_test: (1000,)
```

### 1.2 Linear layers

In this section, we'll implement the forward and backward pass for the linear layers.

The linear layer forward pass is the function affine\_forward in nndl/layers.py and the backward pass is affine\_backward.

After you have implemented these, test your implementation by running the cell below.

### 1.2.1 Affine layer forward pass

Implement affine\_forward and then test your code by running the following cell.

```
[87]: # Test the affine forward function
     num_inputs = 2
      input\_shape = (4, 5, 6)
     output_dim = 3
      input_size = num_inputs * np.prod(input_shape)
      weight_size = output_dim * np.prod(input_shape)
     x = np.linspace(-0.1, 0.5, num=input_size).reshape(num_inputs, *input_shape)
     w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape),_
      →output_dim)
     b = np.linspace(-0.3, 0.1, num=output_dim)
      out, _ = affine_forward(x, w, b)
      correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                              [ 3.25553199, 3.5141327, 3.77273342]])
      # Compare your output with ours. The error should be around 1e-9.
     print('Testing affine_forward function:')
     print('difference: {}'.format(rel_error(out, correct_out)))
```

```
Testing affine_forward function: difference: 9.769849468192957e-10
```

## 1.2.2 Affine layer backward pass

Implement affine\_backward and then test your code by running the following cell.

```
[88]: # Test the affine_backward function
     x = np.random.randn(10, 2, 3)
     w = np.random.randn(6, 5)
     b = np.random.randn(5)
     dout = np.random.randn(10, 5)
     dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0], x,_u
      →dout)
     dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w,__

dout)
      db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0], b,__
      →dout)
      _, cache = affine_forward(x, w, b)
      dx, dw, db = affine_backward(dout, cache)
      # The error should be around 1e-10
     print('Testing affine_backward function:')
     print('dx error: {}'.format(rel_error(dx_num, dx)))
     print('dw error: {}'.format(rel_error(dw_num, dw)))
     print('db error: {}'.format(rel_error(db_num, db)))
```

Testing affine\_backward function: dx error: 5.701568865057545e-10

dw error: 4.037525349210396e-11
db error: 8.912836710516436e-12

### 1.3 Activation layers

In this section you'll implement the ReLU activation.

# 1.3.1 ReLU forward pass

Implement the relu\_forward function in nndl/layers.py and then test your code by running the following cell.

```
[89]: # Test the relu_forward function
x = np.linspace(-0.5, 0.5, num=12).reshape(3, 4)
out, _ = relu_forward(x)
```

Testing relu\_forward function: difference: 4.999999798022158e-08

### 1.3.2 ReLU backward pass

Implement the relu\_backward function in nndl/layers.py and then test your code by running the following cell.

```
[90]: x = np.random.randn(10, 10)
dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be around 1e-12
print('Testing relu_backward function:')
print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing relu\_backward function: dx error: 3.2756257858972667e-12

# 1.4 Combining the affine and ReLU layers

Often times, an affine layer will be followed by a ReLU layer. So let's make one that puts them together. Layers that are combined are stored in nndl/layer\_utils.py.

### 1.4.1 Affine-ReLU layers

We've implemented affine\_relu\_forward() and affine\_relu\_backward in nndl/layer\_utils.py. Take a look at them to make sure you understand what's going on. Then run the following cell to ensure its implemented correctly.

```
[91]: from nndl.layer_utils import affine_relu_forward, affine_relu_backward

x = np.random.randn(2, 3, 4)
w = np.random.randn(12, 10)
b = np.random.randn(10)
dout = np.random.randn(2, 10)
```

```
out, cache = affine_relu_forward(x, w, b)
dx, dw, db = affine_relu_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, u \int b)[0], x, dout)

dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, u \int b)[0], w, dout)

db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, u \int b)[0], b, dout)

print('Testing affine_relu_forward and affine_relu_backward:')

print('dx error: {}'.format(rel_error(dx_num, dx)))

print('dw error: {}'.format(rel_error(db_num, db)))
```

Testing affine\_relu\_forward and affine\_relu\_backward:

dx error: 4.776934873943058e-10 dw error: 1.1193098353710892e-10 db error: 6.812406596671432e-12

## 1.5 Softmax and SVM losses

You've already implemented these, so we have written these in layers.py. The following code will ensure they are working correctly.

```
[92]: num classes, num inputs = 10, 50
     x = 0.001 * np.random.randn(num_inputs, num_classes)
     y = np.random.randint(num_classes, size=num_inputs)
     dx_num = eval_numerical_gradient(lambda x: svm_loss(x, y)[0], x, verbose=False)
     loss, dx = svm loss(x, y)
      # Test sum_loss function. Loss should be around 9 and dx error should be 1e-9
     print('Testing svm_loss:')
     print('loss: {}'.format(loss))
     print('dx error: {}'.format(rel_error(dx_num, dx)))
     dx_num = eval_numerical_gradient(lambda x: softmax_loss(x, y)[0], x,_u
      →verbose=False)
     loss, dx = softmax loss(x, y)
      # Test softmax_loss function. Loss should be 2.3 and dx error should be 1e-8
      print('\nTesting softmax_loss:')
     print('loss: {}'.format(loss))
     print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing svm\_loss:

loss: 8.999326284563985

```
dx error: 8.182894472887002e-10
Testing softmax_loss:
loss: 2.30251810660952
dx error: 6.947660960068788e-09
```

### 1.6 Implementation of a two-layer NN

In nndl/fc\_net.py, implement the class TwoLayerNet which uses the layers you made here. When you have finished, the following cell will test your implementation.

```
[93]: N, D, H, C = 3, 5, 50, 7
     X = np.random.randn(N, D)
     y = np.random.randint(C, size=N)
     std = 1e-2
     model = TwoLayerNet(input_dim=D, hidden_dims=H, num_classes=C, weight_scale=std)
     print('Testing initialization ... ')
     W1_std = abs(model.params['W1'].std() - std)
     b1 = model.params['b1']
     W2 std = abs(model.params['W2'].std() - std)
     b2 = model.params['b2']
     assert W1_std < std / 10, 'First layer weights do not seem right'
     assert np.all(b1 == 0), 'First layer biases do not seem right'
     assert W2_std < std / 10, 'Second layer weights do not seem right'</pre>
     assert np.all(b2 == 0), 'Second layer biases do not seem right'
     print('Testing test-time forward pass ... ')
     model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
     model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
     model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
     model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
     X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
      scores = model.loss(X)
      correct scores = np.asarray(
        [[11.53165108, 12.2917344,
                                     13.05181771, 13.81190102, 14.57198434, 15.
      \rightarrow 33206765, 16.09215096],
         [12.05769098, 12.74614105, 13.43459113, 14.1230412,
                                                                  14.81149128, 15.
      →49994135, 16.18839143],
         [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.
      \rightarrow66781506, 16.2846319 ]])
      scores_diff = np.abs(scores - correct_scores).sum()
      assert scores_diff < 1e-6, 'Problem with test-time forward pass'
     print('Testing training loss (no regularization)')
     y = np.asarray([0, 5, 1])
     loss, grads = model.loss(X, y)
```

```
Testing initialization ...

Testing test-time forward pass ...

Testing training loss (no regularization)

Running numeric gradient check with reg = 0.0

W1 relative error: 1.8336562786695002e-08

W2 relative error: 3.201560569143183e-10

b1 relative error: 9.828315204644842e-09

b2 relative error: 4.329134954569865e-10

Running numeric gradient check with reg = 0.7

W1 relative error: 2.5279152310200606e-07

W2 relative error: 2.8508510893102143e-08

b1 relative error: 1.564679947504764e-08

b2 relative error: 9.089617896905665e-10
```

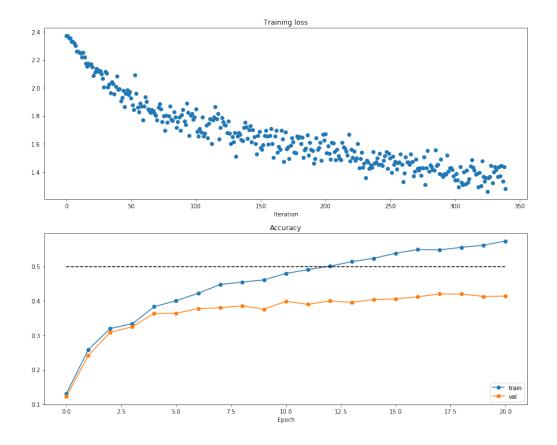
### 1.7 Solver

We will now use the cs231n Solver class to train these networks. Familiarize yourself with the API in cs231n/solver.py. After you have done so, declare an instance of a TwoLayerNet with 200 units and then train it with the Solver. Choose parameters so that your validation accuracy is at least 40%.

```
since you did it in the previous notebook.
# ----- #
H= 190 # to have 200 units need hidden dim to have 190 neurons in hidden layer_
→+ 10 classes
num_train = 3500
small_data = {
 'X train': data['X train'][:num train],
 'y_train': data['y_train'][:num_train],
 'X_val': data['X_val'],
 'y_val': data['y_val'],
model = TwoLayerNet(hidden_dims=H, reg = 0.25)
solver = Solver(model, small_data,
               num_train_samples = num_train,
               update_rule='sgd',
               optim config={
                'learning_rate': 1e-3,
               lr_decay=0.95,
               num epochs=20, batch size=200,
               print_every=100)
solver.train()
# END YOUR CODE HERE
```

```
(Iteration 1 / 340) loss: 2.376366
(Epoch 0 / 20) train acc: 0.156571; val_acc: 0.149000
(Epoch 1 / 20) train acc: 0.291714; val_acc: 0.288000
(Epoch 2 / 20) train acc: 0.302000; val_acc: 0.302000
(Epoch 3 / 20) train acc: 0.353714; val_acc: 0.345000
(Epoch 4 / 20) train acc: 0.377714; val_acc: 0.352000
(Epoch 5 / 20) train acc: 0.410000; val acc: 0.359000
(Iteration 101 / 340) loss: 1.676439
(Epoch 6 / 20) train acc: 0.421143; val_acc: 0.359000
(Epoch 7 / 20) train acc: 0.434000; val acc: 0.371000
(Epoch 8 / 20) train acc: 0.447714; val_acc: 0.384000
(Epoch 9 / 20) train acc: 0.465143; val_acc: 0.385000
(Epoch 10 / 20) train acc: 0.473143; val_acc: 0.386000
(Epoch 11 / 20) train acc: 0.488857; val acc: 0.382000
(Iteration 201 / 340) loss: 1.705794
(Epoch 12 / 20) train acc: 0.497143; val_acc: 0.401000
(Epoch 13 / 20) train acc: 0.514571; val_acc: 0.391000
(Epoch 14 / 20) train acc: 0.527143; val_acc: 0.393000
(Epoch 15 / 20) train acc: 0.530286; val_acc: 0.384000
```

```
(Epoch 16 / 20) train acc: 0.544286; val_acc: 0.398000
     (Epoch 17 / 20) train acc: 0.556000; val_acc: 0.399000
     (Iteration 301 / 340) loss: 1.391876
     (Epoch 18 / 20) train acc: 0.562857; val_acc: 0.405000
     (Epoch 19 / 20) train acc: 0.572000; val_acc: 0.409000
     (Epoch 20 / 20) train acc: 0.583714; val_acc: 0.403000
[95]: # Run this cell to visualize training loss and train / val accuracy
     plt.subplot(2, 1, 1)
     plt.title('Training loss')
     plt.plot(solver.loss_history, 'o')
     plt.xlabel('Iteration')
     plt.subplot(2, 1, 2)
     plt.title('Accuracy')
     plt.plot(solver.train_acc_history, '-o', label='train')
     plt.plot(solver.val_acc_history, '-o', label='val')
     plt.plot([0.5] * len(solver.val_acc_history), 'k--')
     plt.xlabel('Epoch')
     plt.legend(loc='lower right')
     plt.gcf().set_size_inches(15, 12)
     plt.show()
```



# 1.8 Multilayer Neural Network

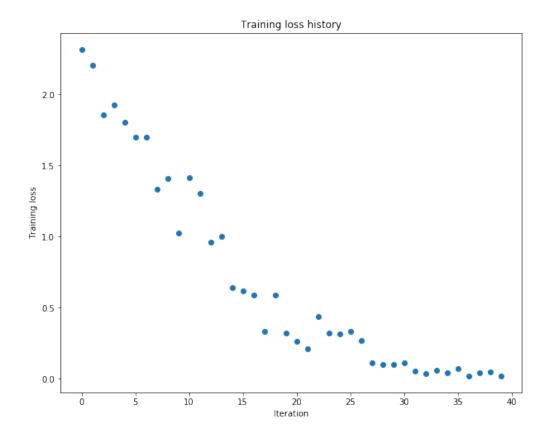
Now, we implement a multi-layer neural network.

Read through the FullyConnectedNet class in the file nndl/fc\_net.py.

Implement the initialization, the forward pass, and the backward pass. There will be lines for batchnorm and dropout layers and caches; ignore these all for now. That'll be in assignment #4.

```
for name in sorted(grads):
           f = lambda _: model.loss(X, y)[0]
           grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,_u
           print('{} relative error: {}'.format(name, rel_error(grad_num,__
        →grads[name])))
      Running check with reg = 0
      Initial loss: 2.301338118358964
      W1 relative error: 2.518507782545864e-05
      W2 relative error: 2.95829151935078e-06
      W3 relative error: 5.272564363922013e-07
      b1 relative error: 3.1930170202722495e-07
      b2 relative error: 2.7755069360690725e-08
      b3 relative error: 1.0799232881582816e-10
      Running check with reg = 3.14
      Initial loss: 6.959815405400122
      W1 relative error: 3.25384033852042e-07
      W2 relative error: 8.55871098153009e-08
      W3 relative error: 2.6949214674732215e-07
      b1 relative error: 1.7710048941573746e-05
      b2 relative error: 3.728046086442281e-09
      b3 relative error: 1.46187782427387e-10
[121]: # Use the three layer neural network to overfit a small dataset.
       num train = 50
       small_data = {
         'X_train': data['X_train'][:num_train],
         'y_train': data['y_train'][:num_train],
         'X_val': data['X_val'],
         'y_val': data['y_val'],
       }
       #### !!!!!!
       # Play around with the weight_scale and learning_rate so that you can overfit a_
       \hookrightarrowsmall dataset.
       # Your training accuracy should be 1.0 to receive full credit on this part.
       weight_scale = 1e-2
       learning_rate = 1e-2
       model = FullyConnectedNet([100, 100],
                     weight_scale=weight_scale, dtype=np.float64)
       solver = Solver(model, small_data,
                       print_every=10, num_epochs=20, batch_size=25,
                       update_rule='sgd',
```

```
optim config={
                  'learning_rate': learning_rate,
solver.train()
plt.plot(solver.loss_history, 'o')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()
(Iteration 1 / 40) loss: 2.317202
(Epoch 0 / 20) train acc: 0.300000; val_acc: 0.158000
(Epoch 1 / 20) train acc: 0.400000; val_acc: 0.146000
(Epoch 2 / 20) train acc: 0.480000; val_acc: 0.165000
(Epoch 3 / 20) train acc: 0.560000; val_acc: 0.156000
(Epoch 4 / 20) train acc: 0.620000; val_acc: 0.178000
(Epoch 5 / 20) train acc: 0.540000; val_acc: 0.143000
(Iteration 11 / 40) loss: 1.411566
(Epoch 6 / 20) train acc: 0.760000; val acc: 0.168000
(Epoch 7 / 20) train acc: 0.880000; val_acc: 0.190000
(Epoch 8 / 20) train acc: 0.880000; val_acc: 0.192000
(Epoch 9 / 20) train acc: 0.860000; val_acc: 0.207000
(Epoch 10 / 20) train acc: 0.940000; val acc: 0.198000
(Iteration 21 / 40) loss: 0.263774
(Epoch 11 / 20) train acc: 0.880000; val_acc: 0.168000
(Epoch 12 / 20) train acc: 0.960000; val_acc: 0.179000
(Epoch 13 / 20) train acc: 0.900000; val_acc: 0.209000
(Epoch 14 / 20) train acc: 0.980000; val_acc: 0.214000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.193000
(Iteration 31 / 40) loss: 0.112390
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.191000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.207000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.202000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.194000
(Epoch 20 / 20) train acc: 1.000000; val_acc: 0.189000
```



## 1.9 layers.py

```
[]: import numpy as np
import pdb

"""

This code was originally written for CS 231n at Stanford University
  (cs231n.stanford.edu). It has been modified in various areas for use in the
  ECE 239AS class at UCLA. This includes the descriptions of what code to
  implement as well as some slight potential changes in variable names to be
  consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
  permission to use this code. To see the original version, please visit
  cs231n.stanford.edu.
"""

def affine_forward(x, w, b):
  """
```

```
Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d \cdot 1 * ... * d \cdot k, and
 then transform it to an output vector of dimension M.
 Inputs:
 -x: A numpy array containing input data, of shape (N, d_1, \ldots, d_k)
 - w: A numpy array of weights, of shape (D, M)
 - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
 - cache: (x, w, b)
 # ----- #
 # YOUR CODE HERE:
 # Calculate the output of the forward pass. Notice the dimensions
 \# of w are D x M, which is the transpose of what we did in earlier
 # assignments.
 # changing x to have shape (N,D) D = d 1* ,... *d k
 x_transform = x.reshape(x.shape[0],-1)
 out = x_transform.dot(w) + b
 # END YOUR CODE HERE
 cache = (x, w, b)
 return out, cache
def affine_backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: Input data, of shape (N, d_1, \ldots, d_k)
   - w: Weights, of shape (D, M)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, \ldots, d_k)
```

```
- dw: Gradient with respect to w, of shape (D, M)
 - db: Gradient with respect to b, of shape (M,)
 x, w, b = cache
 dx, dw, db = None, None, None
 # ----- #
 # YOUR CODE HERE:
   Calculate the gradients for the backward pass.
 # ============= #
 # dout is N x M
 # dx should be N x d1 x ... x dk; it relates to dout through multiplication
\rightarrow with w, which is D x M
 # dw should be D x M; it relates to dout through multiplication with x, which _{\!\!\!\! -}
\hookrightarrow is N x D after reshaping
 # db should be M; it is just the sum over dout examples
 x_transform = x.reshape(x.shape[0],-1) # N x D
 dx = dout.dot(w.T) # N x D
 dx = dx.reshape(x.shape)
 dw = x_transform.T.dot(dout) # D x M
 db = np.sum(dout , axis = 0) # want to sum values in the columns to get M
 # END YOUR CODE HERE
 # ============= #
 return dx, dw, db
def relu forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ----- #
 # YOUR CODE HERE:
   Implement the ReLU forward pass.
 # ----- #
 f = lambda x: x*(x>0)
```

```
out = f(x)
 # END YOUR CODE HERE
 # ----- #
 cache = x
 return out, cache
def relu_backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 Input:
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 x = cache
 # ============= #
 # YOUR CODE HERE:
   Implement the ReLU backward pass
 # ----- #
 # ReLU directs linearly to those > 0
 dx = (x>0)*dout
 # ----- #
 # END YOUR CODE HERE
 # ----- #
 return dx
def svm_loss(x, y):
 Computes the loss and gradient using for multiclass SVM classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
  for the ith input.
 - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
  0 \ll y[i] \ll C
```

```
Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
 N = x.shape[0]
 correct_class_scores = x[np.arange(N), y]
 margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
 margins[np.arange(N), y] = 0
 loss = np.sum(margins) / N
 num_pos = np.sum(margins > 0, axis=1)
  dx = np.zeros_like(x)
 dx[margins > 0] = 1
 dx[np.arange(N), y] -= num_pos
 dx /= N
 return loss, dx
def softmax_loss(x, y):
  Computes the loss and gradient for softmax classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
    0 <= y[i] < C
 Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
 probs = np.exp(x - np.max(x, axis=1, keepdims=True))
 probs /= np.sum(probs, axis=1, keepdims=True)
 N = x.shape[0]
 loss = -np.sum(np.log(probs[np.arange(N), y])) / N
  dx = probs.copy()
 dx[np.arange(N), y] = 1
  dx /= N
 return loss, dx
```

## 1.10 fc\_net.py

```
[]: import numpy as np
from .layers import *
from .layer_utils import *
```

```
11 11 11
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
11 11 11
class TwoLayerNet(object):
  .....
 A two-layer fully-connected neural network with ReLU nonlinearity and
 softmax loss that uses a modular layer design. We assume an input dimension
 of D, a hidden dimension of H, and perform classification over C classes.
 The architecure should be affine - relu - affine - softmax.
 Note that this class does not implement gradient descent; instead, it
 will interact with a separate Solver object that is responsible for running
 optimization.
 The learnable parameters of the model are stored in the dictionary
 self.params that maps parameter names to numpy arrays.
 def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
              dropout=0, weight_scale=1e-3, reg=0.0):
   Initialize a new network.
   Inputs:
   - input_dim: An integer giving the size of the input
   - hidden_dims: An integer giving the size of the hidden layer
   - num_classes: An integer giving the number of classes to classify
   - dropout: Scalar between 0 and 1 giving dropout strength.
   - weight_scale: Scalar giving the standard deviation for random
     initialization of the weights.
    - reg: Scalar giving L2 regularization strength.
   self.params = {}
   self.reg = reg
    # ------ #
    # YOUR CODE HERE:
    # Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
```

```
# self.params['W2'], self.params['b1'] and self.params['b2']. The
 # biases are initialized to zero and the weights are initialized
   so that each parameter has mean O and standard deviation weight_scale.
 # The dimensions of W1 should be (input_dim, hidden_dim) and the
 # dimensions of W2 should be (hidden dims, num classes)
 self.params['W1'] = weight_scale * np.random.randn(input_dim, hidden_dims)
 self.params['b1'] = np.zeros(hidden_dims)
 self.params['W2'] = weight_scale * np.random.randn(hidden_dims, num_classes)
 self.params['b2'] = np.zeros(num_classes)
 # ----- #
 # END YOUR CODE HERE
 # ----- #
def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 - X: Array of input data of shape (N, d_1, \ldots, d_k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns.
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
  scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - grads: Dictionary with the same keys as self.params, mapping parameter
  names to gradients of the loss with respect to those parameters.
 scores = None
 # YOUR CODE HERE:
 # Implement the forward pass of the two-layer neural network. Store
 # the class scores as the variable 'scores'. Be sure to use the layers
   you prior implemented.
 # ------ #
 # Unpack variables from the params dictionary
 W1, b1 = self.params['W1'], self.params['b1']
 W2, b2 = self.params['W2'], self.params['b2']
```

```
h, h_cache = affine_relu_forward(X,W1,b1)
  scores, z_cache = affine_forward(h,W2,b2)
  # END YOUR CODE HERE
   # If y is None then we are in test mode so just return scores
  if y is None:
    return scores
  loss, grads = 0, {}
  # =========== #
   # YOUR CODE HERE:
     Implement the backward pass of the two-layer neural net. Store
     the loss as the variable 'loss' and store the gradients in the
     'grads' dictionary. For the grads dictionary, grads['W1'] holds
    the gradient for W1, grads['b1'] holds the gradient for b1, etc.
     i.e., grads[k] holds the gradient for self.params[k].
  # Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
     for each W. Be sure to include the 0.5 multiplying factor to
  #
     match our implementation.
  # And be sure to use the layers you prior implemented.
   # ----- #
  loss, dLdz = softmax_loss(scores,y)
  loss = loss+0.5*self.reg*(np.sum(W1**2)+np.sum(W2**2))
  dh, dw2, db2 = affine_backward(dLdz,z_cache)
  grads['W2'] = dw2 + self.reg*W2
  grads['b2'] = db2
  dx, dw1, db1 = affine_relu_backward(dh,h_cache)
  grads['W1'] = dw1 + self.reg*W1
  grads['b1'] = db1
  # END YOUR CODE HERE
   return loss, grads
class FullyConnectedNet(object):
 A fully-connected neural network with an arbitrary number of hidden layers,
```

```
ReLU nonlinearities, and a softmax loss function. This will also implement
dropout and batch normalization as options. For a network with L layers,
the architecture will be
\{affine - [batch norm] - relu - [dropout]\} \times (L - 1) - affine - softmax
where batch normalization and dropout are optional, and the {...} block is
repeated L - 1 times.
Similar to the TwoLayerNet above, learnable parameters are stored in the
self.params dictionary and will be learned using the Solver class.
def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
             dropout=0, use_batchnorm=False, reg=0.0,
             weight_scale=1e-2, dtype=np.float32, seed=None):
  Initialize a new FullyConnectedNet.
  Inputs:
  - hidden_dims: A list of integers giving the size of each hidden layer.
  - input_dim: An integer giving the size of the input.
  - num_classes: An integer giving the number of classes to classify.
  - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
    the network should not use dropout at all.
  - use_batchnorm: Whether or not the network should use batch normalization.
  - reg: Scalar giving L2 regularization strength.
  - weight_scale: Scalar giving the standard deviation for random
    initialization of the weights.
  - dtype: A numpy datatype object; all computations will be performed using
   this datatype. float32 is faster but less accurate, so you should use
   float64 for numeric gradient checking.
  - seed: If not None, then pass this random seed to the dropout layers. This
   will make the dropout layers deteriminstic so we can gradient check the
   model.
  self.use_batchnorm = use_batchnorm
  self.use_dropout = dropout > 0
  self.reg = reg
  self.num_layers = 1 + len(hidden_dims)
  self.dtype = dtype
  self.params = {}
    Initialize all parameters of the network in the self.params dictionary.
    The weights and biases of layer 1 are W1 and b1; and in general the
```

```
# weights and biases of layer i are Wi and bi. The
   # biases are initialized to zero and the weights are initialized
  # so that each parameter has mean O and standard deviation weight_scale.
   # ----- #
  for i in np.arange(self.num_layers):
    W_{string} = W' + str(i+1)
    b_string = 'b' + str(i+1)
    #if first layer use input_dim
    if i == 0:
      self.params[W_string] = weight_scale * np.random.randn(input_dim,_
→hidden_dims[i])
      self.params[b_string] = np.zeros(hidden_dims[i])
    #if last layer use num classes
    elif i == self.num_layers - 1:
      self.params[W_string] = weight_scale * np.random.
→randn(hidden_dims[i-1], num_classes)
      self.params[b_string] = np.zeros(num_classes)
      self.params[W_string] = weight_scale * np.random.
→randn(hidden_dims[i-1], hidden_dims[i])
      self.params[b_string] = np.zeros(hidden_dims[i])
  # END YOUR CODE HERE
   # ----- #
  # When using dropout we need to pass a dropout_param dictionary to each
  # dropout layer so that the layer knows the dropout probability and the mode
  # (train / test). You can pass the same dropout param to each dropout layer.
  self.dropout_param = {}
  if self.use_dropout:
    self.dropout_param = {'mode': 'train', 'p': dropout}
    if seed is not None:
      self.dropout_param['seed'] = seed
  # With batch normalization we need to keep track of running means and
  # variances, so we need to pass a special bn_param object to each batch
  # normalization layer. You should pass self.bn_params[0] to the forward pass
  # of the first batch normalization layer, self.bn params[1] to the forward
  # pass of the second batch normalization layer, etc.
  self.bn_params = []
  if self.use_batchnorm:
    self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers -u
<u></u>1)]
  # Cast all parameters to the correct datatype
```

```
for k, v in self.params.items():
    self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
  Compute loss and gradient for the fully-connected net.
  Input / output: Same as TwoLayerNet above.
  X = X.astype(self.dtype)
  mode = 'test' if y is None else 'train'
  # Set train/test mode for batchnorm params and dropout param since they
  # behave differently during training and testing.
  if self.dropout param is not None:
    self.dropout_param['mode'] = mode
  if self.use_batchnorm:
    for bn_param in self.bn_params:
      bn_param[mode] = mode
  scores = None
  # ----- #
  # YOUR CODE HERE:
  # Implement the forward pass of the FC net and store the output
  # scores as the variable "scores".
  h = []
  h_{cache} = []
  for i in np.arange(self.num_layers):
    W_str = 'W' + str(i+1)
    b_str = 'b' + str(i+1)
    if i == 0:
      tmp_h, tmp_h_cache = affine_relu_forward(X,self.params[W_str],self.
→params[b_str])
      h.append(tmp h)
      h_cache.append(tmp_h_cache)
    elif i == self.num_layers - 1:
      scores, z_cache = affine_forward(h[i-1],self.params[W_str],self.
→params[b_str])
    else:
      tmp_h, tmp_h_cache = affine_relu_forward(h[i-1],self.params[W_str],self.
→params[b_str])
      h.append(tmp_h)
      h_cache.append(tmp_h_cache)
```

```
# ----- #
# END YOUR CODE HERE
# ------ #
# If test mode return early
if mode == 'test':
 return scores
loss, grads = 0.0, {}
# ----- #
# YOUR CODE HERE:
# Implement the backwards pass of the FC net and store the gradients
# in the grads dict, so that grads[k] is the gradient of self.params[k]
# Be sure your L2 regularization includes a 0.5 factor.
# ----- #
loss, dLdz = softmax_loss(scores,y)
sqr_sum = 0
for i in np.arange(self.num_layers,0,-1):
 W_str = 'W' + str(i)
 b_str = 'b' + str(i)
 sqr_sum += np.sum(self.params[W_str]**2)
 if i == self.num_layers:
  dhi , dwi, dbi = affine_backward(dLdz,z_cache)
  grads[W_str] = dwi + self.reg*self.params[W_str]
  grads[b_str] = dbi
 else:
  dhi , dwi, dbi = affine_relu_backward(dhi,h_cache[i-1])
  grads[W_str] = dwi + self.reg*self.params[W_str]
  grads[b_str] = dbi
loss += 0.5*self.reg*(sqr_sum)
# END YOUR CODE HERE
return loss, grads
```