



భారతీయ సాంకేతిక విజ్ఞాన సంస్థ హైదరాబాద్
भारतीय प्रौद्योगिकी संस्थान हैदराबाद
Indian Institute of Technology Hyderabad

Biostatistics BT2023

Lecture 10

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Start-up notes

Reading material folder



Standard deviation

Derivations ?

$$\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}} = \sqrt{\frac{\sum x_i^2 - n\bar{x}^2}{n}}$$

n used for Population

$$s = \sqrt{\frac{\sum x_i^2 - n\bar{x}^2}{n - 1}}$$

$n-1$ used for Sample

$$\text{Variance} = \sigma^2$$



Standard deviation by transformation

$$y=ax$$

$$\sigma_y = a\sigma_x$$

$$y=a+x$$

$$\sigma_y = \sigma_x$$

$$y=a+cx$$

$$\sigma_y = c\sigma_x$$



Standard error in Mean

$$\sigma_M = \frac{\sigma}{\sqrt{n}}$$

Z-score

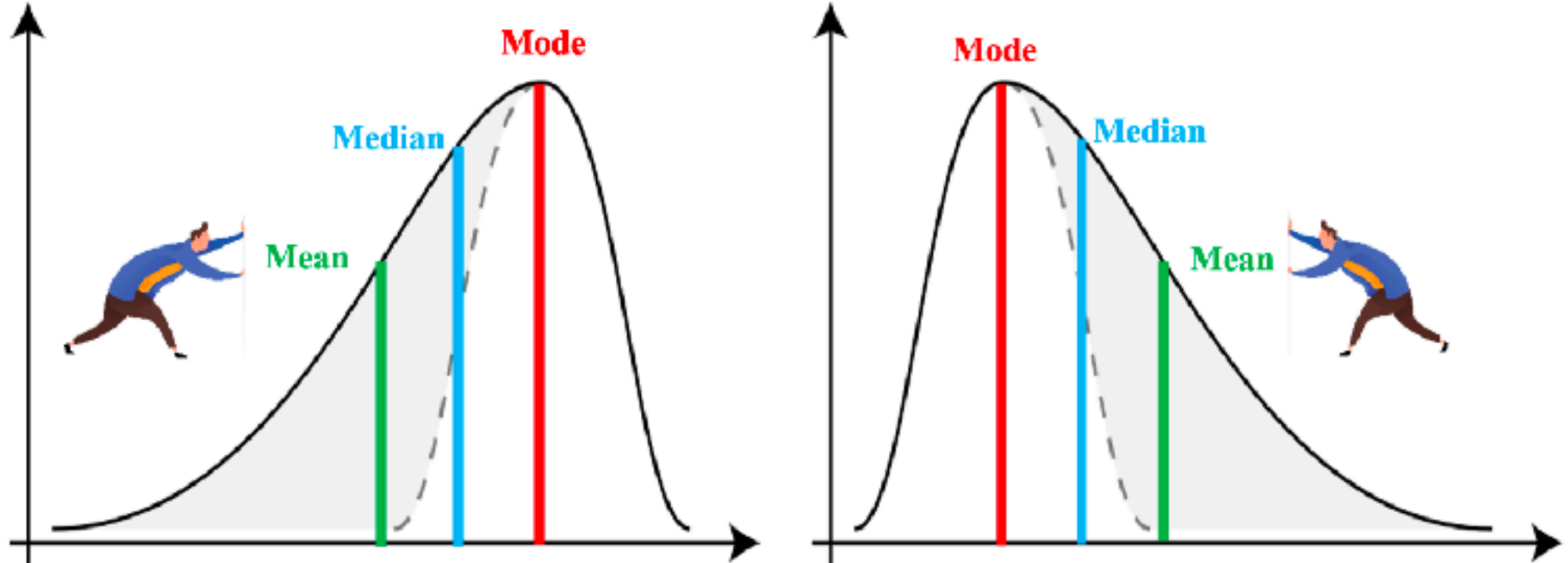
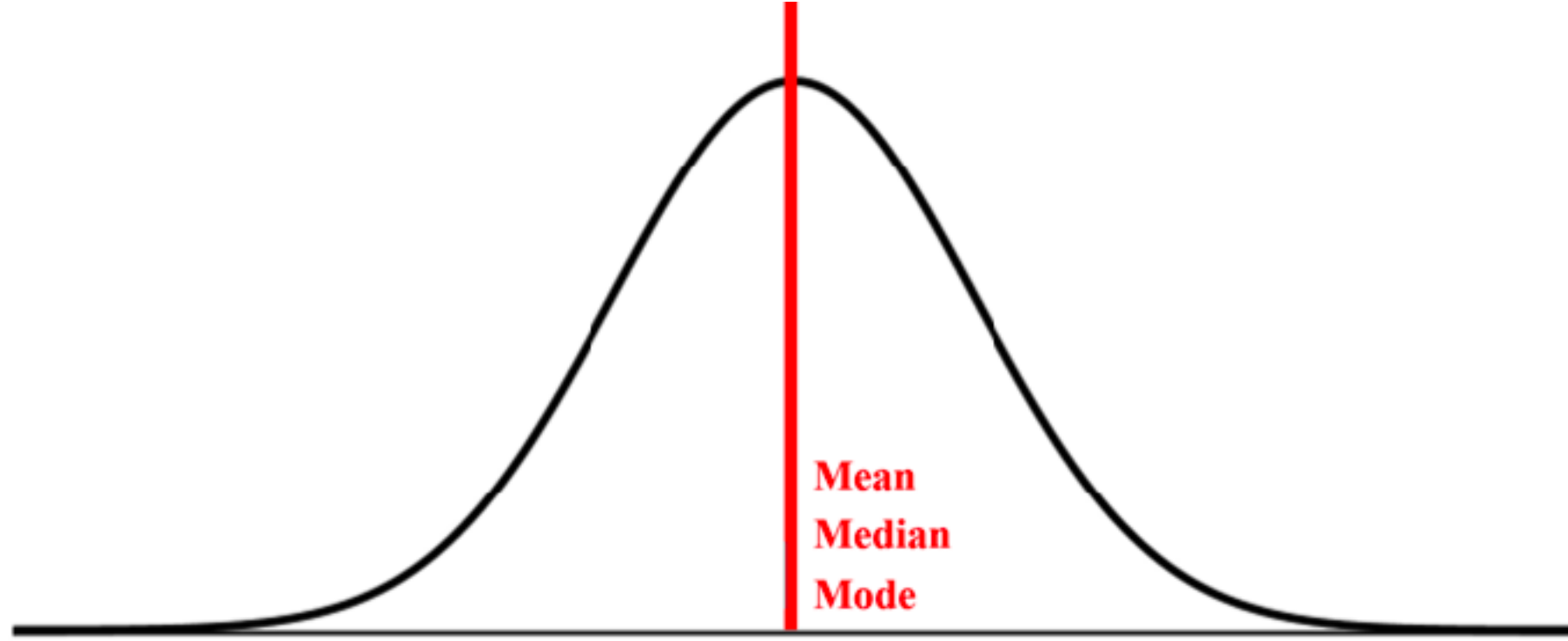
$$Z_{score} = \frac{x - \bar{x}}{\sigma}$$

To find if the data points is to the outliers

Z_score > 3 are called outlier



Skewness





Absolute skewness

Mean - Mode

Karl Pearson coefficient of skewness

$$S_k = \frac{\text{Mean} - \text{Mode}}{\text{Standard deviation}} = \frac{3(\text{Mean} - \text{Median})}{\text{Standard deviation}}$$

Bowley's coefficient of skewness

$$S_k = \frac{Q_3 - Q_1 - 2\text{Median}}{Q_3 - Q_1}$$

$$-1 \geq S_k(\text{Bowley's}) \leq +1$$



Skewness

Kelly's measure of skewness

$$S_k = \frac{P_{10} + P_{90} - 2Median}{P_{90} - P_{10}}$$

Since Bowley's coefficient ignore 50 % of the values in the extreme, hence this method was suggested by Kelly.



Skewness coefficient based on moments

Moments in mechanics is refers to the rotating effect of a force, in statistics it is used to describe the peculiarities in the frequency distribution

$$\begin{array}{ll} \text{First moment : } \mu_1 & \frac{\sum (X - \bar{X})}{N} \quad \frac{\sum f(X - \bar{X})}{N} \\ \text{Always 0} & \end{array}$$

$$\begin{array}{ll} \text{Second moment : } \mu_2 & \frac{\sum (X - \bar{X})^2}{N} \quad \frac{\sum f(X - \bar{X})^2}{N} \\ \text{Measure the} & \\ \text{variance} & \end{array}$$

$$\begin{array}{ll} \text{Third moment : } \mu_3 & \frac{\sum (X - \bar{X})^3}{N} \quad \frac{\sum f(X - \bar{X})^3}{N} \\ \text{Measure skewness} & \end{array}$$

$$\begin{array}{ll} \text{Forth moment : } \mu_4 & \frac{\sum (X - \bar{X})^4}{N} \quad \frac{\sum f(X - \bar{X})^4}{N} \\ \text{Measure Kurtosis} & \end{array}$$

Skewness

Skewness coefficient $\beta_1 = \frac{\mu_3^2}{\mu_2^3}$

adjusted Fisher-Pearson coefficient

$$\frac{\sqrt{N(N-1)}}{N} \frac{\mu_3^2}{\mu_2^3}$$

The pre factor approaches to 1 as N tends to large values

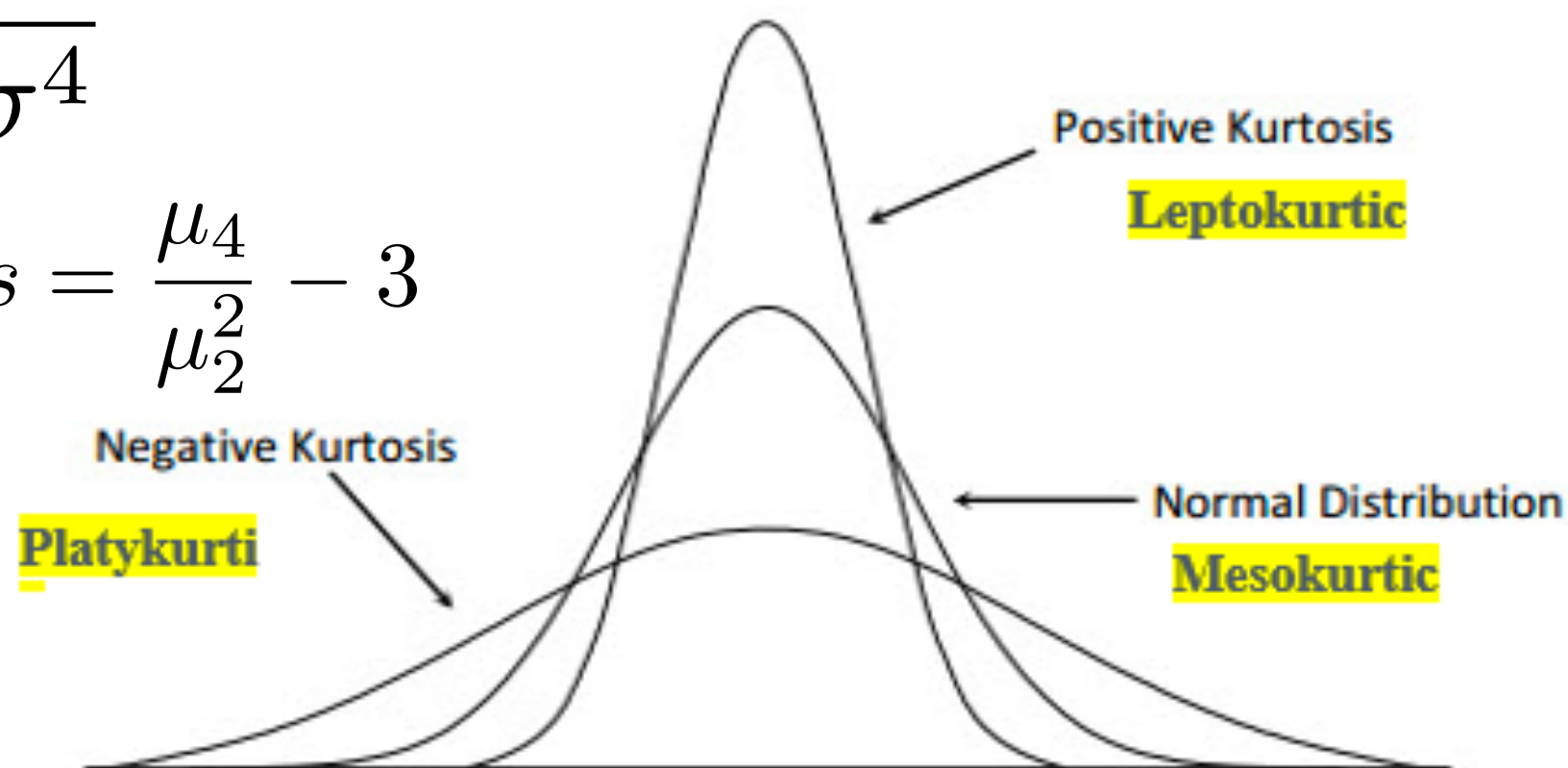


Kurtosis

Measure of “tailedness” or peakedness

$$K|X| = \frac{\mu_4}{\sigma^4}$$

$$\text{Excess Kurtosis} = \frac{\mu_4}{\mu_2^2} - 3$$



Positive kurtosis indicates a "heavy-tailed" distribution >> Leptokurtic
Negative kurtosis indicates a "light tailed" distribution >> Platykurtic

I want you to think about these coefficients, look the formula closely, see if you can relate to a mathematical formula you have seen before

Violin plot

A Violin Plot is used to visualize the distribution of the data and its probability density.

The white dot in the middle shows the median value and the thick black bar in the centre represents the interquartile range

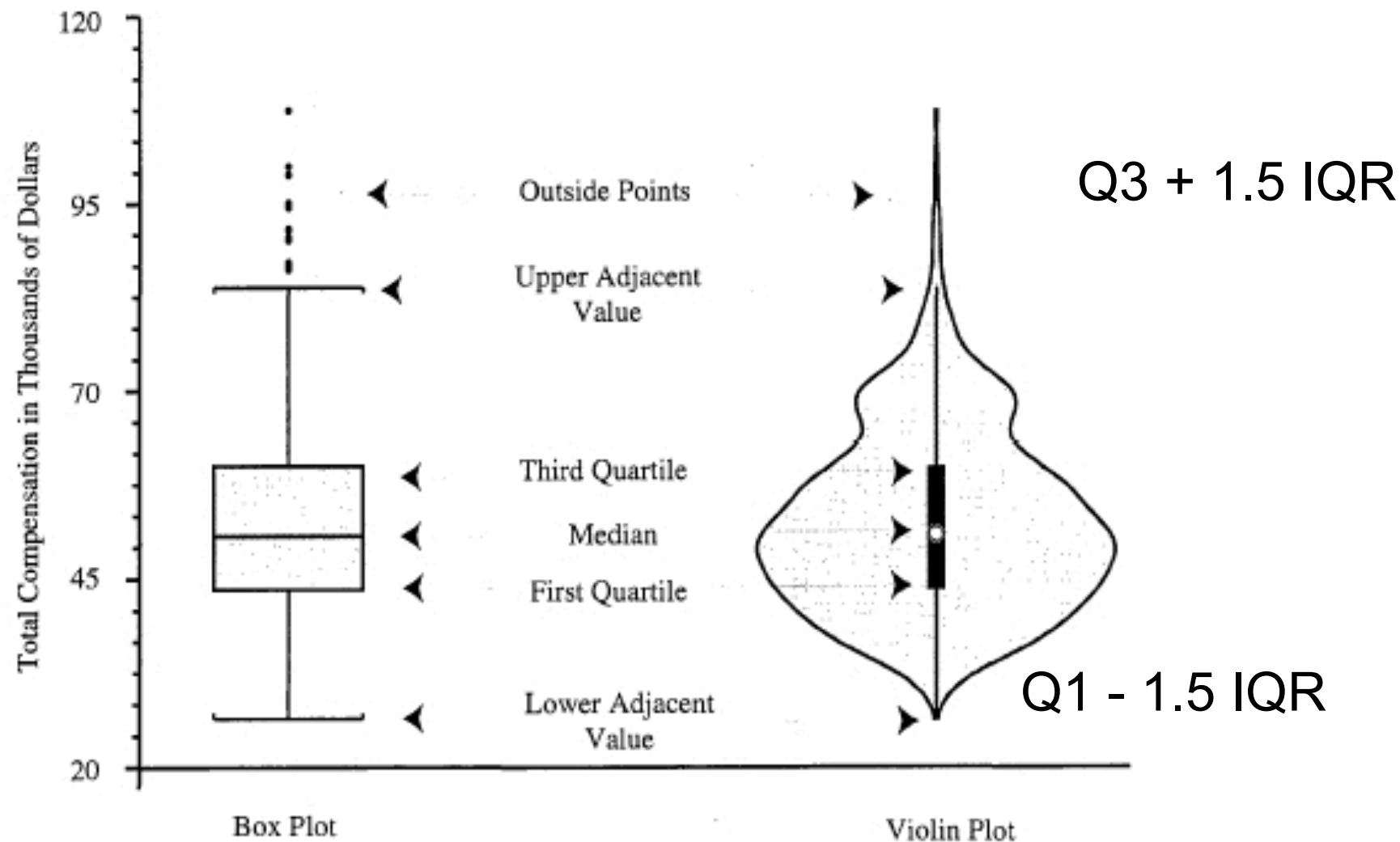


Figure 1. Common Components of Box Plot and Violin Plot. Total compensation for all academic ranks.



Violin plot

