Chapter 1

Preliminaries

1.1 Preliminaries

Multisets

A Multiset M with underlying set S is a set of ordered pairs

$$M = \{(s_i, n_i) | s_i \in S, n_i \in \mathbb{Z}^+, s_i \neq s_j \forall i \neq j\}$$

Matrices

 $\mathcal{M}_{m,n}(F)$: the set of $m \times n$ matrices. Properties of transpose:

- $1. \ \left(A^T\right)^T = A$
- 2. $(A+B)^T = A^T + B^T$
- 3. $(rA)^T = rA^T \ \forall r \in F$
- $4. \ (AB)^T = B^T A^T$