

CLUSTERING

Naumaan Nayyar

EXIT TICKETS

- ▶ Review Logit / Sigmoid
- ▶ What is a [link function](#), conceptually? When would we use arctan?
- ▶ [Neural Networks](#)
- ▶ How to optimize for lower false positives or negatives? ROC Curve
- ▶ Can logistic regression work with more than two classes? [Yep](#) and [see here](#)
- ▶ How would we measure the accuracy of the classification of any given point with logistic regression?
- ▶ Are there any practice notebooks?

CLUSTERING

LEARNING OBJECTIVES

- ▶ Supervised vs unsupervised algorithms
- ▶ Understand and apply k-means clustering
- ▶ Density-based clustering: DBSCAN
- ▶ Silhouette Metric

OPENING

UNSUPERVISED LEARNING

UNSUPERVISED LEARNING

- ▶ So far all the algorithms we have used are *supervised*: each observation (row of data) came with one or more *labels*, either *categorical variables* (classes) or *measurements* (regression)
- ▶ **Unsupervised learning** has a different goal: **feature discovery**
- ▶ **Clustering** is a common and fundamental example of unsupervised learning
- ▶ **Clustering** algorithms try to find meaningful groups within data

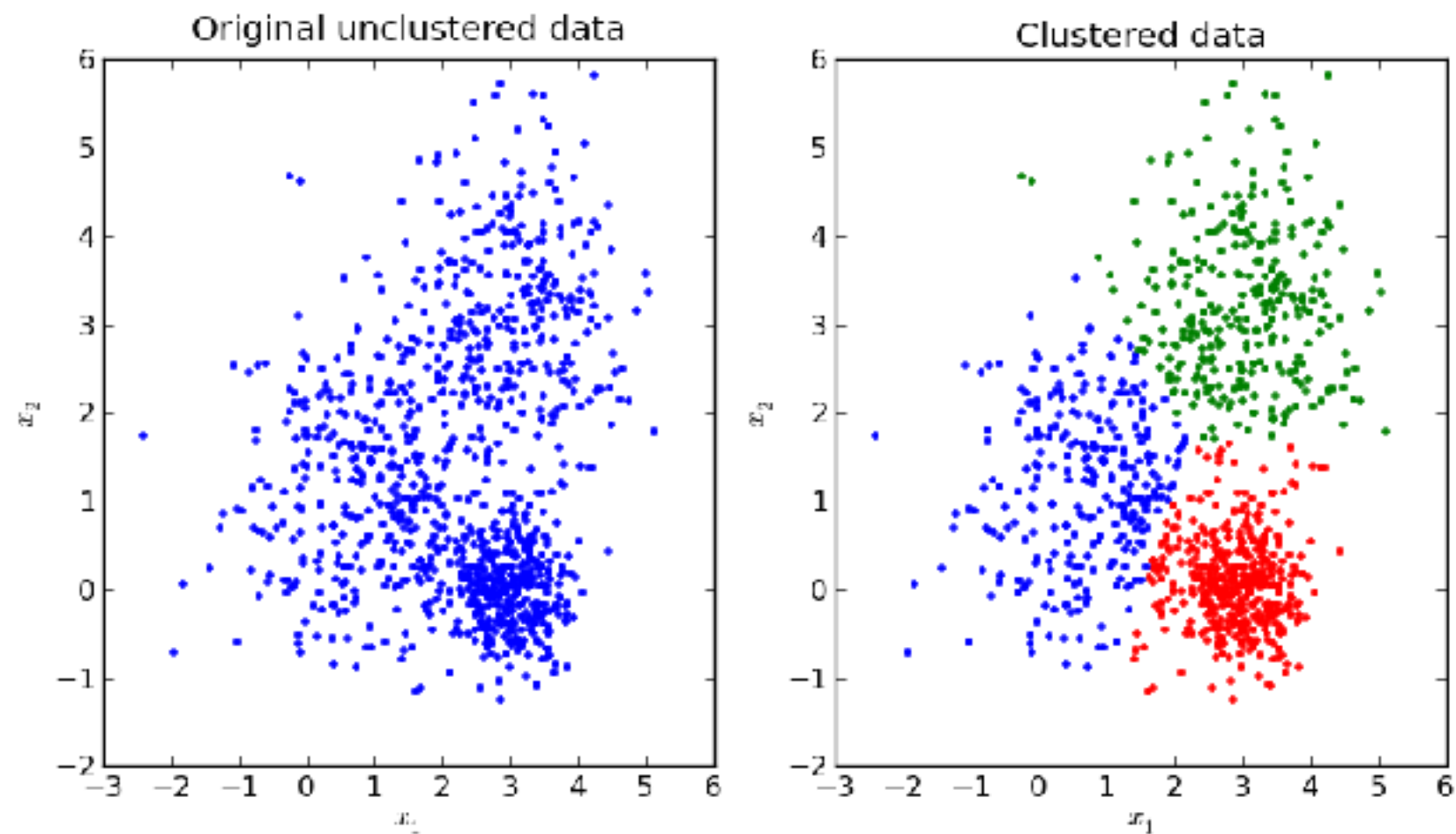
CLUSTERING

CLUSTERING

CLUSTERING: Types of clustering algorithms

- ▶ Clustering algorithms are of several types based on model assumptions:
 - ▶ Centroid-based
 - ▶ Density-based
 - ▶ Hierarchical (connectivity- or linkage-based)
 - ▶ Distribution-based

CLUSTERING: Centroids



Source: <http://stackoverflow.com/questions/24645068/k-means-clustering-major-understanding-issue>

ACTIVITY: KNOWLEDGE CHECK



EXERCISE

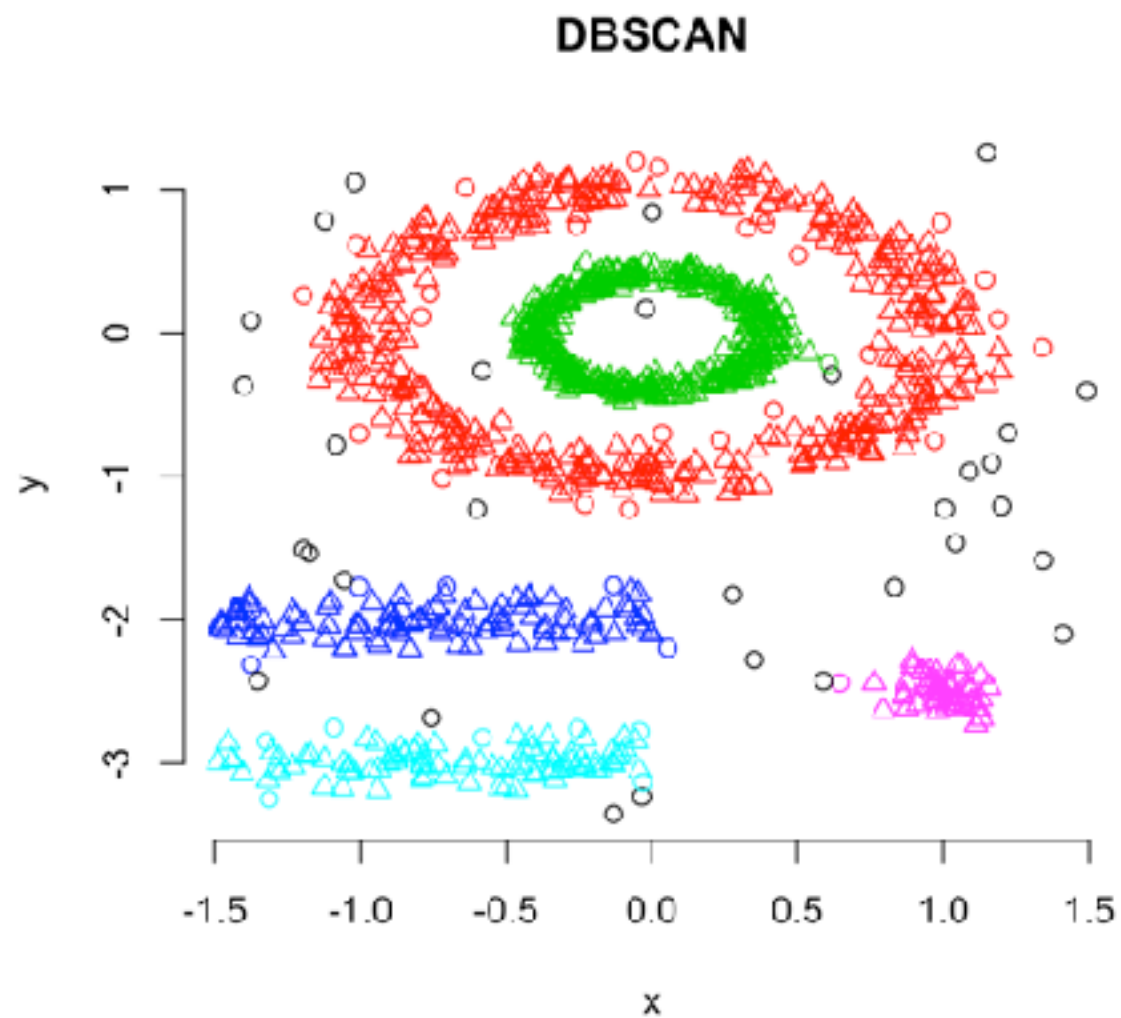
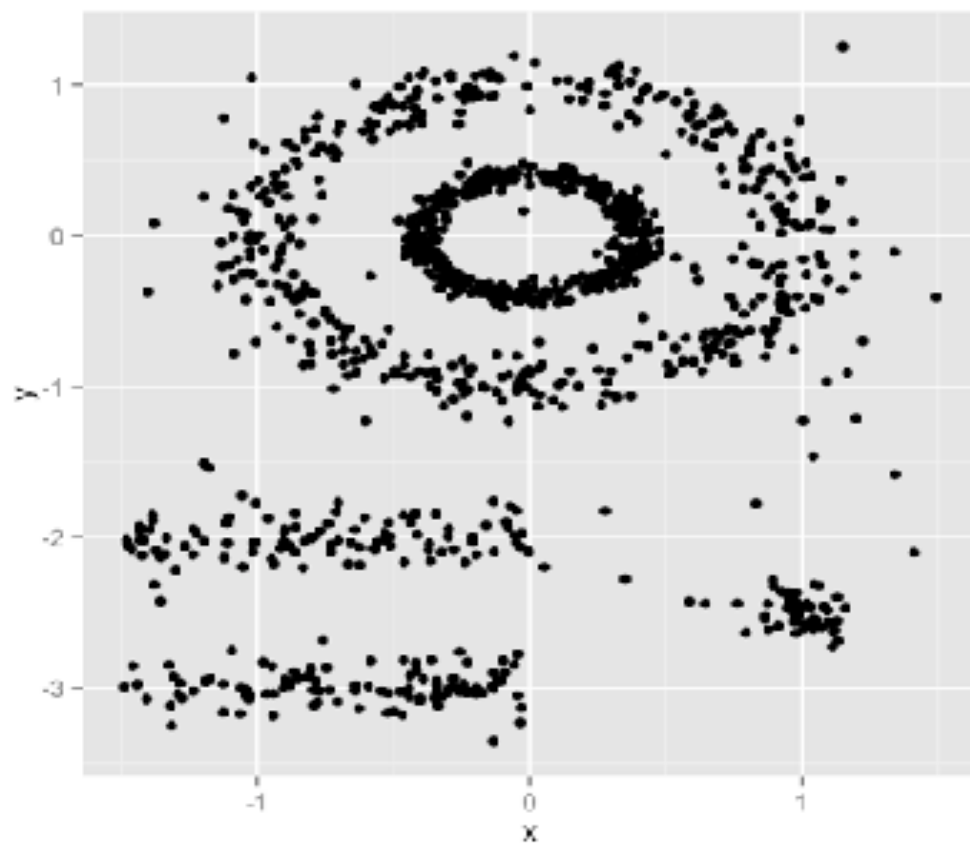
ANSWER THE FOLLOWING QUESTIONS

1. Why might data often appear in centered clusters?

DELIVERABLE

Answers to the above questions

CLUSTERING: Density-Based



ACTIVITY: KNOWLEDGE CHECK



EXERCISE

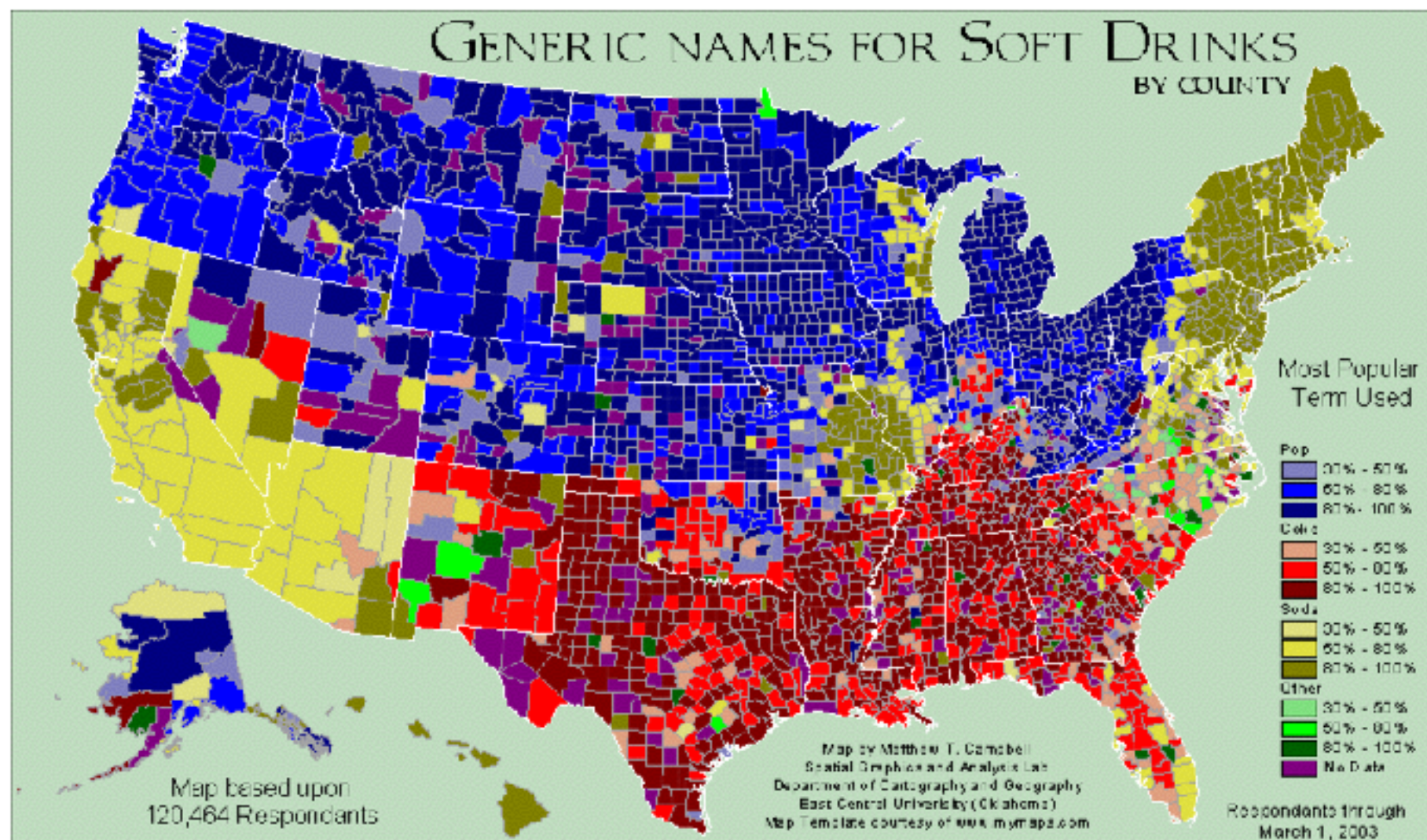
ANSWER THE FOLLOWING QUESTIONS

1. Why might data often appear in density-based clusters?

DELIVERABLE

Answers to the above questions

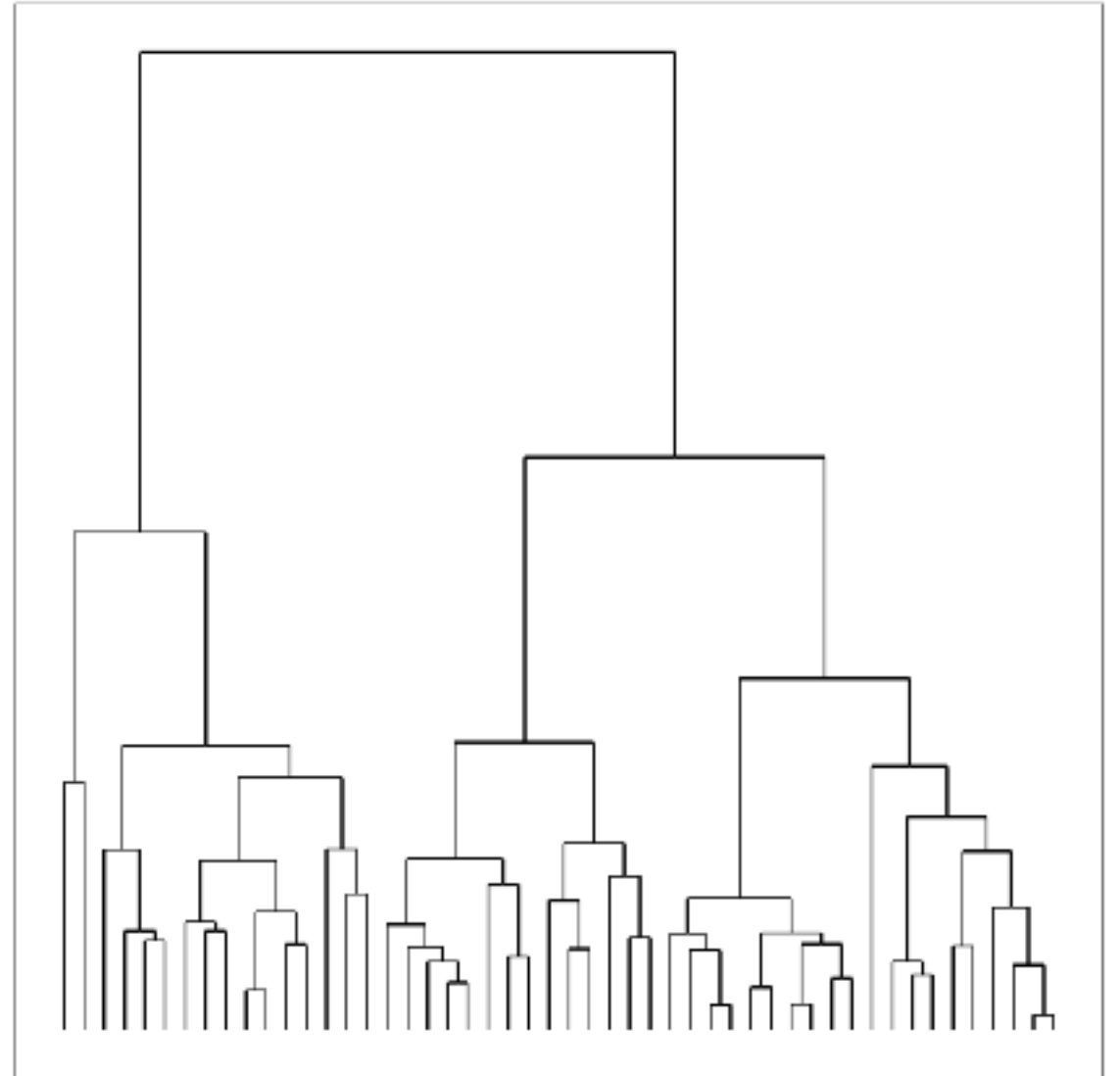
ACTIVITY: KNOWLEDGE CHECK



See also: <http://www4.ncsu.edu/~jakatz2/files/dialectposter.png>

CLUSTERING: Hierarchical

- ▶ Build hierarchies that form clusters
- ▶ Based on classification trees (next lesson)



ACTIVITY: KNOWLEDGE CHECK



EXERCISE

ANSWER THE FOLLOWING QUESTIONS

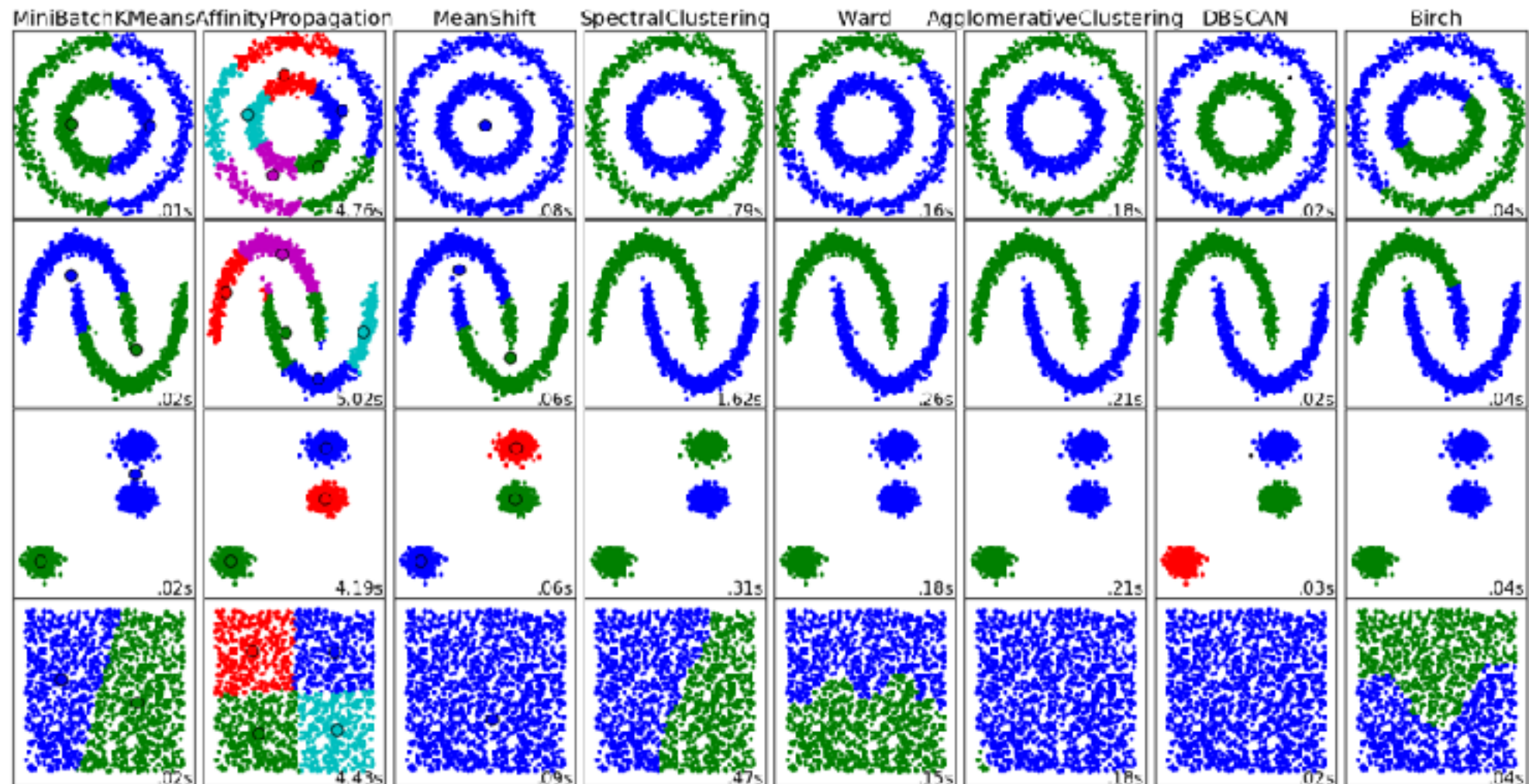
1. How is unsupervised learning different from classification?

DELIVERABLE

Answers to the above questions

CLUSTERING

- There are [many clustering algorithms](#)



ACTIVITY: KNOWLEDGE CHECK



EXERCISE

ANSWER THE FOLLOWING QUESTIONS

1. Can you think of a real-world clustering application?

DELIVERABLE

Answers to the above questions

ACTIVITY: KNOWLEDGE CHECK

ANSWERS



EXERCISE

1. Recommendation Systems e.g. Netflix genres
2. Medical Imaging: differentiate tissues
3. Identifying market segments
4. Discover communities in social networks
5. Lots of applications for genomic sequences (homologous sequences, genotypes)
6. Earthquake epicenters
7. Fraud detection

CLUSTERING

K-MEANS: CENTRIOD CLUSTERING

K-MEANS CLUSTERING

- ▶ [k-Means](#) clustering is a popular centroid-based clustering algorithm
- ▶ Basic idea: find k clusters in the data centrally located around various mean points
- ▶ [Awesome Demo](#)

K-MEANS CLUSTERING

- ▶ k-Means seeks to minimize the sum of squares about the means
- ▶ Precisely, find k subsets S_1, \dots, S_k of the data with means μ_1, \dots, μ_k that minimizes:

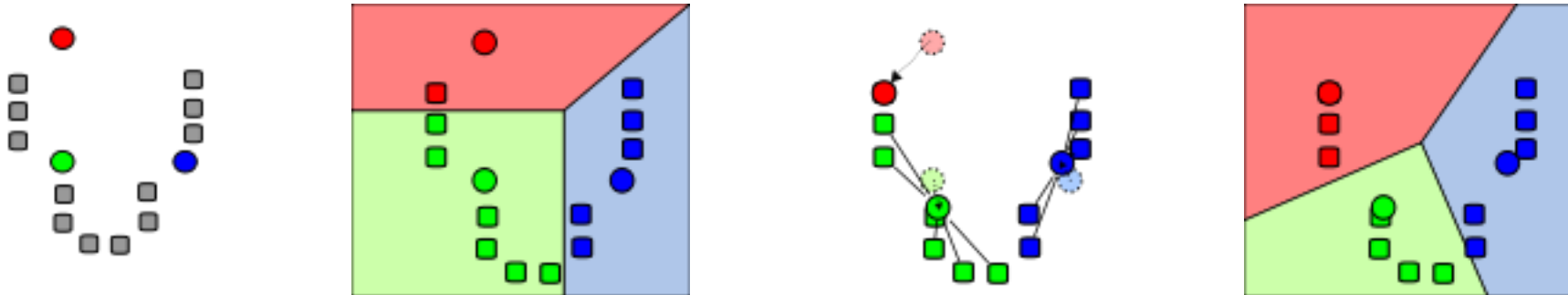
$$\arg \min_{\mathbf{S}} \sum_{i=1}^k \sum_{\mathbf{x} \in S_i} \|\mathbf{x} - \boldsymbol{\mu}_i\|^2$$

K-MEANS CLUSTERING

- ▶ This is a computationally difficult problem to solve so we rely on heuristics
- ▶ The “standard” heuristic is called “Lloyd’s Algorithm”:
 - ▶ Start with k initial mean values
 - ▶ Data points are then split up into a [Voronoi diagram](#)
 - ▶ Each point is assigned to the “closest” mean
 - ▶ Calculate new means based on centroids of points in the cluster
 - ▶ Repeat until clusters do not change

K-MEANS CLUSTERING

- ▶ Start with initial k mean values
- ▶ Data points are then split up into a [Voronoi diagram](#)
- ▶ Calculate new means based on centroids



K-MEANS CLUSTERING

- ▶ from sklearn.cluster import [KMeans](#)
- ▶ est = [KMeans](#)(n_clusters=3)
- ▶ est.fit(X)
- ▶ labels = est.labels_

Let's try it out!

ACTIVITY: KNOWLEDGE CHECK



EXERCISE

ANSWER THE FOLLOWING QUESTIONS

1. How do we assign meaning to the clusters we find?
2. Do clusters always have meaning?

DELIVERABLE

Answers to the above questions

K-MEANS CLUSTERING

- ▶ Assumptions are important! k-Means assumes:
 - ▶ k is the correct number of clusters
 - ▶ the data is isotropically distributed (circular/spherical distribution)
 - ▶ the variance is the same for each variable
 - ▶ clusters are roughly the same size

Nice counterexamples / cases where assumptions are not met:

- <http://varianceexplained.org/r/kmeans-free-lunch/>
- [Scikit-Learn Examples](#)

K-MEANS CLUSTERING

- ▶ Netflix prize: Predict how users will rate a movie
 - ▶ How might you do this with clustering?
 - ▶ Cluster similar users together and take the average rating for a given movie by users in the cluster (which have rated the movie)
 - ▶ Use the average as the prediction for users that have not yet rated the movie
- ▶ In other words, fit a model to users in a cluster for each cluster and make predictions per cluster
- ▶ [k-Means for the Netflix Prize](#)

CLUSTERING

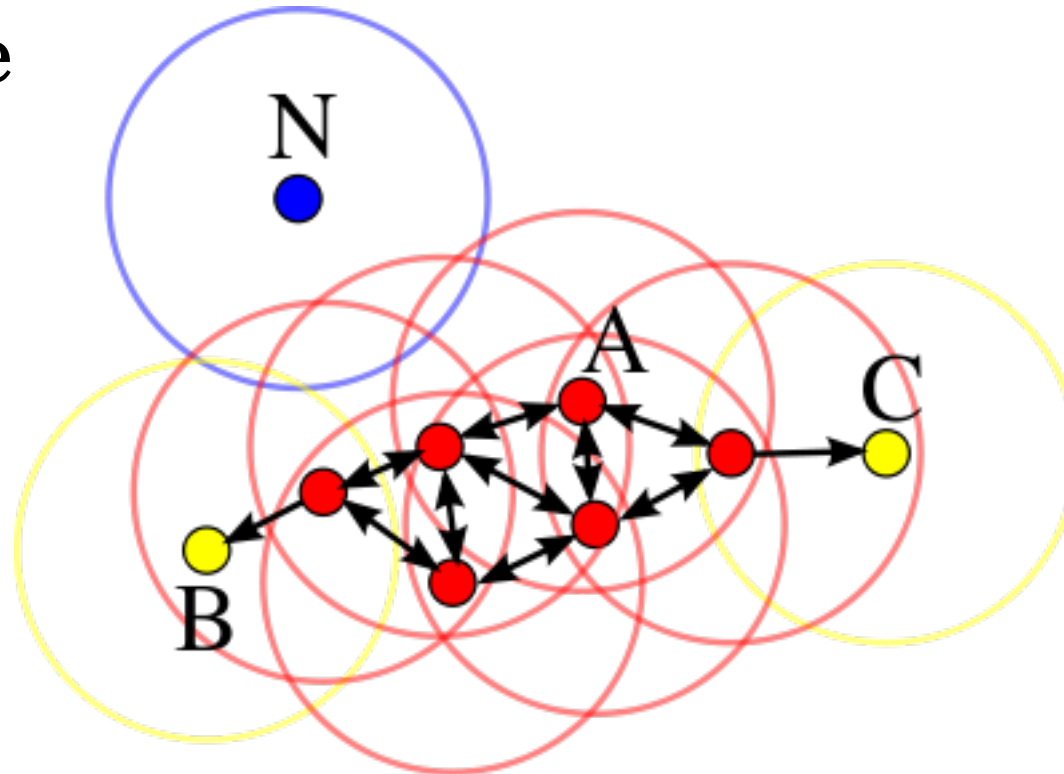
DBSCAN: DENSITY BASED CLUSTERING

DBSCAN CLUSTERING

- ▶ [DBSCAN](#): Density-based spatial clustering of applications with noise (1996)
- ▶ Main idea: Group together closely-packed points by identifying
 - ▶ Core points
 - ▶ Reachable points
 - ▶ Outliers (not reachable)
- ▶ Two parameters:
 - ▶ min_samples
 - ▶ eps

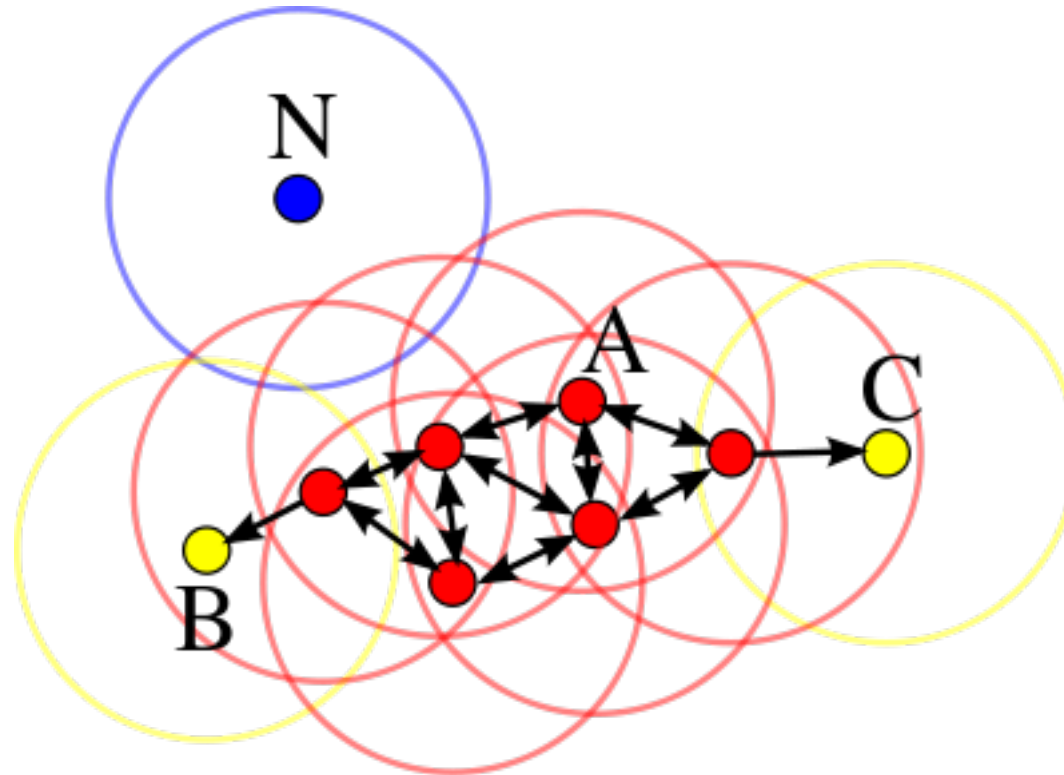
DBSCAN CLUSTERING

- ▶ Core points: at least **min_samples** points within **eps** of the core point
 - ▶ Such points are *directly reachable* from the core point
- ▶ Reachable: point q is reachable from p if there is a path of core points from p to q
- ▶ Outlier: not reachable



DBSCAN CLUSTERING

- ▶ A cluster is a collection of connected core and reachable points



CLUSTERING: Density-Based

- ▶ Another example: [Page 6](#)
- ▶ [Awesome Demo](#)

DBSCAN CLUSTERING

- `from sklearn.cluster import DBSCAN`
- `est = DBSCAN(eps=0.5, min_samples=10)`
- `est.fit(X)`
- `labels = est.labels_`

Let's try it out!

ACTIVITY: KNOWLEDGE CHECK



EXERCISE

ANSWER THE FOLLOWING QUESTIONS

1. How does DBSCAN differ from k-means?

DELIVERABLE

Answers to the above questions

DBSCAN CLUSTERING

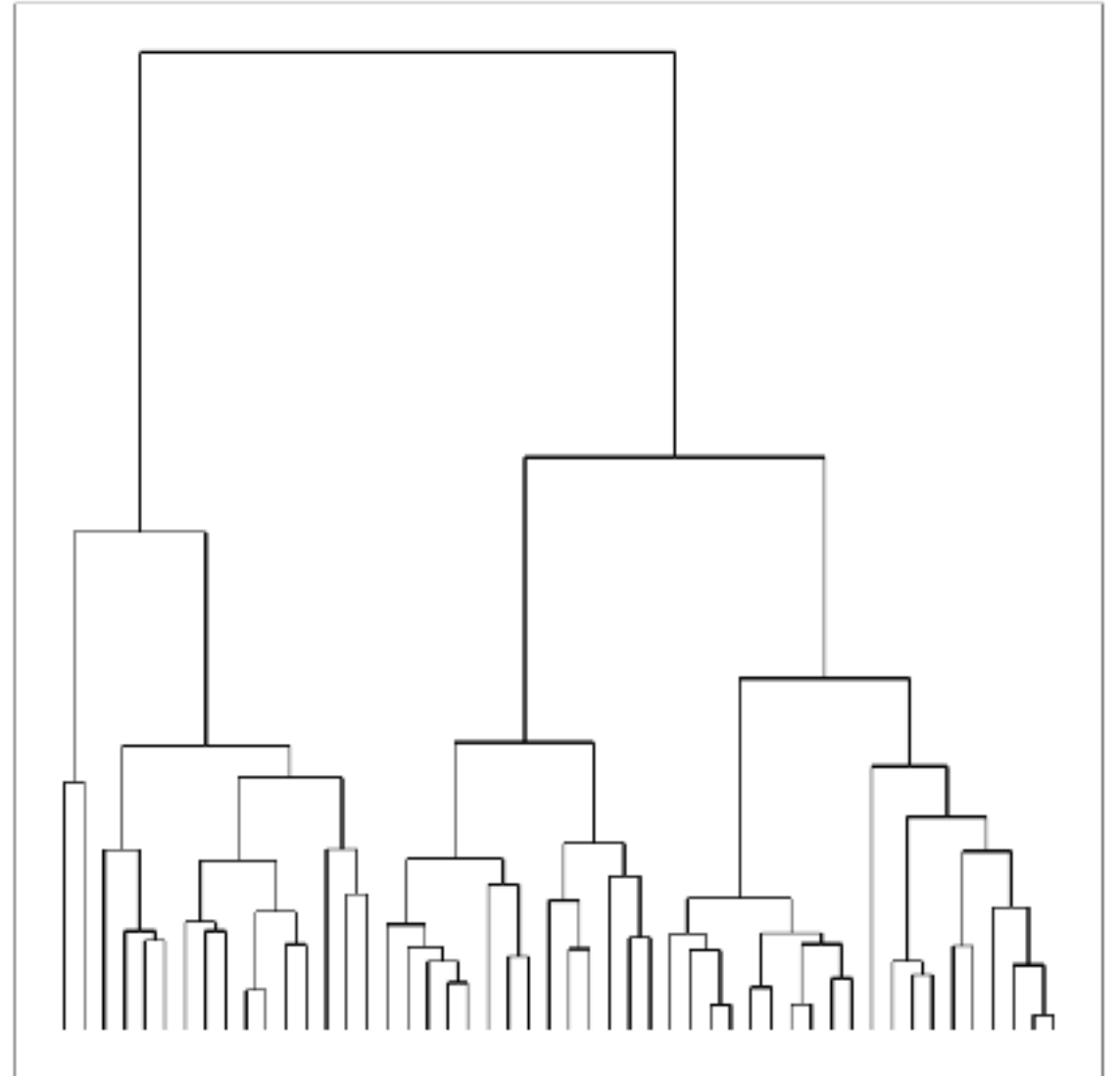
- ▶ DBSCAN advantages:
 - ▶ Can find arbitrarily-shaped clusters
 - ▶ Don't have to specify number of clusters
 - ▶ Robust to outliers
- ▶ DBSCAN disadvantages:
 - ▶ Doesn't work well when clusters are of varying densities
 - ▶ hard to chose parameters that work for all clusters
 - ▶ Can be hard to chose correct parameters regardless

CLUSTERING

HIERARCHICAL CLUSTERING

CLUSTERING: Hierarchical

- ▶ Build hierarchies that form clusters
- ▶ Based on classification trees (next lesson)



HIERARCHICAL CLUSTERING

We'll discuss the details once we cover decision trees. For now we can black box the model and fit with sklearn

```
▶ from sklearn.cluster import AgglomerativeClustering  
▶ est = AgglomerativeClustering(n_clusters=4)  
▶ est.fit(X)  
▶ labels = est.labels_
```

Let's try it out!

CLUSTERING

CLUSTERING METRICS

CLUSTERING METRICS

- As usual we need a metric to evaluate model fit
- For clustering we use a metric called the [Silhouette Coefficient](#)
 - **a** is the mean distance between a sample and all other points in the cluster
 - **b** is the mean distance between a sample and all other points in the *nearest* cluster

- The Silhouette Coefficient is:

$$\frac{b - a}{\max(a, b)}$$

- Ranges between 1 and -1
- Average over all points to judge the cluster algorithm

CLUSTERING METRICS

- ▶ `from sklearn import metrics`
- ▶ `from sklearn.cluster import KMeans`
- ▶ `kmeans_model = KMeans(n_clusters=3, random_state=1).fit(X)`
- ▶ `labels = kmeans_model.labels_`
- ▶ `metrics.silhouette_score(X, labels, metric='euclidean')`

CLUSTERING METRICS

- ▶ There are a number of [other metrics](#) based on:
 - ▶ Mutual Information
 - ▶ Homogeneity
 - ▶ Adjusted Rand Index (when you know the labels on the training data)

PUTTING IT TOGETHER

CLUSTERING, CLASSIFICATION, AND REGRESSION

ACTIVITY: KNOWLEDGE CHECK



EXERCISE

ANSWER THE FOLLOWING QUESTIONS

1. How might we combine clustering and regression or classification?

DELIVERABLE

Answers to the above questions

CLUSTERING, CLASSIFICATION, AND REGRESSION

- ▶ We can use clustering to discover new features and then use those features for either classification or regression
- ▶ For classification, we could use e.g. k-NN to classify new points into the discovered clusters
- ▶ For regression, we could use a dummy variable for the clusters as a variable in our regression

ACTIVITY: CLUSTERING + REGRESSION

EXERCISE



EXERCISE

1. Follow along as we do an example of clustering with regression.

DELIVERABLE

A completed notebook

CONCLUSION

TOPIC REVIEW

REVIEW AND NEXT STEPS

- ▶ Clustering is used to discover features, e.g. segment users or assign labels (such as species)
- ▶ Clustering may be the goal (user marketing) or a step in a data science pipeline

COURSE

BEFORE NEXT CLASS

BEFORE NEXT CLASS

UPCOMING

- ▶ Final Project part 2
 - ▶ Due Date: June 15th

LESSON

Q & A

LESSON

EXIT TICKET

DON'T FORGET TO FILL OUT YOUR EXIT TICKET