

# HW5

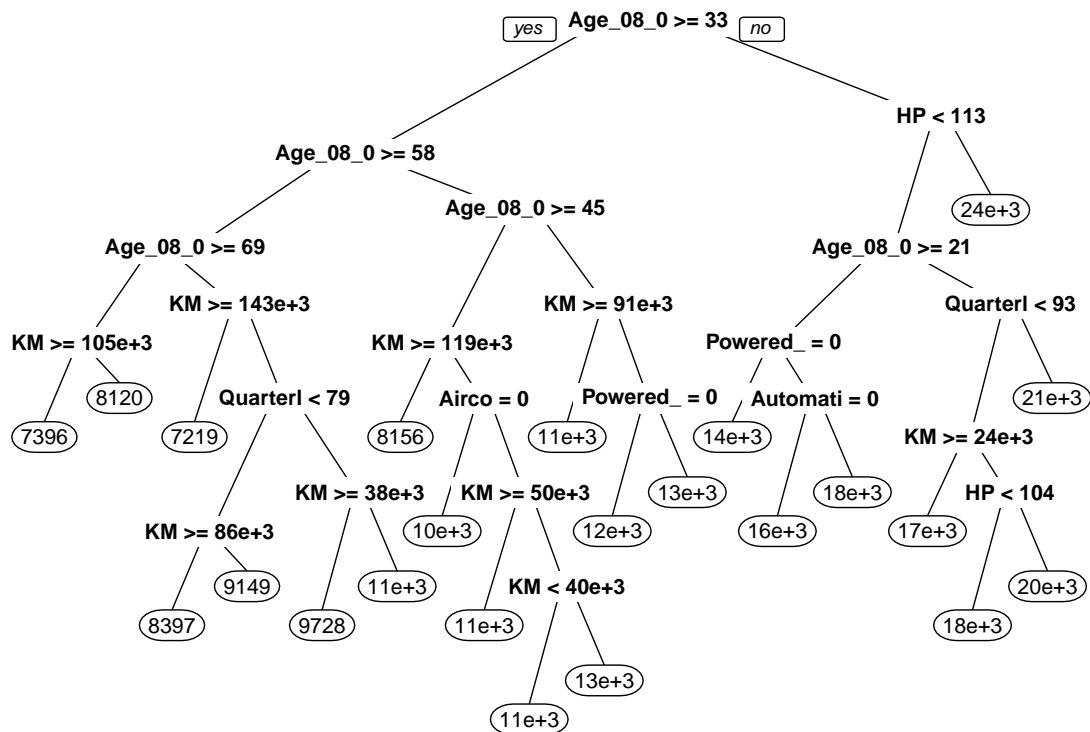
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#Problem 1

# Problem 1(a)(i)

```
rf<- rpart(Price ~ Age_08_04+ KM + Fuel_Type + HP + Automatic + Doors + Quarterly_Tax + Mfr_Guarantee +  
prp(rf)
```



The important predictors for predicting the car's price are - The age of the car, accumulated kilometers and horse power.

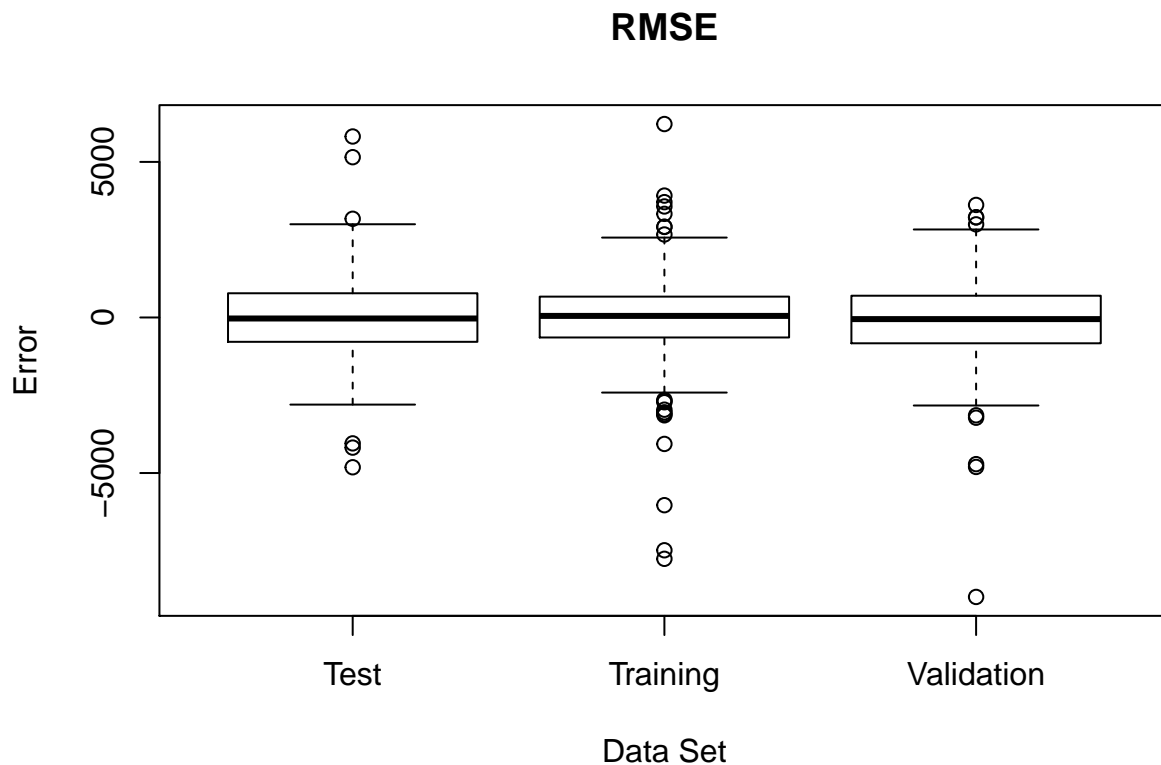
# Problem 1(a)(ii)

```
# Root Mean Square Error for training, validation and test  
rmse_train <- rmse(predict(rf, train_df[,]), train_df$Price)  
rmse_valid <-rmse(predict(rf, valid_df[,]), valid_df$Price)  
rmse_test <-rmse(predict(rf, test_df[,]), test_df$Price)
```

```

train_err <- predict(rf, train_df[,]) - train_df$Price
test_err <- predict(rf, test_df[,]) - test_df$Price
valid_err <- predict(rf, valid_df[,]) - valid_df$Price
# To create a box plot
err <- data.frame(Error = c(train_err, test_err, valid_err),
                   Data = c(rep("Training", length(train_err)),
                           rep("Test", length(test_err)),
                           rep("Validation", length(valid_err))))
boxplot(Error ~ Data, data=err, main="RMSE",
        xlab = "Data Set", ylab = "Error", border="black")

```

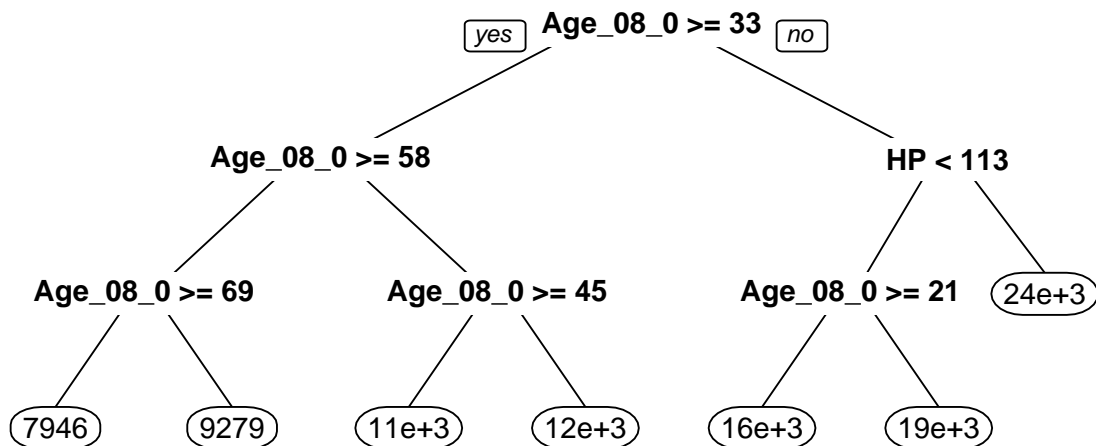


From the box plot we can observe that the test dataset has less number of outliers compared to the other two, meaning that there is a possibility that the above model is underfit. This is probably possible because the training set data is not large enough.

```

#Problem 1(a)(iii)
rf_prune<- prune(rf,cp = 0.01) # cp selected from cptable
prp(rf_prune)

```



```

rmse_prune_train <- rmse(predict(rf_prune,train_df),train_df$Price)
rmse_prune_valid <- rmse(predict(rf_prune,valid_df),valid_df$Price)
rmse_prune_test <- rmse(predict(rf_prune,test_df),test_df$Price)
rmse <- data.frame("Data"=c("Training","Validation","Test"),"Prunned Tree RMSE"=c(rmse_prune_train,rmse_prune_valid,rmse_prune_test))
rmse

```

	Data	Prunned.Tree.RMSE	Full.Tree.RMSE
## 1	Training	1356.185	1131.551
## 2	Validation	1423.283	1252.984
## 3	Test	1470.345	1274.316

Compared to the pruned tree the accuracy of the full tree is more for training set, validation and test set.

```

# Problem 1(b)
bins <- seq(min(cars$Price),
            max(cars$Price),
            (max(cars$Price) - min(cars$Price))/20)
bins

```

```

## [1] 4350.0 5757.5 7165.0 8572.5 9980.0 11387.5 12795.0 14202.5 15610.0
## [10] 17017.5 18425.0 19832.5 21240.0 22647.5 24055.0 25462.5 26870.0 28277.5
## [19] 29685.0 31092.5 32500.0

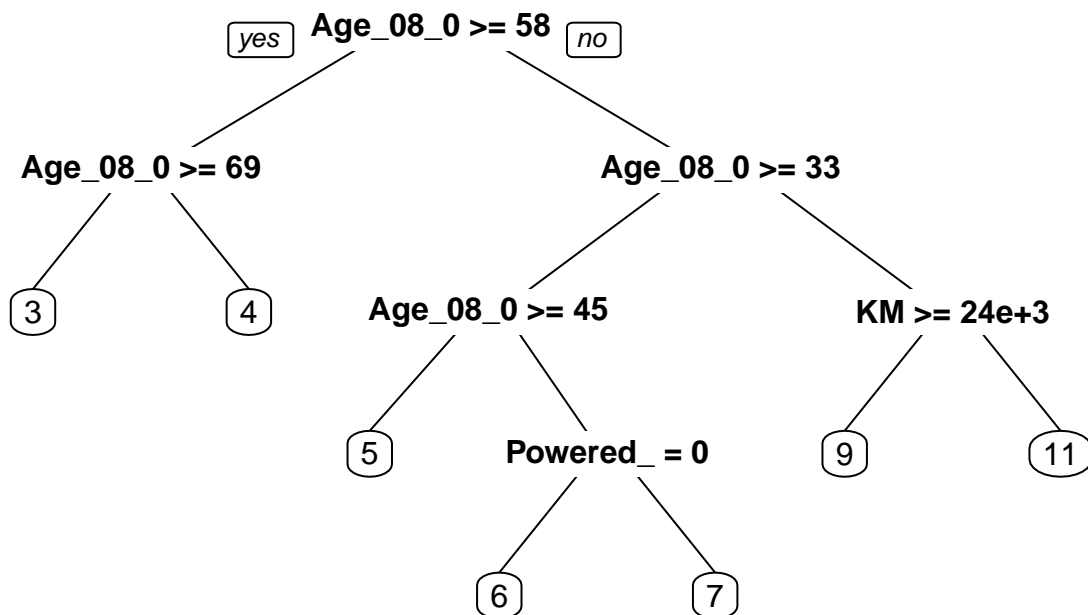
```

```

tags <- c(1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20)
BinnedPrice <- as.data.frame(cut(cars$Price,
                                breaks=bins,
                                include.lowest=TRUE,
                                right=FALSE,labels = tags))

train_df$BinnedPrice<-BinnedPrice[train_set,]
valid_df$BinnedPrice<-BinnedPrice[valid_set,]
test_df$BinnedPrice<-BinnedPrice[test_set,]
# Classification Tree
ct<- rpart(BinnedPrice ~ Age_08_04+ KM + Fuel_Type + HP + Automatic + Doors + Quarterly_Tax + Mfr_Guarantee,
prp(ct)

```



On comparing the two trees we observe that after creating bins the size of the tree has reduced and there is a change in top variables affecting price as well.

```

# Problem 1(b)(ii)
new_data <- data.frame(Age_08_04=77,KM=117000,Fuel_Type="Petrol",HP=110,Automatic=0,Doors=5,Quarterly_Tax=10,Mfr_Guarantee=1)
predict_rt<- predict(rf,new_data)
predict_ct <- bins[predict(ct,new_data,type = "class")]
predict_rt

```

```

##          1
## 7395.714

```

```
predict_ct
```

```
## [1] 7165
```

Problem 1(b)(iii) Our prediction of the two models seem to have a difference of less than \$300. The full regression model returns a more accurate result compared to the classification model. Both models seem to be accurate but the regression model is better trained. The disadvantage of using decision tree is that they are prone to errors in classification, even a slight change in data, will change the entire model.

#Problem 2 Logit -  $-14.188 + 79.964 \text{TotExp}/\text{Assets} + 9.173 \text{TotLns\&Lses}/\text{Assets}$  Odds -  $e^{(-14.188 + 79.964 \text{TotExp}/\text{Assets} + 9.173 \text{TotLns\&Lses}/\text{Assets})}$  Probabilities -  $1 / 1 + e^{(14.188 - 79.964 \text{TotExp}/\text{Assets} - 9.173 \text{TotLns\&Lses}/\text{Assets})}$

```
library(readxl)
bank_df <- read_excel("Banks.xlsx" , sheet = 1)
bank_df <- na.omit(bank_df)
bank_df$`Financial Condition` <- factor(bank_df$`Financial Condition`, levels=c(0,1), labels=c("Strong", "Weak"))

#Problem 2(A)1 creating logistic model
library(AER)
```

```
## Warning: package 'AER' was built under R version 3.6.3
```

```
## Loading required package: car
```

```
## Warning: package 'car' was built under R version 3.6.2
```

```
## Loading required package: carData
```

```
##
```

```
## Attaching package: 'car'
```

```
## The following object is masked from 'package:dplyr':
```

```
##
```

```
##      recode
```

```
## Loading required package: lmtest
```

```
## Loading required package: zoo
```

```
##
```

```
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
##      as.Date, as.Date.numeric
```

```
## Loading required package: sandwich
```

```
## Loading required package: survival
```

```
fit2 <- glm(`Financial Condition` ~ `TotLns&Lses/Assets` + `TotExp/Assets`, data = bank_df, family = "binomial")
summary(fit2)
```

```
##
## Call:
## glm(formula = `Financial Condition` ~ `TotLns&Lses/Assets` +
##     `TotExp/Assets`, family = "binomial", data = bank_df)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.64035  -0.35514   0.02079   0.53234   1.03373
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    -14.188      6.122  -2.317  0.0205 *
## `TotLns&Lses/Assets`    9.173      6.864   1.336  0.1814
## `TotExp/Assets`     79.964     39.263   2.037  0.0417 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##    Null deviance: 27.726  on 19  degrees of freedom
## Residual deviance: 12.831  on 17  degrees of freedom
## AIC: 18.831
##
## Number of Fisher Scoring iterations: 6
```

```
##Problem 2(A)2 odds as function of predictors
coef(fit2)
```

```
##              (Intercept) `TotLns&Lses/Assets`    `TotExp/Assets`
##              -14.187552         9.173215         79.963941
```

```
odds <- exp(coef(fit2))
odds
```

```
##              (Intercept) `TotLns&Lses/Assets`    `TotExp/Assets`
##              6.893258e-07         9.635549e+03         5.344393e+34
```

```
### Problem 2(A)3 probability as function of predictors
bank_df$prob <- predict(fit2, newdata = bank_df, type = "response")
bank_df
```

```
## # A tibble: 20 x 6
##       Obs `Financial Cond~` `TotCap/Assets` `TotExp/Assets` `TotLns&Lses/As~
##   <dbl> <fct>              <dbl>          <dbl>          <dbl>
## 1     1  1 Weak                8.1            0.13            0.64
## 2     2  2 Weak                6.6            0.1            1.04
## 3     3  3 Weak                5.8            0.11            0.66
## 4     4  4 Weak               12.3           0.09            0.8
```

```
## 5      5 Weak      4.5      0.11      0.69
## 6      6 Weak      9.1      0.14      0.74
## 7      7 Weak      1.1      0.12      0.63
## 8      8 Weak      8.9      0.12      0.75
## 9      9 Weak      0.7      0.16      0.56
## 10     10 Weak     9.8      0.12      0.65
## 11     11 Strong    7.3      0.1      0.55
## 12     12 Strong    14      0.08      0.46
## 13     13 Strong    9.6      0.08      0.72
## 14     14 Strong   12.4      0.08      0.43
## 15     15 Strong   18.4      0.07      0.52
## 16     16 Strong     8      0.08      0.54
## 17     17 Strong   12.6      0.09      0.3
## 18     18 Strong    9.8      0.07      0.67
## 19     19 Strong    8.3      0.09      0.51
## 20     20 Strong   20.6      0.13      0.79
## # ... with 1 more variable: prob <dbl>
```

```
##Problem 2(B) creating new data
new_data <- data.frame(0.6,0.11 )
names(new_data)[1] <- "TotLns&Lses/Assets"
names(new_data)[2] <- "TotExp/Assets"
## calculating logit function
new_fit <- predict(fit2 , newdata = new_data , type = "response")
new_fit
```

```
##      1
## 0.5280731
```

```
## calculating the odds
odd <- exp(new_fit)
odd
```

```
##      1
## 1.695662
```

```
## calculating probability
prob <- predict(fit2, newdata=new_data, type="response")
prob
```

```
##      1
## 0.5280731
```

```
library(caret)
```

```
## Warning: package 'caret' was built under R version 3.6.2
```

```
## Loading required package: lattice
```

```
## Warning: package 'lattice' was built under R version 3.6.2
```

```
## Loading required package: ggplot2
```

```
##
```

```
## Attaching package: 'caret'
```

```
## The following object is masked from 'package:survival':
```

```
##
```

```
## cluster
```

```
## The following objects are masked from 'package:Metrics':
```

```
##
```

```
## precision, recall
```

```
fit3<- rpart(`Financial Condition` ~ `TotLns&Lses/Assets` + `TotExp/Assets`, data = bank_df, method = "rpart")
pred3 <- predict(fit3, bank_df, type = "class")
confusionMatrix(pred3, bank_df$`Financial Condition`)
```

```
## Confusion Matrix and Statistics
```

```
##
```

```
##           Reference
```

```
## Prediction Strong Weak
```

```
##      Strong      7      0
```

```
##      Weak       3     10
```

```
##
```

```
##              Accuracy : 0.85
```

```
##              95% CI : (0.6211, 0.9679)
```

```
##      No Information Rate : 0.5
```

```
##      P-Value [Acc > NIR] : 0.001288
```

```
##
```

```
##              Kappa : 0.7
```

```
##
```

```
##      McNemar's Test P-Value : 0.248213
```

```
##
```

```
##              Sensitivity : 0.7000
```

```
##              Specificity : 1.0000
```

```
##      Pos Pred Value : 1.0000
```

```
##      Neg Pred Value : 0.7692
```

```
##              Prevalence : 0.5000
```

```
##      Detection Rate : 0.3500
```

```
##      Detection Prevalence : 0.3500
```

```
##      Balanced Accuracy : 0.8500
```

```
##
```

```
##      'Positive' Class : Strong
```

```
##
```

```
#Problem 2(c)
```

```
cut_off_value<- as.numeric(0.5)
```

```
odds<- cut_off_value/(1- cut_off_value)
```

```
odds
```

```
## [1] 1
```



```
logit<-log(odds)
logit
```

```
## [1] 0
```

```
#Problem 2(D)
```

```
TotLns.Lses.Assets <- 9.173215
```

```
TotExp.Assets <- 79.963941
```

```
Ratio <- TotLns.Lses.Assets/TotExp.Assets
Ratio
```

```
## [1] 0.1147169
```

This ratio is classified as financially strong because ration is less than 0.5

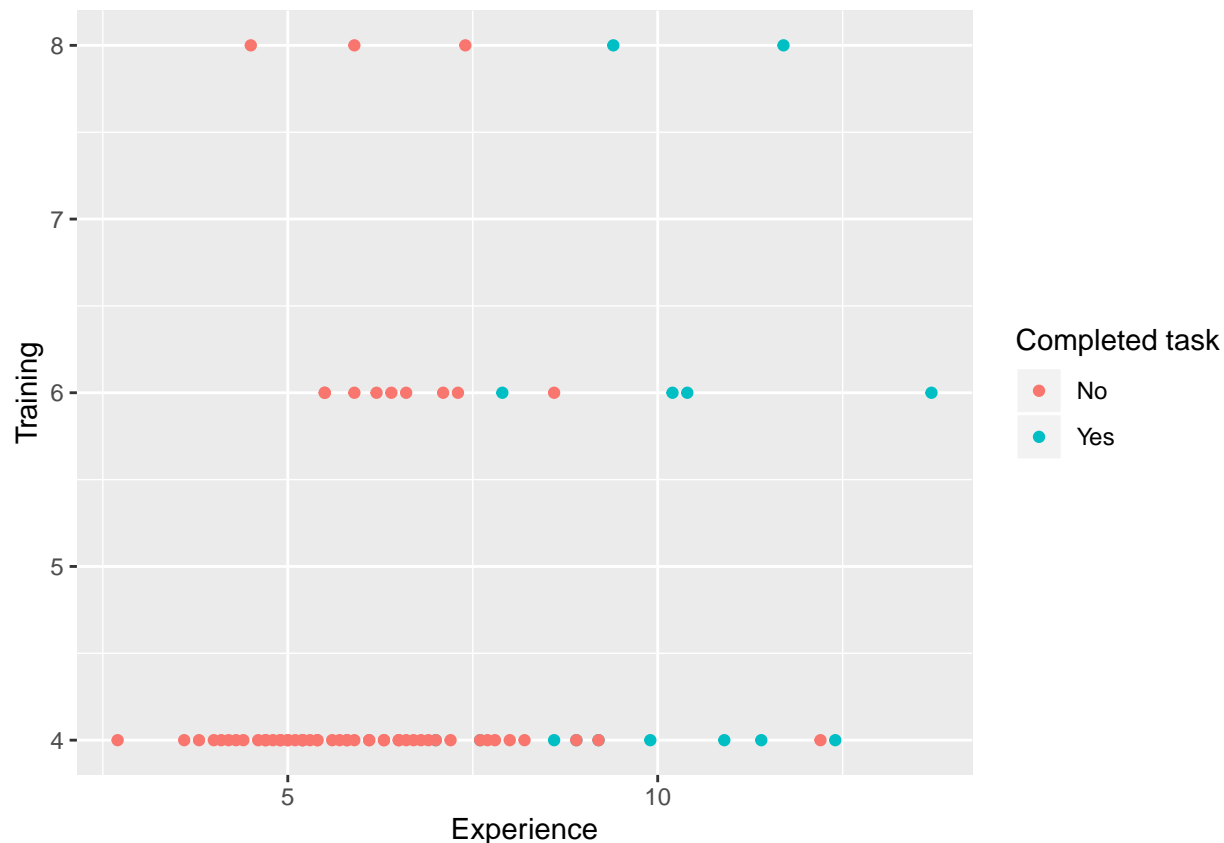
##Problem 2(E) It is given that classification cost is much higher when a bank is declared strong but actually is weak. Therefore , we have to reduce entries being declared as strong. So, we decrease the cutoff value.

#Problem 3

```
stu_df <- read_excel("System Administrators.xlsx" , sheet = 1)
stu_df <- na.omit(stu_df)
test_df <- stu_df
stu_df$Complete <- 1* (stu_df$`Completed task` == "Yes")
stu_df <- stu_df[,-c(3)]
```

```
## Problem 3(a)
```

```
p <- ggplot(test_df, aes(x = Experience, y = Training, colour = `Completed task`)) +
  geom_point() + xlab("Experience") + ylab("Training")
p
```



```
#Problem 3(B)
## creating the model
fit1 <- glm(Complete ~ ., data = stu_df, family = "binomial")
data.frame(summary(fit1)$coefficients, odds = exp(coef(fit1)))
```

```
##           Estimate Std..Error   z.value   Pr...z..      odds
## (Intercept) -10.9813061  2.8919380 -3.7972135 0.0001463318 1.701686e-05
## Experience    1.1269310  0.2908785  3.8742325 0.0001069613 3.086170e+00
## Training      0.1805094  0.3386087  0.5330913 0.5939704002 1.197827e+00
```

```
round(data.frame(summary(fit1)$coefficients, odds = exp(coef(fit1))),5)
```

```
##           Estimate Std..Error   z.value Pr...z..      odds
## (Intercept) -10.98131    2.89194 -3.79721  0.00015 0.00002
## Experience    1.12693    0.29088  3.87423  0.00011 3.08617
## Training      0.18051    0.33861  0.53309  0.59397 1.19783
```

```
summary(fit1)
```

```
##
## Call:
## glm(formula = Complete ~ ., family = "binomial", data = stu_df)
##
## Deviance Residuals:
```

```
##      Min      1Q      Median      3Q      Max
## -2.65306 -0.34959 -0.17479 -0.08196  2.21813
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -10.9813      2.8919  -3.797 0.000146 ***
## Experience   1.1269      0.2909   3.874 0.000107 ***
## Training     0.1805      0.3386   0.533 0.593970
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 75.060  on 74  degrees of freedom
## Residual deviance: 35.713  on 72  degrees of freedom
## AIC: 41.713
##
## Number of Fisher Scoring iterations: 6
```

```
## creating confusion matrix
table(ifelse(fit1$fitted > 0.5, 1, 0), stu_df$Complete)
```

```
##
##      0  1
## 0 58  5
## 1  2 10
```

Total completed task <- 15 Incorrectly classified <- 5

```
percentage <- 5/15 * 100
percentage
```

```
## [1] 33.33333
```

The percentage is 33.33%

##Problem 3(c) To decrease the percentage in part(b) the cutoff probability should be increased

```
##Problem 3(D)
summary(fit1)
```

```
##
## Call:
## glm(formula = Complete ~ ., family = "binomial", data = stu_df)
##
## Deviance Residuals:
##      Min      1Q      Median      3Q      Max
## -2.65306 -0.34959 -0.17479 -0.08196  2.21813
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -10.9813      2.8919  -3.797 0.000146 ***
```

```
## Experience      1.1269      0.2909      3.874 0.000107 ***
## Training       0.1805      0.3386      0.533 0.593970
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 75.060  on 74  degrees of freedom
## Residual deviance: 35.713  on 72  degrees of freedom
## AIC: 41.713
##
## Number of Fisher Scoring iterations: 6
```

```
#intercept
b0 <- -10.98131
# coefficient Expereince
b1 <- 1.12693
# coefficient Training
b2 <- 0.18051
```

So ,  $p < 1/(1+e^{-(b_0+b_1x_1+b_2x_2)})$  here  $b_0, b_1, b_2$  are given  $x_2 < 4$  (given)  $p < 0.5$  solving the equation and substituting the value of each variable we get  $x_1 < 9.11$   $x_1 \sim 9$