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Kyoto University

# Statistical Learning Theory - Introduction -

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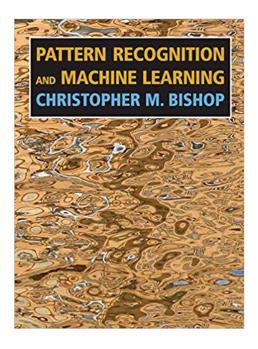
### Statistical learning theory: Foundations of recent data analysis technologies

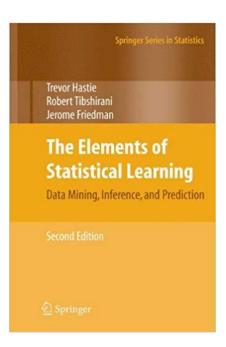
- This lecture will cover:
  - Basic ideas, problems, solutions, and applications of statistical machine learning
    - Supervised & unsupervised learning
    - Models & algorithms: linear regression, SVM, neural nets, ...
  - -Statistical learning theory
    - Theoretical foundation of statistical machine learning
  - Hands-on practice (using Python)
- Advanced topics

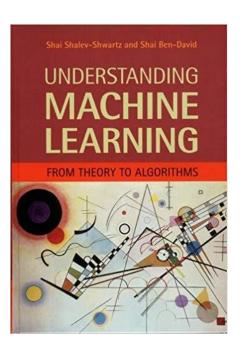
#### Textbooks?:

#### Most of the topics can be found in...

- Pattern recognition and machine learning / Bishop
- The elements of statistical learning / Hastie & Tibshirani
- Understanding machine learning / Shalev-Shwartz & Ben-David







### Evaluations: Final Exam is All You Need

- Evaluation is based on the final exam
  - The examination is a standard written exam and does not allow the use of reference materials
- No attendance checks. No homework.

#### Introduction:

#### Basic ideas of machine learning and applications

- 1. What is machine learning?
- 2. Learning machines
- 3. Machine learning applications:
  - 1. Applications of supervised learning
  - 2. Applications of unsupervised learning: Anomaly detection

### What is machine learning?



#### "The third A.I. boom": Machine learning is a core technology behind the boom

- You can see many successes of "Artificial Intelligence":
  - Q.A. machine beating quiz champions and Go program surpassing top players
  - Protein folding, that was thought to be unsolvable, was solved
  - Are large language models (LLMs) the realization of general-purpose artificial intelligence?
- Current A.I. boom owes machine learning
  - Especially, deep learning



# What is machine learning?: A branch of artificial intelligence

- Originally started as a branch of artificial intelligence
  - has its more-than-50-years history
  - Computer programs that "learns" from experience
  - Based on logical inference
- Pioneers who invented the computer also already dreamed of realizing artificial intelligence

# What is machine learning?: A data analytics technology

- Rise of "statistical" machine learning
  - Successes in bioinformatics, natural language processing, and other business areas
- Recently rather considered as a data analysis technology
  - Buzzwords: "big data" and "data scientist"
    - Data scientist is "the sexiest job in the 21st century" (?)
- Led the success of deep learning
  - The 3rd AI boom

# What can machine learning do?: Prediction, discovery, ... and generation

#### 1. Prediction

- "What will happen in future data?"
- Given past data, predict about future data

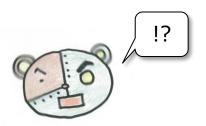
#### 2. Discovery

- "What is happening in data in hand?"
- Given past data, find insights in them

#### 3. Data generation

- "Generate new data satisfying certain properties"
- Given past data, generate similar data

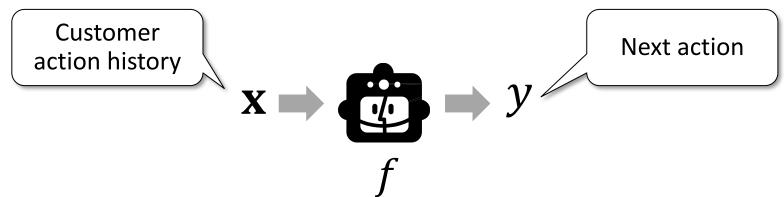
### **Learning Machines**



#### Prediction machine:

#### A function from a vector to a scalar

- We model the intelligent machine as a mathematical function
- Relationship of input and output  $f: \mathbf{x} \to y$ 
  - Input  $\mathbf{x} = (x_1, x_2, ..., x_D)^{\mathsf{T}} \in \mathbb{R}^D$  is a D-dimensional vector
  - Output y is one dimensional
    - Regression: real-valued output  $y \in \mathbb{R}$
    - Classification: discrete output  $y \in \{C_1, C_2, ..., C_M\}$

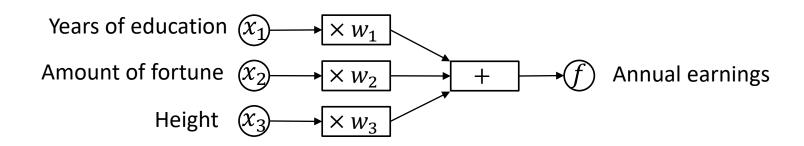


### A model for regression: Linear regression model

• Model f takes an input  $\mathbf{x}=(x_1,x_2,\dots,x_D)^{\mathsf{T}}$  and outputs a real value

$$f(\mathbf{x}) = w_1 x_1 + w_2 x_2 + \dots + w_D x_D$$

- Model parameter  $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$ 

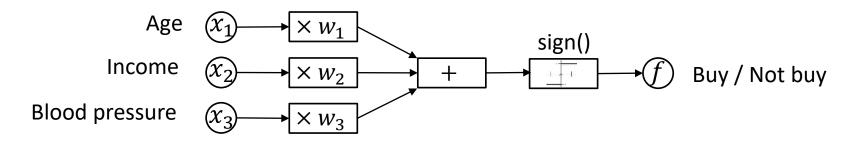


#### A model for classification: Linear classification model

• Model f takes an input  $\mathbf{x} = (x_1, x_2, ..., x_D)^{\mathsf{T}}$  and outputs a value from  $\{+1, -1\}$  (class label)

$$f(\mathbf{x}) = \text{sign}(w_1 x_1 + w_2 x_2 + \dots + w_D x_D)$$

- Model parameter  $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$ :
  - $w_d$ : contribution of  $x_d$  to the output (if  $w_d > 0$ ,  $x_d > 0$  contributes to +1,  $x_d < 0$  contributes to -1)

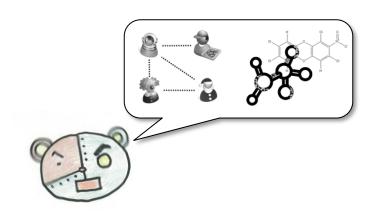


# Formulations of machine learning problems: Supervised learning and unsupervised learning

- What we want is the function f, or its parameters  $\mathbf{w}$ 
  - We estimate f (or  $\mathbf{w}$ ) from data
- Two learning problem settings: supervised and unsupervised
  - Supervised learning: input-output pairs are given
    - $\{(\mathbf{x}^{(1)}, y^{(1)}), (\mathbf{x}^{(2)}, y^{(2)}), \dots, (\mathbf{x}^{(N)}, y^{(N)})\} : N \text{ pairs}$
  - Unsupervised learning: only inputs are given
    - $\{\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, ..., \mathbf{x}^{(N)}\} : N \text{ inputs}$

$$\mathbf{x} \rightarrow \mathbf{f}$$

### Machine learning applications



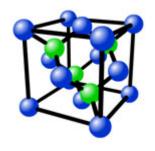
#### Growing ML applications: Emerging applications from IT areas to non-IT areas

- Recent advances in ML offer:
  - Methodologies to handle uncertain and enormous data
  - Black-box tools
- Not limited to IT-related areas, ML is wide-spreading over non-IT areas
  - Healthcare, airline, automobile, material science, education,











### Various applications of machine learning: From on-line shopping to system monitoring

- Marketing
  - Recommendation
  - Sentiment analysis
  - Web ads optimization
- Finance
  - Credit risk estimation
  - Fraud detection
- Science
  - Biology
  - Material science



- Web
  - Search
  - Spam filtering
  - Social media

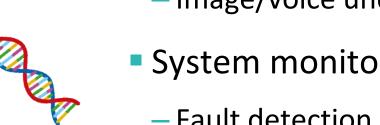




- Multimedia
  - Image/voice understanding
- System monitoring
  - Fault detection







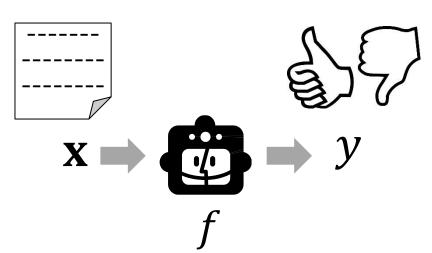


# An application of supervised classification learning: Sentiment analysis

- Judge if a document  $(\mathbf{x})$  is positive or not  $(y \in \{+1, -1\})$  toward a particular product or service
- For example, we want to know reputation of our new product S, and gain marketing insights

• Collect tweets/posts by searching the word "S", and analyze

them

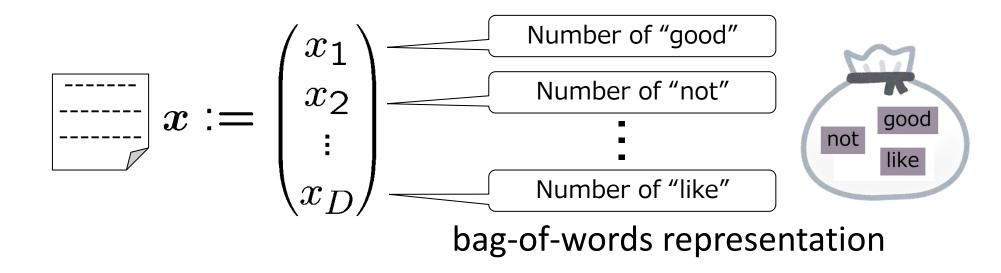


## An application of supervised learning: Some hand labeling followed by supervised learning

- First, give labels to some of the collected documents
  - 10,000 posts hit the word "S"
  - Manually read 300 of them and give sentiment labels
    - "I used S, and found it not bad."  $\rightarrow$   $\clubsuit$
    - "I gave up S. The power was not on."  $\rightarrow \emptyset$
    - "I like S."  $\rightarrow$
- Use the collected 300 labels to train a predictor.
   Then apply the predictor to the rest 9,700 posts

# How to represent a document as a vector: bag-of-words representation

Represent a post x using words appearing in it



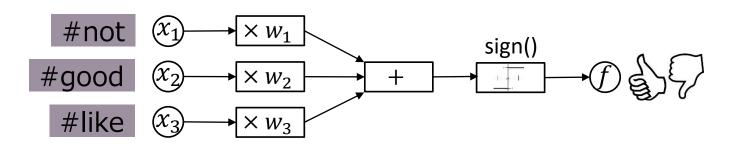
Note: design of the feature vector is left to users

### A simple model for sentiment analysis: Linear binary classification model

• Model f takes a BoW vector  $\mathbf{x} = (x_1, x_2, ..., x_D)^{\mathsf{T}}$  and outputs a sentiment label from  $\{+1, -1\}$ :

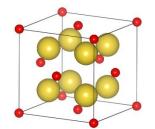
$$f(\mathbf{x}) = \text{sign}(w_1 x_1 + w_2 x_2 + \dots + w_D x_D)$$

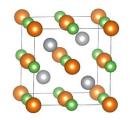
- Model parameter  $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$ :
  - $w_d$ : contribution of the d-th word (e.g. "good") to the sentiment label

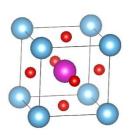


# An application of supervised *regression* learning: Discovering new materials

- Material science aims at discovering and designing new materials with desired properties
  - Volume, density, elastic coefficient, thermal conductivity, ...
- Traditional approach (try-and-error):
  - 1. Determine chemical structure
  - 2. Synthesize the chemical compounds
  - 3. Measure their physical properties
  - 4. If not satisfied, return to 1

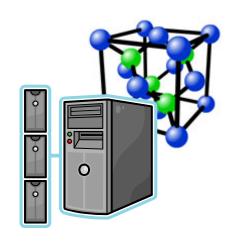






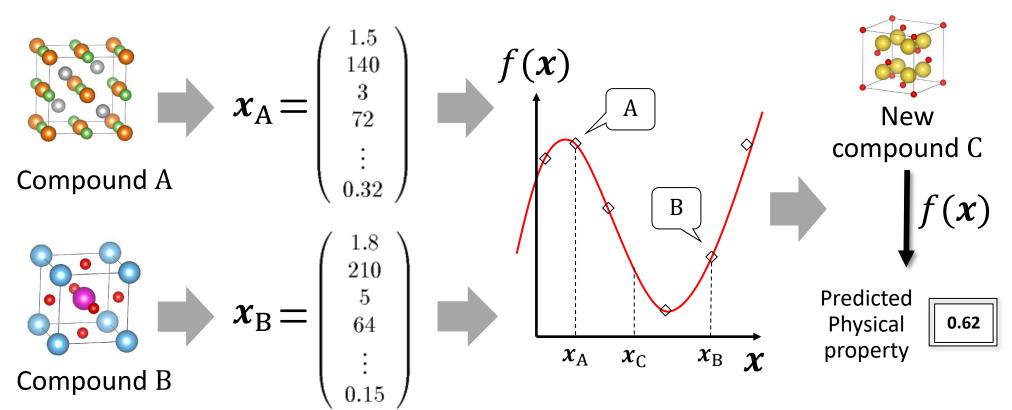
## Computational approach to material discovery: Still needs high computational costs

- Computational approach: First-order principle calculations based on quantum physics to run simulation to estimate physical properties
- First-order principle calculation still requires high computational costs
  - Proportional to the cubic number of atoms
  - -Sometimes more than a week or a month...



### Data driven approach to material discovery: Regression to predict physical properties

Predict the result of first-order principle calculation from data



Feature vector representation of chemical compounds

Estimate regression models of physical properties from data

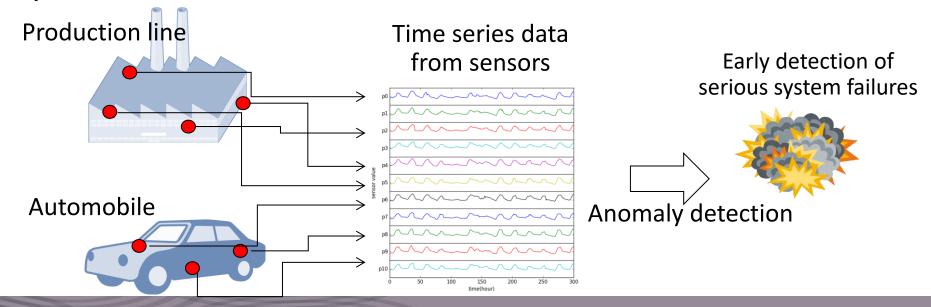
Predict physical properties of new compounds

### **Anomaly detection**



#### Anomaly detection: Early warning for system failures reduces costs

- A failure of a large system can cause a huge loss
  - Breakdown of production lines in a factory, infection of computer virus/intrusion to computer systems, credit card fraud, terrorism, ...
- Modern systems have many sensors to collect data
- Early detection of failures from data collected from sensors



### Anomaly detection techniques: Find "abnormal" behaviors in data

- We want to find precursors of failures in data
  - Assumption: Precursors of failures are hiding in data
- Anomaly: An "abnormal" patterns appearing in data
  - —In a broad sense, state changes are also included: appearance of news topics, configuration changes, ...
- Anomaly detection techniques find such patterns from data and report them to system administrators

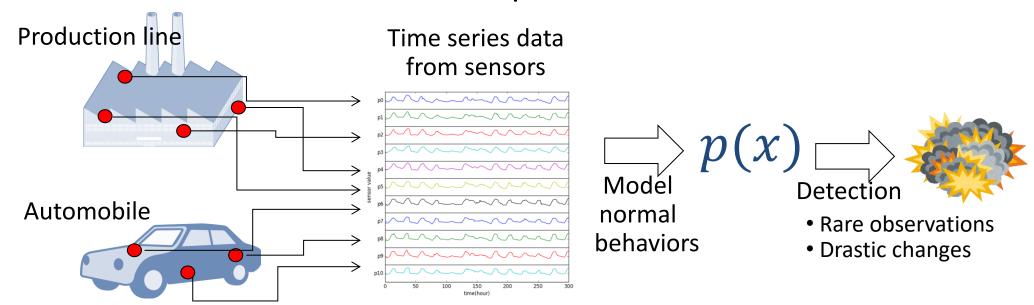
### Difficulty in anomaly detection: Failures are rare events

- If target failures are known ones, they are detected by using supervised learning:
  - 1. Construct a predictive model from past failure data
  - 2. Apply the model to system monitoring
- However, serious failures are usually rare, and often new ones
  - → (Almost) no past data are available
- Supervised learning is not applicable in most cases

#### An alternative idea:

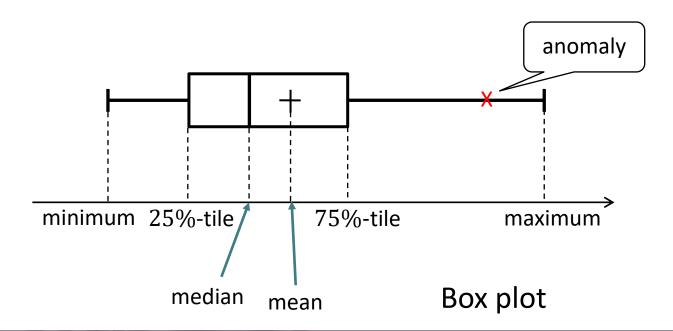
#### Model the normal times, detect deviations from them

- Difficult to model anomalies → Model normal times
  - -Data at normal times are abundant
- Report "strange" data according to the normal time model
  - Observation of rare data is a precursor of failures



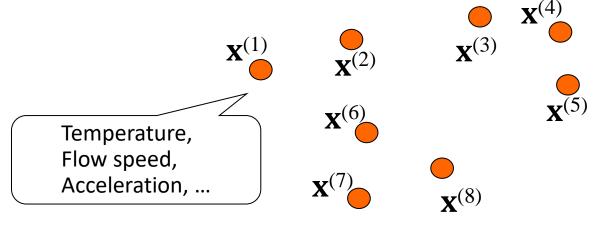
### A simple unsupervised approach: Anomaly detection using thresholds

- Suppose a 1-dimensional case (e.g. temperature)
- Find the value range of the normal data (e.g. 20-50 °C)
- Detect values deviates from the range, and report them as anomalies (e.g. 80°C is not in the normal range)



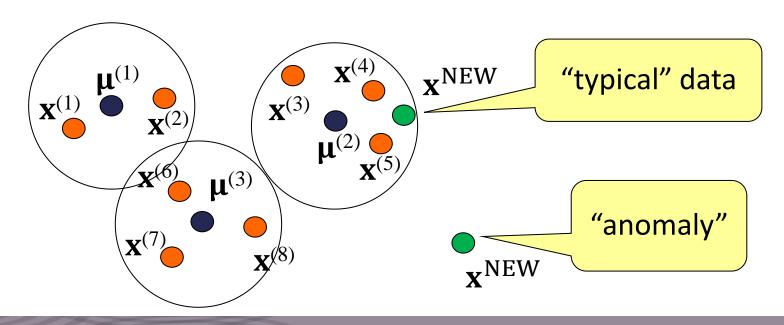
# Clustering for high-dimensional anomaly detection: Model the normal times by grouping the data

- More complex cases:
  - -Multi-dimensional data
  - -Several operation modes in the systems
- Divide normal time data  $\{\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, ..., \mathbf{x}^{(N)}\}$  into K groups
  - –Groups are represented by centers  $\{\mu^{(1)}, \mu^{(2)}, ..., \mu^{(N)}\}$



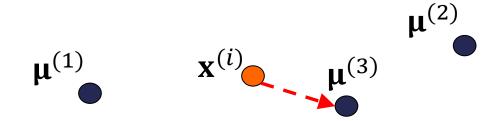
# Clustering for high-dimensional anomaly detection: Find anomalies not belonging to the groups

- Divide normal time data  $\{\mathbf{x}^{(1)},\mathbf{x}^{(2)},...,\mathbf{x}^{(N)}\}$  into K groups
  - -Groups are represented by centers  $\{\mu^{(1)}, \mu^{(2)}, ..., \mu^{(K)}\}$
- Data x is an "anomaly" if it lies far from all of the centers
   = system failures, illegal operations, instrument faults

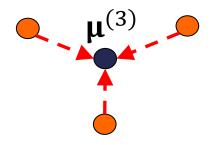


# *K*-means algorithm: Iterative refinement of groups

- Repeat until convergence:
  - 1. Assign each data  $\mathbf{x}^{(i)}$  to its nearest center  $\mathbf{\mu}^{(k)}$



2. Update each center to the mean of the assigned data

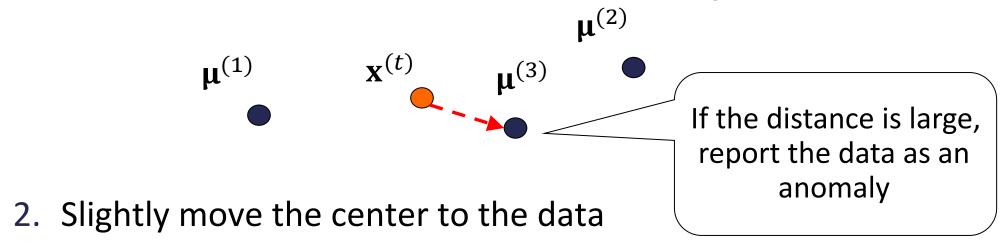


# Anomaly detection in time series: On-line anomaly detection

- Most anomaly detection applications require real-time system monitoring
- Data instances arrive in a streaming manner:
  - $-\mathbf{x}^{(1)},\mathbf{x}^{(2)},...,\mathbf{x}^{(t)},...:$  at each time t, new data  $\mathbf{x}^{(t)}$  arrives
- Each time a new data arrives, evaluate its anomaly
- Also, models are updated in on-line manners:
  - In the one dimensional case, the threshold is sequentially updated
  - In clustering, groups (clusters) are sequentially updated

#### Sequential K-means: Simultaneous estimation of clusters and outliers

- Data arrives in a streaming manner, and apply clustering and anomaly detection at the same time
  - 1. Assign each data  $\mathbf{x}^{(t)}$  to its nearest center  $\mathbf{\mu}^{(k)}$



 $\mathbf{x}^{(t)}$   $\mathbf{\mu}^{(3)}$ 

#### Limitation of unsupervised anomaly detection: Details of failures are unknown

- In supervised anomaly detection, we know what the failures are
- In unsupervised anomaly detection,
   we can know something is happening in the data,
   but cannot know what it is
  - -Failures are not defined in advance
- Based on the reports to system administrators, they have to investigate what is happening, what are the reasons, and what they should do

### **Recent topics: Deep Learning**

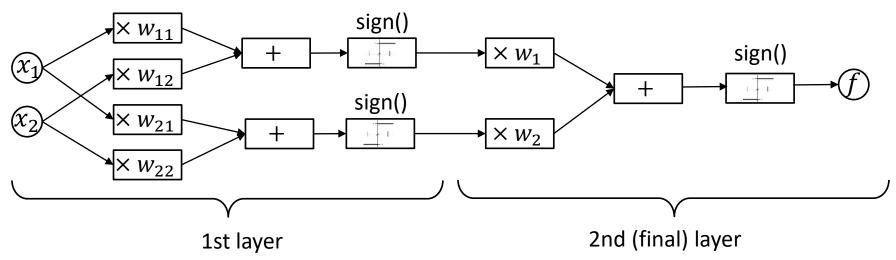


#### Emergence of deep learning: Significant improvement of prediction accuracy

- Artificial neural networks were hot in 1980s, but burnt low after that...
- In 2012, a deep NN system won in the ILSVRC image recognition competition with 10% improvement
- Major IT companies invest much in deep learning technologies
- A big trend in machine learning research

### Deep neural network: Deeply stacked NN for high representational power

- Essentially, multi-layer neural networks
  - -Regarded as stacked linear classification models
    - First to semi-final layers bear feature extraction
    - Final layer makes predictions
- Deep stacking introduces high non-linearity in the model and ensures high representational power

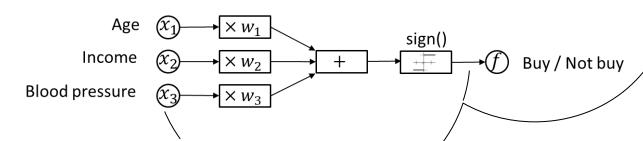


#### A model for classification: Linear classification model

■ Model f takes an input  $\mathbf{x} = (x_1, x_2, ..., x_D)^{\mathsf{T}}$  and outputs a value from  $\{+1, -1\}$ 

$$f(\mathbf{x}) = \operatorname{sign}(w_1 x_1 + w_2 x_2 + \dots + w_D x_D)$$

- -Model parameter  $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$ :
  - $w_d$ : contribution of  $x_d$  to the output  $(x_d > 0 \text{ contributes to } +1, x_d < 0 \text{ contributes to } -1)$



# What is the difference from the past NN?: Deep structures and new techniques with modern flavors

- Differences from the ancient NNs:
  - -Far more computational resources are available now
  - Deep network structure: from wide-and-shallow to narrowand-deep
  - –New techniques and model architectures: Dropout, batch normalization, adversarial learning, ReLU, graph neural networks, attention, ...
- We will look at some of the key ideas in this lecture