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Statistical Learning Theory - Introduction -

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Statistical learning theory:

Foundations of recent data analysis technologies

- This course will cover:
 - Basic ideas, problem, solutions, and applications of statistical machine learning
 - Supervised & unsupervised learning
 - Models & algorithms: linear regression, SVM, perceptron, ...
 - -Statistical learning theory
 - Probably approximately correct (PAC) learning
- Advanced topics:
 - -Online learning, structured prediction, sparse modeling, ...

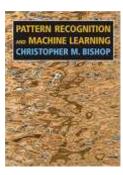
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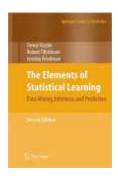
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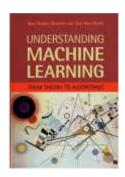
Textbooks?:

Most of the topics can be found in...

- Pattern recognition and machine learning / Bishop
- The elements of statistical learning / Hastie & Tibshirani
- Understanding machine learning / Shalev-Shwartz & Ben-David







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Evaluations:

Report based on data analysis & final exam

- Evaluations will be based on:
 - 1. Report submission
 - 2. Final exam

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Introduction:

Basic ideas of machine learning and applications

- 1. What is machine learning?
- 2. Machine learning applications
- 3. Some machine learning topics
 - 1. Recommender systems
 - 2. Anomaly detection

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What is machine learning?



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"The third A.I. boom":

Machine learning is a core technology

- Many successes of "Artificial Intelligence":
 - Q.A. machine beating quiz champions
 - Go program surpassing top players
 - Machine vision is better at recognizing objects than humans
- Current A.I. boom owes machine learning
 - Especially, deep learning



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What is machine learning?: A branch of artificial intelligence

- Originally started as a branch of artificial intelligence
 - has its more-than-50-years history
 - Computer programs that "learns" from experience
 - Based on logical inference



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What is machine learning?: A data analytics technology

- Rise of "statistical" machine learning
 - Successes in bioinformatics, natural language processing, and other business areas
 - Victory of IBM's Watson QA system, Google's Alpha Go
- Recently rather considered as a data analysis technology
 - "Big data" and "Data scientist"
 - Data scientist is "the sexiest job in the 21st century"
- Success of deep learning
 - The 3rd AI boom

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What can machine learning do?: Prediction and discovery

- Two categories of the use of machine learning:
 - 1. Prediction (supervised learning)
 - "What will happen in future data?"
 - Given past data, predict about future data
 - 2. Discovery (unsupervised learning)
 - "What is happening in data in hand?"
 - Given past data, find insights in them

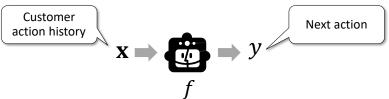
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Prediction machine:

A function from a vector to a scalar

- We model the intelligent machine as a mathematical function
- Relationship of input and output f: x → y
 - Input $\mathbf{x} = (x_1, x_2, ..., x_D)^{\mathsf{T}} \in \mathbb{R}^D$ is a *D*-dimensional vector
 - Output y is one dimensional
 - Regression: real-valued output $y \in \mathbb{R}$
 - Classification: discrete output $y \in \{C_1, C_2, ..., C_M\}$



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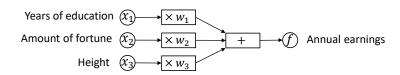
A model for regression:

Linear regression model

■ Model f takes an input $\mathbf{x} = (x_1, x_2, ..., x_D)^{\mathsf{T}}$ and outputs a real value

$$f(\mathbf{x}) = w_1 x_1 + w_2 x_2 + \dots + w_D x_D$$

- Model parameter $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$



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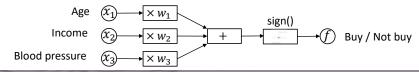
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A model for classification: Linear classification model

■ Model f takes an input $\mathbf{x} = (x_1, x_2, ..., x_D)^{\top}$ and outputs a value from $\{+1, -1\}$

$$f(\mathbf{x}) = \text{sign}(w_1 x_1 + w_2 x_2 + \dots + w_D x_D)$$

- -Model parameter $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$:
 - w_d : contribution of x_d to the output (if $w_d > 0$, $x_d > 0$ contributes to +1, $x_d < 0$ contributes to -1)



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Formulations of machine learning problems: Supervised learning and unsupervised learning

- What we want is the function f
 - We estimate f from data
- Two learning problem settings: supervised and unsupervised
 - Supervised learning: input-output pairs are given

•
$$\{(\mathbf{x}^{(1)}, y^{(1)}), (\mathbf{x}^{(2)}, y^{(2)}), ..., (\mathbf{x}^{(N)}, y^{(N)})\} : N \text{ pairs}$$

Unsupervised learning: only inputs are given

•
$$\{\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \dots, \mathbf{x}^{(N)}\} : N \text{ inputs}$$

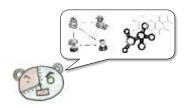


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Growing ML applications:

Emerging applications from IT areas to non-IT areas

- Recent advances in ML:
 - Methodologies to handle uncertain and enormous data
 - Black-box tools
- Not limited to IT areas, ML is wide-spreading over non-IT areas
 - Healthcare, airline, automobile, material science, education,











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Various applications of machine learning: From on-line shopping to system monitoring

- Marketing
 - Recommendation
 - Sentiment analysis
 - Web ads optimization
- Finance
 - Credit risk estimation
 - Fraud detection
- Science



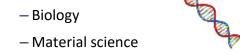
- Search
- Spam filtering
- Social media



- Medical diagnosis
- Multimedia
 - Image/voice understanding
- System monitoring



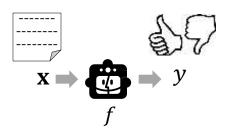
Fault detection



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An application of supervised classification learning: Sentiment analysis

- Judge if a document (x) is positive or not $(y \in \{+1, -1\})$ toward a particular product or service
- For example, we want to know reputation of our newly launched service S
- Collect tweets by searching the word "S", and analyze them



An application of supervised learning: Some hand labeling followed by supervised learning

- First, give labels to some of the collected documents
 - 10,000 tweets hit the word "S"
 - Manually read 300 of them and give labels
 - "I used S, and found it not bad." \rightarrow \diamondsuit

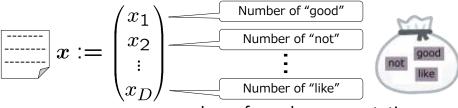
 - "I like S." \rightarrow
- Use the collected 300 labels to train a predictor.
 Then apply the predictor to the rest 9,700 documents

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How to represent a document as a vector: bag-of-words representation

lacktriangle Represent a document $oldsymbol{x}$ using words appearing in it



bag-of-words representation

Note: design of the feature vector is left to users

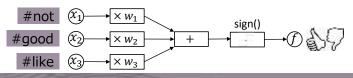
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A model for classification: Linear classification model

■ Model f takes an input $\mathbf{x} = (x_1, x_2, ..., x_D)^{\top}$ and outputs a value from $\{+1, -1\}$

$$f(\mathbf{x}) = \text{sign}(w_1 x_1 + w_2 x_2 + \dots + w_D x_D)$$

- -Model parameter $\mathbf{w} = (w_1, w_2, ..., w_D)^{\mathsf{T}} \in \mathbb{R}^D$:
 - w_d : contribution of x_d to the output $(x_d > 0 \text{ contributes to } +1, x_d < 0 \text{ contributes to } -1)$



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An application of supervised regression learning: Discovering new materials

- Material science aims at discovering and designing new materials with desired properties
 - Volume, density, elastic coefficient, thermal conductivity, ...
- Traditional approach:
 - 1. Determine chemical structure
 - 2. Synthesize the chemical compounds
 - 3. Measure their physical properties







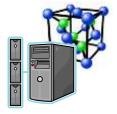
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Computational approach to material discovery:

Still needs high computational costs

- Computational approach: First-order principle calculations based on quantum physics to run simulation to estimate physical properties
- First-order calculation still requires high computational costs
 - -Proportional to the cubic number of atoms
 - -Sometimes more than a month...



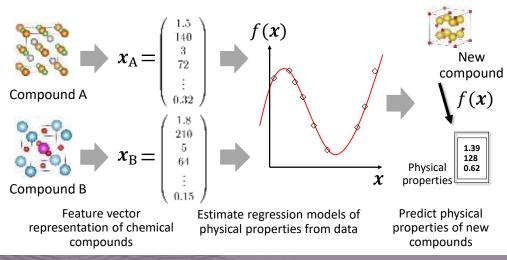
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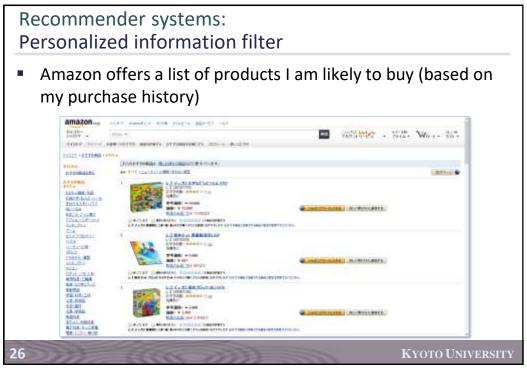
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Data driven approach to material discovery: Regression to predict physical properties

Predict the result of first-order principle calculation from data







Ubiquitous recommender systems: Recommender systems are present everywhere

- A major battlefield of machine learning algorithms
 - Netflix challenge (with \$100 million prize)
- Recommender systems are present everywhere:
 - Product recommendation in online shopping stores
 - Friend recommendation on SNSs
 - Information recommendation (news, music, ...)
 - **–** ...

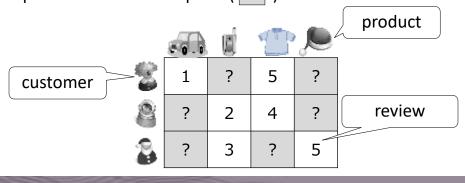


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A formulation of recommendation problem: Matrix completion

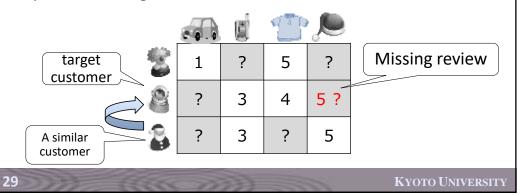
- A matrix with rows (customers) and columns (products)
 - Each element = review score
- Given observed parts of the matrix, predict the unknown parts (?)



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Basic idea of recommendation algorithms: "Find people like you"

- GroupLens: an earliest algorithm (for news recommendation)
 - Inherited by MovieLens (for Movie recommendation)
- Find people similar to the target customer, and predict missing reviews with theirs

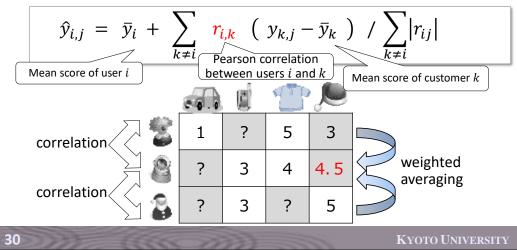


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GroupLens:

Weighted prediction using correlations among customers

- Define customer similarity by correlation (of observed parts)
- Prediction by weighted averaging with correlations:



Low-rank assumption for matrix completion: GroupLens implicitly assumes low-rank matrices

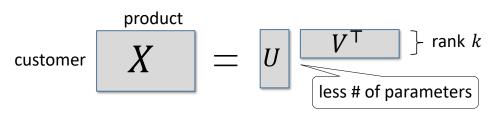
- Assumption of GroupLens algorithm: Each row is represented by a linear combination of the other rows (i.e. linearly dependent)
 - ⇒ The matrix is not full-rank (≒ low-rank)
- Low-rank assumption helps matrix completion

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Low-rank matrix factorization: Projection onto low-dimensional latent space

Low-rank matrix: product of two (thin) matrices



Each row of \boldsymbol{U} and \boldsymbol{V} is an embedding of each customer (or product) onto low-dimensional latent space



Low-rank matrix decomposition methods: Singular value decomposition (SVD)

Find a best low-rank approximation of a given matrix

$$\underset{\mathbf{Y}}{\text{minimize}} \parallel \mathbf{X} - \mathbf{Y} \parallel_{\mathbf{F}}^{2} \text{ s.t. } \text{rank}(\mathbf{Y}) \leq k$$

Singular value decomposition (SVD)

Approx. U Diagonal matrix (singular values)

w.r.t. the constraints: $U^{T}U = I$, $V^{T}V = I$

- The k leading eigenvectors of X^TX best approximate

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Strategies for matrices with missing values: EM algorithm, gradient descent, and trace norm

- SVD is not directly applicable to matrices with missing values
 - Our goal is to fill in missing values in a partially observed matrix
- For completion problem:
 - Direct application of SVD to a (somehow) filled matrix
 - Iterative applications: iterations of completion and decomposition
- For large scale data:
 Gradient descent using only observed parts
- Convex formulation: Trace norm constraint

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Predicting more complex relations: Multinomial relations

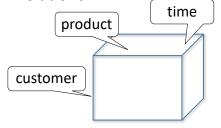
- Matrices can represent only one kind of relations
 - Various kinds of relations (actions):
 Review scores, purchases, browsing product information, ...
 - Correlations among actions might help
- Multinomial relations:
 - (customer, product, action)-relation:
 (Alice, iPad, buy) represents "Alice bought an iPad."
 - (customer, product, time)-relation:
 (John, iPad, July 12th) represents "John bought an iPad on July 12th."

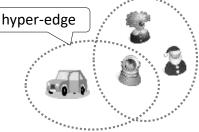
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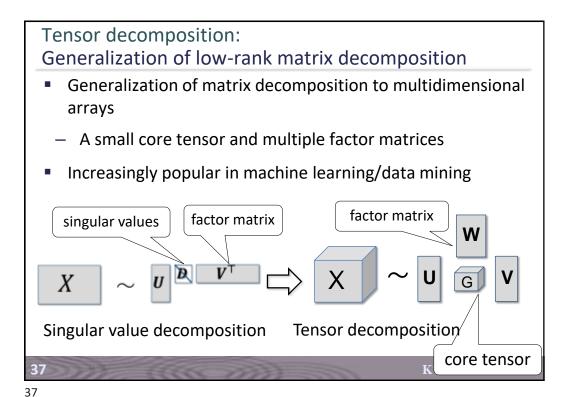
Multi-dimensional arrays: Representation of multinomial relations

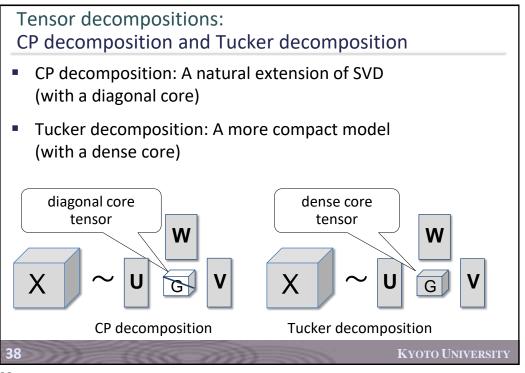
- Multidimensional array: Representation of complex relations among multiple objects
 - -Types of relations (actions, time, conditions, ...)
 - -Relations among more than two objects
- Hypergraph: allows variable number of objects involved in relations





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Applications of tensor decomposition: Tag recommendation, social network analysis, ...

- Personalized tag recommendation (user×webpage×tag)
 - predicts tags a user gives a webpage
- Social network analysis (user×user×time)
 - analyzes time-variant relationships
- Web link analysis (webpage×webpage×anchor text)
- Image analysis (image×person×angle×light×...)

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Anomaly detection

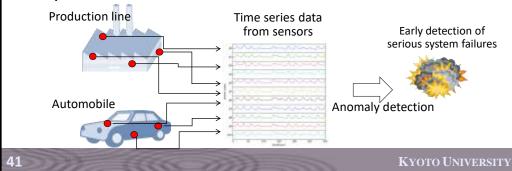


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Anomaly detection:

Early warning for system failures reduces costs

- A failure of a large system can cause a huge loss
 - Breakdown of production lines in a factory, infection of computer virus/intrusion to computer systems, credit card fraud, terrorism, ...
- Modern systems have many sensors to collect data
- Early detection of failures from data collected from sensors



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Anomaly detection techniques: Find "abnormal" behaviors in data

- We want to find precursors of failures in data
 - -Assumption: Precursors of failures are hiding in data
- Anomaly: An "abnormal" patterns appearing in data
 - In a broad sense, state changes are also included:appearance of news topics, configuration changes, ...
- Anomaly detection techniques find such patterns from data and report them to system administrators

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Difficulty in anomaly detection:

Failures are rare events

- If target failures are known ones, they are detected by using supervised learning:
 - 1. Construct a predictive model from past failure data
 - 2. Apply the model to system monitoring
- However, serious failures are usually rare, and often new ones
 → (Almost) no past data are available
- Supervised learning is not applicable

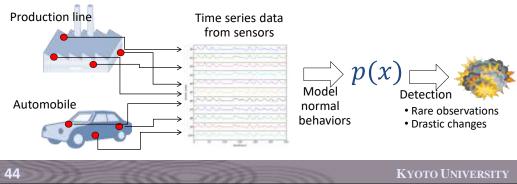
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An alternative idea:

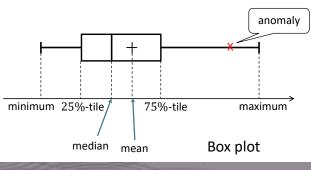
Model the normal times, detect deviations from them

- Difficult to model anomalies → Model normal times
 - -Data at normal times are abundant
- Report "strange" data according to the normal time model
 - -Observation of rare data is a precursor of failures



A simple unsupervised approach: Anomaly detection using thresholds

- Suppose a 1-dimensional case (e.g. temperature)
- Find the value range of the normal data (e.g. 20-50 °C)
- Detect values deviates from the range, and report them as anomalies (e.g. 80°C is not in the normal range)



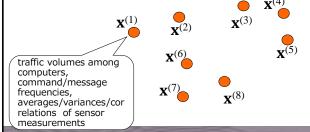
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Clustering for high-dimensional anomaly detection: Model the normal times by grouping the data

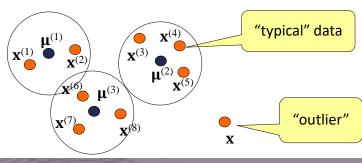
- More complex cases:
- -Multi-dimensional data
- -Several operation modes in the systems
- Divide normal time data $\{\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, ..., \mathbf{x}^{(N)}\}$ into K groups
 - –Groups are represented by centers $\{\boldsymbol{\mu}^{(1)}, \boldsymbol{\mu}^{(2)}, ..., \boldsymbol{\mu}^{(N)}\}$



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Clustering for high-dimensional anomaly detection: Find anomalies not belonging to the groups

- Divide normal time data $\{\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, ..., \mathbf{x}^{(N)}\}$ into K groups
 - -Groups are represented by centers $\{\mu^{(1)}, \mu^{(2)}, ..., \mu^{(N)}\}$
- Data x is an "outlier" if it lies far from all of the centers = system failures, illegal operations, instrument faults



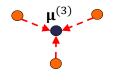
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K-means algorithm: Iterative refinement of groups

- Repeat until convergence:
 - 1. Assign each data $\mathbf{x}^{(i)}$ to its nearest center $\mathbf{\mu}^{(k)}$



2. Update each center to the center of the assigned data



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Anomaly detection in time series:

On-line anomaly detection

- Most anomaly detection applications require real-time system monitoring
- Data instances arrive in a streaming manner:
 - $-\mathbf{x}^{(1)},\mathbf{x}^{(2)},...,\mathbf{x}^{(t)},...$: at each time t, new data $\mathbf{x}^{(t)}$ arrives
- Each time a new data arrives, evaluate its anomaly
- Also, models are updated in on-line manners:
 - In the one dimensional case, the threshold is sequentially updated
 - -In clustering, groups (clusters) are sequentially updated

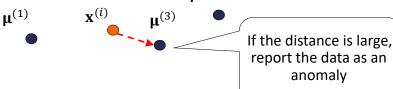
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Sequential *K*-means:

Simultaneous estimation of clusters and outliers

- Data arrives in a streaming manner, and apply clustering and anomaly detection at the same time
 - 1. Assign each data $\mathbf{x}^{(i)}$ to its nearest center $\mathbf{\mu}^{(k)}$



2. Slightly move the center to the data



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Limitation of unsupervised anomaly detection: Details of failures are unknown

- In supervised anomaly detection, we know what the failures are
- In unsupervised anomaly detection,
 we can know something is happening in the data,
 but cannot know what it is
 - -Failures are not defined in advance
- Based on the reports to system administrators, they have to investigate what is happening, what are the reasons, and what they should do

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Recent topics



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Emergence of deep learning:

Significant improvement of prediction accuracy

- Artificial neural networks were hot in 1980s, but burnt low after that...
- In 2012, a deep NN system won in the ILSVRC image recognition competition with 10% improvement
- Major IT companies (such as Google and Facebook) invest much in deep learning technologies
- Big trend in machine learning research

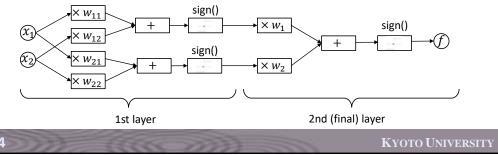
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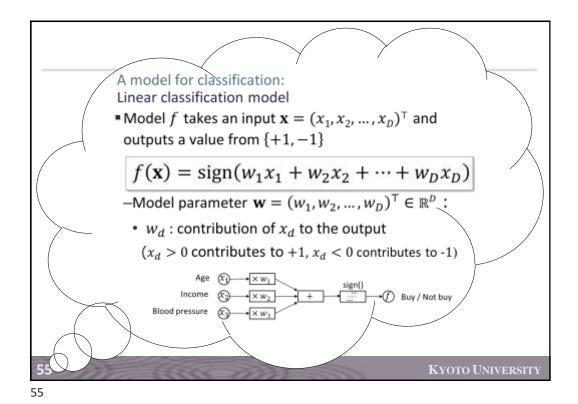
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Deep neural network:

Deeply stacked NN for high representational power

- Essentially, multi-layer neural networks
 - Regarded as stacked linear classification models
 - First to semi-final layers bear feature extraction
 - Final layer makes predictions
- Deep stacking introduces high non-linearity in the model and ensures high representational power





What is the difference from the past NN?: Deep structures and new techniques with modern flavors

- Differences from the ancient NNs:
 - -Far more computational resources are available now
 - Deep network structure: from wide-and-shallow to narrowand-deep
 - -New techniques: Dropout, ReLU, Adversarial learning, ...
- Unfortunately we will not cover DNNs in this lecture

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