CSE141 Introduction to Programming (Fall'23)

Lab # 6

Sep 29, 2023

1. *Matrix addition:* Write a program matrix_add.cpp to add two matrices a, b of the same size and print the result. You don't need to take input from command-line or standard-input. Input matrices can be initialized as follows.

- 2. Column sum: Given a 2d-array a[][] and an index j, write a program sum_col.cpp that compute sum of elements in column j of a[][]. You don't need to take input from command-line or standard-input.
- 3. *Matrix transpose:* Write a program transpose.cpp that compute the transpose of matrix given as 2d-array a[][]. Store the transpose in matrix b[][] and also print it. You don't need to take input from command-line or standard-input.

Example: Following two matrices are transpose of each other.

4. Upper-triangular matrix: Write a program that checks whether a given square matrix is an upper-triangular matrix. A matrix is said to be an upper-triangular matrix if all values under the main diagonal are zeros. Example:

```
{ {1, 2, 3, 4},
 {0, 5, 6, 7},
 {0, 0, 8, 9},
 {0, 0, 0, 1} }
```

5. *Magic square:* Write a program called is_magic_square.cpp that given a two-dimensional array of integers, prints true if it is a magic square, and false otherwise.

A square matrix is a magic square if it is square in shape (same number of rows as columns, and every row the same length), and all of its row, column, and diagonal sums are equal. For example, following two matrices are magic squares because all eight of the sums are exactly 15 and 65 respectively.

```
{ {2, 7, 6},
 {9, 5, 1},
 {14, 20, 21, 2, 8},
 {4, 3, 8} }
 {22, 3, 9, 15, 16},
 {10, 11, 17, 23, 4},
 {18, 24, 5, 6, 12} }
```

6. Checking an expression for 'well-bracketedness'

Read a string representing a bracketed expression as input. Maintain a count of how many opening parentheses '(' and closing parentheses ')' have been encountered.

Declare an integer variable level, initialized to zero. At each opening parenthesis, increase its value by one, and print its new value. At each closing parenthesis, decrease its value by one, and print its new value. If the level becomes negative, print "Unmatched ')'", just once regardless of the number of unmatched ')'s. At the end, if the level is positive print "Unmatched '('". If the level is zero and there have been no unmatched ')'s then print "Well-bracketed expression". E.g.:

```
Input: (a*(b-c)-((d/e)+f))
Output:
```

```
Level 1
Level 2
Level 1
Level 2
Level 3
Level 2
Level 1
Level 0
Well-bracketed expression
```

Note: Use std::getline(std::cin, str) to read a line of input from the standard input stream into a string variable str. Since std::string behaves like an array of char, you can iterate over the characters in a string str using the either the range-based for loop:

```
for (char c : str) {
    // do something with c
}

or the traditional for loop (the size() method returns the length of the string):

for (int i = 0; i < str.size(); i++) {
    char c = str[i];
    // do something with c</pre>
```

7. Smallest/Longest words: Write a program that prints the first longest and smallest word in a given sentence. For example, if the input string is

Gedanken means *thoughts* in German. The term was popularized by Albert Einstein, who applied gedankenexperiment to his work conceptualizing the theory of relativity.

then your program should print

```
Smallest word: in
Longest word: gedankenexperiment
```

}

8. Longest run: Write a program longest_run.cpp that given an array of integers, prints out both the integer that appears in a longest consecutive run and the length of the run. For example, if the array is 1 2 2 1 5 7 7 7 7 2 2 2 1 1, then your program should print

Longest run: 4 consecutive 7s

9. The Sieve of Eratosthenes: This is a nice exercise that involves writing a program named sieve.cpp to generate all the prime numbers less than a given number n. (Remember that a prime number is a number whose only factors are 1 and itself or, put another way, is not exactly divisible by any numbers other than 1 and itself. So the first few primes are $2, 3, 5, 7, 11, 13, 17, 19, \ldots$)

Only attempt the program if you understand Eratosthenes' sieve method as follows:

- 1. Start with the first number not crossed off (i.e. 2). Call this k.
- 2. Cross off (or 'sieve out') all the multiples of k that are less than or equal to n (since these are obviously not prime).
- 3. Repeat steps 2 and 3 with the next number k that is not crossed off. Terminate when you have reached n.

The prime numbers are all the numbers not sieved out.

Using paper and pencil run Eratosthenes sieve by hand on the numbers 2..30.

To write a program to carry out this method, use a **bool** array of size N with all elements initially set to false. Crossing off a number k involves setting the kth array element to true.

Make your program print out the number of primes less than N as well as the primes themselves.

Question: How many prime numbers are there less than 1 million?

Optional question: Can you make your program more 'efficient' by stopping one of your loops at the square root of N, rather than N itself? Explain why.

10. Frequency table: Read an input integer n from the keyboard. Generate 100,000 random integers in the range 1 to n. Use an array A to keep count of the frequency of occurrence of each integer (i.e. use A[1] to keep track of the number of occurrences of the integer 1, A[2] for the integer 2 and so on). Print out the number of times each integer from 1 to n was generated.

Question: what happens if the number input from the keyboard is larger than the size of the array A?

11. Finding your sherbet: A large number of IBA students are attending an Iftar party. Each guest is drinking a glass of Rooh-Afza sherbet. An emergency causes the lights to go out and the fire alarm to go off. The guests calmly put down their glass and exit the building. When the alarm goes off, they re-enter and try to retrieve their glass. However, the lights are still off, so each student randomly grabs a glass of Rooh-Afza. What are the chances that at least one student gets his or her original glass? Write a program my_sherbet.cpp that takes an input n and runs 1,000 simulations this event, assuming their are n guests. Print the fraction of times that at least one guest gets their original glass. As n gets large, does this fraction approach 0 or 1 or something in between?

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- 12. Random permutation: Write a program permutation.cpp so that it takes an input N and prints a random permutation of the integers 0 through N-1. Also print a checkerboard visualization of the permutation. As an example, the permutation {2, 3, 1, 4, 0} corresponds to:
 - * * * * Q * * Q * * Q * * * * * Q * * *

Hint: Use the shuffle algorithm discussed in the lectures to get a random permutation.

- 13. 8 queens checker: A permutation of the integer 0 to n-1 corresponds to a placement of queens on an n-by-n chessboard so that no two queens are in the same row or column. Write a program queens_checker.cpp that determines whether or not a permutation corresponds to a placement of queens so that no two are in the same row, column, or diagonal. As an example, the permutation { 4, 1, 3, 0, 2 } is a legal placement:

Try to do it without using any extra arrays besides the length n input permutation q. Hint: to determine whether setting q[i] conflicts with q[j] for i < j.

- if q[i] equals q[j]: two queens are placed in the same row
- if q[i] q[j] equals j i: two queens are on same major diagonal
- if q[j] q[i] equals j i: two queens are on same minor diagonal