

Recall that **(**)** $y[i-1] = x[i]$ and **(*)** $x[i-1] = y[i] - q[i-1]x[i]$
 and we want $j[i]x[i] + k[i]y[i] = \gcd(k[i], j[i])$

Example: $k = 184, j = 69$

i	$k[i]$	$=$	$j[i]q[i]$	$+$	$r[i]$	$k[i]$	$j[i]$	$r[i]$	$q[i]$	$y[i]$	$x[i]$
0	184	$=$	$69(2)$	$+$	46	184	69	46	2	-1	3
1	69	$=$	$46(1)$	$+$	23	69	46	23	1	1	-1
2	46	$=$	$23(2)$	$+$	0	46	23	0	2	0	1

- 1) First run the regular GCD algorithm: get $\gcd(184, 69) = 23$
- 2) Then calculate $y[2] = 0, x[2] = 1$
- 3) Continue bottom-up, calculating the $x[i], y[i]$ from **(*)** and **(**)**
- 4) We are done! Note that $184(-1) + 69(3) = 23 = \gcd(184, 69)$.

Recall that **(**)** $y[i-1] = x[i]$ and **(*)** $x[i-1] = y[i] - q[i-1]x[i]$
 and we want $j[i]x[i] + k[i]y[i] = \gcd(k[i], j[i])$

Example: $k = 99, j = 63$

i	$k[i]$	$=$	$j[i]q[i]$	$+$	$r[i]$	$k[i]$	$j[i]$	$r[i]$	$q[i]$	$y[i]$	$x[i]$
0	99	$=$	$63(1)$	$+$	36	99	63	36	1	2	-3
1	63	$=$	$36(1)$	$+$	27	63	36	27	1	-1	2
2	36	$=$	$27(1)$	$+$	9	36	27	9	1	1	-1
3	27	$=$	$9(3)$	$+$	0	27	9	0	3	0	1

- 1) First run the regular GCD algorithm: get $\gcd(99, 63) = 9$
- 2) Then calculate $y[3] = 0, x[3] = 1$
- 3) Continue bottom-up, calculating the $x[i], y[i]$ from **(*)** and **(**)**
- 4) We are done! Note that $99(2) + 63(-3) = 9 = \gcd(99, 63)$.