### Computing 'nullable' for regular expressions

If e is regular expression (its syntax tree), then L(e) is the language denoted by it. For  $L \subseteq A^*$  we defined nullable(L) as  $\varepsilon \in L$  If e is a regular expression, we can compute nullable(e) to be equal to nullable(L(e)), as follows:

```
nullable(\emptyset) = false
nullable(\varepsilon) = true
nullable(a) = false
nullable(e_1|e_2) = nullable(e_1) \lor nullable(e_2)
nullable(e^*) = true
nullable(e_1e_2) = nullable(e_1) \land nullable(e_2)
```

### Computing 'first' for regular expressions

For  $L \subseteq A^*$  we defined:  $first(L) = \{a \in A \mid \exists v \in A^*. \ av \in L\}$ . If e is a regular expression, we can compute first(e) to be equal to first(L(e)), as follows:

```
first(\emptyset) = \emptyset
    first(\varepsilon) = \emptyset
    first(a) = \{a\}, \text{ for } a \in A
first(e_1|e_2) = first(e_1) \cup first(e_2)
   first(e*) = first(e)
first(e_1e_2) = if(nullable(e_1)) then first(e_1) \cup first(e_2)
                      else first(e_1)
```

### Clarification for first of concatenation

Let 
$$e$$
 be  $\mathbf{a}^*\mathbf{b}$ . Then  $L(e) = \{b, ab, aab, aaab, ...\}$  first $(L(e)) = \{a, b\}$ 

 $e = e_1 e_2$  where  $e_1 = a^*$  and  $e_2 = b$ . Thus,  $nullable(e_1)$ .

$$first(e_1e_2) = first(e_1) \cup first(e_2) = \{a\} \cup \{b\} = \{a, b\}$$

It is not correct to use  $first(e) = ? first(e_1) = \{a\}.$ 

Nor is it correct to use  $first(e) = {}^{?} first(e_2) = {b}$ .

We must use their union.

### Converting Simple Regular Expresssions into a Lexer

regular expression	lexercode
$a (a \in A)$	if $(current = a)$ next else
$r_1 r_2$	$code(r_1)$ ; $code(r_2)$
$r_1 r_2$	if $(current \in first(r_1))$
	$code(r_1)$
	else $code(r_2)$
r*	while $(current \in first(r))$
	code(r)

#### More complex cases

In other cases, a few upcoming characters ("lookahead") are not sufficient to determine which token is coming up.

#### Examples:

A language might have separate numeric literal tokens to simplify type checking:

- integer constants: digit digit\*
- ▶ floating point constants: digit digit\* . digit digit\*

Floating point constants must contain a period (e.g., Modula-2).

Division sign begins with same character as  $\//$  comments. Equality can begin several different tokens.

In such cases, we process characters and store them until we have enough information to make the decision on the current token.

### Example of a part of a lexical analyzer

```
ch.current match {
 case '(' ⇒ {current = OPAREN: ch.next: return}
 case ')' ⇒ {current = CPAREN; ch.next; return}
 case '+' ⇒ {current = PLUS: ch.next: return}
 case '/' ⇒ {current = DIV; ch.next; return}
 case '*' ⇒ {current = MUL; ch.next; return}
 case '=' ⇒ { // more tricky because there can be =. ==
  ch.next
  if (ch.current = '=') {ch.next; current = CompareEQ; return}
  else {current = AssignEQ: return}
 case '<' ⇒ { // more tricky because there can be <. <=
  ch.next
  if (ch.current = '=') {ch.next: current = LEO: return}
  else {current = LESS; return}
```

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What if we omit ch.next?
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  if (ch.current = '=') {ch.next; current = LEQ; return}
  else {current = LESS; return}
What if we omit ch.next?
                   Lexer could generate a non-existing equality token!
```

### White spaces and comments

Whitespace can be defined as a token, using space character, tabs, and various end of line characters. Similarly for comments.

In most languages (Java, ML, C) white spaces and comments can occur between any two other tokens have no meaning, so parser does not want to see them.

Convention: the lexical analyzer removes those "tokens" from its output. Instead, it always finds the next non-whitespace non-comment token.

Other conventions and interpretations of new line became popular to make code more concise (sensitivity to end of line or indentation). Not our problem in this course! Tools that do formatting of source also must remember comments. We ignore those.

```
if (ch.current='/') {
  ch.next
  if (ch.current='/') {
    while (!isEOL & !isEOF) {
      ch.next
    }
  } else {
```

```
if (ch.current='/') {
  ch.next
  if (ch.current='/') {
    while (!isEOL & !isEOF) {
      ch.next
    }
  } else {
    ch.current = DIV
}
```

```
if (ch.current='/') {
 ch.next
 if (ch.current='/') {
    while (!isEOL & !isEOF) {
     ch.next
 } else {
   ch.current = DIV
Nested comments: this is a single comment:
/* foo /* bar */ baz */
Solution:
```

```
if (ch.current='/') {
 ch.next
 if (ch.current='/') {
    while (!isEOL & !isEOF) {
      ch.next
  } else {
   ch.current = DIV
Nested comments: this is a single comment:
/* foo /* bar */ baz */
Solution: use a counter for nesting depth
```

Lexical analyzer is required to be greedy: always get the longest possible token at this time. Otherwise, there would be too many ways to split input into tokens!

Consider language with the following tokens:

Lexical analyzer is required to be greedy: always get the longest possible token at this time. Otherwise, there would be too many ways to split input into tokens!

ID: letter(digit | letter)\*
LE: <=
LT: <

EQ: = How can we split this input into subsequences, each of which in a token:

interpreters <= compilers

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1 F· <=

EQ: =

How can we split this input into subsequences, each of which in a token:

interpreters <= compilers

ID(interpreters) LE ID(compilers) - OK, longest match rule ID(inter) ID(preters) LE ID(compilers)

Some solutions:

ID(interpreters) LT EQ ID(compilers)

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ID(inter) ID(preters) LE ID(compilers)

Some solutions:

- not longest match: ID(inter)

ID(interpreters) LT EQ ID(compilers)

- not longest match: LT

### Longest match rule is greedy, but that's OK

Consider language with ONLY these three operators:

IMP: =>

LT: LE:

For sequence:

<=>

lexer will first return LE as token, then report unknown token >. This is the behavior that we expect.

This is despite the fact that one could in principle split the input into < and =>, which correspond to sequence LT IMP. But a split into < and => would not satisfy longest match rule, so we do *not* want it. Reporting error is the right thing to do here.

This behavior is not a restriction in practice: programmers we can insert extra spaces to stop maximal munch from taking too many characters.

### Token priority

What if our token classes intersect?

Longest match rule does not help, because the same string belongs to two regular expressions

#### Examples:

- a keyword is also an identifier
- a constant that can be integer or floating point

Solution is priority: order all tokens and in case of overlap take one earlier in the list (higher priority).

#### Examples:

- ▶ if it matches regular expression for both a keyword and an identifier, then we define that it is a keyword.
- ▶ if it matches both integer constant and floating point constant regular expression, then we define it to be (for example) integer constant.

Token priorities for overlapping tokens must be specified in language definition.