

Advanced Deep Learning Architectures

COMP 5214 & ELEC 5680

Instructor: Dr. Qifeng Chen

<https://cqf.io>

The Rise of Deep Learning

'Deep Voice' Software Can Clone Anyone's Voice With Just 3.7 Seconds of Audio

Using snippets of voices, Baidu's 'Deep Voice' can generate new speech, accents, and tones.

Let There Be Sight: How Deep Learning Is Helping the Blind 'See'



Technology outpacing security measures

Facial Recognition | Features and Interviews

AI beats docs in cancer spotting

A new study provides a fresh example of machine learning as an important diagnostic tool. Paul Biegler reports.

AI Can Help In Predicting Cryptocurrency Value



DEEPMIND STARCRRAFT TRIUMPH



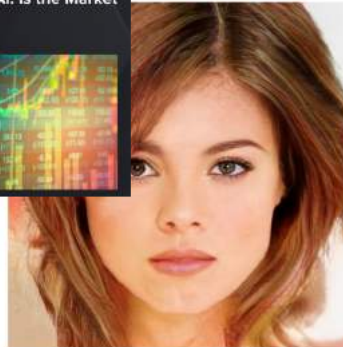
'Creative' AlphaZero leads way for chess computers and, maybe, science

Former chess world champion Garry Kasparov likes what he sees of computer that could be used to find cures for diseases



How an A.I. 'Cat-and-Mouse Game' Generates Believable Fake Photos

By CADE METZ and KEITH COLLINS JAN 2, 2018



Stock Predictions Based On AI: Is the Market Truly Predictable?



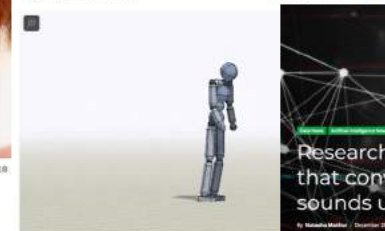
Complex of bacteria-infecting viral proteins modeled in CASP-13. The complex contained proteins that were modeled individually. PROTEIN DATA BANK

Google's DeepMind acs protein folding

By Robert F. Service | Dec. 6, 2018, 12:05 PM

After Millions of Trials, These Simulated Humans Learned to Do Perfect Backflips and Cartwheels

George Dornier 4/10/18 11:55am | Pinned to AI



Neural networks everywhere

New chip reduces neural networks' power consumption by up to 95 percent, making them practical for battery-powered devices.

Wed, 01/16/2019 - 6:00am | Comment by Kenney Walker - Digital Reporter - @RandDMagazine



AI faces show how far AI image generation has advanced in just four years

AI faces on the right aren't real; they're the product of machine learning



Automation And Algorithms: De-Risking Manufacturing With Artificial Intelligence

Sarah Goehrlke Contributor Manufacturing 1 focus on the industrialization of additive manufacturing

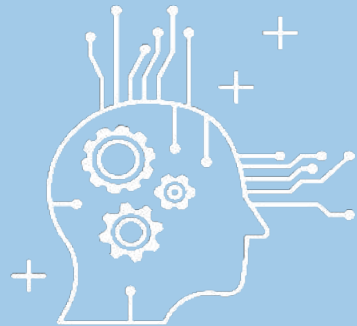
TWEET THIS

The two key applications of AI in manufacturing are pricing and manufacturability feedback

What is Deep Learning?

ARTIFICIAL INTELLIGENCE

Any technique that enables computers to mimic human behavior



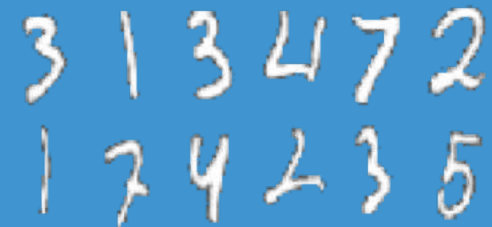
MACHINE LEARNING

Ability to learn without explicitly being programmed



DEEP LEARNING

Extract patterns from data using neural networks



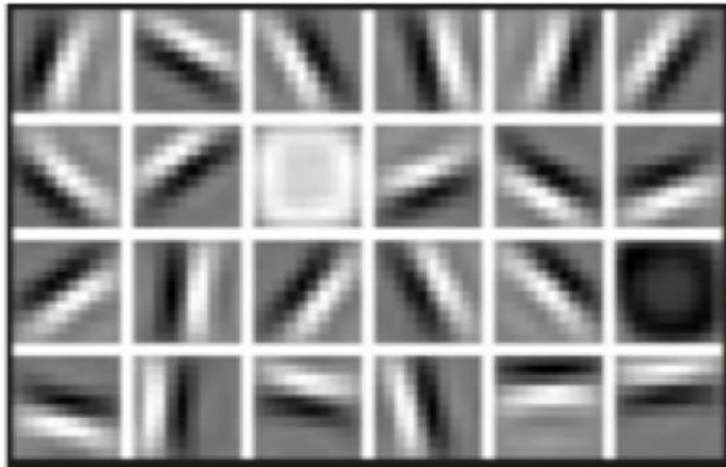
Why Deep Learning and Why Now?

Why Deep Learning?

Hand engineered features are time consuming, brittle and not scalable in practice

Can we learn the **underlying features** directly from data?

Low Level Features



Lines & Edges

Mid Level Features



Eyes & Nose & Ears

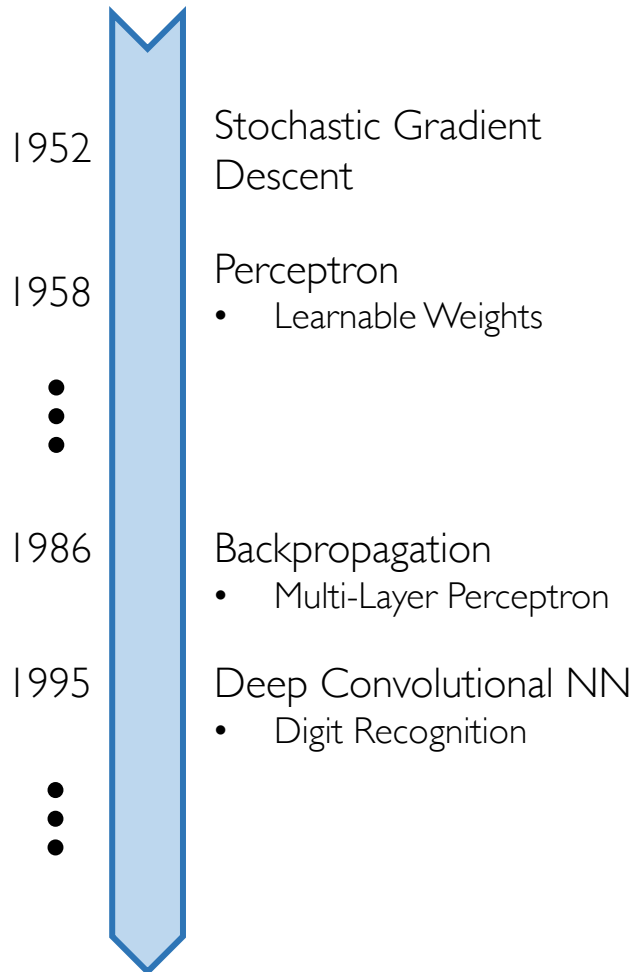
High Level Features



Facial Structure

Why Now?

Neural Networks date back decades, so why the resurgence?



1. Big Data

- Larger Datasets
- Easier Collection & Storage

IMAGENET



2. Hardware

- Graphics Processing Units (GPUs)
- Massively Parallelizable



3. Software

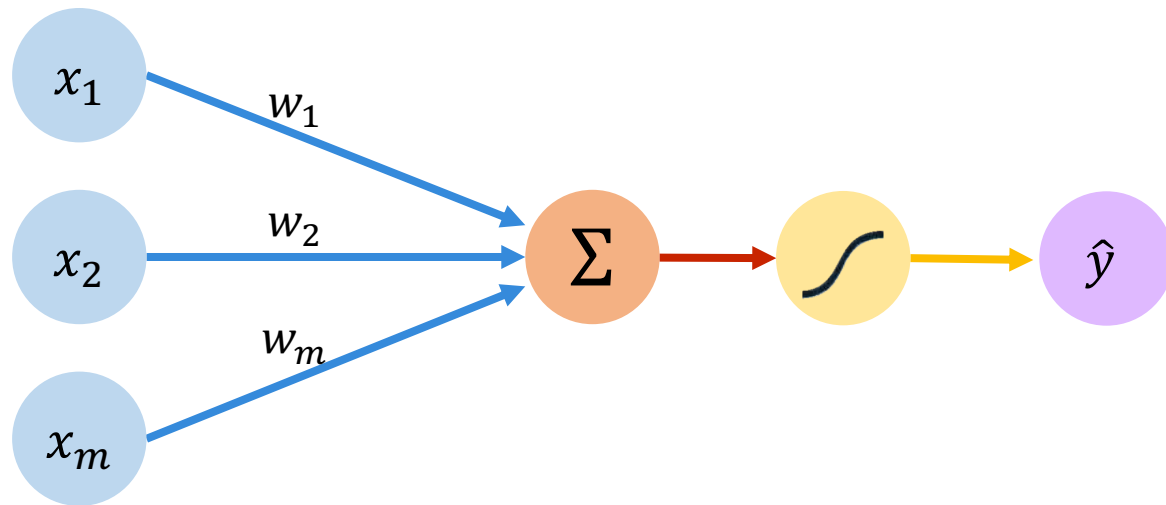
- Improved Techniques
- New Models
- Toolboxes



The Perceptron

The structural building block of deep learning

The Perceptron: Forward Propagation



Inputs Weights Sum Non-Linearity Output

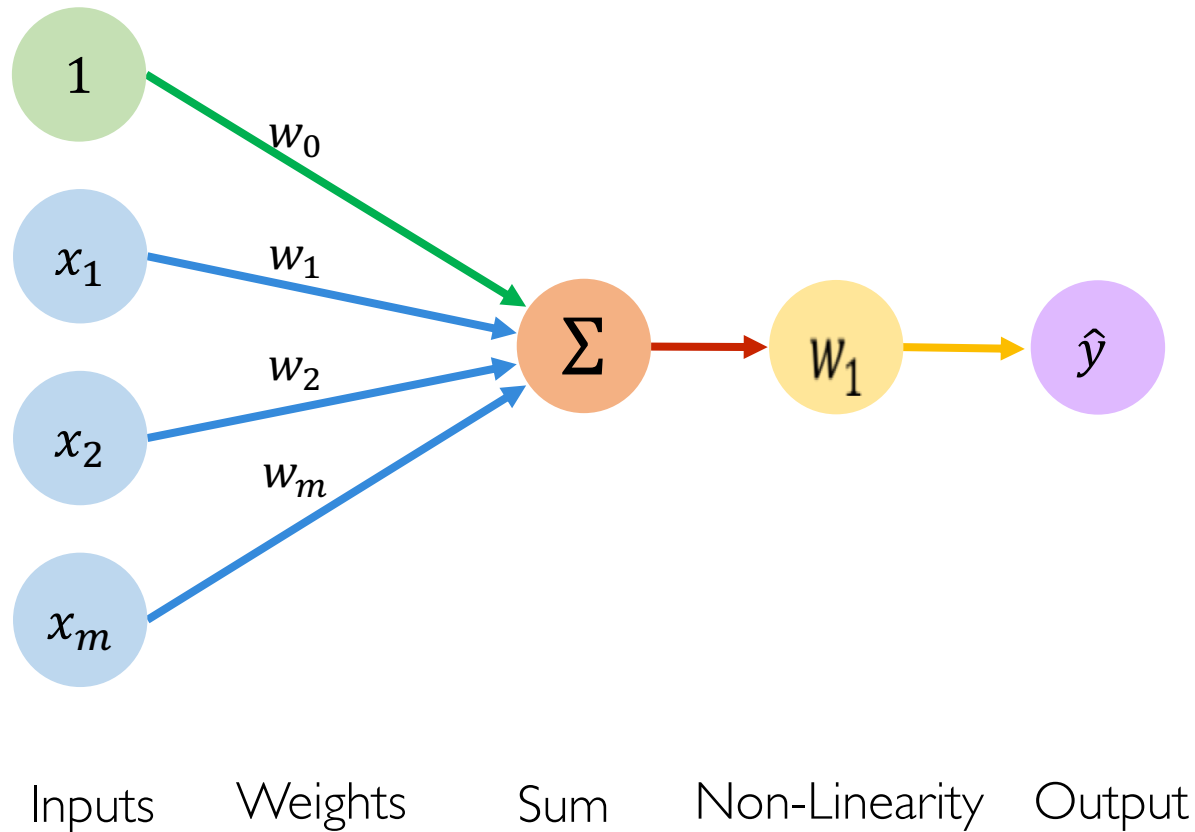
Output

Linear combination of inputs

$$\hat{y} = g \left(\sum_{i=1}^m x_i w_i \right)$$

Non-linear activation function

The Perceptron: Forward Propagation



Output

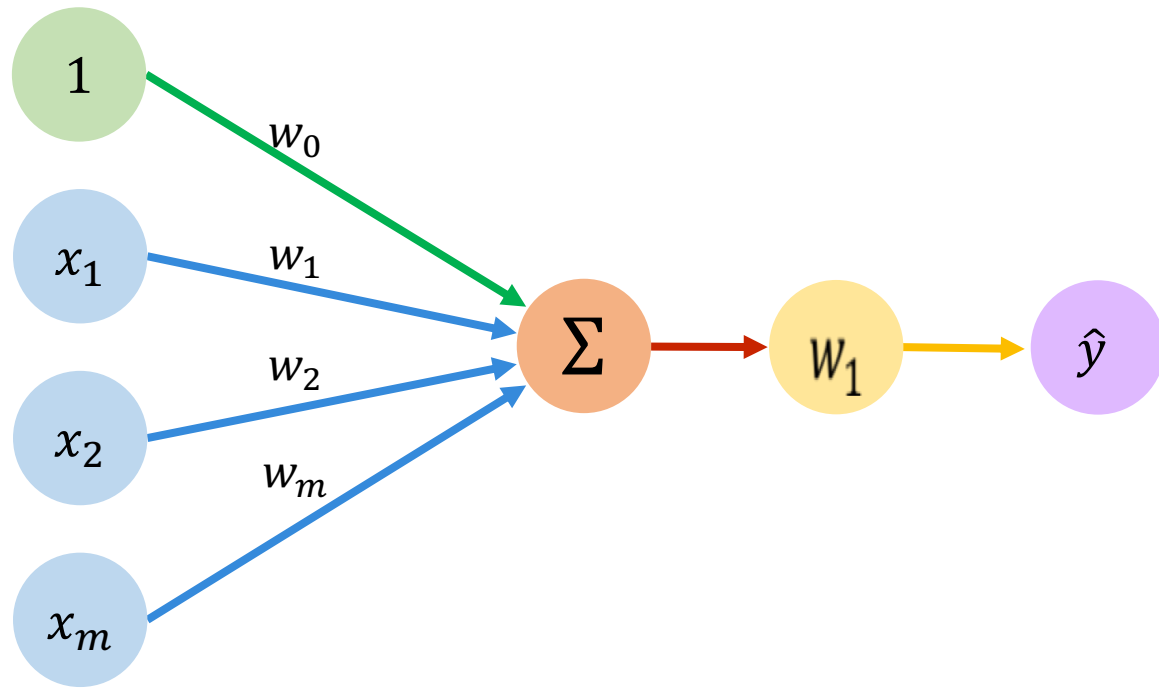
Linear combination of inputs

$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

Non-linear activation function

Bias

The Perceptron: Forward Propagation



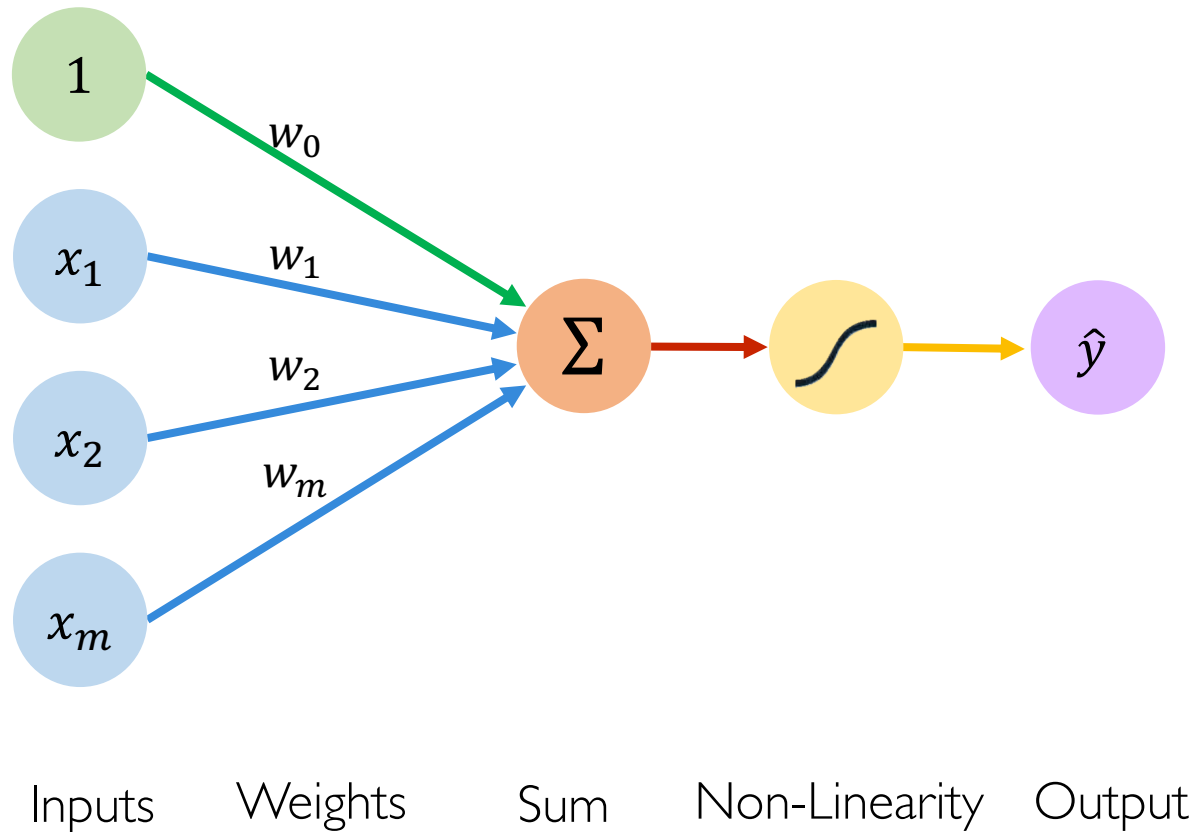
$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

$$\hat{y} = g (w_0 + \mathbf{X}^T \mathbf{W})$$

$$\text{where: } \mathbf{X} = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix} \text{ and } \mathbf{W} = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$$

Inputs Weights Sum Non-Linearity Output

The Perceptron: Forward Propagation

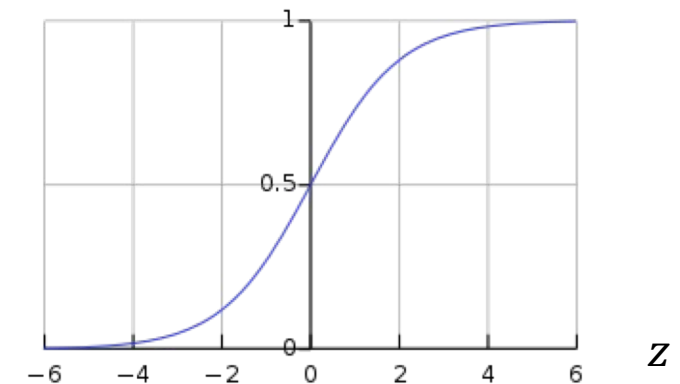


Activation Functions

$$\hat{y} = g(w_0 + \mathbf{X}^T \mathbf{W})$$

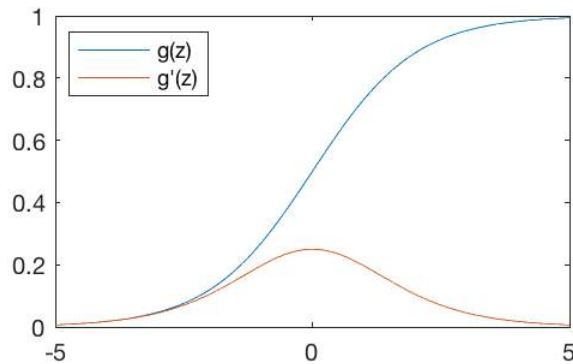
- Example: sigmoid function

$$g(z) = \sigma(z) = \frac{1}{1 + e^{-z}}$$



Common Activation Functions

Sigmoid Function



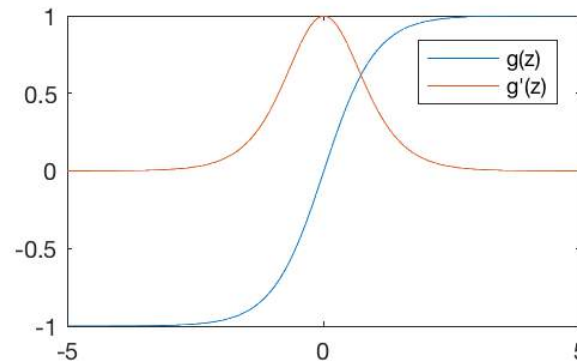
$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g'(z) = g(z)(1 - g(z))$$



`tf.nn.sigmoid(z)`

Hyperbolic Tangent



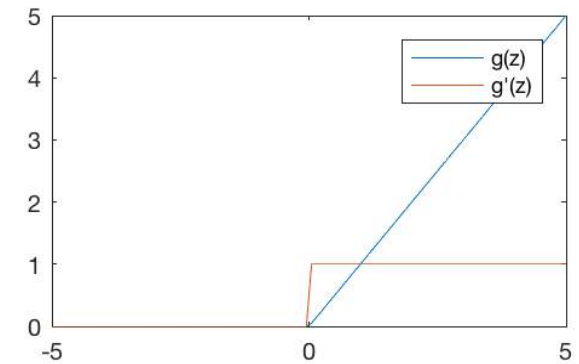
$$g(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

$$g'(z) = 1 - g(z)^2$$



`tf.nn.tanh(z)`

Rectified Linear Unit (ReLU)



$$g(z) = \max(0, z)$$

$$g'(z) = \begin{cases} 1, & z > 0 \\ 0, & \text{otherwise} \end{cases}$$

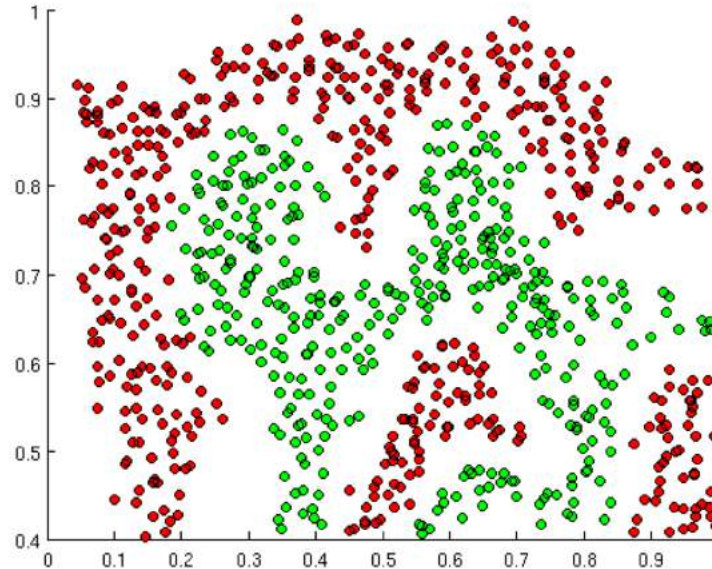


`tf.nn.relu(z)`

NOTE: All activation functions are non-linear

Importance of Activation Functions

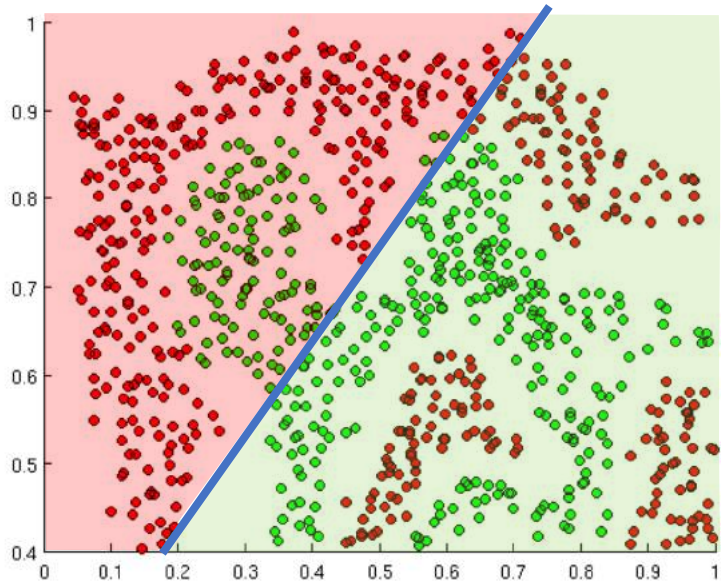
*The purpose of activation functions is to **introduce non-linearities** into the network*



What if we wanted to build a Neural Network to distinguish green vs red points?

Importance of Activation Functions

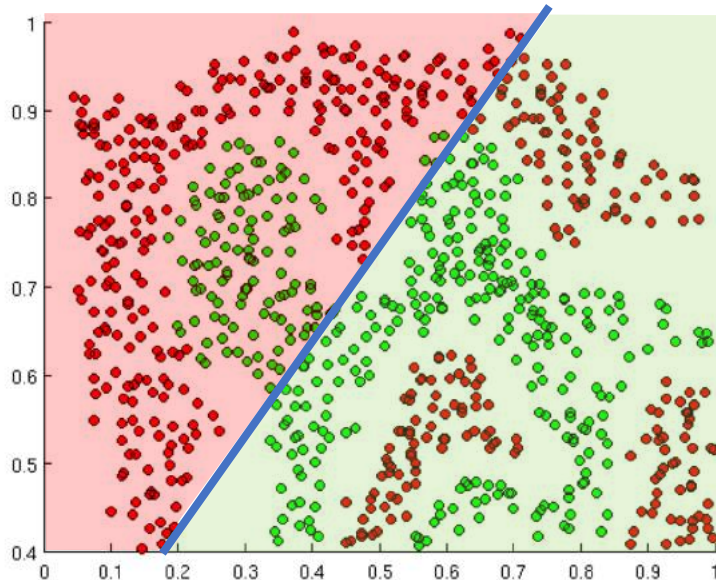
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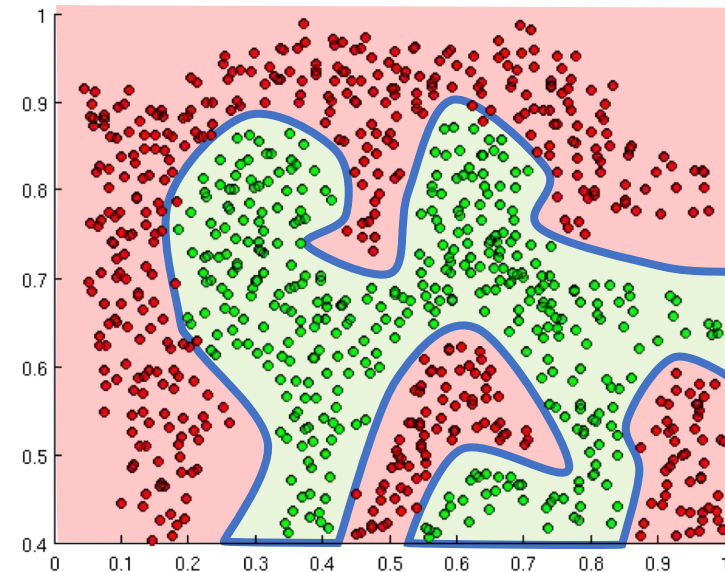
Linear Activation functions produce linear decisions no matter the network size

Importance of Activation Functions

*The purpose of activation functions is to **introduce non-linearities** into the network*

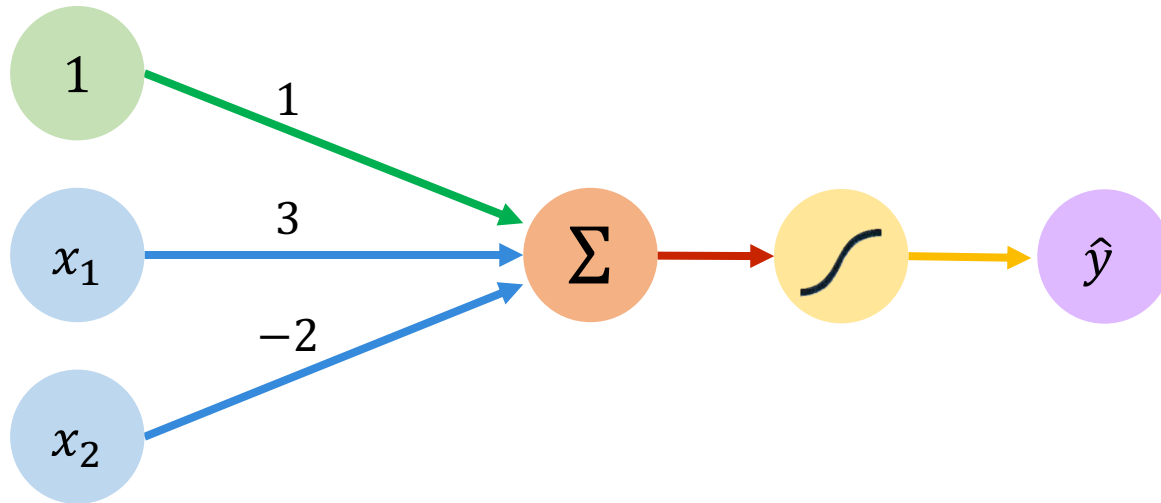


Linear Activation functions produce linear decisions no matter the network size



Non-linearities allow us to approximate arbitrarily complex functions

The Perceptron: Example

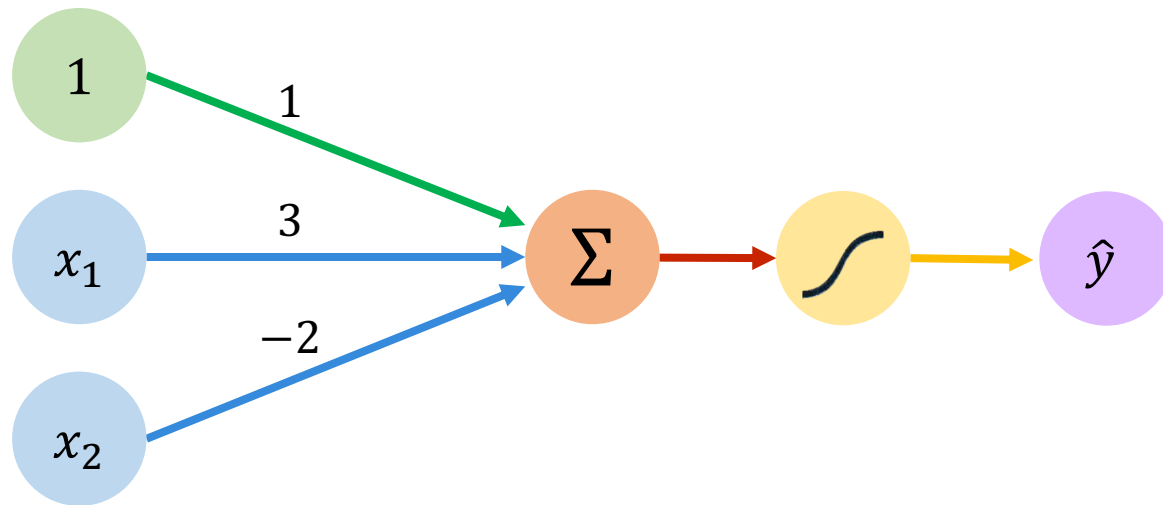


We have: $w_0 = 1$ and $\mathbf{W} = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$

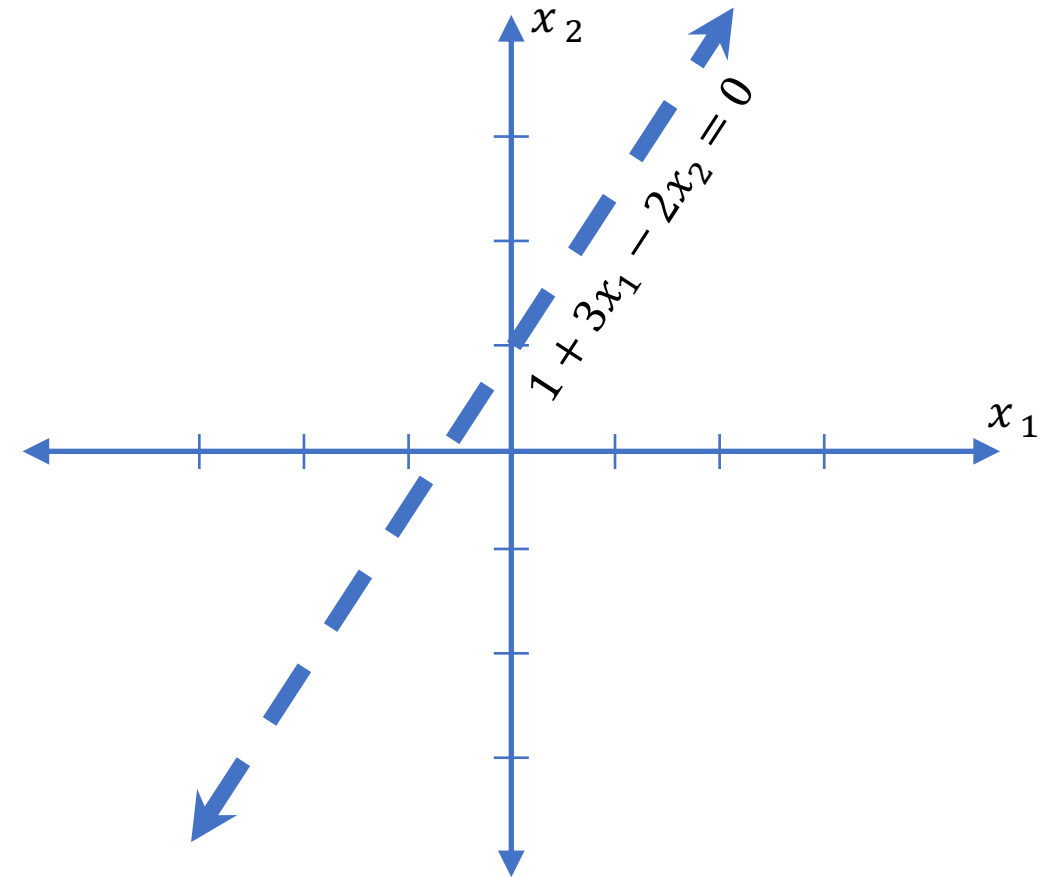
$$\begin{aligned}\hat{y} &= g(w_0 + \mathbf{X}^T \mathbf{W}) \\ &= g\left(1 + \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}^T \begin{bmatrix} 3 \\ -2 \end{bmatrix}\right) \\ \hat{y} &= g(1 + \underbrace{3x_1 - 2x_2})\end{aligned}$$

This is just a line in 2D!

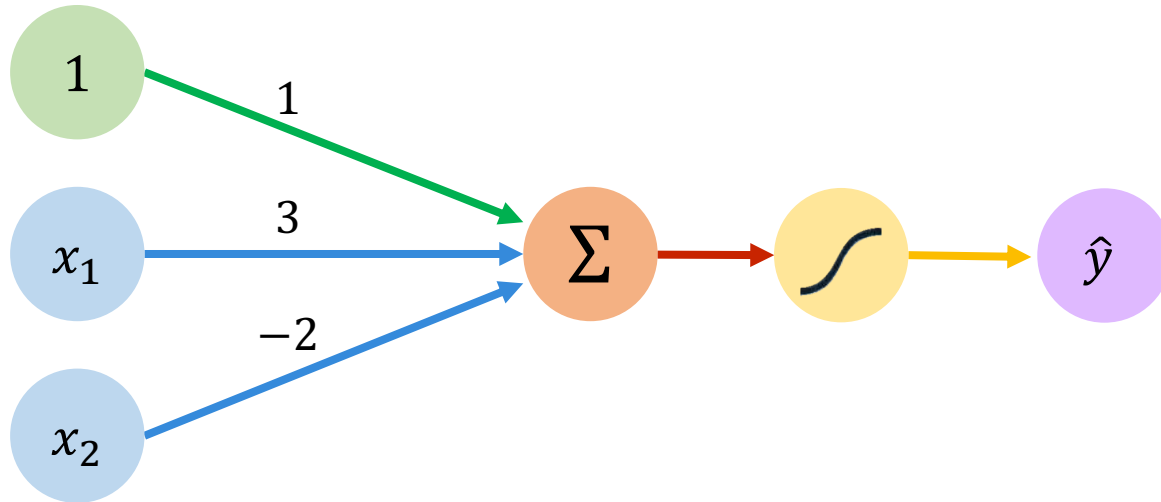
The Perceptron: Example



$$\hat{y} = g(1 + 3x_1 - 2x_2)$$



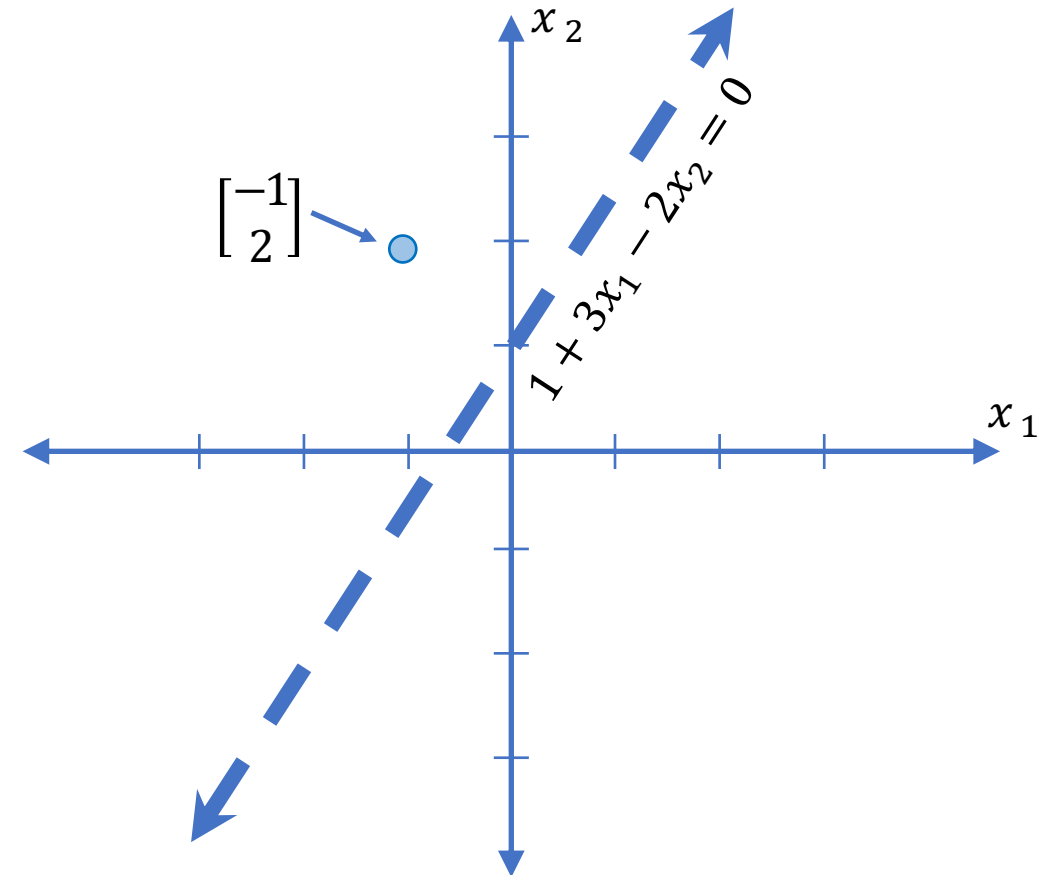
The Perceptron: Example



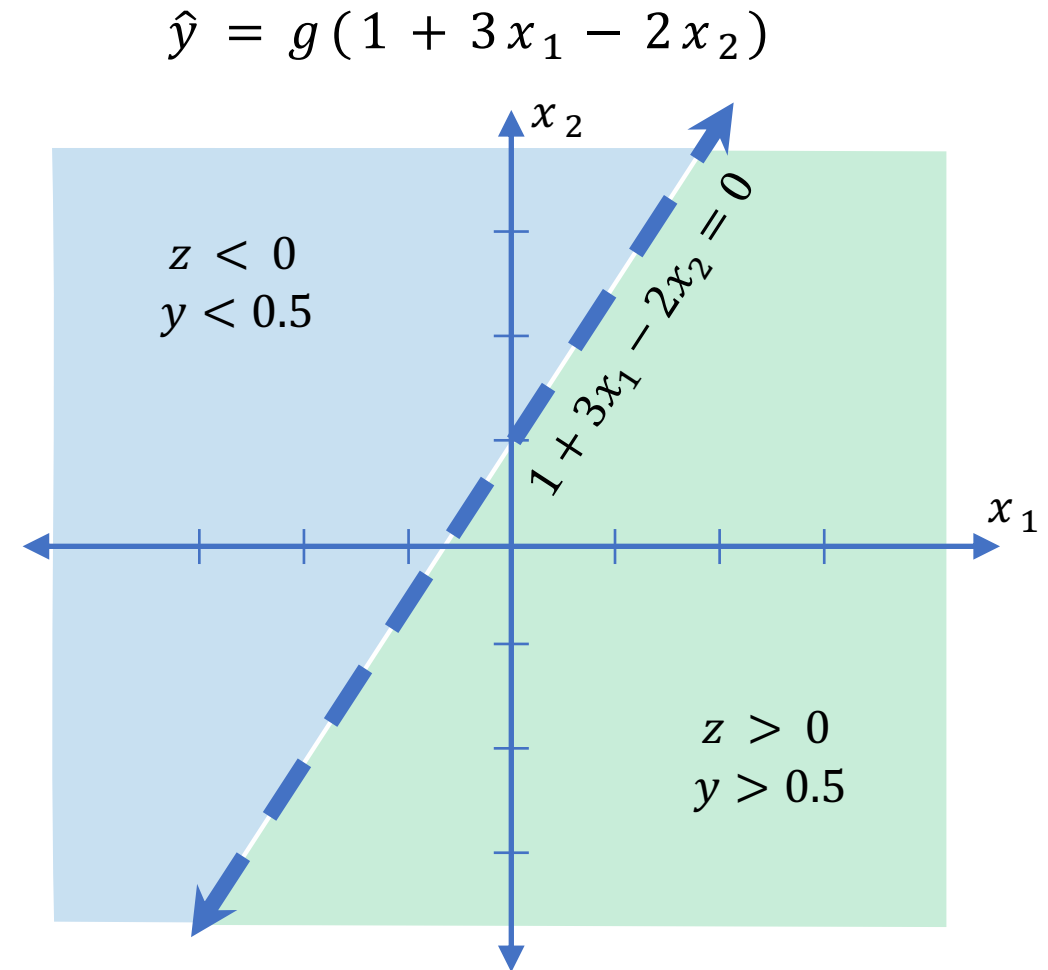
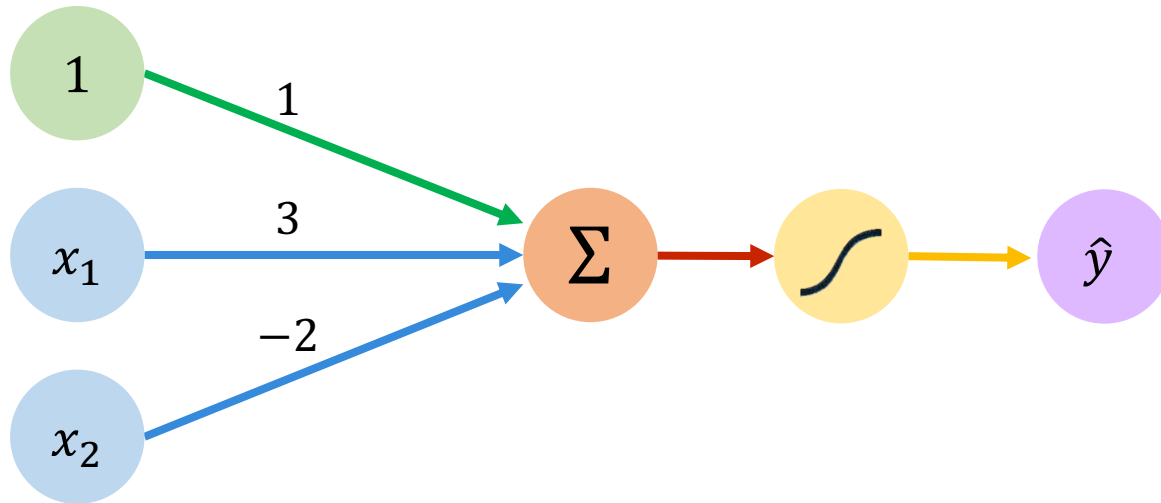
Assume we have input: $\mathbf{X} = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$

$$\begin{aligned}\hat{y} &= g(1 + (3 * -1) - (2 * 2)) \\ &= g(-6) \approx 0.002\end{aligned}$$

$$\hat{y} = g(1 + 3x_1 - 2x_2)$$

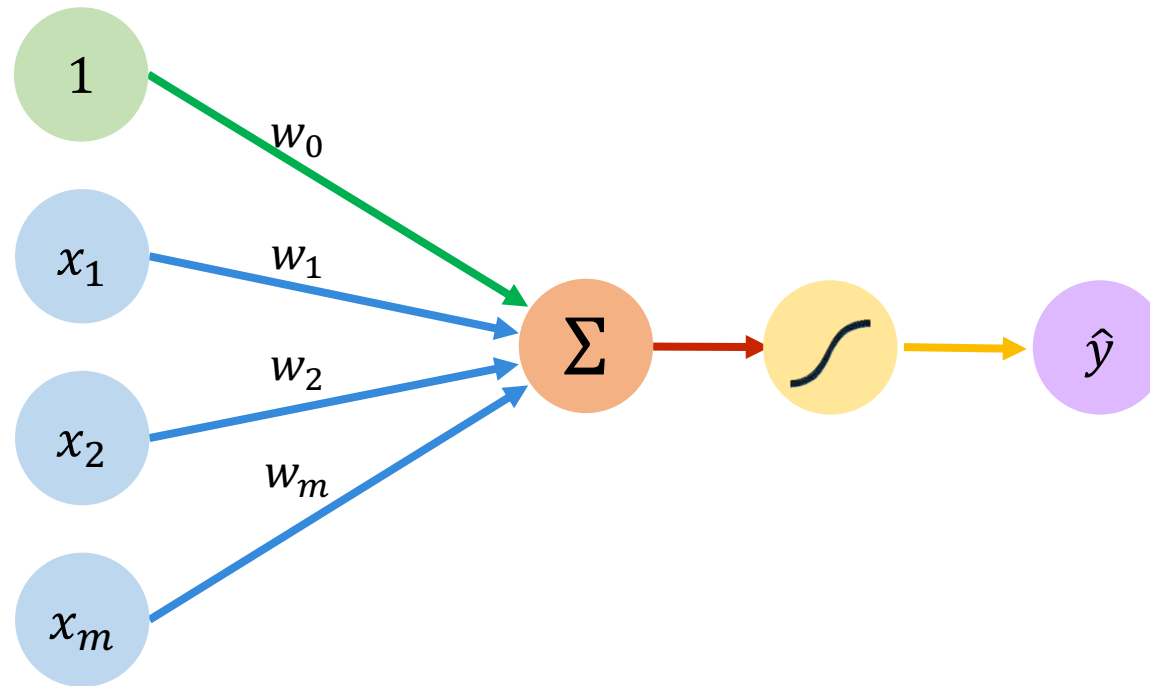


The Perceptron: Example



Building Neural Networks with Perceptrons

The Perceptron: Simplified



Inputs

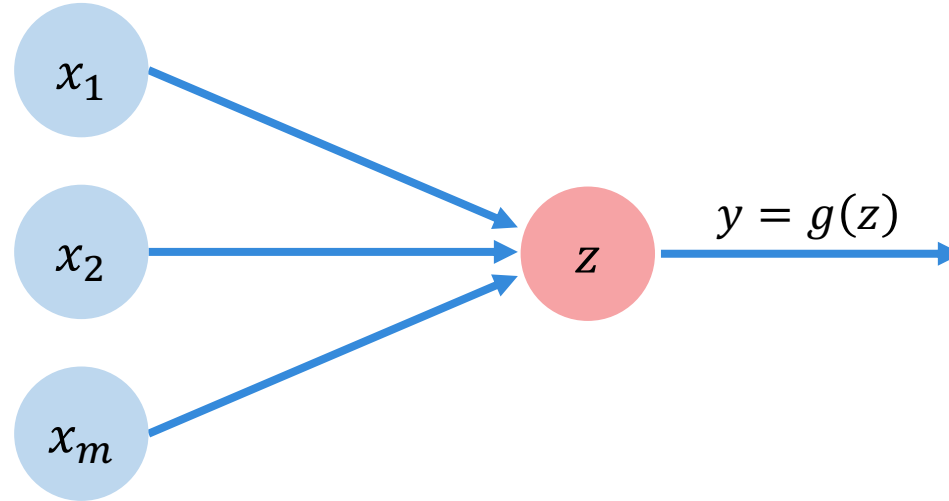
Weights

Sum

Non-Linearity

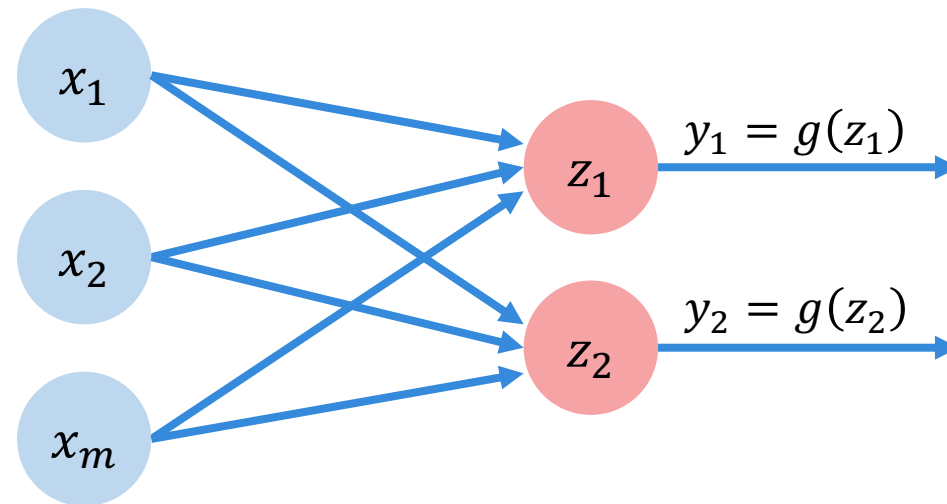
Output

The Perceptron: Simplified



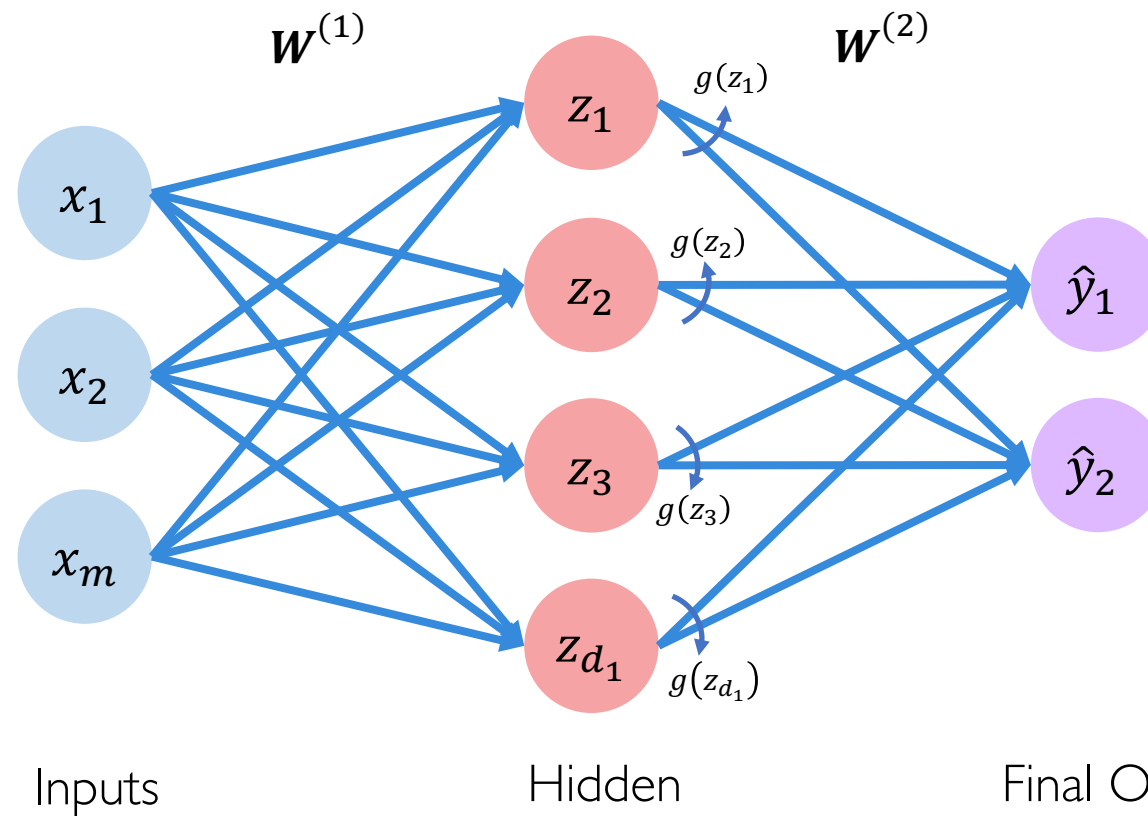
$$z = w_0 + \sum_{j=1}^m x_j w_j$$

Multi Output Perceptron



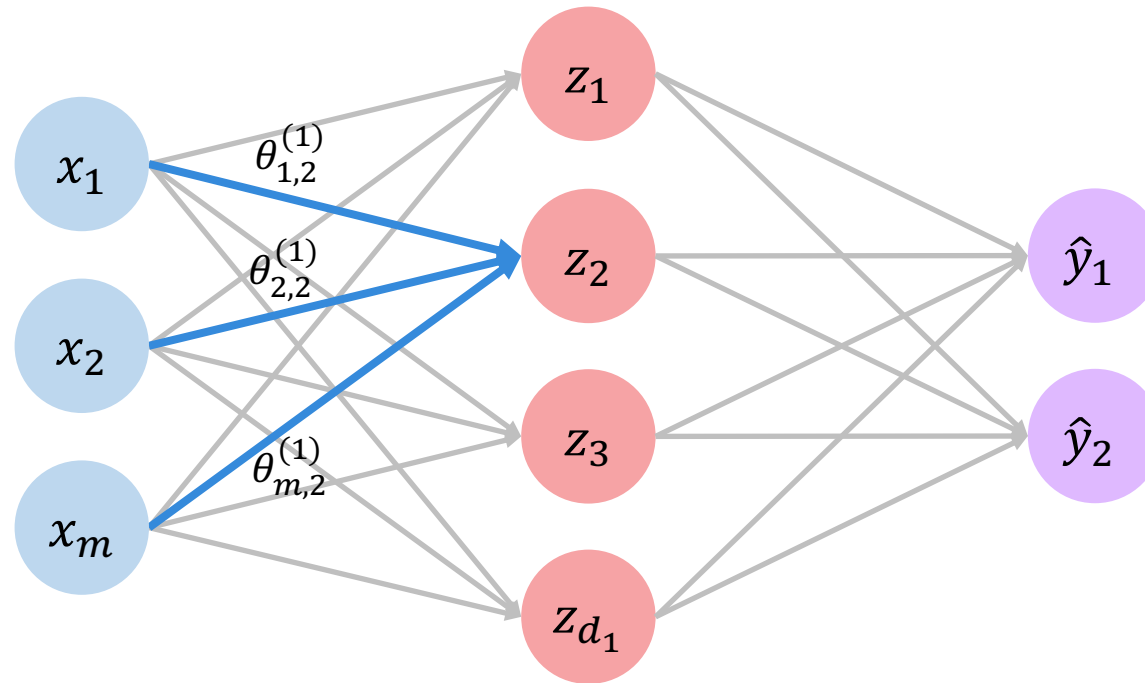
$$z_i = w_{0,i} + \sum_{j=1}^m x_j w_{j,i}$$

Single Layer Neural Network



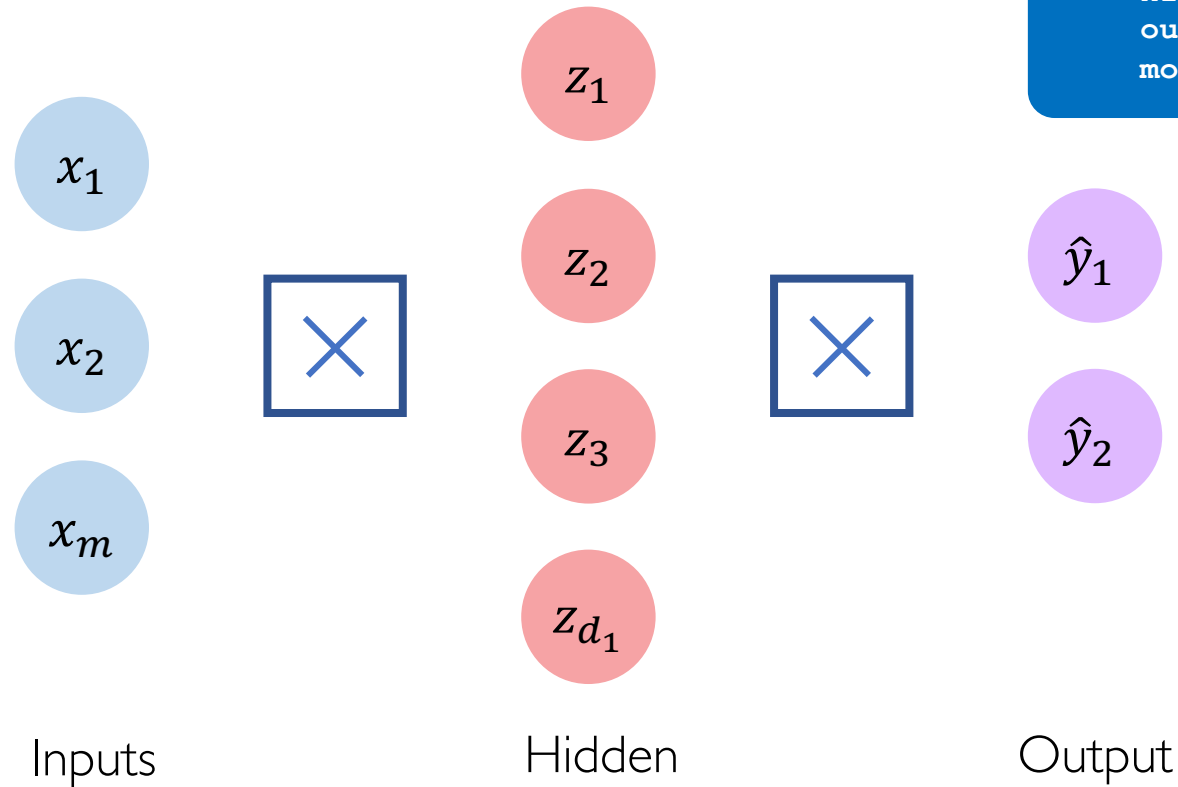
$$z_i = w_{0,i}^{(1)} + \sum_{j=1}^m x_j w_{j,i}^{(1)} \quad \hat{y}_i = g \left(w_{0,i}^{(2)} + \sum_{j=1}^{d_1} z_j w_{j,i}^{(2)} \right)$$

Single Layer Neural Network



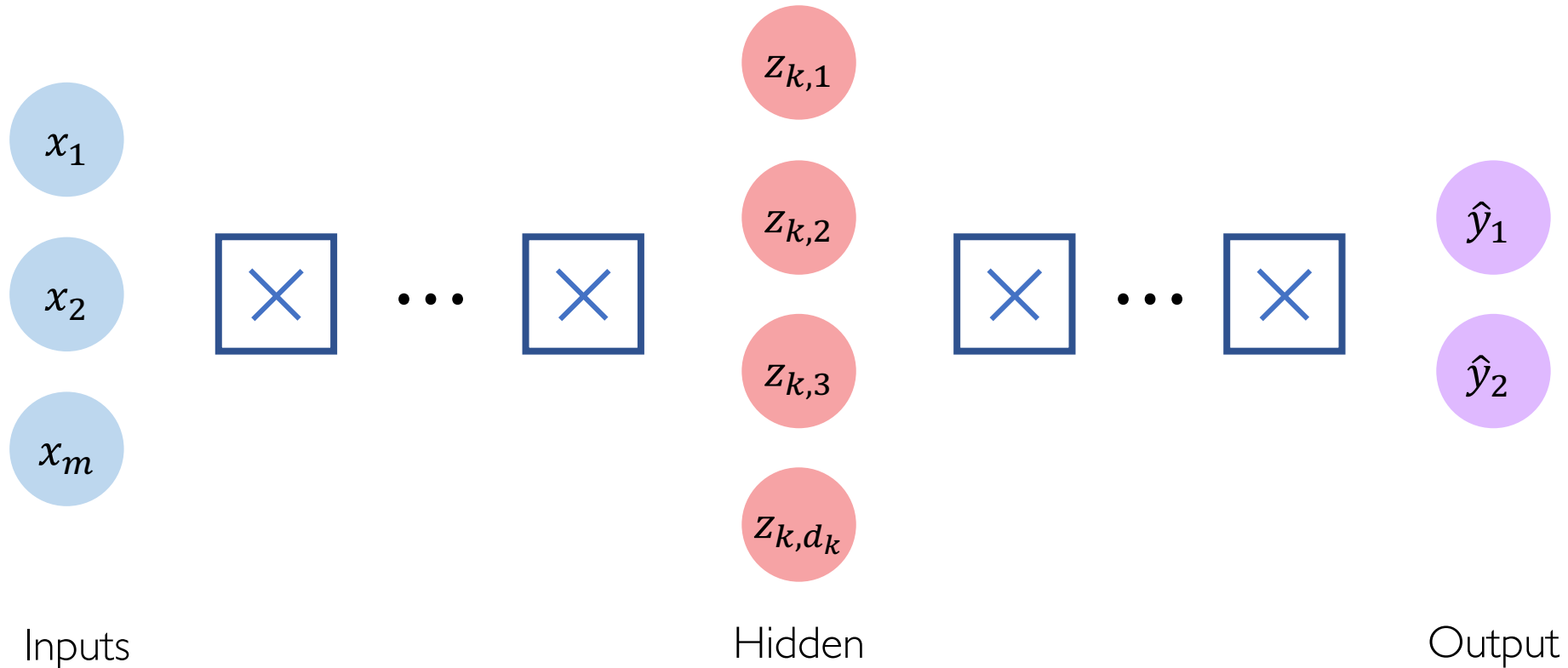
$$\begin{aligned} z_2 &= w_{0,2}^{(1)} + \sum_{j=1}^m x_j w_{j,2}^{(1)} \\ &= w_{0,2}^{(1)} + x_1 w_{1,2}^{(1)} + x_2 w_{2,2}^{(1)} + x_m w_{m,2}^{(1)} \end{aligned}$$

Multi Output Perceptron



```
from tf.keras.layers import *  
  
inputs = Inputs(m)  
hidden = Dense(d1)(inputs)  
outputs = Dense(2)(hidden)  
model = Model(inputs, outputs)
```

Deep Neural Network



$$z_{k,i} = w_{0,i}^{(k)} + \sum_{j=1}^{d_{k-1}} g(z_{k-1,j}) w_{j,i}^{(k)}$$

Applying Neural Networks

Example Problem

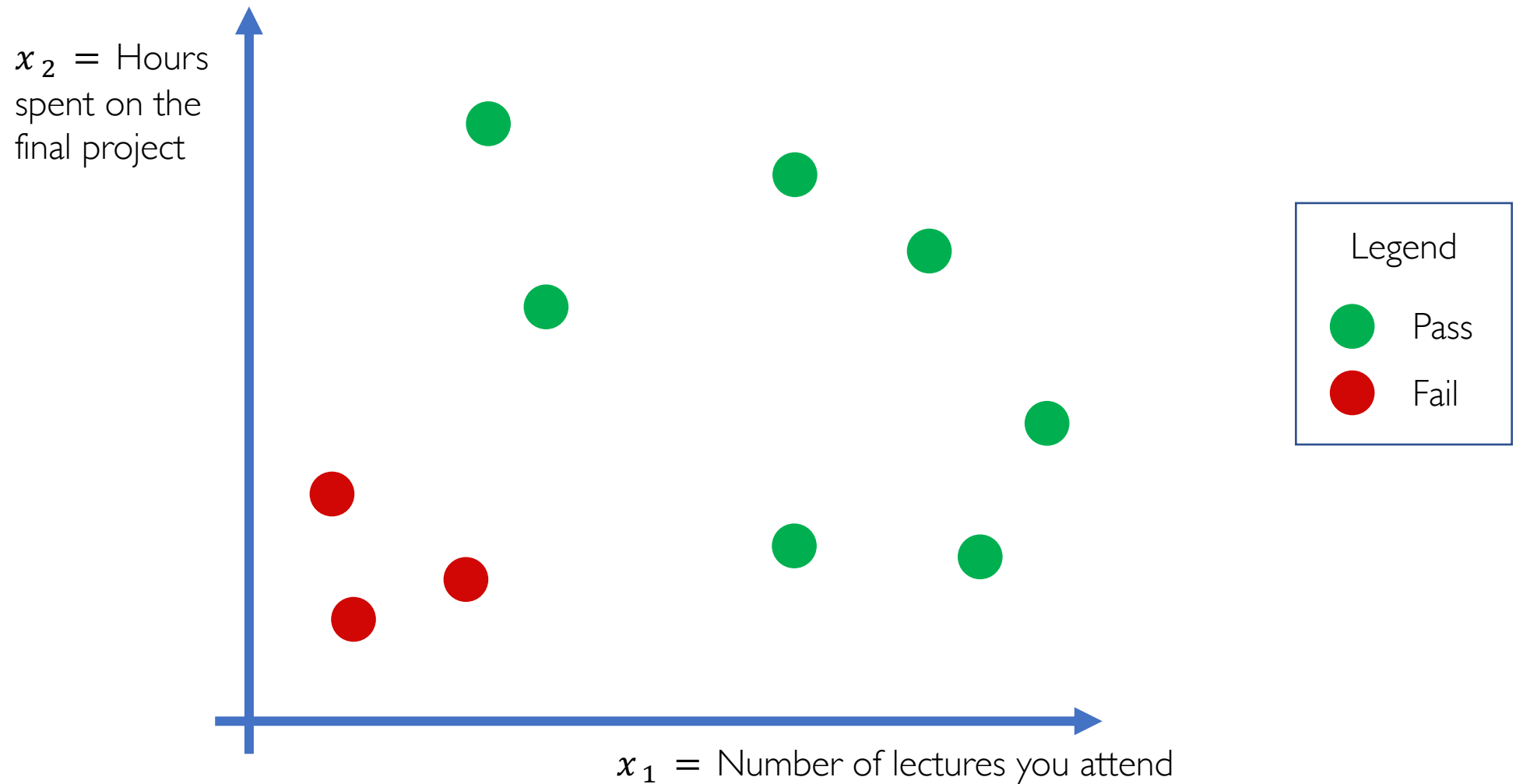
Will I pass this class?

Let's start with a simple two feature model

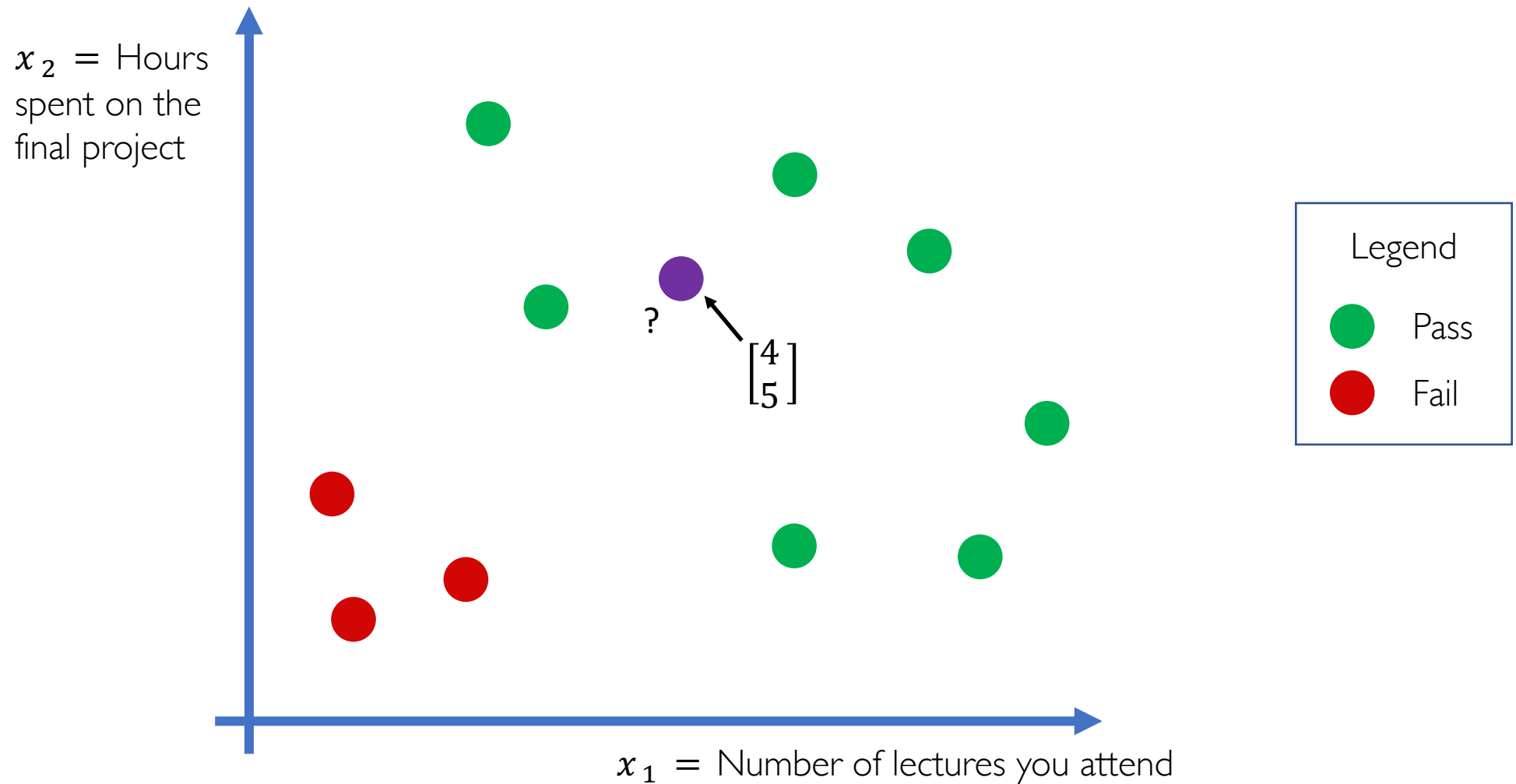
x_1 = Number of lectures you attend

x_2 = Hours spent on the final project

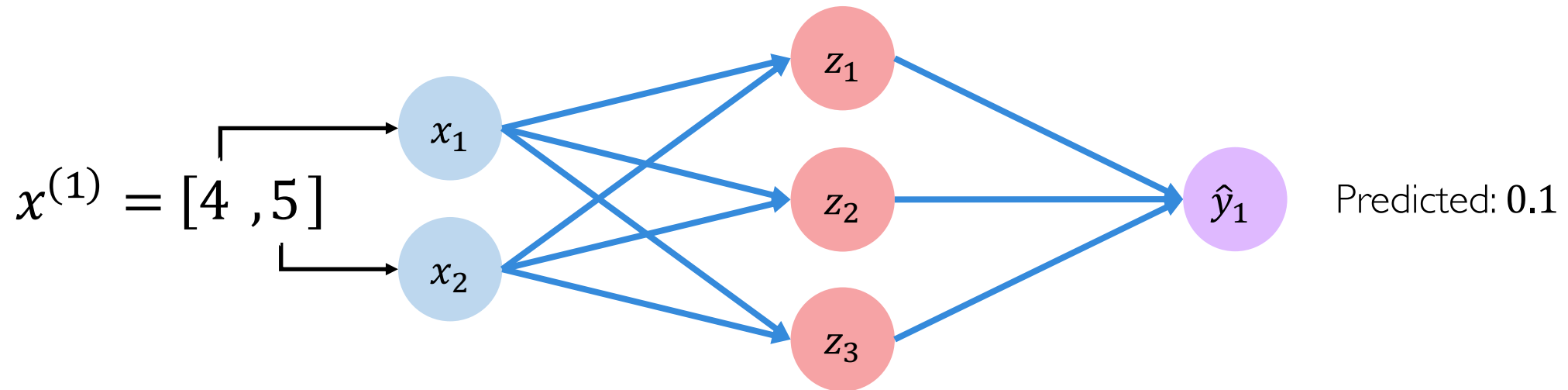
Example Problem: Will I pass this class?



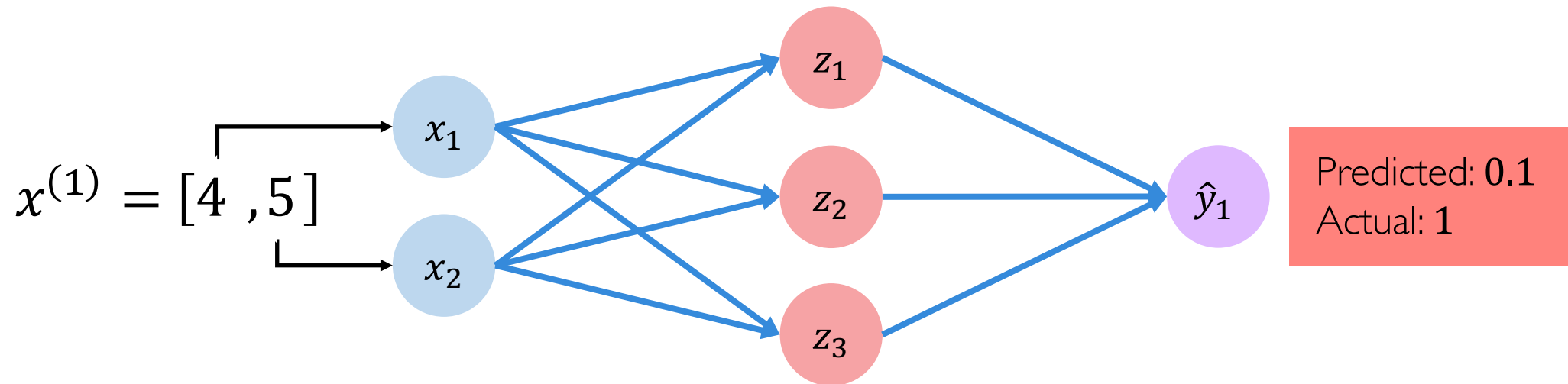
Example Problem: Will I pass this class?



Example Problem: Will I pass this class?

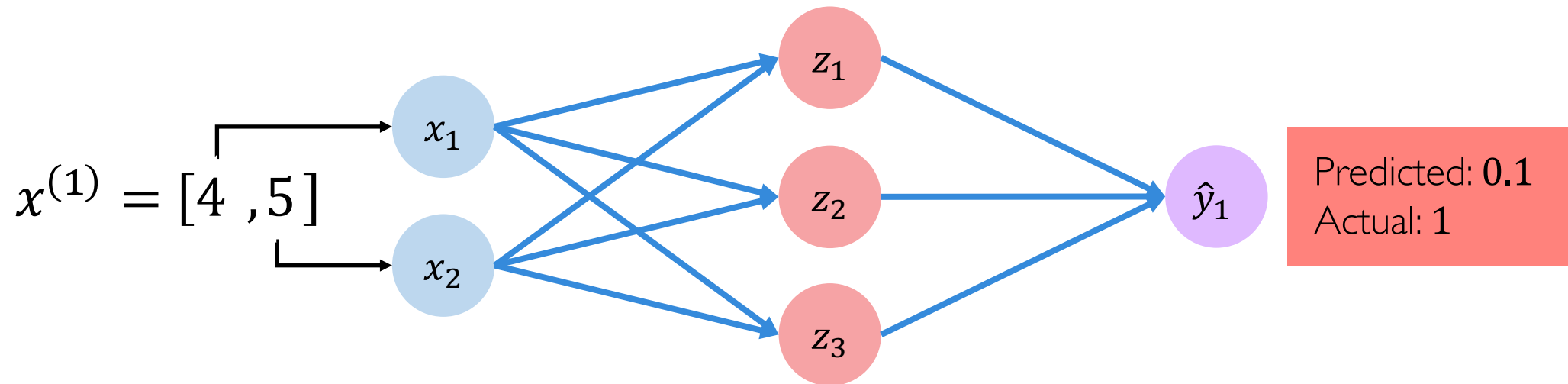


Example Problem: Will I pass this class?



Quantifying Loss

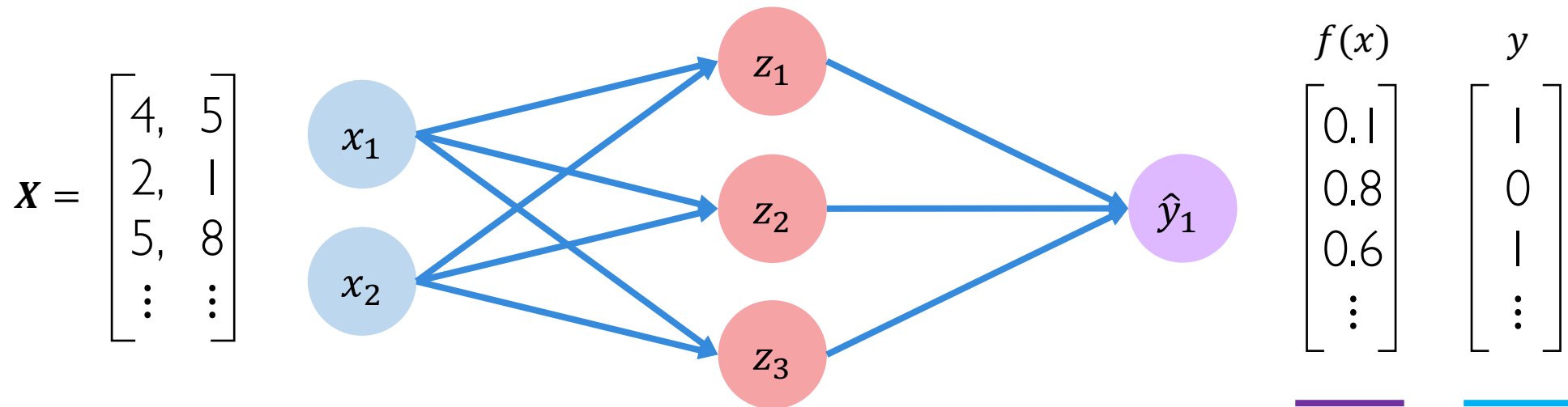
The **loss** of our network measures the cost incurred from incorrect predictions



$$\mathcal{L}(\underbrace{f(x^{(i)}; \mathbf{W})}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}})$$

Empirical Loss

The **empirical loss** measures the total loss over our entire dataset



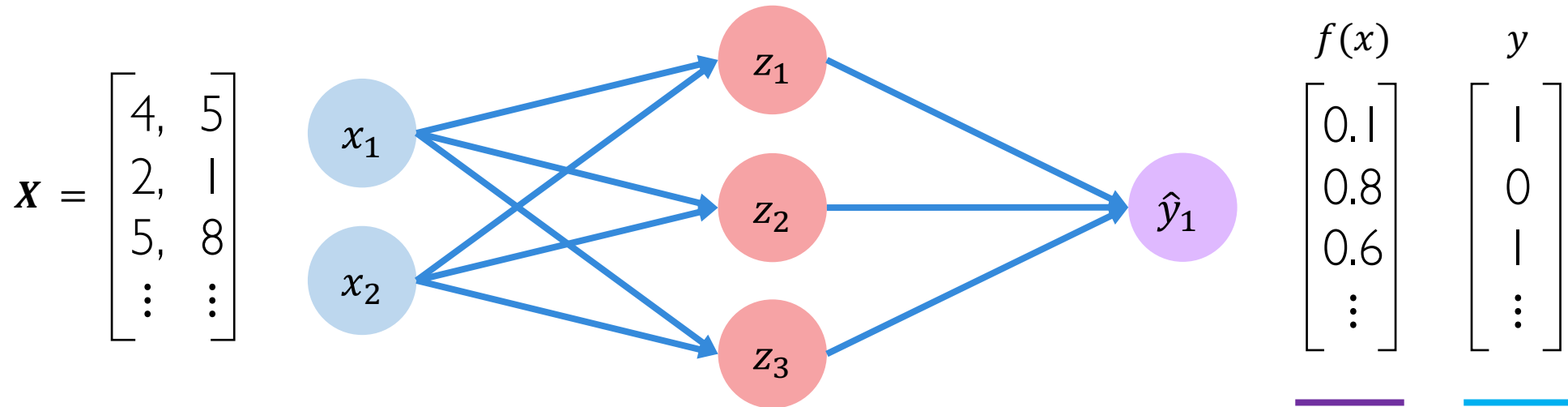
Also known as:

- Objective function
- Cost function
- Empirical Risk

$$J(\mathbf{W}) = \frac{1}{n} \sum_{i=1}^n \mathcal{L}(\underbrace{f(x^{(i)}; \mathbf{W})}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}})$$

Binary Cross Entropy Loss

Cross entropy loss can be used with models that output a probability between 0 and 1



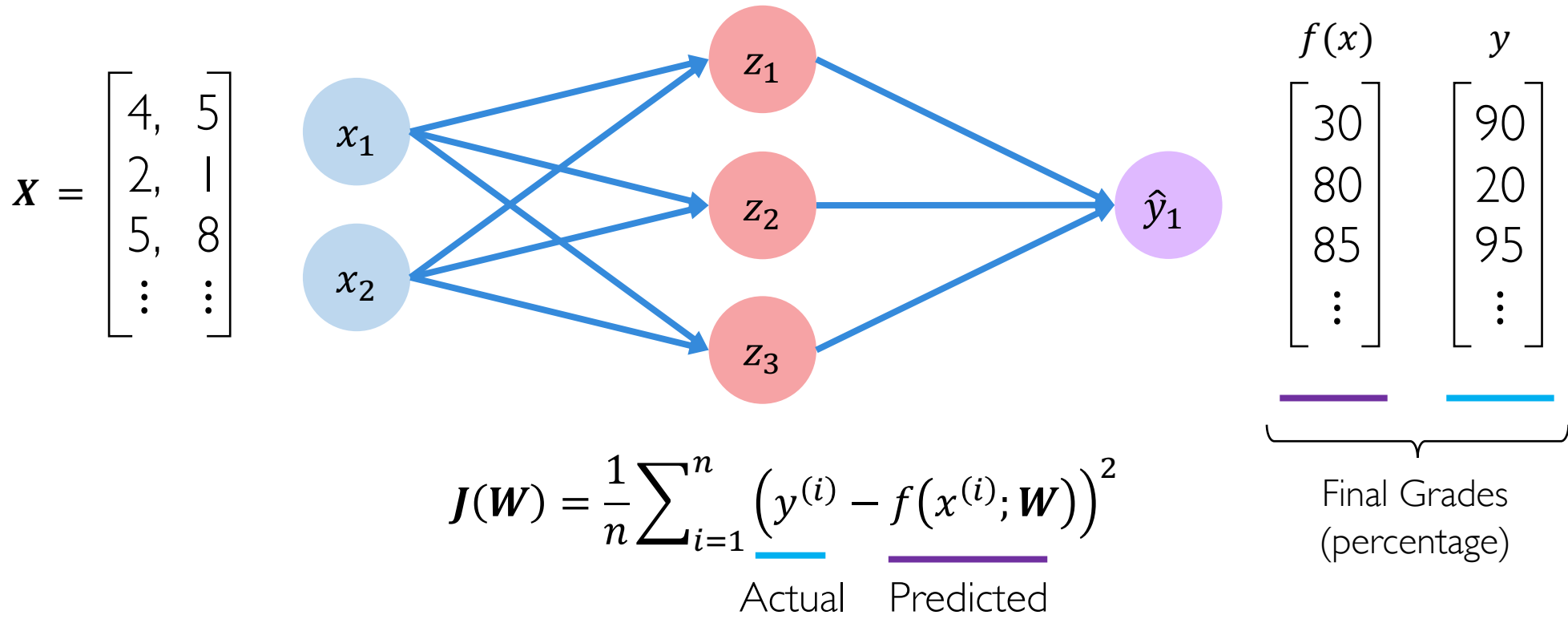
$$J(W) = \frac{1}{n} \sum_{i=1}^n \underbrace{y^{(i)}}_{\text{Actual}} \log \left(\underbrace{f(x^{(i)}; W)}_{\text{Predicted}} \right) + (1 - \underbrace{y^{(i)}}_{\text{Actual}}) \log \left(1 - \underbrace{f(x^{(i)}; W)}_{\text{Predicted}} \right)$$



```
loss = tf.reduce_mean( tf.nn.softmax_cross_entropy_with_logits(model.y, model.pred) )
```


Mean Squared Error Loss

Mean squared error loss can be used with regression models that output continuous real numbers



```
loss = tf.reduce_mean( tf.square( tf.subtract( model.y, model.pred ) ) )
```

Training Neural Networks

Loss Optimization

We want to find the network weights that *achieve the lowest loss*

$$\mathbf{W}^* = \operatorname{argmin}_{\mathbf{W}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(f(x^{(i)}; \mathbf{W}), y^{(i)})$$

$$\mathbf{W}^* = \operatorname{argmin}_{\mathbf{W}} J(\mathbf{W})$$

Loss Optimization

We want to find the network weights that *achieve the lowest loss*

$$\mathbf{W}^* = \operatorname{argmin}_{\mathbf{W}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(f(x^{(i)}; \mathbf{W}), y^{(i)})$$

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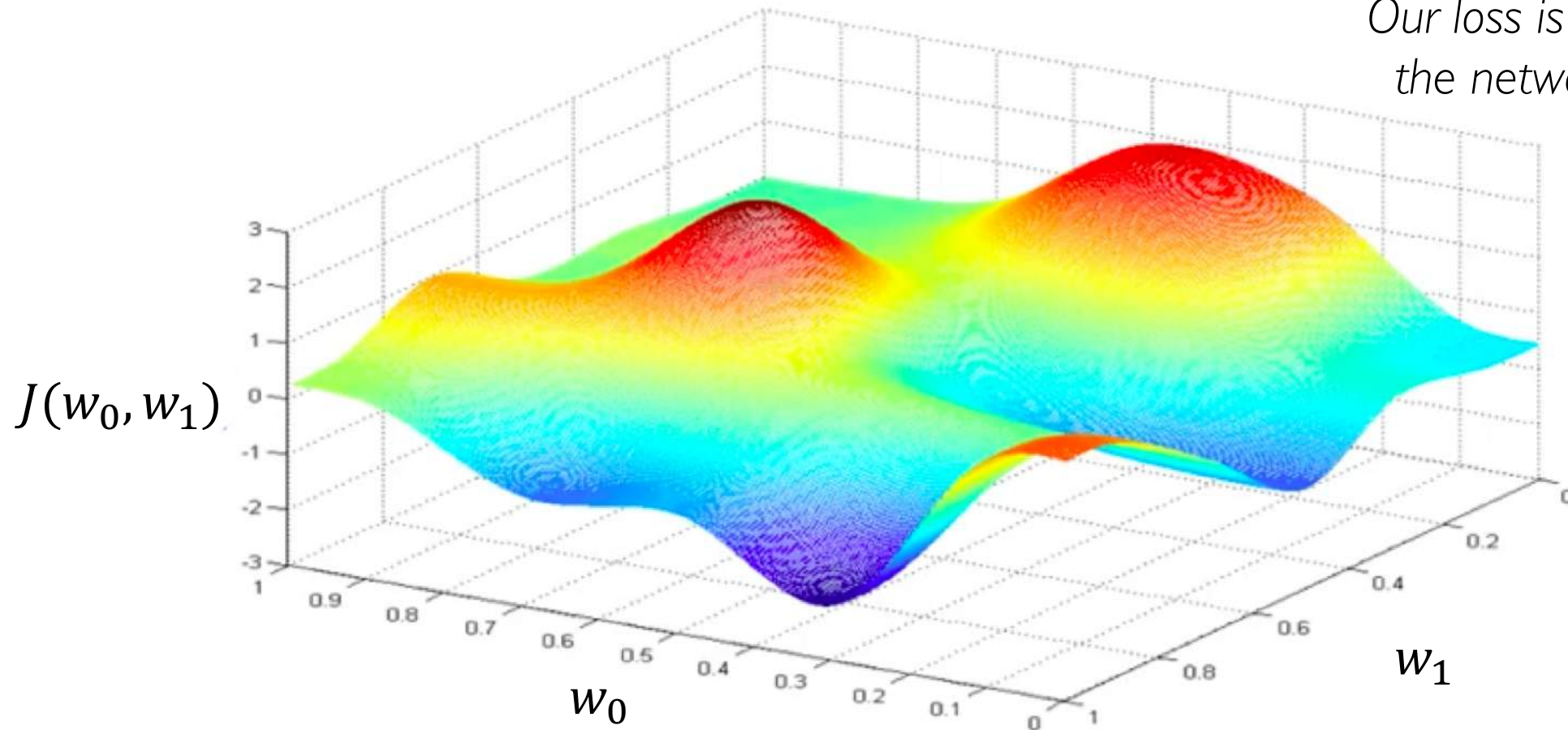
Remember:

$$\mathbf{W} = \{\mathbf{W}^{(0)}, \mathbf{W}^{(1)}, \dots\}$$

Loss Optimization

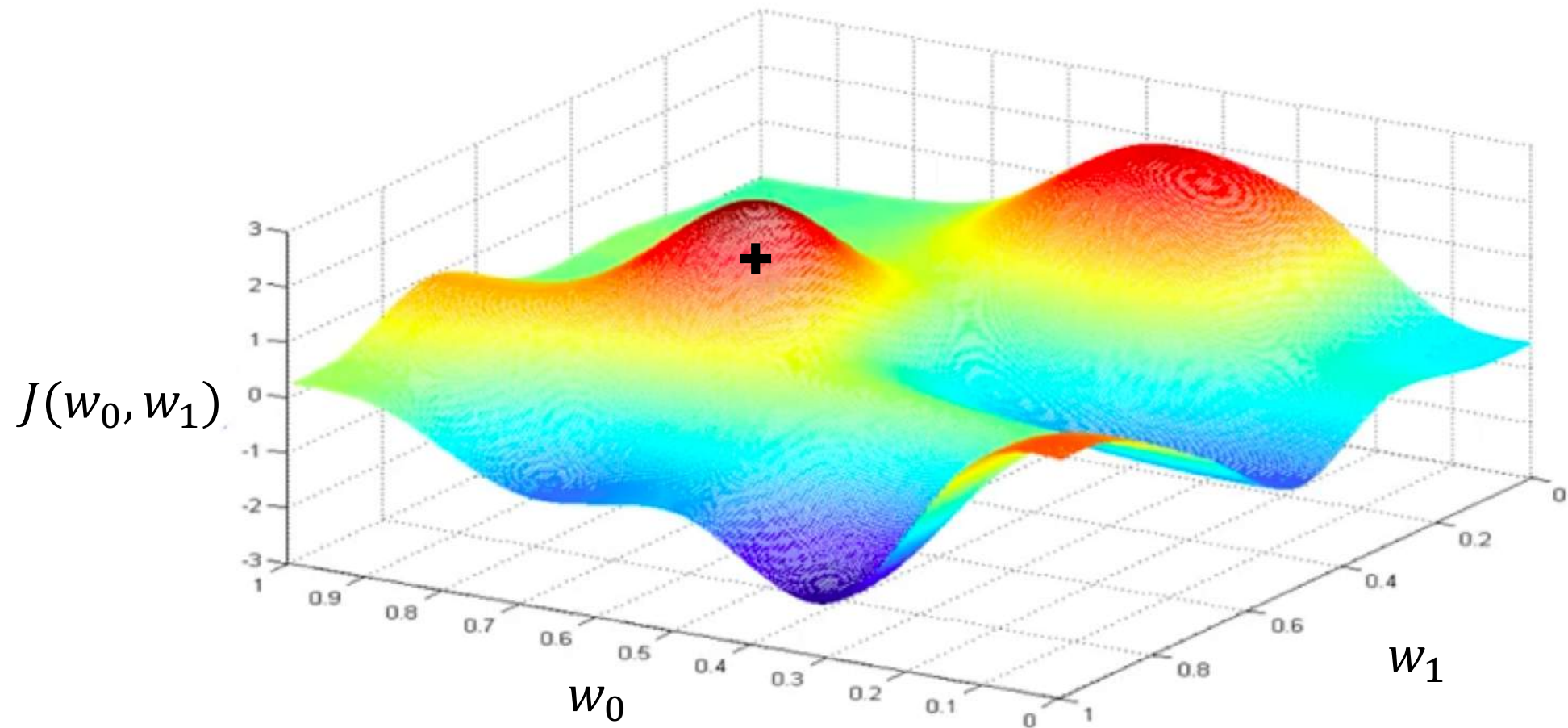
$$W^* = \underset{W}{\operatorname{argmin}} J(W)$$

Remember:
*Our loss is a function of
the network weights!*



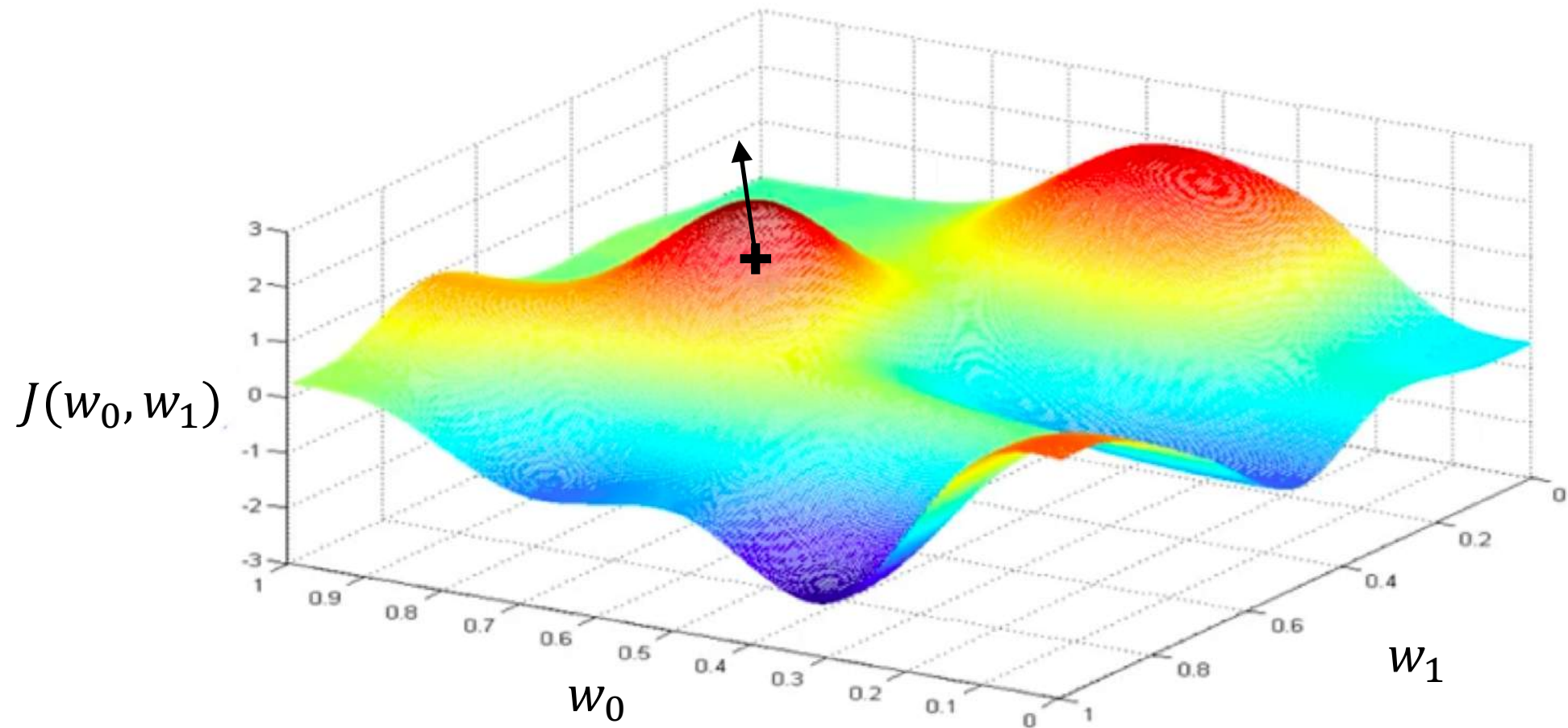
Loss Optimization

Randomly pick an initial (w_0, w_1)



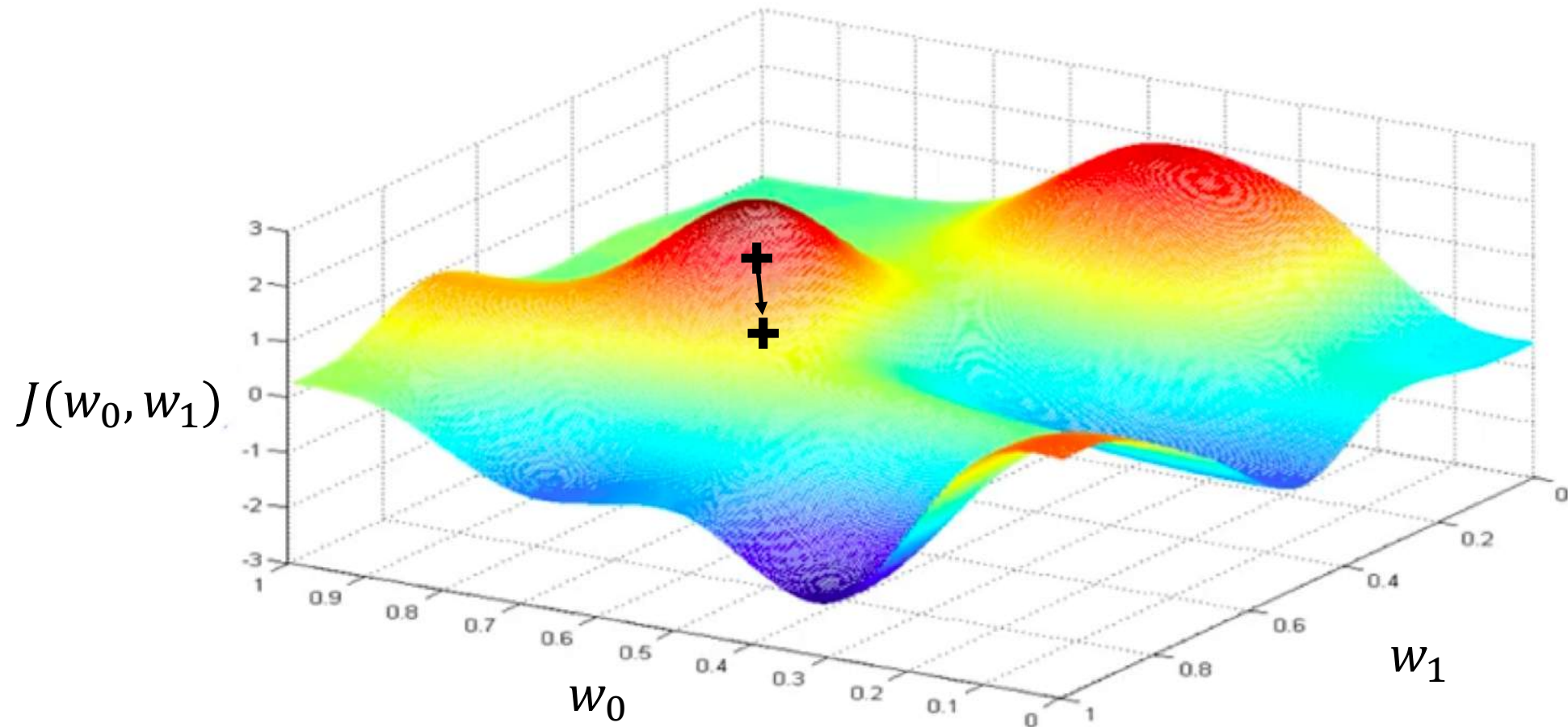
Loss Optimization

Compute gradient, $\frac{\partial J(\mathbf{w})}{\partial \mathbf{w}}$



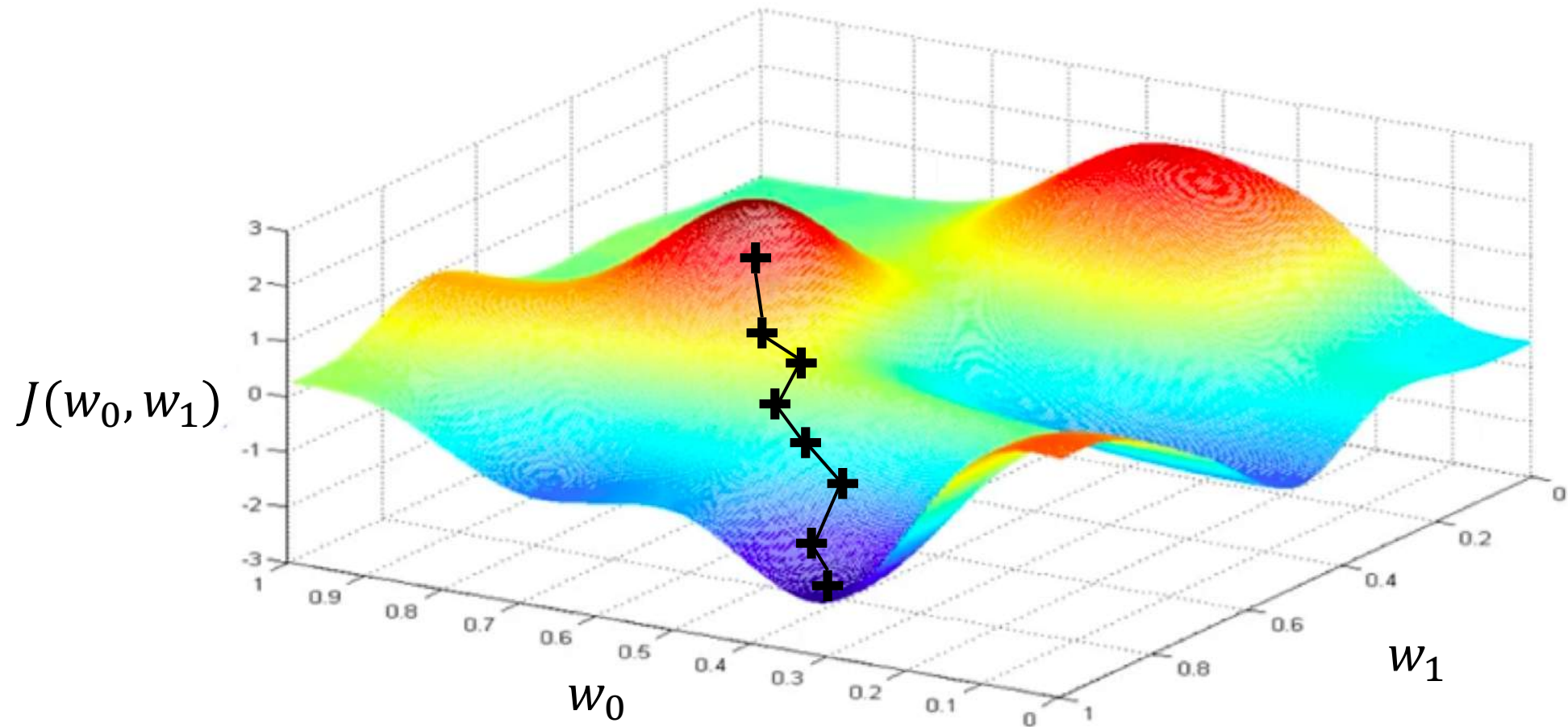
Loss Optimization

Take small step in opposite direction of gradient



Gradient Descent

Repeat until convergence



Gradient Descent

Algorithm

1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
2. Loop until convergence:
3. Compute gradient, $\frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
4. Update weights, $\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
5. Return weights

 `weights = tf.random_normal(shape, stddev=sigma)`

 `grads = tf.gradients(ys=loss, xs=weights)`

 `weights_new = weights.assign(weights - lr * grads)`

Gradient Descent

Algorithm

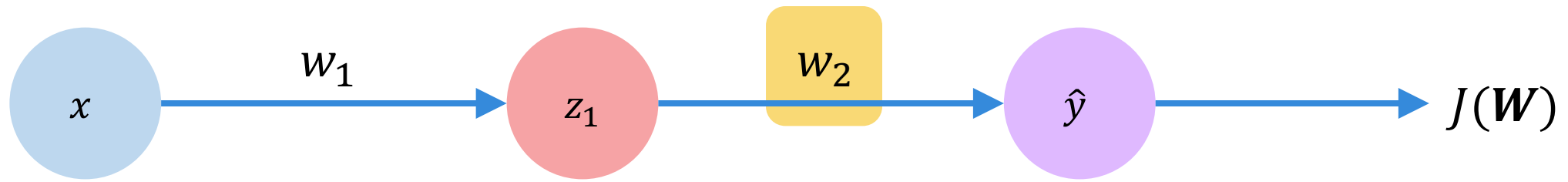
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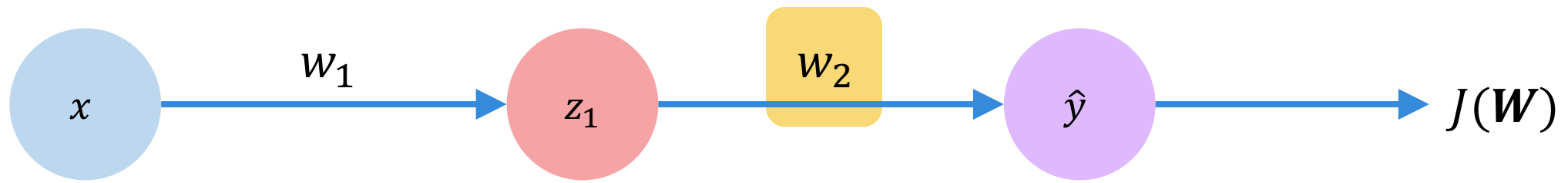
 `weights_new = weights.assign(weights - lr * grads)`

Computing Gradients: Backpropagation



How does a small change in one weight (ex. w_2) affect the final loss $J(\mathbf{W})$?

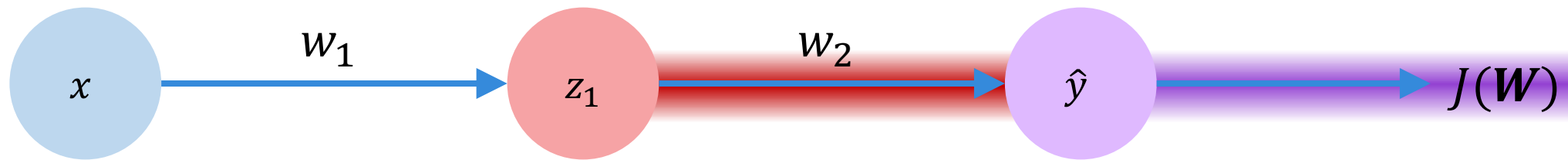
Computing Gradients: Backpropagation



$$\frac{\partial J(W)}{\partial w_2} =$$

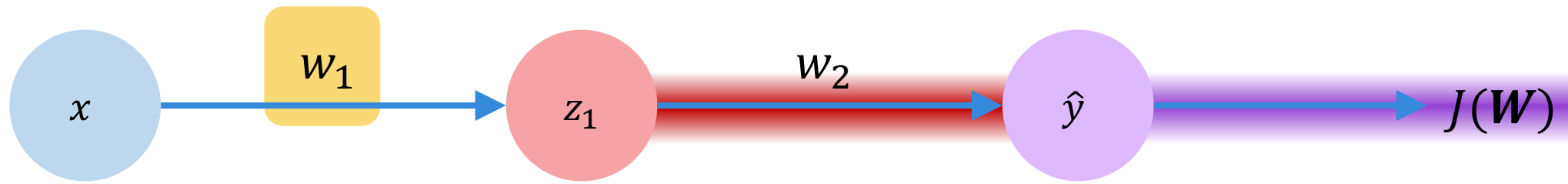
Let's use the chain rule!

Computing Gradients: Backpropagation



$$\frac{\partial J(W)}{\partial w_2} = \underbrace{\frac{\partial J(W)}{\partial \hat{y}}}_{\text{purple}} * \underbrace{\frac{\partial \hat{y}}{\partial w_2}}_{\text{red}}$$

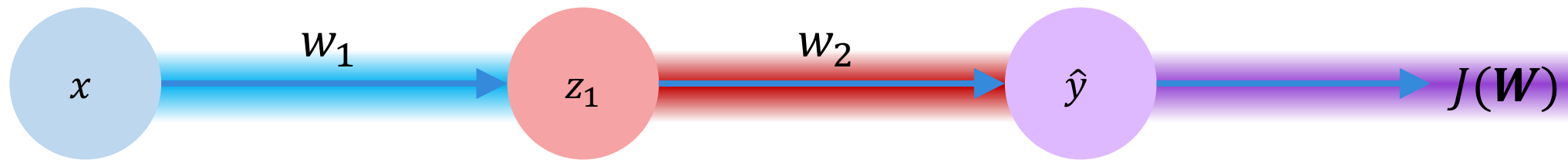
Computing Gradients: Backpropagation



$$\frac{\partial J(W)}{\partial w_1} = \frac{\partial J(W)}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial w_1}$$

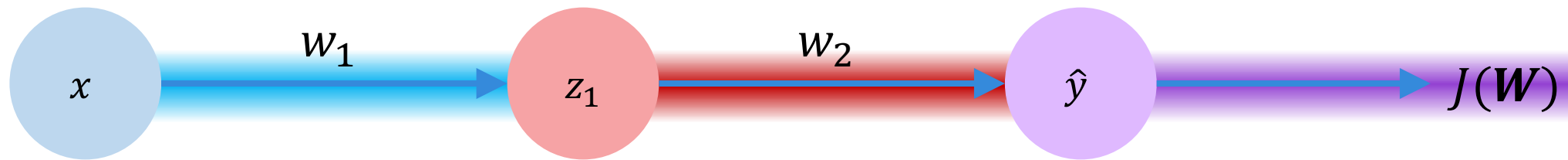
Apply chain rule! Apply chain rule!

Computing Gradients: Backpropagation



$$\frac{\partial J(W)}{\partial w_1} = \underbrace{\frac{\partial J(W)}{\partial \hat{y}}}_{\text{purple}} * \underbrace{\frac{\partial \hat{y}}{\partial z_1}}_{\text{red}} * \underbrace{\frac{\partial z_1}{\partial w_1}}_{\text{blue}}$$

Computing Gradients: Backpropagation

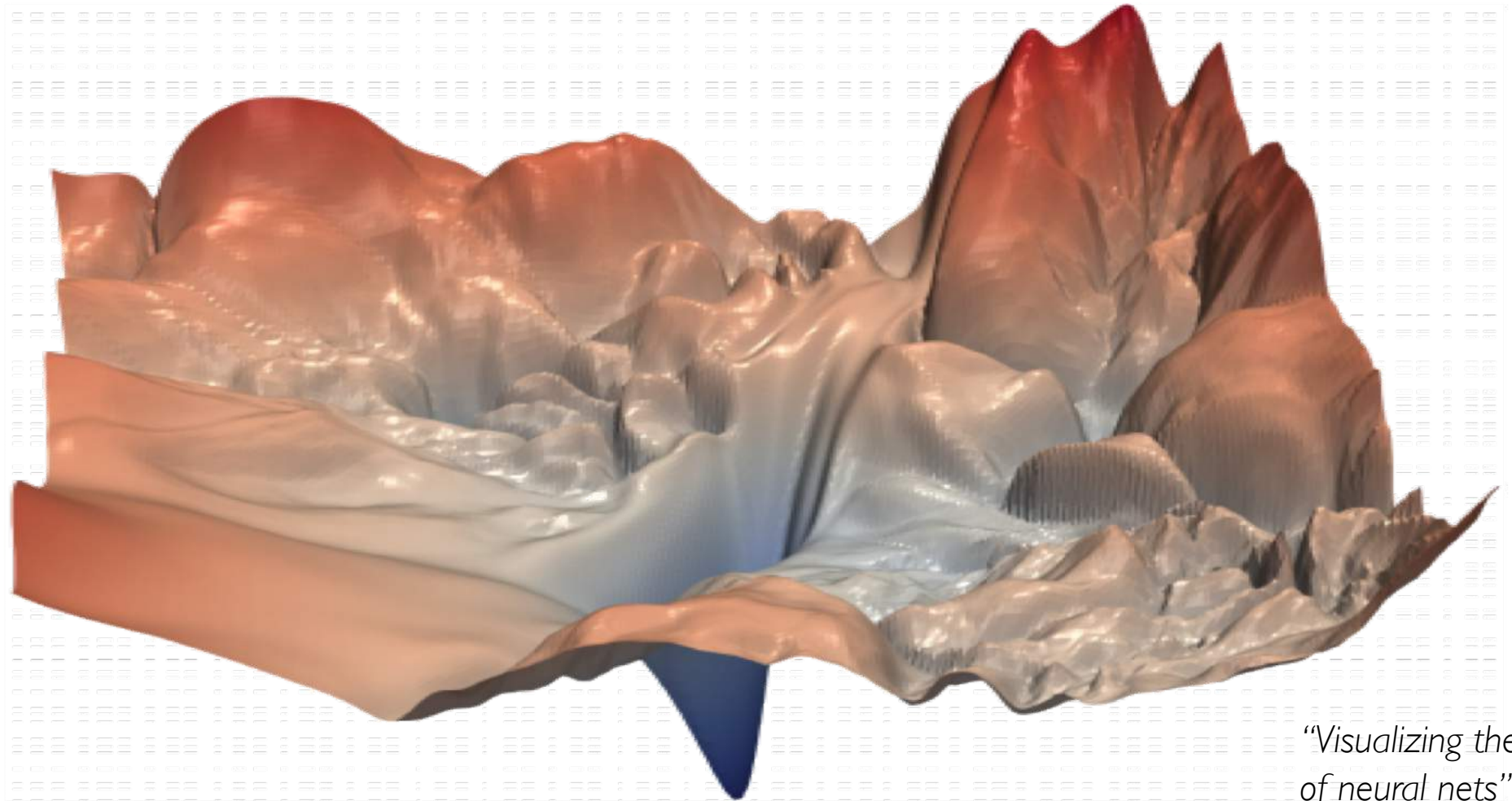


$$\frac{\partial J(W)}{\partial w_1} = \underbrace{\frac{\partial J(W)}{\partial \hat{y}}}_{\text{purple}} * \underbrace{\frac{\partial \hat{y}}{\partial z_1}}_{\text{red}} * \underbrace{\frac{\partial z_1}{\partial w_1}}_{\text{blue}}$$

Repeat this for **every weight in the network** using gradients from later layers

Neural Networks in Practice: Optimization

Training Neural Networks is Difficult



“Visualizing the loss landscape of neural nets”. Dec 2017.

Loss Functions Can Be Difficult to Optimize

Remember:

Optimization through gradient descent

$$\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$$

Loss Functions Can Be Difficult to Optimize

Remember:

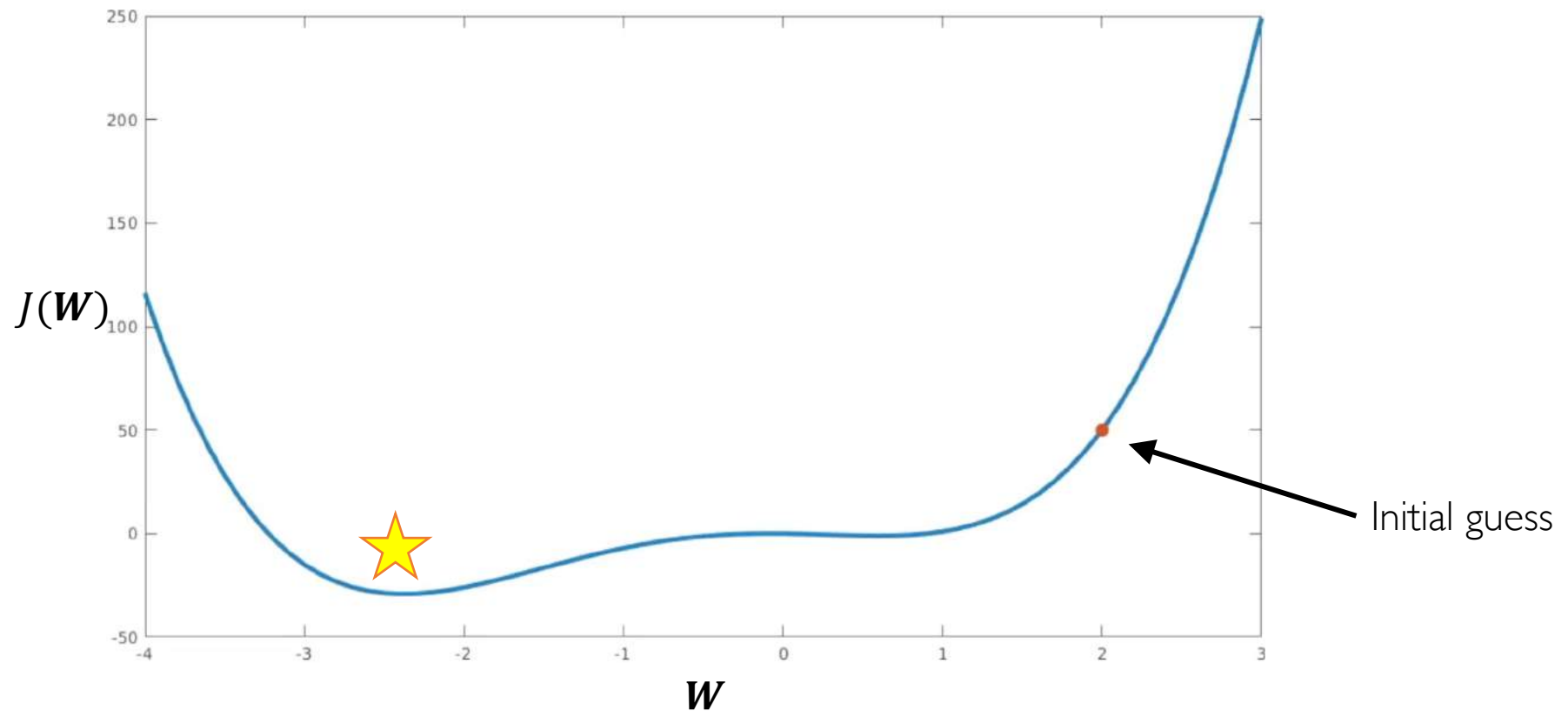
Optimization through gradient descent

$$\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$$

How can we set the
learning rate?

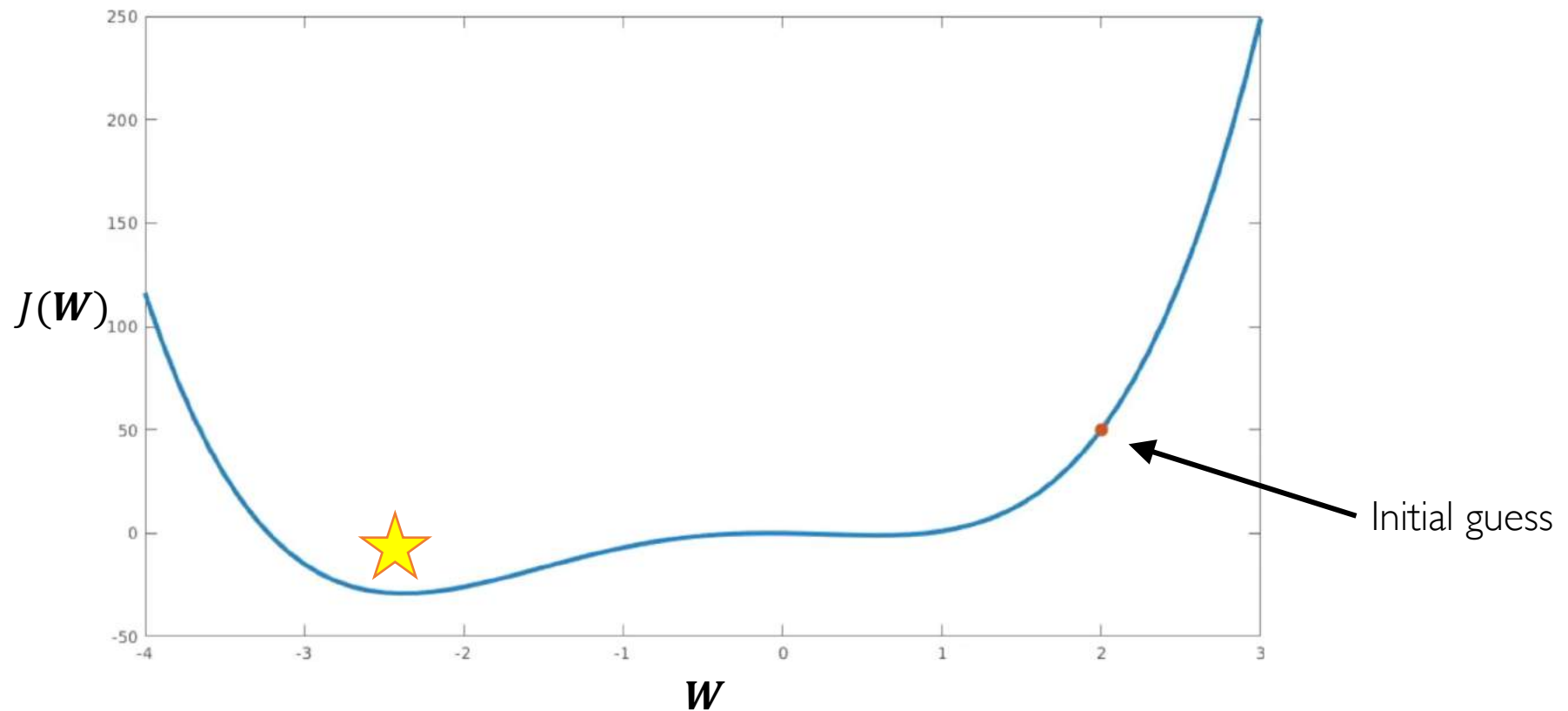
Setting the Learning Rate

Small learning rate converges slowly and gets stuck in false local minima



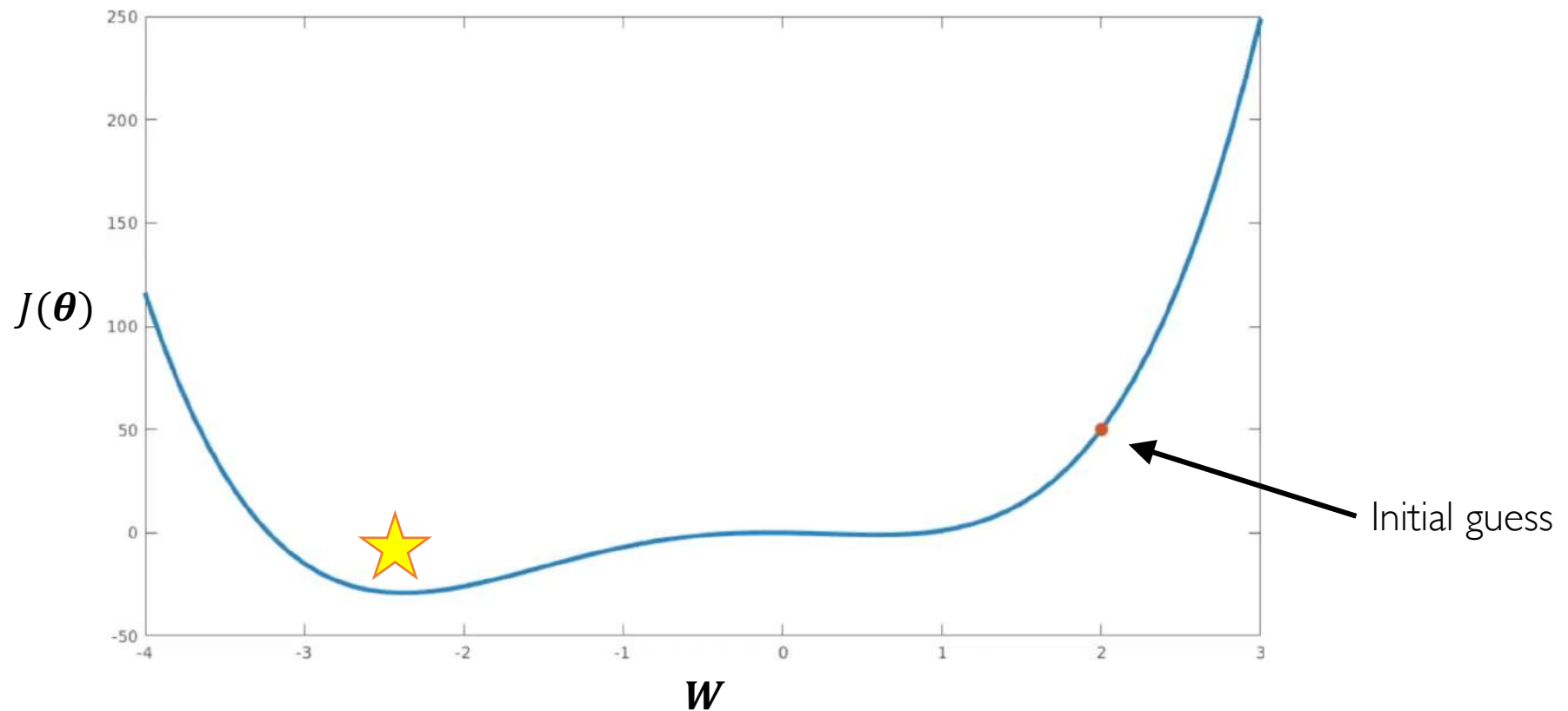
Setting the Learning Rate

Large learning rates overshoot, become unstable and diverge



Setting the Learning Rate

Stable learning rates converge smoothly and avoid local minima



How to deal with this?

Idea 1:

Try lots of different learning rates and see what works “just right”

How to deal with this?

Idea 1:

Try lots of different learning rates and see what works “just right”

Idea 2:

Do something smarter!

Design an adaptive learning rate that “adapts” to the landscape

Adaptive Learning Rates

- Learning rates are no longer fixed
- Can be made larger or smaller depending on:
 - how large gradient is
 - how fast learning is happening
 - size of particular weights
 - etc...

Adaptive Learning Rate Algorithms

- Momentum



`tf.train.MomentumOptimizer`

Qian et al. "On the momentum term in gradient descent learning algorithms." 1999.

- Adagrad



`tf.train.AdagradOptimizer`

Duchi et al. "Adaptive Subgradient Methods for Online Learning and Stochastic Optimization." 2011.

- Adadelata



`tf.train.AdadeltaOptimizer`

Zeiler et al. "ADADELTA: An Adaptive Learning Rate Method." 2012.

- Adam



`tf.train.AdamOptimizer`

Kingma et al. "Adam: A Method for Stochastic Optimization." 2014.

- RMSProp



`tf.train.RMSPropOptimizer`

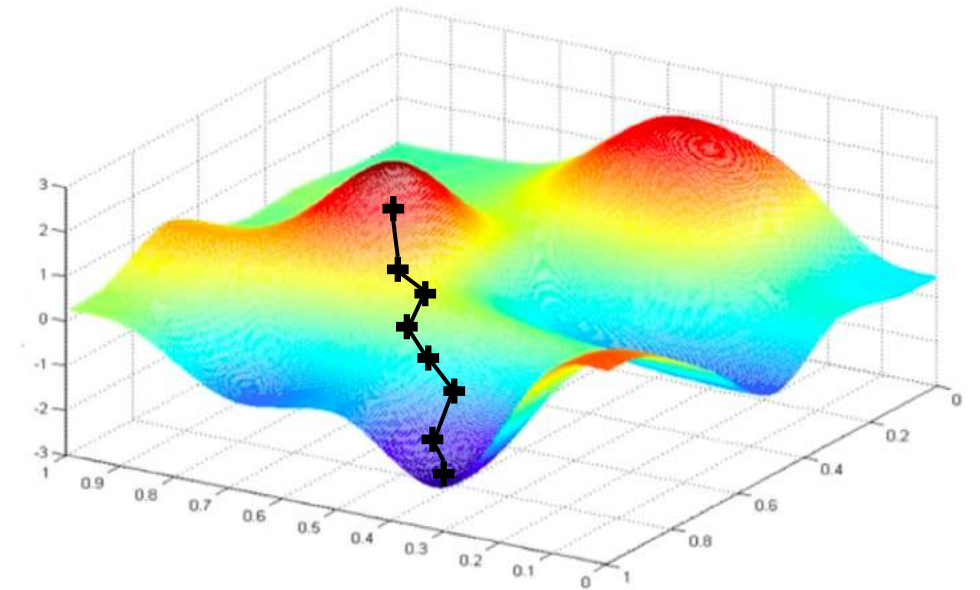
Additional details: <http://runderio/optimizing-gradient-descent/>

Neural Networks in Practice: Mini-batches

Gradient Descent

Algorithm

1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
2. Loop until convergence:
3. Compute gradient, $\frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
4. Update weights, $\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
5. Return weights

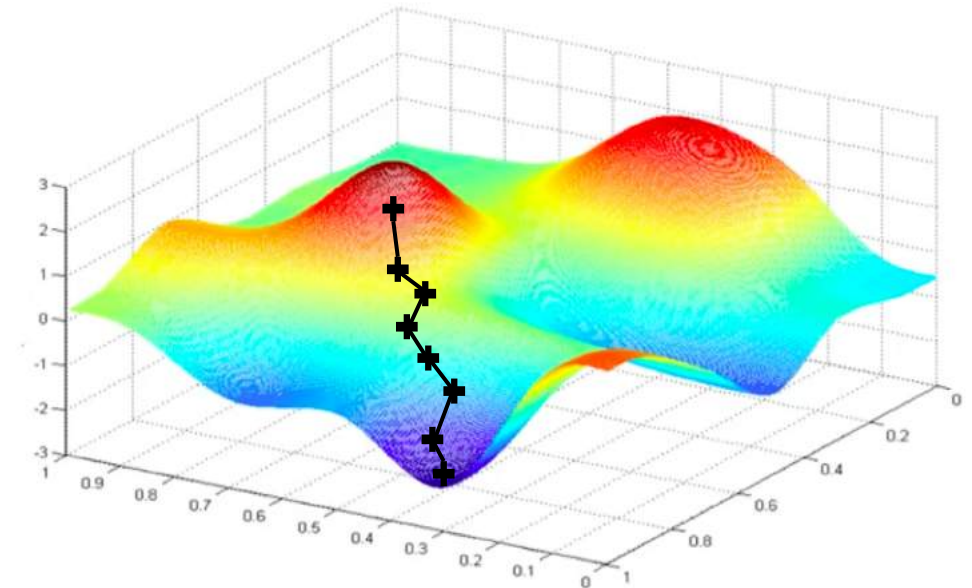


Gradient Descent

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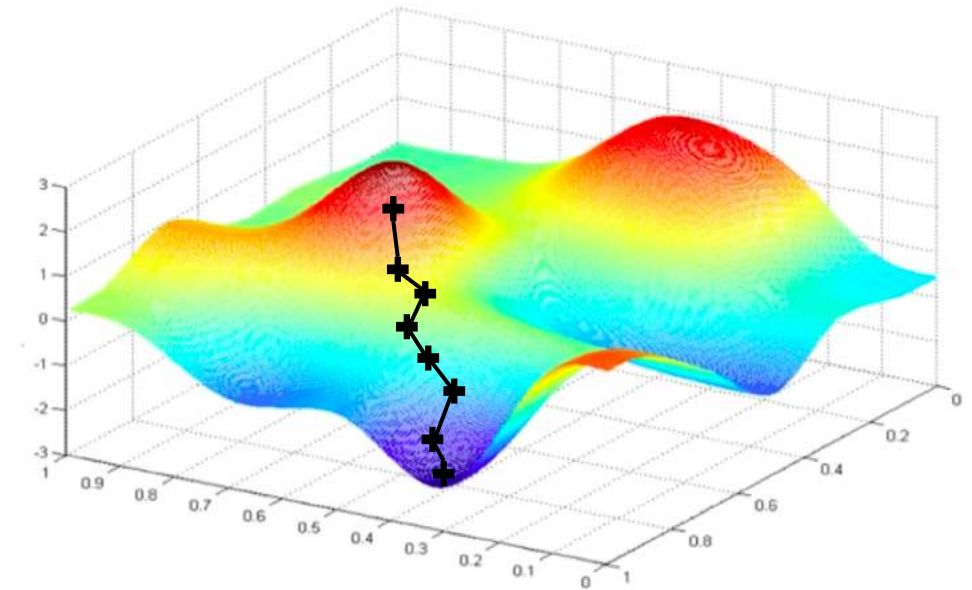
Can be very
computational to
compute!



Stochastic Gradient Descent

Algorithm

1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
2. Loop until convergence:
3. Pick single data point i
4. Compute gradient, $\frac{\partial J_i(\mathbf{W})}{\partial \mathbf{W}}$
5. Update weights, $\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
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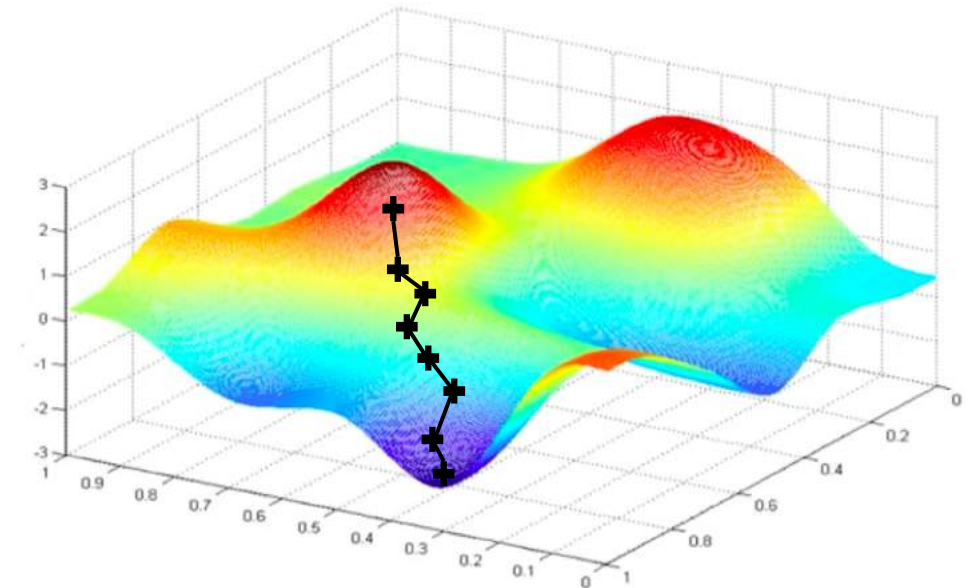


Stochastic Gradient Descent

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6. Return weights

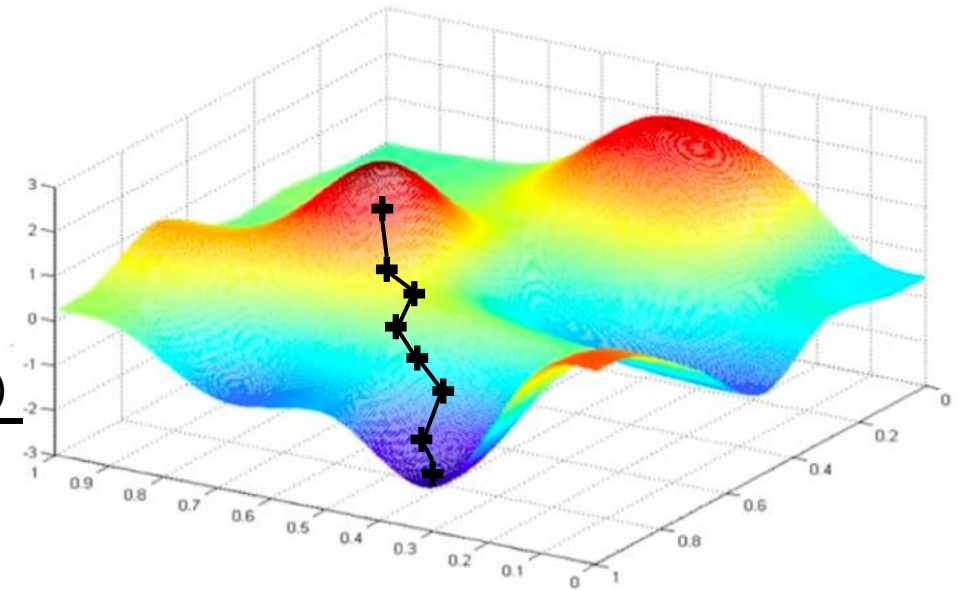
Easy to compute but
very noisy
(stochastic)!



Stochastic Gradient Descent

Algorithm

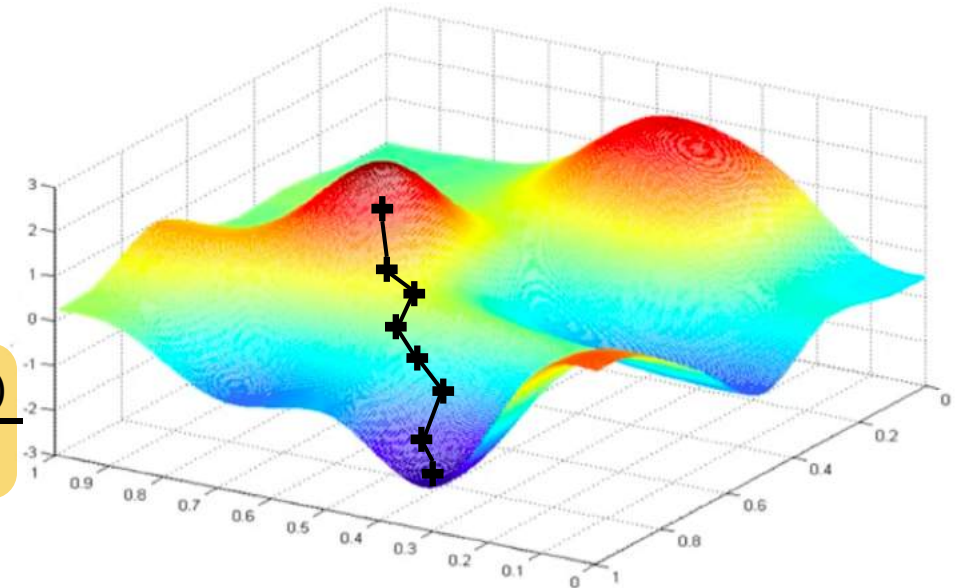
1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
2. Loop until convergence:
3. Pick batch of B data points
4. Compute gradient, $\frac{\partial J(\mathbf{W})}{\partial \mathbf{W}} = \frac{1}{B} \sum_{k=1}^B \frac{\partial J_k(\mathbf{W})}{\partial \mathbf{W}}$
5. Update weights, $\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
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Stochastic Gradient Descent

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Fast to compute and a much better
estimate of the true gradient!

Mini-batches while training

More accurate estimation of gradient

Smoother convergence
Allows for larger learning rates

Mini-batches while training

More accurate estimation of gradient

Smoother convergence

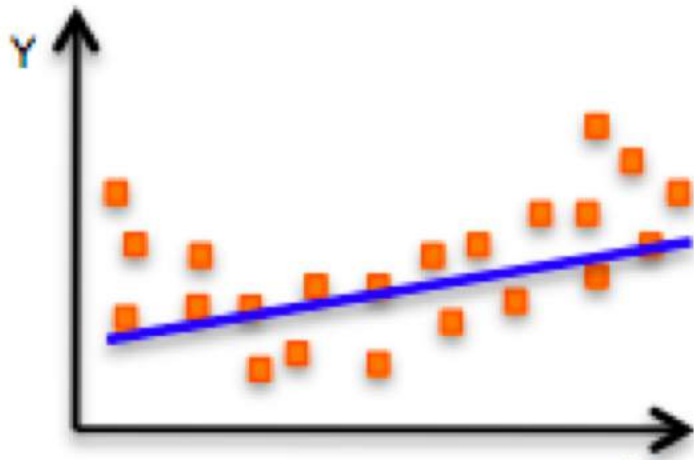
Allows for larger learning rates

Mini-batches lead to fast training!

Can parallelize computation + achieve significant speed increases on GPU's

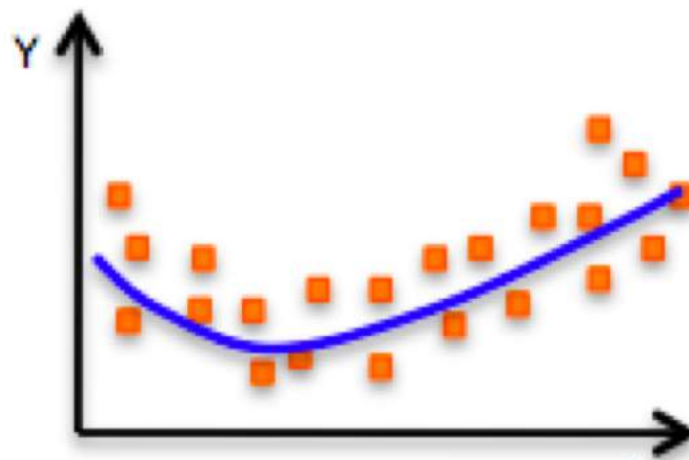
Neural Networks in Practice: Overfitting

The Problem of Overfitting

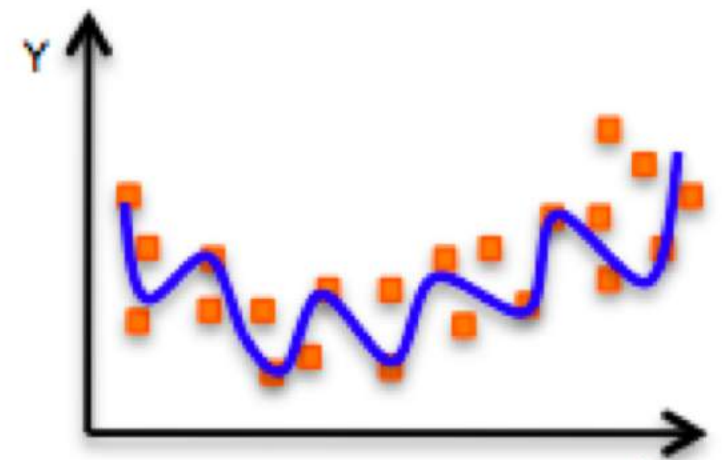


Underfitting

Model does not have capacity to fully learn the data



Ideal fit



Overfitting

Too complex, extra parameters, does not generalize well

Regularization

What is it?

Technique that constrains our optimization problem to discourage complex models

Regularization

What is it?

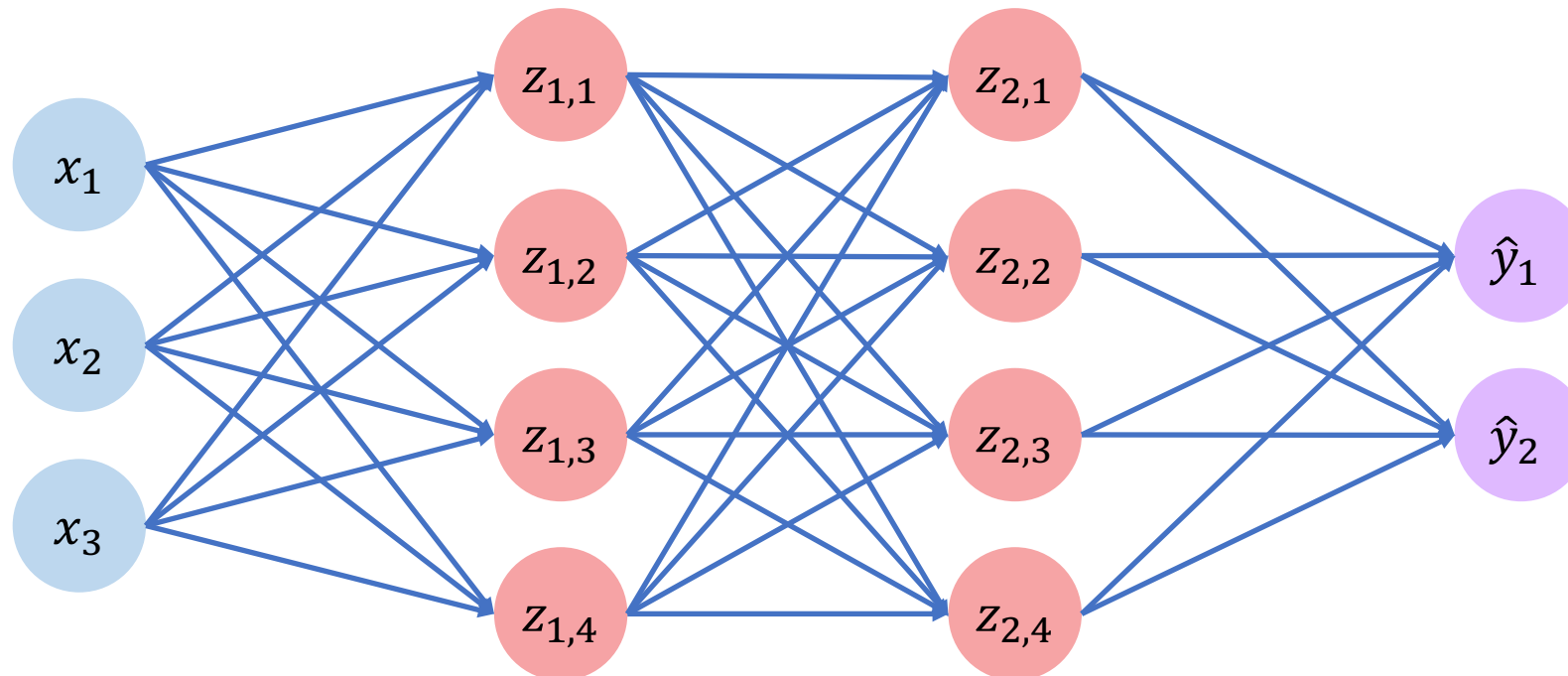
Technique that constrains our optimization problem to discourage complex models

Why do we need it?

Improve generalization of our model on unseen data

Regularization I: Dropout

- During training, randomly set some activations to 0

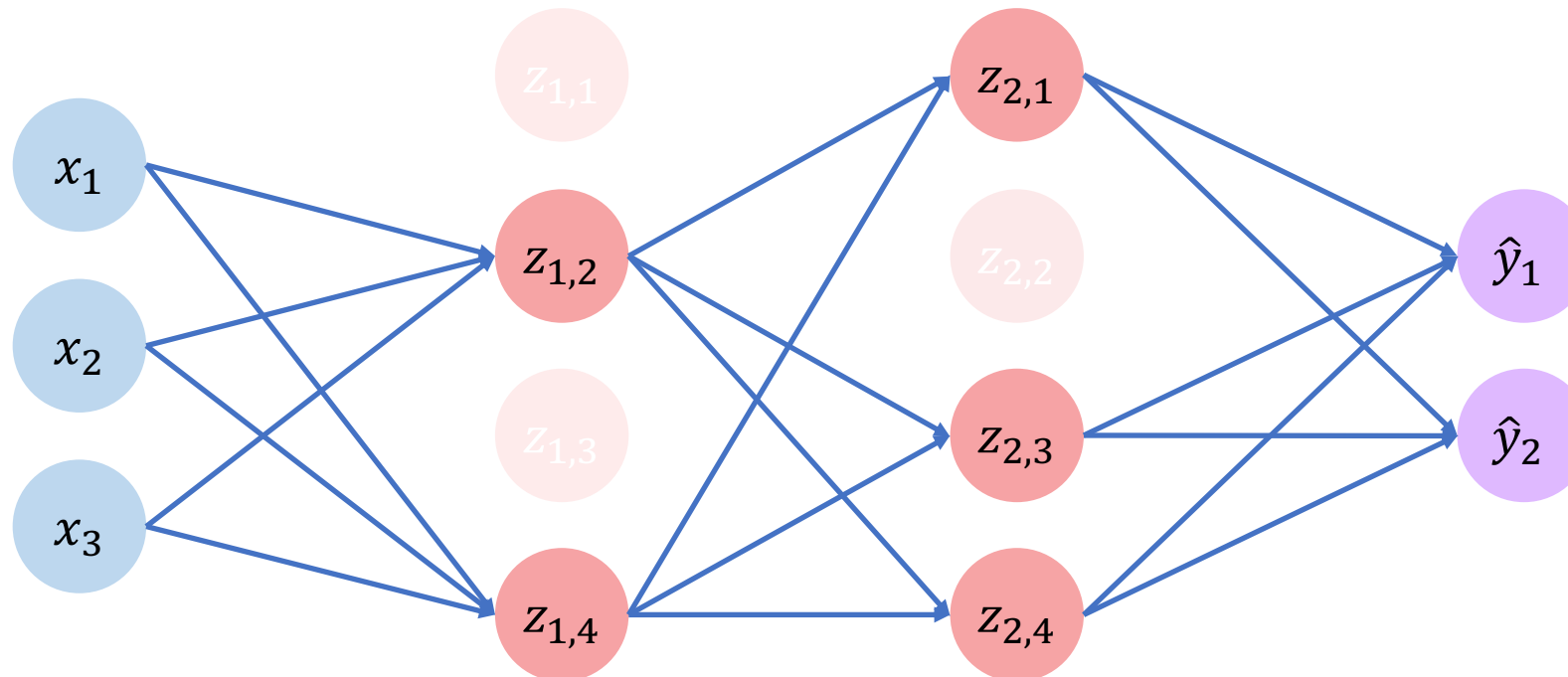


Regularization I: Dropout

- During training, randomly set some activations to 0
 - Typically 'drop' 50% of activations in layer
 - Forces network to not rely on any 1 node



`tf.keras.layers.Dropout (p=0.5)`

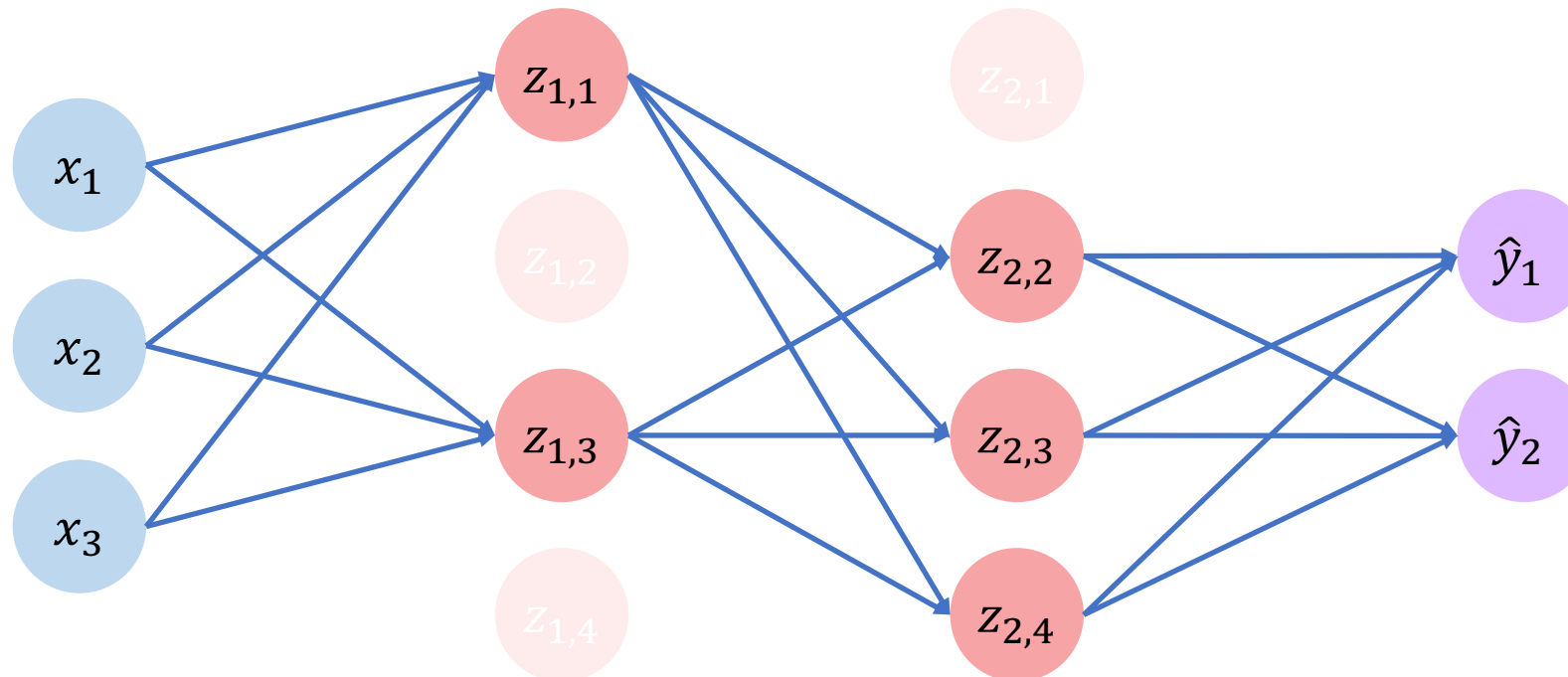


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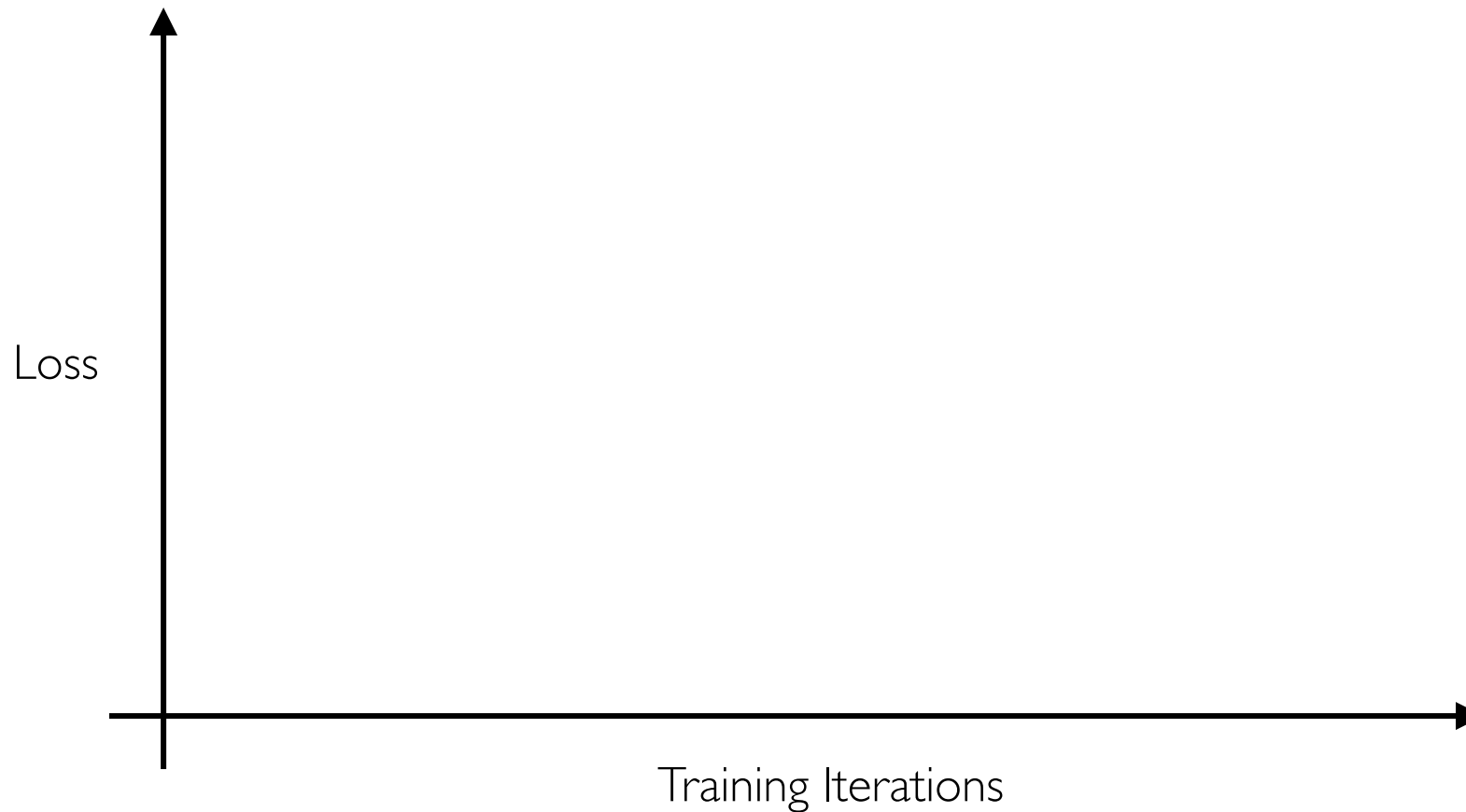


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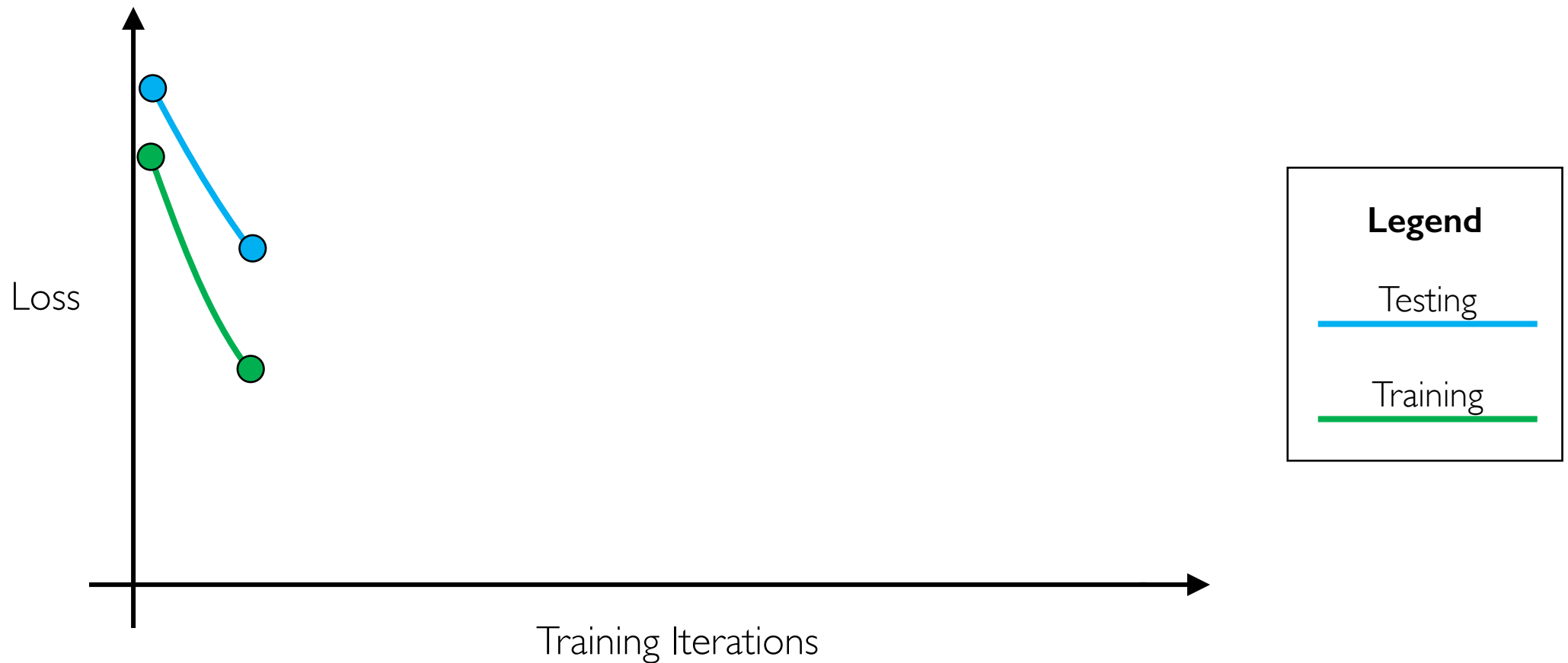
Regularization 2: Early Stopping

- Stop training before we have a chance to overfit



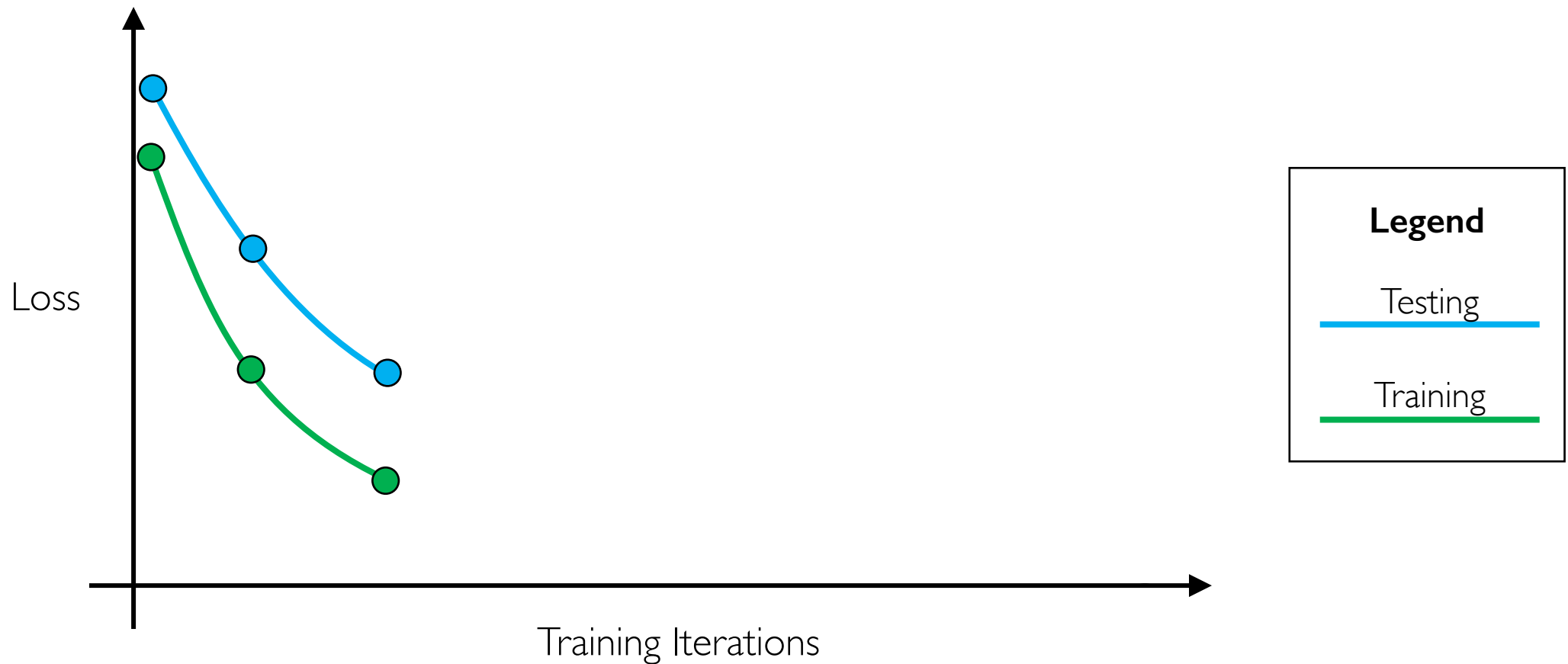
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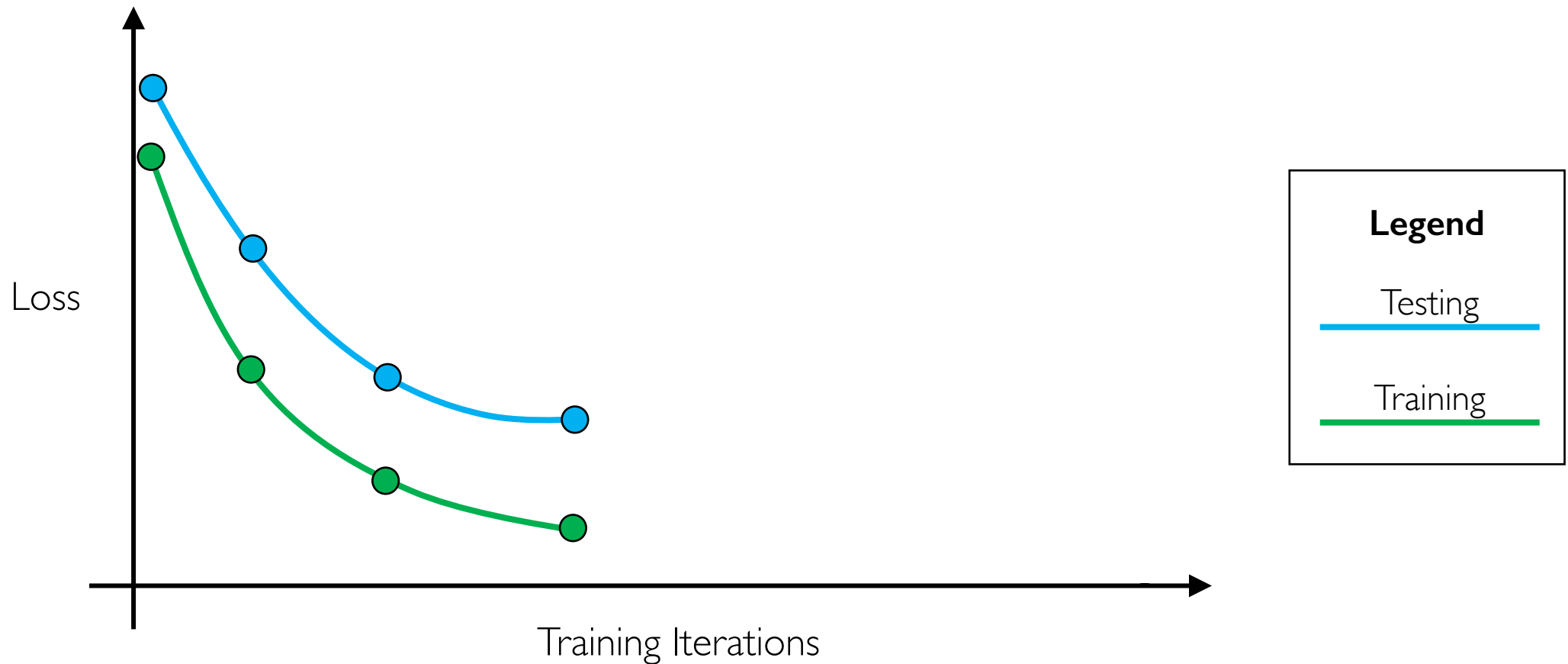
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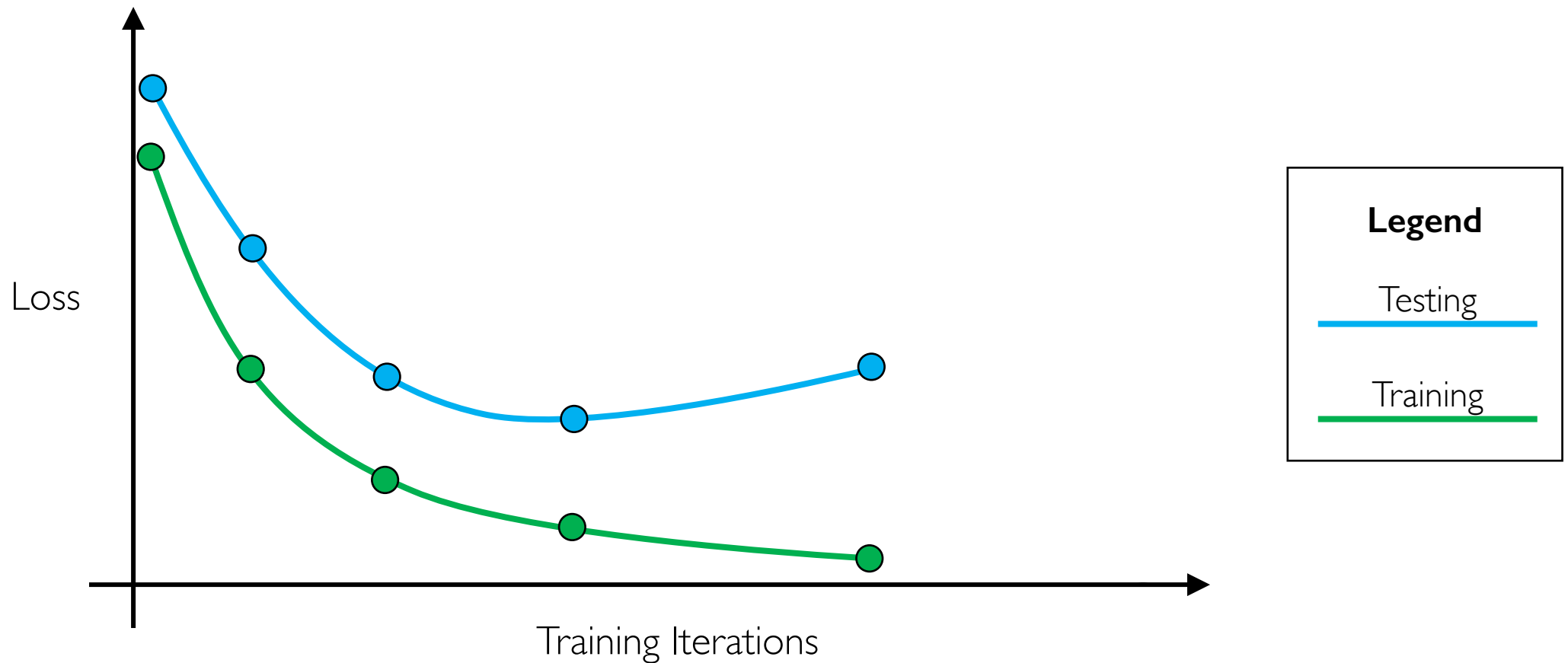
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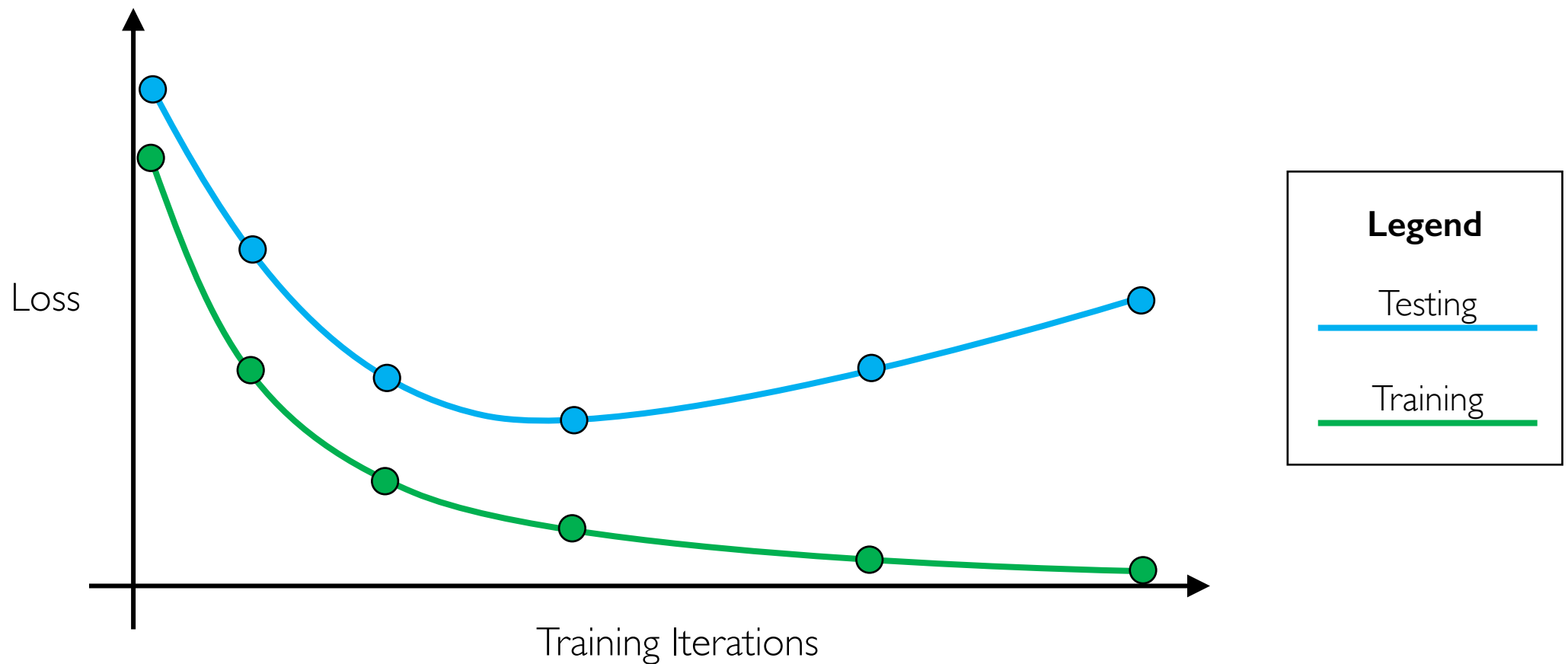
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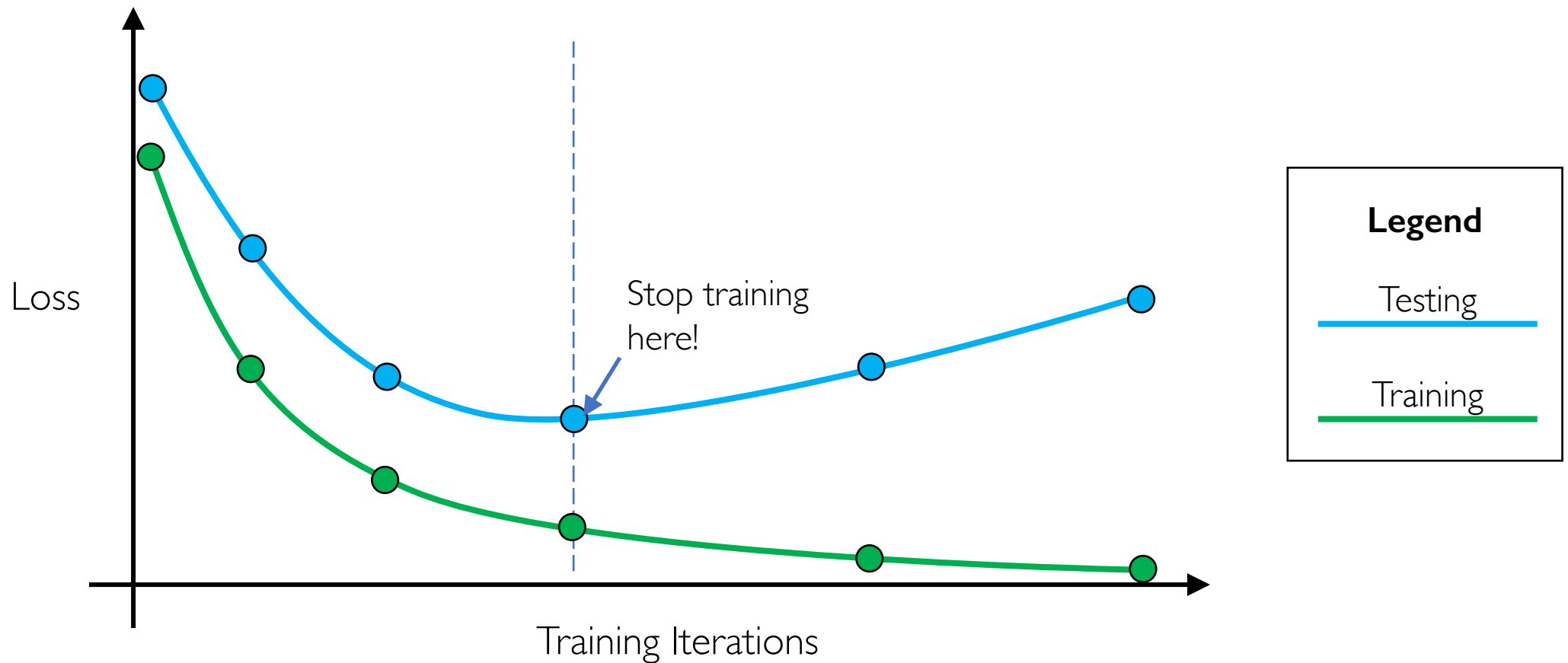
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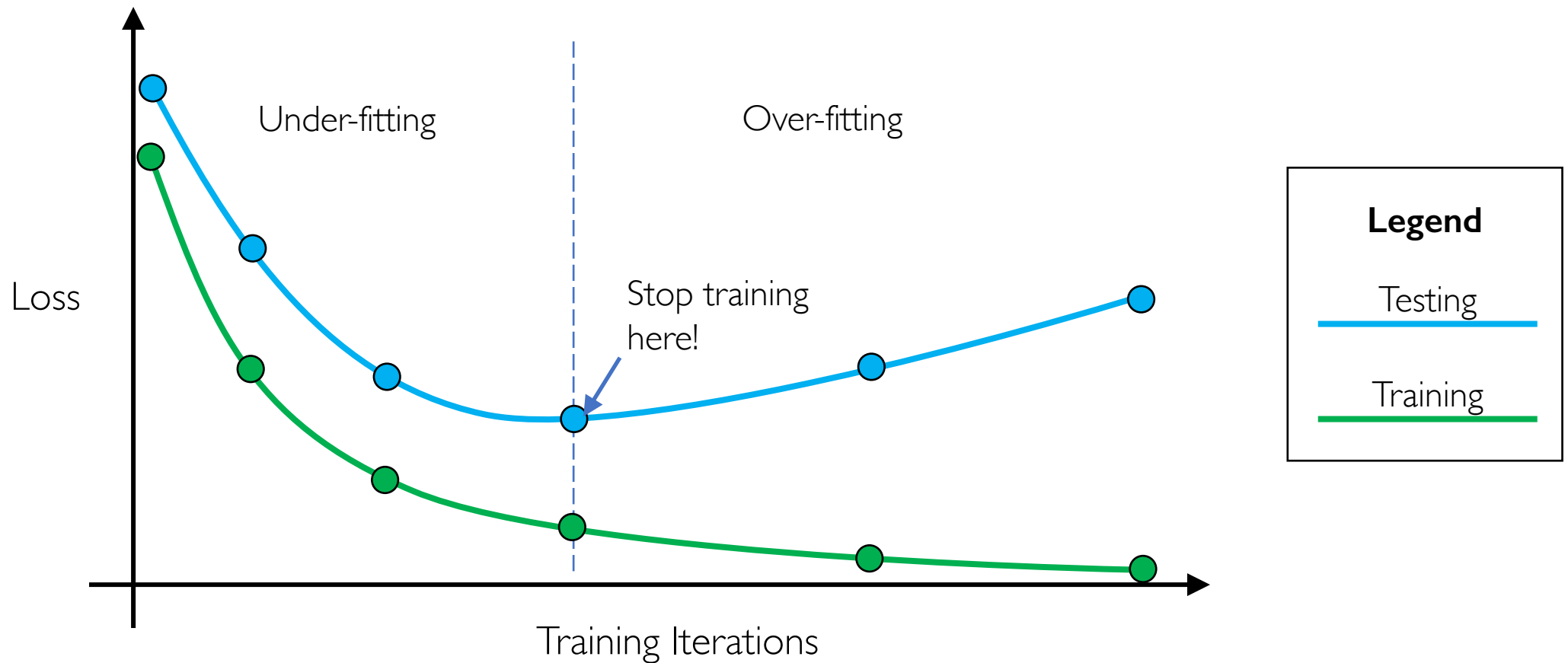
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Regularization 2: Early Stopping

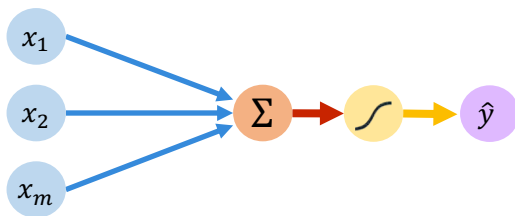
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Core Foundation Review

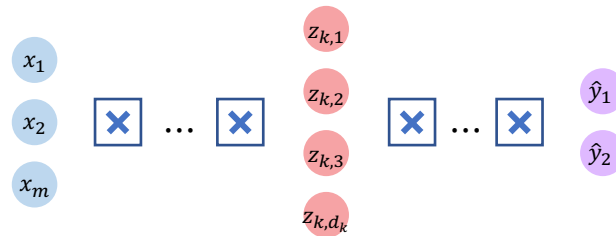
The Perceptron

- Structural building blocks
- Nonlinear activation functions



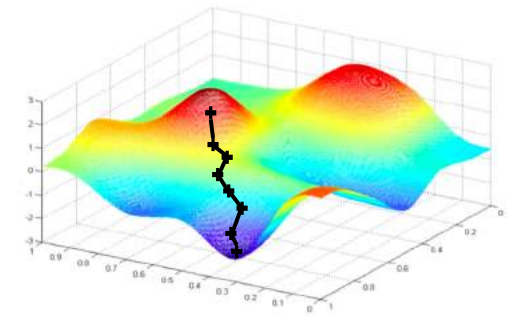
Neural Networks

- Stacking Perceptrons to form neural networks
- Optimization through backpropagation



Training in Practice

- Adaptive learning
- Batching
- Regularization



Questions?