

## Recapitulation from Previous Lectures

## Recap: Parser Implementation

Use of ***recursive descent***:

mutually-recursive methods corresponding to each production of a grammar

For easy implementation, the grammar should be LL(1)

*NULLABLE, FIRST, FOLLOW* allow us know what to do next

We build ***abstract syntax trees*** from the parser input

*Precedence, associativity* of operators: tricky and cumbersome...

## Recap: Example Language

```
// lexing: "A + B * C"  $\Rightarrow$  Ident("A"),Plus,Ident("B"),Times, ...
```

```
enum Token:  
  case Ident(name: String)  
  case OpenParen  
  case CloseParen  
  case Plus  
  case Times
```

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enum Token:  
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  case CloseParen  
  case Plus  
  case Times
```

```
// parsing: ...  $\Rightarrow$  Add( Var("A") , Mult(Var("B"), Var("C"))) )
```

```
enum Expr:  
  case Var(name: String)  
  case Add(lhs: Expr, rhs: Expr)  
  case Mult(lhs: Expr, rhs: Expr)
```

## Recap: Mutable Parser Architecture

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class Parser(ite: Iterator[Token]):  
    var cur: Option[Token] = ite.nextOption
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class Parser(ite: Iterator[Token]):  
  
  var cur: Option[Token] = ite.nextOption  
  def consume: Unit = { cur = ite.nextOption }  
  def skip(tk: Token): Unit =  
    if cur != Some(tk)  
      then fail("expected " + tk + ", found " + cur)  
    consume
```

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    if cur != Some(tk)  
      then fail("expected " + tk + ", found " + cur)  
    consume  
  
  // define parser:  
  def expr = ... atom ...  
  def atom: Expr = cur match  
    case Some(Ident(nme)) ⇒ consume; Var(nme)  
    case OpenParen ⇒ consume;  
      val e = expr; skip(CloseParen); e  
    case _ ⇒ fail("expected atomic expression, found " + cur)
```

## Recap: Implementing Precedence and Associativity Right

**Idea:** make operator-parsing methods return *lists*,  
then *fold* these into ASTs with correct associativity (*foldLeft*, *foldRight*).

```
def atom = ... // as before

def multiplyAtoms: List[Expr] = ??? // parses: * atom * atom * ...

def product: Expr = ??? // parses: atom * atom * ...

def addProducts: List[Expr] = ??? // parses: + prod + prod + ...

def expr: Expr = ??? // parses: prod + prod + ...
```



# Pratt Parsing

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Irritating questions about parsing operators:

- ▶ How to avoid having to manually transform grammars?

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Irritating questions about parsing operators:

- ▶ How to avoid having to manually transform grammars?  
We'd like to separately specify operator precedence/associativity.
- ▶ How to support user-defined operators and parse them correctly?

# Pratt Parsing: Idea

Simplest way of describing precedence and associativity:

operators have *distinct **left** and **right** precedences*

E.g., '+' has (3, 4) and '\*' has (5, 6)

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tokens	A	+	B	*	C
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# Pratt Parsing: Implementation (1)

Defining the precedences:

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def opPrec(opStr: String): (Int, Int)
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def opPrec(opStr: String): (Int, Int) = opStr match
  case "*" => (50, 51)
  case "+" => (30, 31)
  case "=>" => (21, 20)
  case ...
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**Example language.** Tokens and abstract syntax:

```
enum Token { case OpenParen; case CloseParen
  case Ident(name: String); case Oper(name: String) }
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```

**Example language.** Tokens and abstract syntax:

```
enum Token { case OpenParen; case CloseParen
  case Ident(name: String); case Oper(name: String) }

enum Expr { case Var(name: String)
  case Infix(lhs: Expr, op: String, rhs: Expr) }
```

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```
def expr(prec: Int): Expr
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```
def expr(prec: Int): Expr = cur match  
  case Some(Ident(nme))  $\Rightarrow$   
    consume; exprCont(Var(nme), prec)
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## Pratt Parsing: Implementation (2)

```
def expr(prec: Int): Expr = cur match  
  case Some(Ident(nme))  $\Rightarrow$   
    consume; exprCont(Var(nme), prec)  
  case Some(OpenParen)  $\Rightarrow$   
    consume; val res = expr(0); skip(CloseParen)  
    exprCont(res, prec)
```



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def expr(prec: Int): Expr = cur match
  case Some(Ident(nme)) =>
    consume; exprCont(Var(nme), prec)
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    exprCont(res, prec)
  case _ => fail(rest)
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// Having parsed acc, what to do next at this precedence?

```
def exprCont(acc: Expr, prec: Int): Expr
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def expr(prec: Int): Expr = cur match
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    consume; exprCont(Var(nme), prec)
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def exprCont(acc: Expr, prec: Int): Expr = cur match
  case Some(Oper(opStr))
```

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def expr(prec: Int): Expr = cur match
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    consume; exprCont(Var(nme), prec)
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```

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```
def exprCont(acc: Expr, prec: Int): Expr = cur match
  case Some(Oper(opStr)) if opPrec(opStr)._1 > prec =>
```

## Pratt Parsing: Implementation (2)

```
def expr(prec: Int): Expr = cur match  
  case Some(Ident(nme))  $\Rightarrow$   
    consume; exprCont(Var(nme), prec)  
  case Some(OpenParen)  $\Rightarrow$   
    consume; val res = expr(0); skip(CloseParen)  
    exprCont(res, prec)  
  case _  $\Rightarrow$  fail(rest)
```

// Having parsed acc, what to do next at this precedence?

```
def exprCont(acc: Expr, prec: Int): Expr = cur match  
  case Some(Oper(opStr)) if opPrec(opStr)._1 > prec  $\Rightarrow$   
    consume  
    val rhs = expr(opPrec(opStr)._2)  
    exprCont(Infix(acc, opStr, rhs), prec)
```

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```
def expr(prec: Int): Expr = cur match
  case Some(Ident(nme)) =>
    consume; exprCont(Var(nme), prec)
  case Some(OpenParen) =>
    consume; val res = expr(0); skip(CloseParen)
    exprCont(res, prec)
  case _ => fail(rest)
```

// Having parsed acc, what to do next at this precedence?

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def exprCont(acc: Expr, prec: Int): Expr = cur match
  case Some(Oper(opStr)) if opPrec(opStr)._1 > prec =>
    consume
    val rhs = expr(opPrec(opStr)._2)
    exprCont(Infix(acc, opStr, rhs), prec)
  case _ => acc
```

# Pratt Parsing: Example 1

tokens	expression	prec	acc
A,+,B,*,C	expr(0)	0	
+,B,*,C	consume	0	
+,B,*,C	exprCont(Var("A"), 0)	0	"A"
B,*,C	consume	0	"A"
B,*,C	expr(opPrec("+")._2)	4	
*,C	consume	4	
*,C	exprCont(Var("B"), 4)	4	"B"
C	consume	4	"B"
C	expr(opPrec("*")._2)	6	
	consume	6	
	exprCont(Var("C"), 6)	6	"C"
	acc	6	"C"
	exprCont(Infix(acc, "*", rhs), 6)	6	("B" * "C")
	acc	6	("B" * "C")
	exprCont(Infix(acc, "+", rhs), 6)	6	("A" + ("B" * "C"))
	acc	6	("A" + ("B" * "C"))

## Pratt Parsing: Example 2

tokens	expression	prec	acc
A,+,B,+,C	expr(0)	0	
+,B,+,C	consume	0	
+,B,+,C	exprCont(Var("A"), 0)	0	"A"
B,+,C	consume	0	"A"
B,+,C	expr(opPrec("+")._2)	4	
+,C	consume	4	
+,C	exprCont(Var("B"), 4)	4	"B"
+,C	acc	4	"B"
+,C	exprCont(Infix(acc, "+", rhs), 0)	0	("A" + "B")
C	consume	0	"B"
C	expr(opPrec("+")._2)	4	
	consume	4	
	exprCont(Var("C"), 0)	4	"C"
	acc	4	"C"
	exprCont(Infix(acc, "+", rhs), prec)	0	((("A" + "B") + "C")
	acc	0	((("A" + "B") + "C")



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Examples: Haskell, Coq

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Examples: Haskell, Coq

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While Haskell's approach is more flexible,

it makes ***reading*** code for people unfamiliar with your operators *a lot **harder***

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(all letters)

|  
^

&

= !

< >

:

+ -

\* / %

(all other special characters)

Scala operators are **right-associative** only when they *end with a colon* ':'

Q: What to do when mixing associativity with same precedence?

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Q: What to do when mixing associativity with same precedence?  $\Rightarrow$  report error

## Example Character Precedence Table

```
val prec: Map[Char, Int] = ""  
=  
@  
:  
|  
^  
&  
!  
< >  
+ -  
* / %  
"".split('\n').zipWithIndex.flatMap { (cs, i) =>  
  cs.filterNot(_.isWhitespace).map(_ -> i)  
}.toMap.withDefaultValue(Int.MaxValue) // prec('~') = 2147483647
```

⇒ returns Map('=' -> 0, '@' -> 1, ... , '<' -> 7, '>' -> 7, ... )



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*why not use the **first** and **last** characters*

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“ $a + b \mid > f \mid > g$ ” *parses as* “ $((a + b) \mid > f) \mid > g$ ”

Makes *symmetric operators* like  $\mid >$  and  $< \mid$  behave *symmetrically*

Determines *associativity* naturally:

“ $S \rightarrow T \rightarrow U$ ” *parses as* “ $S \rightarrow (T \rightarrow U)$ ”

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“S -> T -> U” *parses as* “S -> (T -> U)”

```
def opPrec(opStr: String): (Int, Int) =  
    (prec(opStr.head), prec(opStr.last))
```

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A more recent ***alternative*** to *context-free grammars* (CFG)

**Parsing-Expression Grammars** remove ambiguities through ***biased choice***:

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which tries to parse  $Y$  ***only if parsing  $X$  fails!***

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Example:

$$E \rightarrow F + E / F$$

$$F \rightarrow T * F / T$$

$$T \rightarrow D^* / '(' E ')'$$

$$D \rightarrow 0 / 1 / 2 / 3 / 4 / 5 / 6 / 7 / 8 / 9$$



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CFGs: more natural algebraic properties (e.g., disjunctions are commut. and assoc.)

Composition of PEGs is trickier & can be confusing

However, PEGs can be more natural for programmers (parsing follows grammar)  
especially compared with advanced bottom up parsing algorithms like LR(1)

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(Becket and Somogyi, 2008; Grimm, 2004).

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(Becket and Somogyi, 2008; Grimm, 2004).

Some approaches can also handle left recursion (with worse complexity)

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## Examples

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Haskell libraries: Parsec, ...

etc.

**However**, the library you will use in this project, **Scallion**,

is based on **LL(1)** parsing (internally using derivatives), *not* Packrat