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$$T(n) = \begin{cases} 1 & \text{if } n = 0 \\ 1 + \sum_{i=0}^{n-1} T(i) & \text{if } n > 0 \end{cases}$$

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Proof:

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