

**Exam 2:** Learning Objectives under Evaluation

Exam 2 will cover:		
LOs 01.00 – 09.00 (Exam 1)	10.00 Cumulative Distribution Plots	12.00 Regression
	11.00 User-Defined Functions	13.00 Function Discovery

## 10.00 Create and interpret cumulative distribution plots

Learning Objective	Evidence
10.01 Compute the relative fractional values given the bin intervals	<p>Call the <code>histogramRight</code> function (with the correct input arguments) to generate the histogram properties</p> <p>Determine the frequencies for each bin in a right-bin inclusive histogram</p> <p>Determine the total number of data points accounted for in the overall histogram</p> <p>Calculate the fractional values by dividing the frequency in each bin by the total number of data points accounted for in the overall histogram</p>
10.02 Compute cumulative fractional values given the bin intervals	<p>Correct syntax for <code>cumsum</code> function</p> <p>Perform the cumulative sum to get vector of cumulative fractional values</p> <p>Start the cumulative sum vector at 0</p>
10.03 Create a cumulative distribution plot using the companion histogram's bin right edges	<p>Correct syntax for the plot command: <code>plot(x, y, 'line/marker formatting')</code></p> <p>Independent variable (x) is the bin edge values from a right-bin inclusive histogram</p> <p>Dependent variable (y) is the cumulative fractional values corresponding to the right-bin inclusive histogram</p> <p>Correct use of data markers and lines: data markers (for the bin edges) with an overlaid line (for the model)</p>
10.04 Format a cumulative distribution plot for technical presentation	<p>Correct syntax for title</p> <p>Correct syntax for xlabel</p> <p>Correct syntax for ylabel</p> <p>Descriptive title that references the problem context and x-variable data</p> <p>Clear x-axis label with units</p> <p>Clear y-axis label that is cumulative fractional value</p> <p>y-axis scale range of 0 to 1</p> <p>x-axis scales that match each other, when using subplots to compare data</p>

**Exam 2:** Learning Objectives under Evaluation

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	<p>Color and marker/line style(s) that are as specified or distinctive (when multiple data sets)</p> <p>Proper formatting of a legend, when multiple data sets and/or models</p> <p>Gridlines</p>
10.05 Determine the likelihood of event occurrences using a cumulative distribution plot	<p>Determine the likelihood of an occurrence of a value:</p> <p>less than specified criteria</p> <p>greater than specified criteria</p> <p>between specified criteria reading the fractional value for given data point</p> <p>Clear explanation of how the likelihood is determined</p>
10.06 Estimate and/or describe the process for determining the characteristics of the underlying data set from a cumulative distribution plot	<p>Estimate the median of the data by reading the CDP at 0.5 cumulative fractional value (within 2% of solution answer)</p> <p>Estimate the range of the data by reading the CDP at 0 and 1 cumulative fractional values (within 2% of solution answer)</p> <p>Clear description of a process for determining the median</p> <p>Clear description of a process for determining the range</p>
10.07 Determine the data distribution type from the shape of a cumulative distribution plot	<p>Identify the shape of the distribution (uniform, unimodal, bimodal, normal, etc)</p> <p>Justify shape identification</p> <p>Identify the skew of the distribution (positive, negative, undefined, etc)</p> <p>Justify skew identification</p>
10.08 Draw inferences from the analysis of data with evidence from a cumulative distribution	<p>For a given data set and a problem context, appropriately use a cumulative distribution as described in 10.05 – 10.07 to draw conclusions.</p>

**Exam 2:** Learning Objectives under Evaluation

## 11.00 Create and execute a user-defined function

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11.01 Describe at least two reasons why MATLAB user-defined functions as opposed to scripts are used	<p>Recognition that UDFs enable one to create an easily re-usable piece of code</p> <p>Recognition that UDFs can be shared with others without them having to know what variables were used by the author</p> <p>Recognition that UDFs enable a larger program to be broken into smaller parts that can be more easily tested &amp; debugged</p> <p>Recognition that UDFs allow team members to work on separate parts of a larger program with less coordination</p>
11.02 Describe three ways a user-defined function is different from a script	<p>Recognition that the first line of a UDF is the function definition line; the first line of a script can be any executable line of code</p> <p>Recognition that the variables created in a UDF are not available in the Workspace; all variables created in script are available in the Workspace</p> <p>Recognition that a UDF must be called from the command line or from within another function or script; the green run button will not work for a UDF that has input arguments</p>
11.03 Create a user-defined function that adheres to programming standards	<p>Help lines contain input and output argument definitions, with units as appropriate</p> <p>Help lines contain concise description of the program</p> <p>Help lines show the call to the function</p> <p>Complete programmer and contributor information in the header (names and emails)</p> <p>Complete problem details including assignment number, problem number</p> <p>Code items are in the correct section (e.g. Initialization, Calculations, ...)</p> <p>Computed values are assigned to variables</p> <p>Code blocks have explanatory comments</p> <p>Variables have commented definitions and units</p> <p>Minimal use of hardcoding</p>
11.04 Construct an appropriate function definition line	<p>Correct syntax for a function:</p> <ul style="list-style-type: none"> <li><code>function</code> [output1,...,outputN] = function_name(input1,...,inputM)</li> <li>Function starts with the keyword <code>function</code></li> <li>Order is output arguments, equal sign, function name, input arguments</li> </ul>

**Exam 2:** Learning Objectives under Evaluation

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	<ul style="list-style-type: none"> <li>• Functions with no inputs have no input list; use of ( ) is optional</li> <li>• Functions with no output arguments have no output list and no equal sign</li> <li>• Multiple output arguments are listed inside square brackets, separated by spaces or commas</li> <li>• Multiple input arguments are listed inside parentheses and are comma-separated</li> </ul> <p>Function definition line is the first line in the function file (above help lines)</p> <p>Function file name matches the function name in the definition line</p> <p>Input arguments must meet the problem specifications (with no extraneous input arguments) or be appropriate for the purpose of the function</p> <p>Output arguments must meet the problem specifications or be appropriate for the purpose of the function</p> <p>Output arguments must be assigned within the function code</p>
11.05 Match the variables names used in the function definition line to those used in the function code	<p>All input arguments are used in the code</p> <p>All input arguments necessary to perform computations are provided in the function definition</p> <p>Input arguments are not overwritten (e.g. by hardcoded values) before being used in calculations</p> <p>All output arguments are appropriately assigned in the function code</p>
11.06 Execute a user-defined function	<p>Correct syntax to call a function:</p> <ul style="list-style-type: none"> <li>• <code>[output1,...,outputN] = function_name(input1,...,inputM)</code></li> <li>• Call does not contain keyword <code>function</code></li> <li>• Order is output arguments, equal sign, function name, input arguments, with output arguments and equal sign being optional for a no-output function</li> <li>• Functions with no inputs have no input list; use of ( ) is optional</li> <li>• Functions with no output arguments have no output list and no equal sign</li> <li>• Multiple output arguments are listed inside square brackets, separated by spaces or commas</li> </ul>

**Exam 2:** Learning Objectives under Evaluation

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	<ul style="list-style-type: none"> <li>Multiple input arguments are listed inside parentheses and are comma-separated</li> </ul> <p>Calls the correct function filename</p> <p>Number of input arguments matches the number required by the function</p> <p>Input argument list corresponds to the function's expected inputs</p> <p>Number of output argument(s) matches the number required by the function</p> <p>Output argument list corresponds to the function's expected outputs</p>
11.07 Create test cases to evaluate a user-defined function	<p>Running the UDF with a variety of reasonable values for each input argument to ensure no computation or execution errors occur</p> <p>Running the UDF with both scalar and array input arguments to ensure no errors occur</p>
11.08 Convert a script to a user-defined function	<p>First line of code is a function definition line</p> <p>Replacement of script header with function header</p> <p>Removal of hardcoded variable assignments for all variables in the input argument list</p>
11.09 Track the passing of information to and from a user-defined function	<p>Being able to take given input argument values to one UDF and manually track the value of all computed and passed output arguments and input arguments through a series of UDFs linked through function calls</p>
11.10 Break a problem into a series of sub-functions	<p>Being able to take a complex task and break it into a series of unique UDFs that are each purposeful and easy to test and debug</p>
11.11 Coordinate the passing of information between functions	<p>Call to a user-defined function occurs in the proper function or script</p> <p>Variables passed into a user-defined function are defined prior to calling the user-defined function</p> <p>User-defined functions are called in the order necessary to complete the coding task</p> <p>No use of global variables (to circumvent proper passing of information through function calls)</p>

**Exam 2:** Learning Objectives under Evaluation

## 12.00 Perform linear regression

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13.01 Estimate $\log_{10}x$ for any $x$	<p>Sketch a pair of linear and log number lines representing a range of one order of magnitude</p> <p>Label the tick marks on the pair of linear and log number lines</p> <p>Place <math>x</math> on the log number line</p> <p>Read across from the log number line to the linear line to estimate the <math>\log_{10}x</math> value to the nearest tens decimal place</p>
13.02 Identify function types from graphs of bivariate data, specifically linear, power, exponential, and logarithmic	<p>Use intercept, behavior at or near the origin, and asymptotic behavior to identify the function type</p> <ul style="list-style-type: none"> <li>Linear: <math>y = mx + b</math>: has a <math>y</math> intercept and data falls approximately on a line</li> <li>Exponential: <math>y = b10^{mx}</math>: has a <math>y</math> intercept <ul style="list-style-type: none"> <li>for <math>m &gt; 0</math>, as <math>x</math> increases, <math>y</math> increases (concave up)</li> <li>for <math>m &lt; 0</math>, as <math>x</math> increases, <math>y</math> decreases and asymptotically approaches <math>y = 0</math></li> </ul> </li> <li>Power: <math>y = b x^m</math> <ul style="list-style-type: none"> <li>for <math>m &gt; 0</math>, passes through the origin, as <math>x</math> increases, <math>y</math> increases (concave up for <math>m &gt; 1</math>, concave down for <math>0 &lt; m &lt; 1</math>)</li> <li>for <math>m &lt; 0</math>, there is no intercept; as <math>x</math> approaches 0, <math>y</math> asymptotically approaches <math>x = 0</math>; and as <math>x</math> increases - <math>y</math> asymptotically approaches <math>y = 0</math></li> </ul> </li> <li>Logarithmic: <math>x = b10^{my}</math>: has an <math>x</math> intercept; as <math>x</math> approaches 0, <math>y</math> approaches negative infinity; as <math>x</math> increases, <math>y</math> increases (concave down)</li> </ul>
13.03 Confirm function identification using a combination of linear and log transformations of the independent and dependent data variables	<p>Identify the independent and dependent data variables that need transformation (or log scaling) to linearize the data</p> <p>Identify the function type that correspond to the transformations (or log scaling) needed to linearize the data</p>
13.04 Create plots with linear and/or log axis scales (by-hand)	<p>Plots of data using different axis scales to show relationships useful for function discovery</p> <ul style="list-style-type: none"> <li>Linear scale: linear scale on <math>x</math>-axis, linear scale on <math>y</math>-axis</li> <li>Log-linear scale: log scale on <math>x</math>-axis, linear scale on <math>y</math>-axis</li> <li>Linear-log scale: linear scale on <math>x</math>-axis, log scale on <math>y</math>-axis</li> <li>Log-log scale: log scale on <math>x</math>-axis, log scale on <math>y</math>-axis</li> </ul>

**Exam 2:** Learning Objectives under Evaluation

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	<p>Data points are plotted correctly on any given graph</p> <p>Function discovery plots display original independent and dependent data (i.e., non-linearized data) whose relationship is being examined</p> <p>Each plot has x- and y-axis labels that reference the data in the plot and do not reference the type of scale used</p>
13.05 Create plots with linear and/or log axis scales (Excel)	<p>Plots of data using different axis scales to show relationships useful for function discovery</p> <ul style="list-style-type: none"> <li>• Linear scale: linear scale on x-axis, linear scale on y-axis</li> <li>• Log-linear scale: log scale on x-axis, linear scale on y-axis</li> <li>• Linear-log scale: linear scale on x-axis, log scale on y-axis</li> <li>• Log-log scale: log scale on x-axis, log scale on y-axis</li> </ul> <p>Function discovery plots display original independent and dependent data (i.e., non-linearized data) whose relationship is being examined</p> <p>Each plot has x- and y-axis labels that reference the data in the plot and do not reference the type of scale used</p> <p>Show the minor gridlines on log scaled axes</p> <p>Manage the horizontal axis crosses option so that the x-axis tick labels are at the bottom of the plot</p> <p>Manage the decimal places shown on the x and y axis tick marks</p>
13.06 Create plots with linear and/or log axis scales (MATLAB)	<p>Plots of data with different axis scales to show relationships useful for function discovery are generated using the correct syntax for plotting on different scales</p> <ul style="list-style-type: none"> <li>• Linear scale plot: plot command used for linear scale on x-axis, linear scale on y-axis</li> <li>• Log-linear scale plot: semilogx command used for log scale on x-axis, linear scale on y-axis</li> <li>• Linear-log scale plot: semilogy command used for linear scale on x-axis, log scale on y-axis</li> <li>• Log-log scale plot: loglog command used for log scale on x-axis, log scale on y-axis</li> </ul> <p>Function discovery plots display original independent and dependent data (i.e., non-linearized data) whose relationship is being examined</p> <p>Each plot has x- and y-axis labels that reference the data in the plot and do not reference the type of scale used</p>

**Exam 2:** Learning Objectives under Evaluation

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13.07 Linearize and plot data appropriately	<p>Linearize the independent variable data correctly based on the diagnosed function type</p> <ul style="list-style-type: none"> <li>• Linear: no change to data</li> <li>• Logarithmic: log of independent data</li> <li>• Exponential: no change to independent data</li> <li>• Power: log of independent data</li> </ul> <p>Linearize the dependent variable data correctly based on the diagnosed function type</p> <ul style="list-style-type: none"> <li>• Linear: no change to data</li> <li>• Logarithmic: no change to dependent data</li> <li>• Exponential: log of dependent data</li> <li>• Power: log of dependent data</li> </ul> <p>Axes labels (description and units) are correct based on the plotted data</p>
13.08 Linearize a power, exponential, and logarithmic functions	<p>Take the log of both sides of the general form and arrange the terms in the linear form of the equation: <math>Y = MX + B</math></p> <ul style="list-style-type: none"> <li>• Linear: <math>y = mx + b</math> - the linear and general forms are the same</li> <li>• Exponential: <math>y = b10^{mx}</math> becomes <math>\log(y) = mx + \log(b)</math></li> <li>• Power: <math>y = bx^m</math> becomes <math>\log(y) = m\log(x) + \log(b)</math></li> <li>• Logarithmic: <math>x = b10^{my}</math> becomes <math>y = (1/m)\log(x) - (1/m)\log(b)</math></li> </ul>
13.09 Determine the linear and general forms of the equations for linear, power, exponential, and logarithmic functions	<p>Identify slope (M) and intercept (B) coefficients for the best-fit linear model of the linearized data</p> <ul style="list-style-type: none"> <li>• Linear: use x and y data</li> <li>• Exponential: use x and <math>\log(y)</math> transformed data</li> <li>• Power: use <math>\log(x)</math> and <math>\log(y)</math> transformed data</li> <li>• Logarithmic: use <math>\log(x)</math> and y transformed data</li> </ul> <p>Place M and B correctly within the linear form of the equation</p> <p>Correctly determine the general form constant m from the linear form slope M</p> <ul style="list-style-type: none"> <li>• Linear: <math>M = m</math></li> <li>• Exponential: <math>M = m</math></li> <li>• Power: <math>M = m</math></li> <li>• Logarithmic: <math>M = 1/m</math></li> </ul> <p>Correctly determine the general form constant b from the linear form intercept B</p>



**Exam 2:** Learning Objectives under Evaluation

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	<ul style="list-style-type: none"> <li>• Linear: <math>B = b</math></li> <li>• Exponential: <math>B = \log(b)</math></li> <li>• Power: <math>B = \log(b)</math></li> <li>• Logarithmic: <math>B = 1/m \cdot \log(b)</math></li> </ul> <p>Replace (m) correctly within the general form of the equation</p> <ul style="list-style-type: none"> <li>• Linear: <math>y = mx + b</math></li> <li>• Exponential: <math>y = b10^{mx}</math></li> <li>• Power: <math>y = bx^m</math></li> <li>• Logarithmic: <math>x = b10^{my}</math></li> </ul> <p>Replace (b) correctly within the general form of the equation</p> <ul style="list-style-type: none"> <li>• Linear: <math>y = mx + b</math></li> <li>• Exponential: <math>y = b10^{mx}</math></li> <li>• Power: <math>y = bx^m</math></li> <li>• Logarithmic: <math>x = b10^{my}</math></li> </ul>
13.11 Use the function to make predictions only when appropriate	<p>Independent variable values within the range of the original data set (domain of the function model) can be used to make predictions</p> <p>Independent variable values outside the range of the original data set (domain of the function model) must be acknowledged or justified when making predictions</p> <p>Predicted numerical values must be consistent with the equation used to make the prediction</p> <p>Presentation of numerical predictions with appropriate units</p> <p>Management of the decimal places of numerical predictions</p>

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