HW#3

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LMR 4.1

1

1.45

3.62

25 0.300

```
##
## Call:
## lm(formula = lpsa ~ ., data = prostate)
## Residuals:
##
       Min
                1Q Median
                               ЗQ
                                       Max
## -1.7331 -0.3713 -0.0170 0.4141 1.6381
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                          1.296387
                                     0.516 0.60693
## (Intercept) 0.669337
## lcavol
               0.587022
                          0.087920
                                     6.677 2.11e-09 ***
## lweight
                           0.170012
               0.454467
                                    2.673 0.00896 **
               -0.019637
                          0.011173 -1.758 0.08229
## age
## lbph
               0.107054
                          0.058449
                                     1.832 0.07040 .
                                     3.136 0.00233 **
## svi
               0.766157
                          0.244309
## lcp
              -0.105474
                          0.091013 -1.159 0.24964
## gleason
               0.045142
                          0.157465
                                    0.287 0.77503
               0.004525
                          0.004421
                                     1.024 0.30886
## pgg45
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.7084 on 88 degrees of freedom
## Multiple R-squared: 0.6548, Adjusted R-squared: 0.6234
## F-statistic: 20.86 on 8 and 88 DF, p-value: < 2.2e-16
  a)
          fit
                  lwr
## 1 2.389053 2.172437 2.605669
## [1] 63.86598
  b)
## # A tibble: 1 x 8
     lcavol lweight
                     age lbph
                                 svi
                                         1cp gleason pgg45
      <dbl>
              <dbl> <dbl> <dbl> <dbl> <dbl> <
                                               <dbl> <dbl>
```

7

0 - 0.799

```
## fit lwr upr
## 1 3.17454 2.270398 4.078682
```

In the case of the 65 year old, their data fit within the original data. The mean age of the data set was 63.87 which is quite close to the patient's age. The 20 year was too far from the mean of the original data and there fore introduced higher variance.

```
c)
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + svi, data = prostate)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                            Max
## -1.72964 -0.45764 0.02812 0.46403
                                       1.57013
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.26809
                           0.54350
                                    -0.493
                                           0.62298
## lcavol
                0.55164
                           0.07467
                                     7.388
                                            6.3e-11 ***
## lweight
                                            0.00104 **
                0.50854
                           0.15017
                                     3.386
                0.66616
                           0.20978
                                     3.176 0.00203 **
## svi
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7168 on 93 degrees of freedom
## Multiple R-squared: 0.6264, Adjusted R-squared: 0.6144
## F-statistic: 51.99 on 3 and 93 DF, p-value: < 2.2e-16
##
          fit
                   lwr
## 1 2.372534 2.197274 2.547794
##
                    lwr
## 1 2.372534 0.9383436 3.806724
## Analysis of Variance Table
##
## Model 1: lpsa ~ lcavol + lweight + svi
## Model 2: lpsa ~ lcavol + lweight + age + lbph + svi + lcp + gleason +
       pgg45
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
         93 47.785
## 1
## 2
         88 44.163 5
                         3.6218 1.4434 0.2167
```

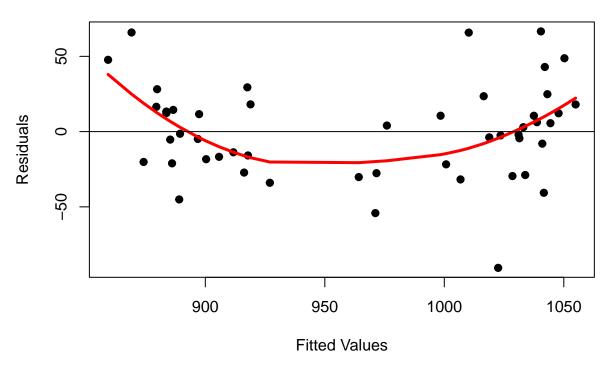
There is less error in the reduced model due to the less degrees of freedom. This reduced the uncertainty in the prediction. The reduced model is preferable due to less error and less likely to be overfit to the original data.

LMR 6.1

a)

```
##
## Call:
## lm(formula = total ~ expend + salary + ratio + takers, data = sat)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
##
   -90.531 -20.855
                    -1.746
                             15.979
                                     66.571
##
##
  Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
   (Intercept) 1045.9715
##
                             52.8698
                                      19.784
                                               < 2e-16 ***
                                                 0.674
   expend
                   4.4626
                             10.5465
                                        0.423
                              2.3872
                                        0.686
                                                 0.496
## salary
                   1.6379
## ratio
                  -3.6242
                              3.2154
                                      -1.127
                                                 0.266
                 -2.9045
                              0.2313 -12.559 2.61e-16 ***
## takers
##
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Signif. codes:
\mbox{\tt \#\#} Residual standard error: 32.7 on 45 degrees of freedom
## Multiple R-squared: 0.8246, Adjusted R-squared: 0.809
## F-statistic: 52.88 on 4 and 45 DF, p-value: < 2.2e-16
```

Residuals vs Fitted Values



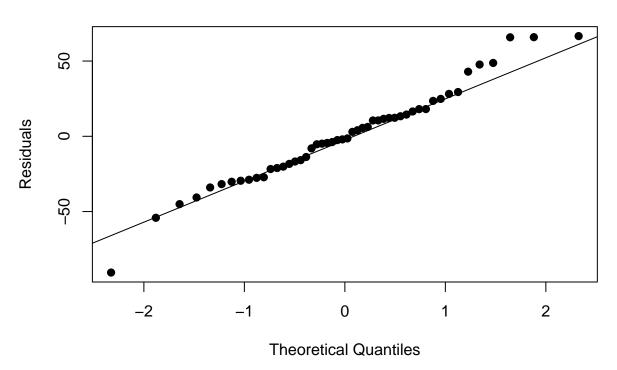
Results of the Breusch - Pagan Test

The plot seems to show that there is a slight curve to the residuals which would point to the data variance not being constant but the Breusch Pagan test results indicate otherwise. The test did not provide sufficient

evidence to reject the null hypothesis which states that the data variance is constant (alternate hypothesis states it is not constant).

```
##
## Breusch-Pagan test
##
## data: sat_model1
## BP = 2.7234, df = 4, p-value = 0.6051
The results of the Non Constant Variance Test
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 0.6972119, Df = 1, p = 0.40372
b)
```

Q-Q Plot (Normality)



Results of the Shapiro and the Durbin-Watson Tests

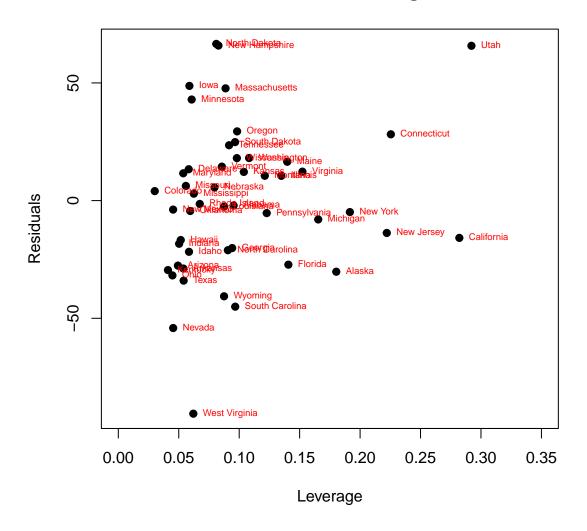
```
##
## Shapiro-Wilk normality test
##
## data: sat_model1$residuals
## W = 0.97691, p-value = 0.4304
##
##
Durbin-Watson test
##
```

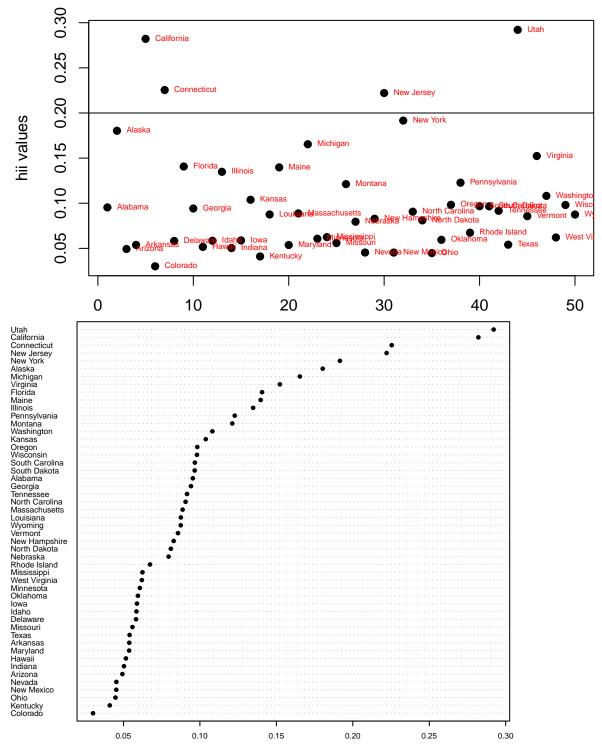
```
## data: sat_model1
## DW = 2.4525, p-value = 0.9459
## alternative hypothesis: true autocorrelation is greater than 0
```

The QQ plot does indicate some deviation from normality at higher quantiles, but the shapiro test did not provide enough evidence to reject the null hypothesis of the data being normal.

c)

Residuals vs Leverage



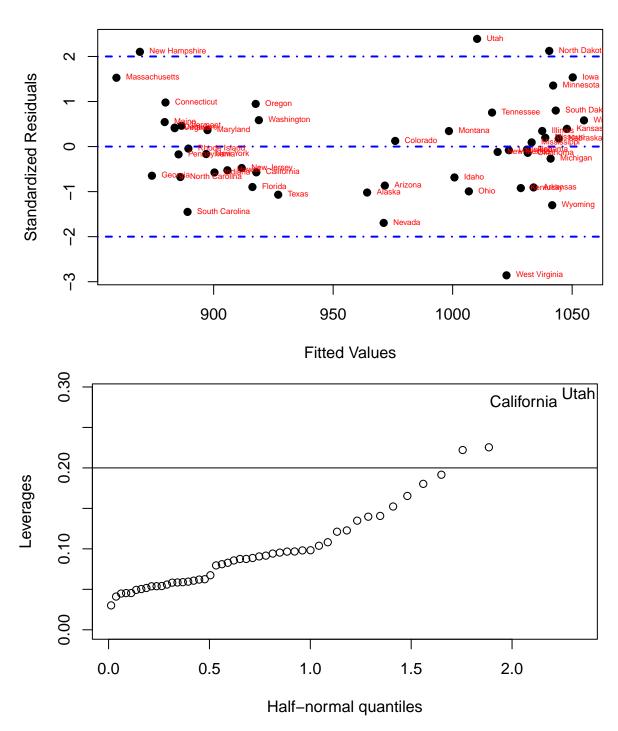


A number of high leverage points exists. Mainly Utah and California but also Connecticut and New Jersey. Dropping Utah and California and refitting the model should be considered. Centering is also an option.

d)

No Studentized residuals with Bonferroni p < 0.05 ## Largest |rstudent|:

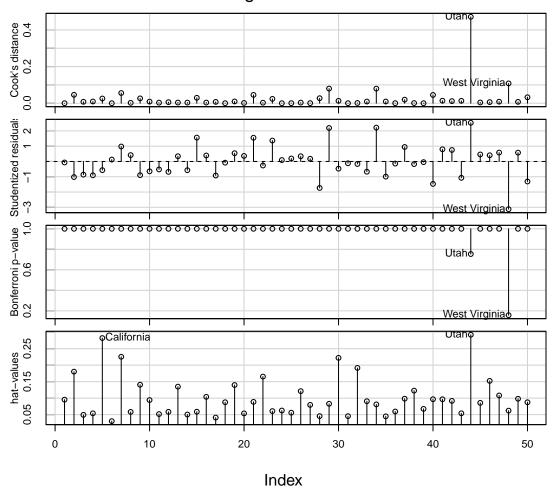
Standardized Residuals vs Fitted Values

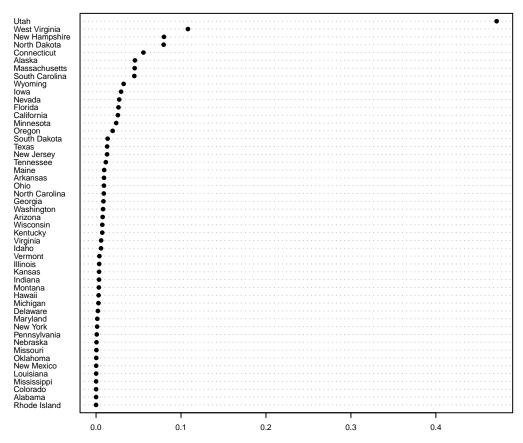


The outlier test did not reveal any outliers, but some of the plots indicate that Utah and California do stand out. Dropping them should be considered.

e)

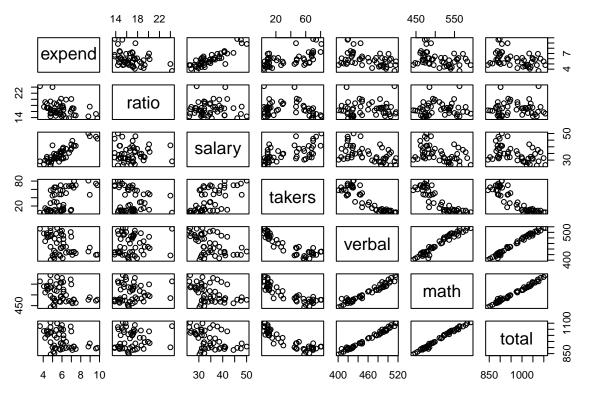
Diagnostic Plots





Utah appears to be influential, in addition to having high leverage and being an outlier. Refitting the model without Utah would be recommended.

f)



Total is strongly linear with verbal and math, but this is not surprising. Takers indicates somewhat of a negative relationship with total. The remaining three appear not to have a strong relationship with total.

LMR 7.8

```
a)
```

```
1.00000 17.47144 25.30482 58.60610 83.59121 100.63222 137.89717
##
    [8] 175.28623 192.61449 213.00748 228.15747 268.20620 555.67072
## # A tibble: 13 x 2
##
      'colnames(X)' vif_x
##
      <chr>>
                    <dbl>
                      2.25
##
   1 age
##
    2 weight
                    33.5
##
    3 height
                     1.67
##
   4 neck
                     4.32
##
   5 chest
                     9.46
##
   6 abdom
                    11.8
##
    7 hip
                    14.8
##
   8 thigh
                     7.78
  9 knee
                     4.61
## 10 ankle
                      1.91
## 11 biceps
                      3.62
## 12 forearm
                     2.19
## 13 wrist
                      3.38
```

We can see some quite large condition and VIF numbers. Eigenvalues over 30 point to collinearity, of which there are a few. Inspecting the VIF table, shows a number of values over 10 (weight. abdom, hip, and maybe chest). Overall, it can be said that there is a high degree of collinearity in the data.

b)

```
26.21547 61.53224 91.07633 114.44792 148.72518
          1.00000 18.39787
    [8] 178.80871 202.08708 211.78359 240.69468 276.35018 554.79777
## # A tibble: 13 x 2
      'colnames(X2)' vif_x2
##
##
      <chr>
                       <dbl>
                        2.28
##
    1 age
                       45.3
##
    2 weight
##
    3 height
                        3.44
                        3.98
##
   4 neck
##
    5 chest
                       10.7
##
    6 abdom
                       12.0
##
    7 hip
                       12.1
##
    8 thigh
                        7.15
## 9 knee
                        4.44
## 10 ankle
                        1.81
## 11 biceps
                        3.41
## 12 forearm
                        2.42
## 13 wrist
                        3.26
```

Dropping the values did not improve collinearity in the model. It made is worse in some cases.

c)

```
##
## Call:
## lm(formula = brozek ~ age + weight + height, data = new_fat)
##
## Residuals:
##
        Min
                       Median
                                     3Q
                  1Q
                                             Max
  -11.0260 -3.6537
                       0.0569
                                3.7588
                                        11.9011
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
  (Intercept) 54.31985
                           9.63347
                                     5.639 4.69e-08 ***
                0.12575
                           0.02599
                                     4.838 2.31e-06 ***
## age
## weight
                0.23519
                           0.01373
                                    17.124 < 2e-16 ***
                                    -8.067 3.17e-14 ***
## height
               -1.18089
                           0.14638
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 4.986 on 246 degrees of freedom
## Multiple R-squared: 0.5838, Adjusted R-squared: 0.5787
## F-statistic:
                  115 on 3 and 246 DF, p-value: < 2.2e-16
## [1]
       1.00000 13.87911 25.03771
##
                 vif_x3
## [1,] "age"
                 "1.08330491018921"
## [2,] "weight" "1.3811645842945"
## [3,] "height" "1.46966479387396"
```

The reduced model significantly mitigated collinearity. All condition and VIF numbers are well within desired limits. This model is much better than the full model in terms of collinearity.

```
d)

## fit lwr upr

## 1 18.48834 8.647863 28.32882

e)

## fit lwr upr

## 1 20.18367 10.32046 30.04688
```

The two predictions both spanned roughly 20. This indicates the model is good for that range of values.

```
f)
## fit lwr upr
## 1 3.720148 -6.28208 13.72238
```

Negative values are in the range which are impossible. The values for age, weight, and height are too far different than the original dataset. This introduces a lot of error into the prediction.

Question 4

Part A

```
##
## -- Column specification -------
## cols(
##
    rental_rates = col_double(),
    age = col_double(),
##
##
    opp_expenses = col_double(),
    vac_rates = col_double(),
##
    tot_squft = col_double()
##
## )
                       10 15 20
                                              0.0
                                                    0.4
     rental_rates
20
0
                      age
                                 opp_expenses
4.0
                                                 vac_rates
                                                                tot_squft
                                                        တ
     12
          16
                                     8
                                         12
                                                             1e+05
                                                                     4e+05
```

The only pair of variables that show a relationship is between tot_sqft and rental_rates which displays a slight linear relationship. The other pairs do not show strong relationship, linear or otherwise.

Part B

```
##
                rental_rates
                                    age opp_expenses
                                                       vac_rates tot_squft
## rental_rates
                  1.00000000 -0.2502846
                                           0.4137872
                                                      0.06652647 0.53526237
                 -0.25028456
                             1.0000000
                                           0.3888264 -0.25266347 0.28858350
## opp_expenses
                  0.41378716
                             0.3888264
                                           1.0000000 -0.37976174 0.44069713
                                                      1.00000000 0.08061073
## vac_rates
                  0.06652647 -0.2526635
                                          -0.3797617
                  0.53526237
                             0.2885835
                                           0.4406971 0.08061073 1.00000000
## tot_squft
```

The strongest positive correlation is the one between tot_sqft and rental_rates. The strongest negative is the one between opp_expenses and vac_rates. In both of those cases, the relationship was moderate. Age showed a moderate negative ralation with rental_rates and vac_rates. It also had a moderate positive

relationship with tot_squft and opp_expenses. Overall, the only two pairs that did not indicate a significant relationship is vac_rates/rental_rates and vac_rates/tot_squft.

Part C

```
##
## Call:
## lm(formula = rental_rates ~ ., data = df_commercial)
##
## Residuals:
##
       Min
                 1Q Median
                                   30
                                          Max
   -3.1872 -0.5911 -0.0910
                              0.5579
                                       2.9441
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  1.220e+01
                              5.780e-01
                                          21.110 < 2e-16 ***
                                          -6.655 3.89e-09 ***
                 -1.420e-01
                              2.134e-02
## age
                  2.820e-01
                              6.317e-02
                                            4.464 2.75e-05 ***
## opp_expenses
## vac_rates
                  6.193e-01
                              1.087e+00
                                           0.570
                                                      0.57
## tot_squft
                  7.924e-06
                              1.385e-06
                                           5.722 1.98e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.137 on 76 degrees of freedom
## Multiple R-squared: 0.5847, Adjusted R-squared: 0.5629
## F-statistic: 26.76 on 4 and 76 DF, p-value: 7.272e-14
##
     (Intercept)
                             age opp expenses
                                                     vac rates
                                                                     tot squft
    1.220059e+01 -1.420336e-01 2.820165e-01 6.193435e-01
##
                                                                7.924302e-06
c. part a) through c)
y = 12.2 - 0.142 x_1 + 0.282 x_2 + 0.620 x_3 + 0.000000792 x_4
x_1 \rightarrow age of dwelling (age)
x_2 -> operating expenses and taxes (opp_expenses)
x_3 \rightarrow \text{vacancy rates (vac\_rates)}
x_4 \rightarrow \text{total square footage (tot\_squft)}
```

The predictor with seemingly the smallest effect on rental rates is total square footage as can be seen by the near zero value, but it is still statistically significant. The small coefficient value is offset by the large values of the predictor itself. Vacancy rates were the least statistically significant predictor as can be seen with the low p value. If this predictor is dropped from the model, the model prediction will still produce a reasonably accurate result. Age and operating expenses were both statistically significant to the model and produced a large effect on the resulting prediction.

```
## [1] "The R squared values is 0.585"
## [1] "The adjusted R squared values is 0.563"
```

c. part d) The null hypothesis, H_0 , states that all 4 coefficients are equal to zero. The alternate hypothesis, H_A states that at least one of the coefficients is not zero. The test statistic is given as a the F-statistic in the model summary which is equal to 26.76. This results in a p value of nearly zero using an f distribution

of degrees of freedom of 4 and 76. Since the p value is less than the 0.05 significance level, we have enough evidence to reject the null hypothesis in favor of the alternative hypothesis.

c. part e)

```
Generalized least squares fit by REML
##
     Model: rental_rates
##
     Data: df_commercial
##
          AIC
                  BIC
                         logLik
     293.2916 307.276 -140.6458
##
##
##
  Coefficients:
##
                    Value Std.Error
                                       t-value p-value
##
  (Intercept)
                12.200586 0.5779562 21.109881
                                                0.0000
## age
                -0.142034 0.0213426 -6.654933
                                                0.0000
## opp expenses 0.282017 0.0631723
                                     4.464240
                                                0.0000
## vac_rates
                 0.619344 1.0868128
                                     0.569871
                                                0.5704
## tot_squft
                 0.000008 0.0000014 5.722446
##
##
    Correlation:
##
                (Intr) age
                               opp_xp vc_rts
## age
                -0.032
## opp_expenses -0.889 -0.201
                -0.516 0.175 0.412
## vac_rates
                 0.200 -0.189 -0.454 -0.322
## tot_squft
##
## Standardized residuals:
##
          Min
                      Q1
                                Med
                                             Q3
                                                       Max
## -2.8034364 -0.5198884 -0.0800025
                                      0.4907637
                                                 2.5896591
##
## Residual standard error: 1.136885
## Degrees of freedom: 81 total; 76 residual
```

c. part f)

The test statistic for β_3 is 0.570 which gives a p value of 0.5704. If H_0 states that $\beta_3 = 0$ and H_A states that β_3 is not equal to zero, then in this case we do no have enough evidence to reject the null hypothesis. This means that there is not enough evidence to reject the possibility that β_3 is zero. We can then say that β is not statistically significant to the model.

c. part h)

```
##
## lm(formula = rental_rates ~ . - vac_rates, data = df_commercial)
##
## Residuals:
                1Q Median
                                3Q
##
                                       Max
  -3.0620 -0.6437 -0.1013 0.5672
                                   2.9583
##
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 1.237e+01 4.928e-01
                                       25.100 < 2e-16 ***
                                       -6.891 1.33e-09 ***
                -1.442e-01
                           2.092e-02
## opp_expenses 2.672e-01 5.729e-02
                                        4.663 1.29e-05 ***
```

```
## tot_squft 8.178e-06 1.305e-06 6.265 1.97e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.132 on 77 degrees of freedom
## Multiple R-squared: 0.583, Adjusted R-squared: 0.5667
## F-statistic: 35.88 on 3 and 77 DF, p-value: 1.295e-14
```

Part D d. part I)

| Estimate | Error | t value | $\Pr(> t)$ | CI90neg | CI90pos |
|------------|-----------|-----------|-------------|------------|------------|
| 12.3705818 | 0.4928469 | 25.100251 | 0.00e+00 | 11.5500486 | 13.1911150 |
| -0.1441646 | 0.0209201 | -6.891195 | 0.00e+00 | -0.1789942 | -0.1093351 |
| 0.2671670 | 0.0572949 | 4.663018 | 1.29e-05 | 0.1717777 | 0.3625564 |
| 0.0000082 | 0.0000013 | 6.265018 | 0.00e+00 | 0.0000060 | 0.0000104 |

d. part II

```
## (Intercept) age opp_expenses tot_squft
## 1.237058e+01 -1.441646e-01 2.671670e-01 8.178210e-06
```

d. part III

```
## # A tibble: 4 x 5
##
      age opp_expenses vac_rates tot_squft pred_rrates
              <dbl> <dbl>
##
    <dbl>
                                <dbl>
                                          <dbl>
## 1
      5
                8.25
                          0
                                250000
                                             15.9
                            0 270000
## 2
       6
                8.5
                                             16.0
## 3
      14
               11.5
                            0 300000
                                             15.9
## 4
               10.2
                                310000
      12
                            0
                                             15.9
```

d. part IV

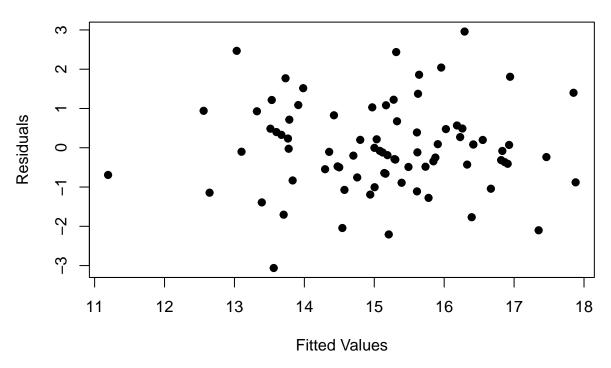
```
## # A tibble: 3 x 5
      age opp_expenses vac_rates tot_squft pred_rrates
##
   <dbl>
               <dbl> <dbl>
                                   <dbl>
                                              <dbl>
## 1
      4
                 10
                             0
                                   80000
                                               15.1
## 2
       6
                              0 120000
                                               15.6
                 11.5
## 3
     12
                 12.5
                             0
                                  340000
                                               16.8
##
         fit
                 lwr
## 1 15.11985 12.83659 17.40311
## 2 15.55940 13.27329 17.84551
```

3 16.76079 14.45322 19.06835

Part E

e. part a)

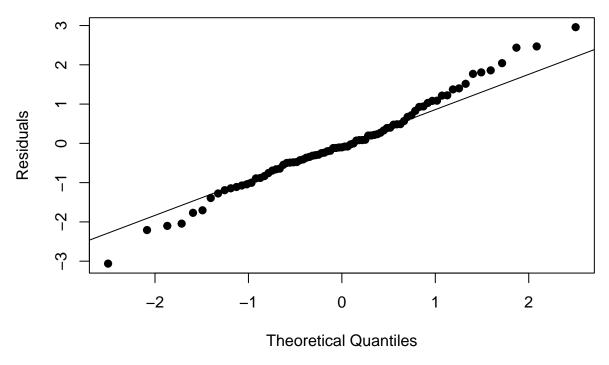
Residuals vs Fitted Values



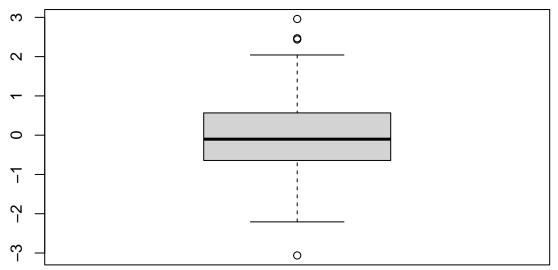
The plot indicates that variance is constant and that the data is normal. A deeper investigation is needed in order to confirm the strength of these assessments.

e. part b)

Q-Q Plot (Normality)

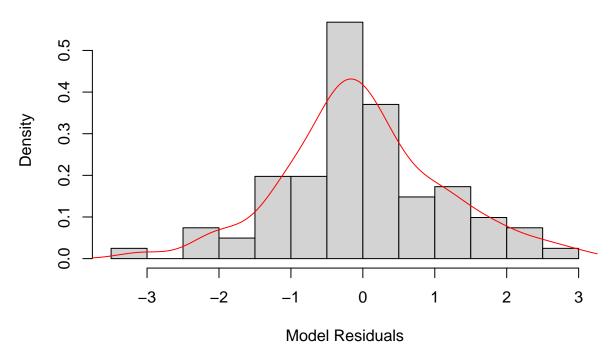


The QQ plot shows some deviation from normality. This means that the data was not strictly following a normal distribution.



The boxplot shows a number of outliers at both ends of the distribution. These should be investigated more using specific outlier testing methods.

Histogram of Residuals

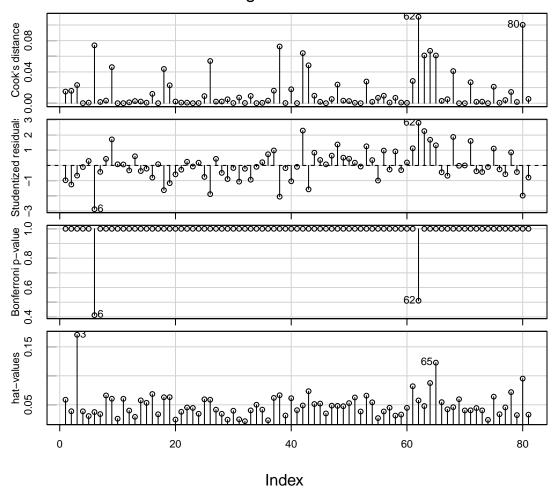


The histogram shows more evidence for outliers and even some skew in the data.

```
##
## Breusch-Pagan test
##
## data: comm_model2
## BP = 17.281, df = 3, p-value = 0.0006187
e part d and g)
```

e. part c)

Diagnostic Plots



The diagnostic plots do reveal a few outliers, high leverage, and influential points. Data points 6 and 62 are outliers, while 3, 62, 65, and 80 indicate high leverage/influence. 3, 6, 62, and 80 can be dropped from the model. 65 can be left in the model since it is not too much higher in leverage than the other points.

e part e and f)

```
##
## Shapiro-Wilk normality test
##
## data: comm_model2$residuals
## W = 0.98776, p-value = 0.6406

##
## Durbin-Watson test
##
## data: comm_model2
## DW = 1.5867, p-value = 0.02463
## alternative hypothesis: true autocorrelation is greater than 0
```

The high p value calculated from the Shapiro-Wilk test, means that we do not have enough evidence to reject the null hypothesis (H_0 : the data is normal). This means our assumption of the normality of the data is held true. The Durbin-Watson test indicates that the model errors are correlated (H_0 : errors are not

correlated, H_A : They are correlated). The small p value (< 0.05) means that we have enough evidence to reject the null hypothesis.

Part F

```
##
## Call:
## lm(formula = rental_rates ~ . - vac_rates, data = df_commercial[-c(3,
       6, 62, 80), ])
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                           Max
## -2.35002 -0.62221 -0.04052 0.62566
                                       2.24922
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                1.239e+01 4.716e-01 26.261 < 2e-16 ***
## (Intercept)
                -1.239e-01
                           1.987e-02 -6.236 2.62e-08 ***
## age
                                       4.685 1.27e-05 ***
## opp_expenses 2.571e-01 5.487e-02
## tot_squft
                7.957e-06 1.236e-06
                                       6.438 1.12e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.01 on 73 degrees of freedom
## Multiple R-squared: 0.5778, Adjusted R-squared: 0.5605
## F-statistic: 33.31 on 3 and 73 DF, p-value: 1.13e-13
```

By dropping outliers, R^2 values did not improve in the new model. They actually dropped slightly, indicating that outliers might not have had a strong effect on the model after all.

```
##
## Call:
## lm(formula = rental_rates ~ . - vac_rates, data = df_commercial[-c(6,
       62, 80), ])
##
##
## Residuals:
##
                 1Q
                      Median
                                   3Q
## -2.29323 -0.62754 -0.04509 0.58356 2.32591
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                1.224e+01 4.432e-01 27.626 < 2e-16 ***
## (Intercept)
               -1.291e-01 1.899e-02 -6.796 2.36e-09 ***
## age
## opp expenses 2.739e-01
                           5.148e-02
                                       5.320 1.06e-06 ***
## tot_squft
                8.003e-06 1.233e-06
                                       6.491 8.62e-09 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.008 on 74 degrees of freedom
## Multiple R-squared: 0.6203, Adjusted R-squared: 0.6049
## F-statistic: 40.3 on 3 and 74 DF, p-value: 1.515e-15
```

Leaving data point 3 in the model improved the R^2 values a little.

```
##
## Call:
## lm(formula = rental_rates ~ . - vac_rates, data = df_commercial[-c(6,
      62), ])
##
##
## Residuals:
                 1Q Median
                                   30
                                           Max
## -2.15356 -0.66614 -0.08314 0.63095 2.34999
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                1.226e+01 4.521e-01 27.121 < 2e-16 ***
## (Intercept)
               -1.283e-01 1.937e-02 -6.625 4.65e-09 ***
## opp_expenses 2.804e-01 5.241e-02
                                       5.350 9.22e-07 ***
## tot_squft
                7.296e-06 1.206e-06
                                       6.050 5.26e-08 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.029 on 75 degrees of freedom
## Multiple R-squared: 0.5995, Adjusted R-squared: 0.5834
## F-statistic: 37.42 on 3 and 75 DF, p-value: 6.844e-15
```

Removing outliers and ignoring high leverage also improved the model slightly as can be seen by the higher \mathbb{R}^2 values.

Part G

```
## fit lwr upr
## 1 15.75576 14.01053 17.50099
```

```
5A
```

```
## -- Column specification --------
## cols(
    Rep = col_double(),
##
##
    Software = col_double(),
    SalesLastQuarter = col_double(),
##
##
    SalesThisQuarter = col_double()
## )
##
## Call:
## lm(formula = SalesThisQuarter ~ . - SalesLastQuarter - Rep, data = df_software)
## Residuals:
      Min
               1Q Median
                               3Q
## -19.583 -6.833 1.417 7.583 32.417
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 81.583 3.281 24.866
                                          <2e-16 ***
                -2.000
## Software2
                            4.640 -0.431
                                            0.669
                -7.667
## Software3
                            4.640 -1.652
                                            0.108
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 11.37 on 33 degrees of freedom
## Multiple R-squared: 0.08176,
                                Adjusted R-squared: 0.02611
## F-statistic: 1.469 on 2 and 33 DF, p-value: 0.2448
Part I
y = 81.6 - 2.00 x_1 - 7.67 x_2
x_1 -> Whether Software 2 was used
x_2 -> Whether Software 3 was used
E(y|x_1 = 1, x_2 = 0) = (81.6 - 2.00) - 7.67 * 0 = 79.42
E(y|x_1 = 0, x_2 = 1) = (81.6 - 7.67) - 2.00 * 0 = 73.93
Part II
## Analysis of Variance Table
## Response: SalesThisQuarter
            Df Sum Sq Mean Sq F value Pr(>F)
## Software 2 379.6 189.78 1.4692 0.2448
## Residuals 33 4262.8 129.17
## [1] "Variance explained by the software is 0.082"
```

Part III

 H_0 states that software has no effect on sales.

 H_A states that software does have an effect on sales.

The f statistic given from the anova table, 1.47, and the corresponding p value, 0.25, indicate that we do not have enough evidence to reject the null hypothesis at the 0.05 significance level.

5B

```
##
## Call:
## lm(formula = SalesThisQuarter ~ . - Rep, data = df_software)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -18.974 -4.194
                     0.554
                             3.536
                                    16.049
##
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
                    -36.4423
                                16.4223
                                         -2.219
## (Intercept)
                                                  0.0337 *
## Software2
                                 2.9249
                                          0.258
                                                  0.7984
                      0.7535
                     -1.2835
## Software3
                                 3.0311
                                         -0.423
                                                  0.6748
                      1.5019
                                 0.2073
                                          7.244 3.14e-08 ***
## SalesLastQuarter
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 7.104 on 32 degrees of freedom
## Multiple R-squared: 0.6521, Adjusted R-squared: 0.6195
## F-statistic:
                   20 on 3 and 32 DF, p-value: 1.741e-07
```

Part I

```
y = -36.44 + 0.754 x_1 - 1.284 x_2 + 1.502 x_3 where:

x_1 -> Whether Software 2 was used

x_2 -> Whether Software 3 was used

x_3 -> Sales from last quarter

E(y|x_1=1,x_2=0) = (-36.44+0.754) - 1.284*0 + 1.502x_3 = -35.69 + 1.502x_3
E(y|x_1=0,x_2=1) = (-36.44-1.284) + 0.754*0 + 1.502x_3 = -37.72 + 1.502x_3
```

Part II - V

 H_0 states that software has no effect on sales.

 H_A states that software does have an effect on sales.

The f statistic given from the anova table, 3.76, and the corresponding p value, 0.0341, indicates that we do have enough evidence to reject the null hypothesis at the 0.05 significance level.

Part VI

Analysis of Variance Table

```
##
## Response: SalesThisQuarter
##
                      Df Sum Sq Mean Sq F value
                       2 379.56 189.78 3.7606
                                                      0.03413 *
## Software
## SalesLastQuarter
                      1 2647.88 2647.88 52.4699 3.141e-08 ***
                      32 1614.87
## Residuals
                                    50.46
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## [1] "Variance explained by the software is 0.082"
5C
##
## Call:
  lm(formula = SalesThisQuarter ~ Software + SalesLastQuarter:Software +
       SalesLastQuarter, data = df_software)
##
## Residuals:
##
       Min
                 1Q Median
                                   3Q
                                           Max
## -9.6222 -3.9426 0.8822 2.8198 11.7895
##
## Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                              20.6075
                                                        -4.477 0.000102 ***
                                 -92.2593
                                              31.9049
## Software2
                                 144.6516
                                                         4.534 8.66e-05 ***
## Software3
                                  48.1097
                                              29.6808
                                                          1.621 0.115504
## SalesLastQuarter
                                   2.2122
                                               0.2614
                                                          8.462 1.92e-09 ***
## Software2:SalesLastQuarter -1.8579
                                               0.4106
                                                        -4.525 8.88e-05 ***
## Software3:SalesLastQuarter -0.6239
                                               0.3879 -1.609 0.118200
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 5.649 on 30 degrees of freedom
## Multiple R-squared: 0.7938, Adjusted R-squared: 0.7594
## F-statistic: 23.1 on 5 and 30 DF, p-value: 1.849e-09
Part I
y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_1 x_3 + \beta_5 x_2 x_3
y = -92.26 + 144.65 x_1 + 48.11 x_2 + 2.21 x_3 - 1.86 x_1x_3 - 0.64 x_2x_3
where:
x_1 \rightarrow Indicator that Software 2 was used
x_2 \rightarrow Indicator that Software 3 was used
x_3 \rightarrow \text{Sales last quarter}
x_1x_3 -> Interaction term between sales last quarter and software 2
x_2x_3 -> Interaction term between sales last quarter and software 3
E(y|x_1 = 1, x_2 = 0) = -92.26 + 2.21x_3
E(y|x_1 = 0, x_2 = 1) = -92.26 + 48.11 + 2.21x_3 - 0.624x_4 = -44.15 + 1.59x_3
E(y|x_1 = 0, x_2 = 0) = -92.26 + 144.65 + 2.21x_3 - 1.86x_3 = 52.39 + 0.35x_3
```

Part II

 H_0 states that $\beta_0 = \beta_1 = \beta_2 = \beta_3 = \beta_4 = \beta_5 = 0$. H_A At least one β_i is not equal to zero.

Part III

```
H_0: \beta_3 = 0<br/>H_0: \beta_3 \neq 0
```

Part IV

A: F stat = 23.1 B: p value = ~ 0 C: Yes, we have enough evidence to reject the null in support of the alternate hypothesis. D: Yes, the p value is near zero.

Part V

A: $H_0: E(\beta_0|x_2=1)=0$ B: t statistic = 4.534 C: p value = ~ 0 D: Yes, the p value is less than $\alpha=0.05$, therefore statistically significant.

5D

One way of testing if Software 2 was different than 1 and 3 is to relevel the software factors to make 2 the reference and compare the results for 1 and 3. This can be accomplished as follows:

```
##
## Call:
## lm(formula = SalesThisQuarter ~ software + SalesLastQuarter:software +
       SalesLastQuarter, data = df_software)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -9.6222 -3.9426 0.8822
                           2.8198 11.7895
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                52.3922
                                           24.3568
                                                     2.151 0.03965 *
                                                    -4.534 8.66e-05 ***
## software1
                              -144.6516
                                           31.9049
## software3
                               -96.5419
                                           32.3965
                                                    -2.980
                                                             0.00567 **
## SalesLastQuarter
                                 0.3543
                                            0.3166
                                                      1.119 0.27207
## software1:SalesLastQuarter
                                 1.8579
                                            0.4106
                                                      4.525 8.88e-05 ***
## software3:SalesLastQuarter
                                 1.2341
                                            0.4270
                                                     2.890 0.00710 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.649 on 30 degrees of freedom
## Multiple R-squared: 0.7938, Adjusted R-squared: 0.7594
## F-statistic: 23.1 on 5 and 30 DF, p-value: 1.849e-09
```

As can be seen in the results the intercept when using Software 2 is 52.4 and the other two are -144.7 and -96.5 for 1 and 3 respectively. Furthermore, the individual p values indicate that the results are statistically

significant. This indicates that Software 2 produced very different results than software 1 and 3. The null hypothesis in this case would state that $\beta_{software2}$ is equal to $\beta_{software1}$ and $\beta_{software3}$. The alternative hypothesis states that it is not equal to the other two coefficients.

```
6
```

```
part a
## cols(
##
     Drug = col_double(),
##
     Momweight = col_double(),
##
    Dadweight = col_double(),
     Pigweight = col_double()
##
## )
##
## lm(formula = Pigweight ~ ., data = df_pigs)
##
## Residuals:
     Min
              1Q Median
                            3Q
                                  Max
## -3.905 -1.174 0.187 1.351 3.657
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 7.48163
                           9.14917
                                    0.818 0.41628
                           0.52788 -3.042 0.00331 **
## Drug2
               -1.60557
                           0.52871 -1.333 0.18684
## Drug3
               -0.70480
                                     5.578 4.28e-07 ***
## Momweight
               0.26363
                           0.04727
## Dadweight
                0.17442
                           0.03465
                                    5.034 3.58e-06 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 1.855 on 70 degrees of freedom
## Multiple R-squared: 0.4561, Adjusted R-squared: 0.425
## F-statistic: 14.67 on 4 and 70 DF, p-value: 9.393e-09
   (Intercept)
      5.876066
##
## (Intercept)
##
      6.776831
                            y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \epsilon
x_1 \rightarrow Whether drug 2 was administered
x_2 \rightarrow Whether drug 3 was administered
x_3 \rightarrow \text{Mom weight}
x_4 \rightarrow \text{Dad weight}
part b
```

| Drug | E(y x) |
|------|------------------------------------|
| 1 | $7.48 - 0.264 \ x_3 + 0.174 \ x_4$ |
| 2 | $5.88 - 0.264 \ x_3 + 0.174 \ x_4$ |
| 3 | $6.78 - 0.264 \ x_3 + 0.174 \ x_4$ |

part c

```
## fit lwr upr
## 1 75.05263 71.15725 78.94801
```

part d

The 95% confidence interval is

$$\Delta_{drug2,drug3} \pm t_{criticalvalue} * SE_{drug2+drug3}$$

which calculates to be -2.6627036, 0.8611729.

part e. i)

```
## Analysis of Variance Table
##
## Model 1: Pigweight ~ Momweight + Dadweight
## Model 2: Pigweight ~ Drug + Momweight + Dadweight
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 72 272.70
## 2 70 240.81 2 31.894 4.6356 0.01286 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
H_0: \beta_0 = \beta_1 = \beta_2 = 0

H_A: \beta_0 \neq 0 \text{ or } \beta_1 \neq 0 \text{ or } \beta_2 \neq 0
```

In this case, the null hypothesis can be rejected at the 0.05 significance level according to the ANOVA table. The type of drug does have an effect on the final pig weight.

part e. ii)

Drug 1 on average allows the pig to gain more weight than Drug 2. This is indicated by the negative coefficient for Drug 2 when Drug 1 is the reference. This points to a weight penalty when using Drug 2.

part e. iii)

Whether Drug 3 or Drug 1 allows the pig to gain more weight is inconclusive. We do not have enough evidence to reject the hypothesis that Drug 1 and Drug 3 result in equal effects to pig weight. This is shown by the high p value, indicating that the possible effect of Drug 3 is zero.

part e. iv)

Whether Drug 3 or Drug 2 allows the pig to gain more weight is inconclusive. We do not have enough evidence to reject the hypothesis that Drug 1 and Drug 3 result in equal effects to pig weight. This is shown by the high p value, indicating that the possible effect of Drug 3 is zero.

Code

```
library(faraway)
library(car)
library(MASS)
library(lmtest)
library(tidyverse)
library(nlme)
pros_model1 <- lm(lpsa ~ ., data = prostate)</pre>
summary(pros_model1)
new_patient <- tibble(lcavol = 1.44692, lweight = 3.62301, age = 65.00000,
                      lbph = 0.30010, svi = 0.00000, lcp = -0.79851,
                      gleason = 7.0000, pgg45 = 15.0000)
predict(pros_model1, newdata = new_patient, interval = "confidence")
#predict(pros_model1, newdata = new_patient, interval = "prediction")
mean(prostate$age)
new_patient1 <- tibble(lcavol = 1.44692, lweight = 3.62301, age = 25.00000,
                      lbph = 0.30010, svi = 0.00000, lcp = -0.79851,
                      gleason = 7.0000, pgg45 = 15.0000)
print(new_patient1)
predict(pros_model1, newdata = new_patient1, interval = "confidence")
#predict(pros_model1, newdata = new_patient1, interval = "prediction")
pros_model2 <- lm(lpsa ~ lcavol + lweight + svi, data = prostate)</pre>
summary(pros_model2)
predict(pros_model2, newdata = new_patient1, interval = "confidence")
predict(pros model2, newdata = new patient1, interval = "prediction")
print(anova(pros_model2, pros_model1))
sat_model1 <- lm(total ~ expend + salary + ratio + takers, data = sat)</pre>
summary(sat_model1)
plot(x = sat_model1$fitted.values, y = sat_model1$residuals, pch = 19,
     main = "Residuals vs Fitted Values", xlab = "Fitted Values", ylab = "Residuals")
res_line <- loess(sat_model1$residuals ~ sat_model1$fitted.values)</pre>
j <- order(sat_model1$fitted.values)</pre>
lines(sat_model1$fitted.values[j], res_line$fitted[j], col = "red", lwd = 3)
abline(h = 0)
bptest(sat_model1, studentize = FALSE)
ncvTest(sat_model1)
qqnorm(sat_model1$residuals, ylab = "Residuals", main = "Q-Q Plot (Normality)", pch = 19)
qqline(sat_model1$residuals)
shapiro.test(sat_model1$residuals)
dwtest(sat_model1)
X <- sat %>% select(expend, salary, ratio, takers)
X \leftarrow cbind(rep(1, nrow(X)), X)
X <- data.matrix(X)</pre>
#print(X)
Xt \leftarrow t(X)
XtX_inv <- solve(Xt %*% X)</pre>
```

```
XtY <- Xt %*% sat$total</pre>
beta_hat <- XtX_inv %*% XtY
P <- X %*% XtX_inv %*% Xt
res_mean <- mean(sat_model1$residuals)</pre>
res sd <- sd(sat model1$residuals)</pre>
stan_res <- (sat_model1$residuals - res_mean) / res_sd</pre>
plot(x = diag(P),
     y = sat_model1$residuals,
     pch = 19,
     main = "Residuals vs Leverage",
     xlab = "Leverage",
     ylab = "Residuals",
     xlim = c(0, 0.35))
text(diag(P), sat_model1$residuals, rownames(P),
     cex = 0.6, pos = 4, col = "red")
hat_data <- cbind(1:50, diag(P))</pre>
plot(hat_data, pch = 19, xlab = "", ylab = "hii values")
abline(h = 2 * 5 / 50)
text(hat_data[,1], hat_data[,2], names(diag(P)),
     cex = 0.5, pos = 4, col = "red")
dotchart(sort(diag(P)), pch = 19, cex = 0.5)
outlierTest(sat_model1)
plot(x = sat_model1$fitted.values, y = rstandard(sat_model1), pch = 19,
     main = "Standardized Residuals vs Fitted Values", xlab = "Fitted Values", ylab = "Standardized Res
abline(h = c(0, 2, -2), col = "blue", lty = 4, lwd = 2)
text(x = sat_model1$fitted.values, y = rstandard(sat_model1), rownames(sat),
     cex = 0.5, pos = 4, col = "red")
#cooks.distance(sat_model1)
halfnorm(diag(P), labs = rownames(P), ylab = "Leverages")
abline(h = 2 * sat_model1$rank / nrow(sat))
SST <- sum((sat$total - mean(sat$total))^2)</pre>
SSR <- sum((sat_model1$fitted.values - mean(sat$total))^2)</pre>
SSE <- sum((sat$total - sat_model1$fitted.values)^2)</pre>
MSR <- SSR/(sat_model1$rank - 1)
MSE <- SSE/(nrow(sat) - sat_model1$rank)</pre>
influenceIndexPlot(sat model1)
cooks_dis_calc <- sat_model1$residuals^2 /</pre>
  (sat_model1$rank * MSE) * (diag(P)/(1-diag(P))^2)
dotchart(sort(cooks_dis_calc), cex = 0.5, pch = 19)
pairs(sat)
fat_model1 <- lm(brozek ~ age + weight + height + neck + chest +</pre>
                    abdom + hip + thigh + knee + ankle + biceps +
                    forearm + wrist, data = fat)
```

```
X <- model.matrix(fat_model1)[,-1]</pre>
eigen_X <- eigen(t(X) %*% X)</pre>
sqrt(eigen_X$values[1]/eigen_X$values)
vif_x \leftarrow rep(0, ncol(X))
for(i in 1:ncol(X)){
    vif_x[i] \leftarrow 1 / (1 - summary(lm(X[,i] \sim X[,-i])) r.squared)
}
vif_x <- tibble(colnames(X), vif_x)</pre>
print(vif_x)
new_fat \leftarrow fat[-c(39,42),]
fat_model2 <- lm(brozek ~ age + weight + height + neck + chest +</pre>
                     abdom + hip + thigh + knee + ankle + biceps +
                     forearm + wrist, data = new_fat)
X2 <- model.matrix(fat_model2)[,-1]</pre>
eigen_X2 <- eigen(t(X2) %*% X2)
sqrt(eigen_X2$values[1]/eigen_X2$values)
vif_x2 \leftarrow rep(0, ncol(X2))
for(i in 1:ncol(X2)){
    vif_x2[i] <- 1 / (1 - summary(lm(X2[,i] ~ X2[,-i]))$r.squared)</pre>
vif_x2 <- tibble(colnames(X2), vif_x2)</pre>
print(vif_x2)
fat_model3 <- lm(brozek ~ age + weight + height, data = new_fat)</pre>
summary(fat_model3)
X3 <- model.matrix(fat_model3)[,-1]</pre>
eigen_X3 <- eigen(t(X3) %*% X3)
sqrt(eigen_X3$values[1]/eigen_X3$values)
vif_x3 \leftarrow rep(0, ncol(X3))
for(i in 1:ncol(X3)){
    vif_x3[i] <- 1 / (1 - summary(lm(X3[,i] ~ X3[,-i]))$r.squared)</pre>
}
vif_x3 <- cbind(colnames(X3), vif_x3)</pre>
print(vif_x3)
```

```
fat_1 <- as.data.frame(t(apply(X3, 2, median)))</pre>
predict(fat model3, newdata = fat 1, interval = "prediction")
fat_2 <- as.data.frame(cbind(age = 40, weight = 200, height = 73))</pre>
predict(fat model3, newdata = fat 2, interval = "prediction")
fat_3 <- as.data.frame(cbind(age = 40, weight = 130, height = 73))
predict(fat_model3, newdata = fat_3, interval = "prediction")
df_commercial <- read_table("commercial_property.txt")</pre>
#a)
options(repr.plot.width = 8, repr.plot.height = 6, repr.plot.res = 150)
df_commercial %>% pairs()
#b)
cor(df_commercial)
#c)
comm_model1 <- lm(rental_rates ~ ., data = df_commercial)</pre>
summary(comm model1)
comm_model1$coefficients
sprintf("The R squared values is %.3f", summary(comm_model1)$r.squared)
sprintf("The adjusted R squared values is %.3f", summary(comm_model1)$adj.r.squared)
#c. part e)
summary(gls(rental_rates ~ ., data = df_commercial))
# c. part h)
comm_model2 <- lm(rental_rates ~ .-vac_rates, data = df_commercial)</pre>
summary(comm_model2)
#d. part I)
model_coeff <- summary(comm_model2)$coefficients</pre>
model_coeff <- as_tibble(model_coeff)</pre>
colnames(model coeff)[2] = 'Error'
model_coeff <- model_coeff %>% mutate(CI90neg = Estimate - qt(0.95, 77) * Error, CI90pos = Estimate + q
knitr::kable(model_coeff)
#d. part II)
pvals <- summary(comm_model2)$coef[,4]</pre>
padj <- p.adjust(pvals, method="bonferroni")</pre>
print(coef(comm_model2)[padj < 0.1])</pre>
#d. part III)
new_dwellings <- tibble(age = c(5.0, 6.0, 14.0, 12.0),
                         opp_{expenses} = c(8.25, 8.50, 11.50, 10.25),
                         vac_rates = rep(0, 4),
                         tot_squft = c(250000, 270000, 300000, 310000))
new_dwellings <- new_dwellings %>% mutate(pred_rrates = predict(comm_model2, newdata = new_dwellings))
```

```
print(new_dwellings)
#d part IV)
new_dwellings2 <- tibble(age = c(4.0, 6.0, 12.0),
                         opp_{expenses} = c(10.0, 11.50, 12.5),
                         vac_rates = rep(0, 3),
                         tot_squft = c(80000, 120000, 340000))
new_dwellings2 <- new_dwellings2 %>% mutate(pred_rrates = predict(comm_model2, newdata = new_dwellings2
print(new dwellings2)
predict(comm_model2, newdata = new_dwellings2, interval = "prediction", level = 0.95)
plot(x = comm_model2\$fitted.values, y = comm_model2\$residuals, pch = 19,
     main = "Residuals vs Fitted Values", xlab = "Fitted Values", ylab = "Residuals")
# e part b)
qqnorm(comm_model2$residuals, ylab = "Residuals", main = "Q-Q Plot (Normality)", pch = 19)
qqline(comm_model2$residuals)
boxplot(comm_model2$residuals)
hist(comm_model2$residuals, breaks = 20, xlab = "Model Residuals", main = "Histogram of Residuals", pro
lines(density(comm_model2$residuals), col = "red")
#e part c)
bptest(comm_model2, studentize = FALSE)
#e part d and g
influenceIndexPlot(comm_model2)
#e part e and f)
shapiro.test(comm_model2$residuals)
dwtest(comm model2)
# Part F
comm_model3 <- lm(rental_rates ~ . - vac_rates, df_commercial[-c(3, 6, 62, 80), ])</pre>
summary(comm_model3)
comm_model4 <- lm(rental_rates ~ . - vac_rates, df_commercial[-c(6, 62, 80), ])</pre>
summary(comm_model4)
comm_model5 <- lm(rental_rates ~ . - vac_rates, df_commercial[-c(6, 62), ])</pre>
summary(comm_model5)
single_unit <- tibble(age = 5, opp_expenses = 8.25, vac_rates = 0, tot_squft = 250000)
predict(comm_model5, newdata = single_unit, level = 0.90, interval = "prediction")
df_software <- read_table("software_sales.txt")</pre>
df_software$Software <- as.factor(df_software$Software)</pre>
sw_model1 <- lm(SalesThisQuarter ~ . - SalesLastQuarter - Rep, data = df_software)</pre>
summary(sw_model1)
# Part ii)
anova(sw_model1)
sprintf("Variance explained by the software is %0.3f", (anova(sw_model1)[1,2] / sum(anova(sw_model1)[,2
sw_model2 <- lm(SalesThisQuarter ~ . -Rep, data = df_software)</pre>
```

```
summary(sw_model2)
anova(sw_model2)
sprintf("Variance explained by the software is %0.3f", (anova(sw_model2)[1,2] / sum(anova(sw_model2)[,2
sw_model3 <- lm(SalesThisQuarter ~ Software + SalesLastQuarter:Software + SalesLastQuarter, data = df_s</pre>
summary(sw_model3)
software <- relevel(df_software$Software, ref = 2)</pre>
sw_model4 <- lm(SalesThisQuarter ~ software + SalesLastQuarter:software + SalesLastQuarter, data = df_s</pre>
summary(sw_model4)
df_pigs <- read_table("pig_weight.txt")</pre>
df_pigs$Drug <- as.factor(df_pigs$Drug)</pre>
pig_model1 <- lm(Pigweight ~ ., data = df_pigs)</pre>
summary(pig_model1)
pig_model1$coefficients[1] + pig_model1$coefficients[2]
pig_model1$coefficients[1] + pig_model1$coefficients[3]
new_pig <- tibble(Drug = as.factor(2), Momweight = 140, Dadweight = 185)</pre>
predict(pig_model1, newdata = new_pig, interval = "prediction", level = 0.95)
delta_2_3 <- summary(pig_model1)$coefficient[2,1] - summary(pig_model1)$coefficient[3,1]</pre>
SE_delta <- summary(pig_model1)$coefficient[2,2] + summary(pig_model1)$coefficient[3,2]
t_{cv} \leftarrow qt(0.95, 68)
d2d3_CI \leftarrow delta_2_3 + c(-1, 1) * SE_delta * t_cv
#Part e
pig_model_nodrug <- lm(Pigweight ~ Momweight + Dadweight, data = df_pigs)</pre>
pig_model_noparent <- lm(Pigweight ~ Drug, data = df_pigs)</pre>
anova(pig_model_nodrug, pig_model1)
#anova(pig_model_noparent, pig_model1)
#anova(piq_model1)
```