ST_518 Project MA, HK, BA, JF 2022-11-21

Executive Summary

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Introduction

We need to define some kind of goal for the paper. A driver for this study. Are we trying to find a difference between store and name brand? Does stirring have an effect?

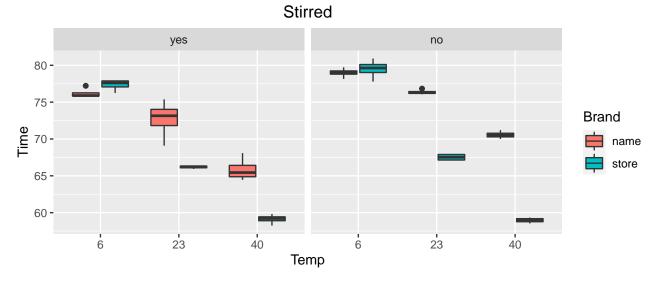
Experimental Design

Description here

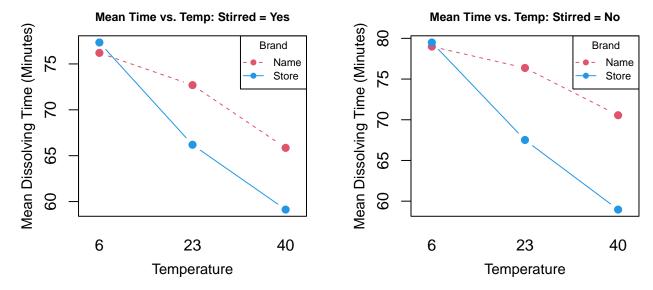
Exploratory Data Analysis

For this study we are presented with data from an 'Effervescent Experiment'. The data contained dissolving times of two different brands of cold medicine tablets that were obtained under various conditions. Those conditions included varying water temperatures (6°C, 23°C, 40°C) and the presence of stirring (magnetic stir bar at 350 rpm). This was a complete block design with stirring acting as the blocking effect. In all, the data contained 48 rows and 6 columns. The 6 columns include 3 explanatory variables (Brand, Temp, Stirred categorical factors), 2 response variables (Time and Org Time, both numerical) and 1 descriptor (sample order). Prior to starting any analysis, we will explore the data to gain an understanding of what to expect and to check for violations of any assumptions.

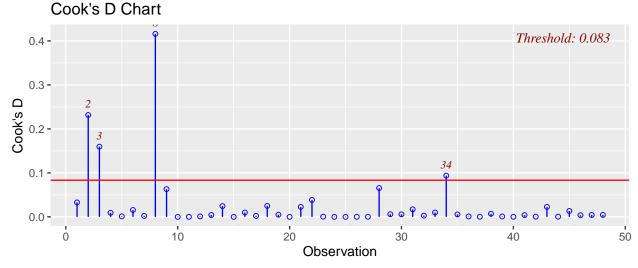
From the summary statistics table (see Appendix 1, Table 1), we can see that each group has exactly 4 entries, so no imbalance concerns. The variance seems to jump by quite a large amount between the groups, so contrast analysis might be a concern due to the small sample size.



Immediately it can be seen that stirring seems to increase the variance of the name brand medicine. Also, an interaction effect between temperature and brand can be deduced if lines are drawn through the centers of the boxes. We can also see that temperature has an inverse effect on dissolving times whether stirring is present or not. Stirring might have an additive effect regardless of temperature.

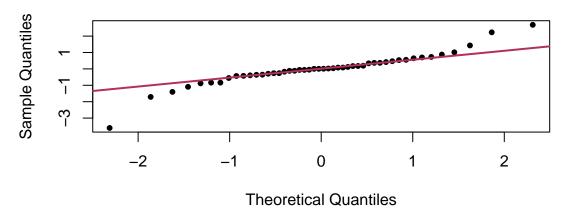


The possible interaction between brand and temperature becomes even more noticeable in the preceding three factor interaction plots. Specifically the brand and temperature interaction can be seen with increasing temperature the store brand line has a more negative slope than the name brand line. In addition, there might be a slight three factor interaction between brand, temperature, and stirring as the name and store brand lines appear to be closer together in the stirred=yes plot than the stirred=no plot.



From the boxplots, we were able to see a small amount of outliers. To confirm if there are any of concern we plotted the Cook's Distance for each point based on a full linear model. Point 8 has a higher Cook's distance than the rest of the points which may require removal for analysis if it is suspected of causing issues in the analysis. This would have to be weighed against the risks cause by introducing imbalances.

Normal Q-Q Plot



Finally, we check the normality of the data. Here a QQ plot is generated for the full model residuals. The data seems to be indicative of heavy tails. This might pose a problem for some of our analyses.

Analysis and Results

Contrasts

Conducting a linear contrast analysis on each of the explanatory variables reveals that there are significant differences between groups based on factors, see Appendix 1 Table 2, 3, 4, and 5 for full results.

In the first case, we contrasted the means of stirred versus not stirred. Here the difference in means is -2.41 with an upper 95% confidence limit of -3.04 and a lower 95% CI limit of -1.78. In other words, on average stirring medicine reduces dissolving time by between 3.04 and 1.78 minutes regardless of brand or temperature. When looking only at brand, name brand dissolving times were on average between 4.71 and 5.97 (95% CI) minutes slower than store brand. Since neither of the intervals contained zero we can conclude that there is a difference between brands and between the presence of stirring.

While significant for both store and name brands, stirring had more of an impact to dissolving times for name brand than it did for the store brand. Stirring reduced name brand dissolving times by 2.83 and 4.61 minutes whereas for the store brand that interval was 0.22 and 2 minutes.

A similar analysis was completed for the three levels of temperature. Completing a contrast analysis using a Bonferroni correction we found that in pairwise cases each level was significantly different from the other. The 95% confidence limits were (6.25, 8.38), (13.32, 15.44), and (6.00, 8.13) for the pair wise comparisons of $6^{\circ}C$ vs $23^{\circ}C$, $6^{\circ}C$ vs $40^{\circ}C$, and $23^{\circ}C$ vs $40^{\circ}C$, respectively. Zero did not fall in any of those ranges. When comparing individual levels versus the remainder of the group, $23^{\circ}C$ was found not to be significantly different from the rest of the levels. That confidence interval ranged from -1.04 to 0.80 minutes of dissolving time. Due to that, we do not have enough evidence to say $23^{\circ}C$ is different from either $6^{\circ}C$ or $40^{\circ}C$.

Model Development

The following models were developed and analyzed for this paper:

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\begin{aligned} & Model \ 1: Y_{ijkl} = \mu + \alpha_i + \beta_j + \gamma_k + (\alpha\beta)_{ij} + (\alpha\gamma)_{ik} + (\gamma\beta)_{jk} + (\alpha\beta\gamma)_{ijk} + \epsilon_{ijkl} \\ & Model \ 2: Y_{ijkl} = \mu + \alpha_i + \beta_j + \gamma_k + (\alpha\beta)_{ij} + \epsilon_{ijkl} \\ & Model \ 3: Y_{ijkl} = \mu + \alpha_i + \beta_j + \gamma_k + \epsilon_{ijkl} \end{aligned}
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Where α is brand effect, β is temperature effect, γ is stir effect. i, j, k are (1, 2), (1,2,3), and (1,2), respectively. ϵ_{ijkl} is assumed to be normally distributed with a μ_{ϵ} of 0 and a variance of σ_{ϵ}^2 . μ is the overall mean and is an unknown value.

Mixed Effects models:

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Model 4: Y_{ijk} = \mu + \alpha_i + \beta_j + \gamma_k + (\alpha\beta)_{ij} + \epsilon_{ijk}
Where both temperature and brand are random.
Model 5: Y_{ijk} = \mu + A_i + \beta_j + \gamma_k + (A\beta)_{ij} + \epsilon_{ijk}
Where temperature is fixed and brand is random.
Model 6: Y_{ijk} = \mu + \alpha_i + B_j + \gamma_k + (\alpha B)_{ij} + \epsilon_{ijk}
Where temperature is random and brand is fixed.
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With order as a factor:

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Model 7: Y_{ijklm} = \mu + \alpha_i + \beta_j + \gamma_k + \nu_l + (\alpha\beta)_{ij} + \epsilon_{ijklm}
Similar to model 2, but with an introduced effect, \nu, to represent order.
```

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Model 8: Y_{ijklm} = \mu + \alpha_i + \beta_j + \gamma_k + \nu_l + (\alpha\beta)_{ij} + (\alpha\gamma)_{ik} + (\gamma\beta)_{jk} + (\alpha\beta\gamma)_{ijk} + \epsilon_{ijklm}
Similar to model 1, but with an introduced effect, \nu, to represent order.
```

Model Selection

Model	Root MSE	R^2	$adj R^2$
1	1.074835	0.9824498	0.9770873
2	1.3185414	0.9699208	0.965519
3	2.655107	0.8720833	0.860184
7	1.302961	0.9713439	0.966329
8	1.0868873	0.9825525	0.9765706

Results

Conclusion

Appendix I: Analysis Tables and Figures

Table 2: Data Summary Table

Brand	Temp	Stirred	25%	Mean	Median	75%	Var	n
name	6	yes	75.83358	76.20241	75.89223	76.26107	0.4593492	4
name	6	no	78.79910	78.99061	79.04435	79.23586	0.4146440	4
name	23	yes	71.82180	72.69145	73.14894	74.01859	6.9869087	4
name	23	no	76.20492	76.36351	76.27622	76.43481	0.1078134	4
name	40	yes	64.87321	65.85343	65.43863	66.41886	2.5499751	4
name	40	no	70.28754	70.55511	70.50947	70.77705	0.2544033	4
store	6	yes	77.06561	77.33703	77.60659	77.87801	0.5964884	4
store	6	no	79.01994	79.49240	79.63219	80.10465	1.6942517	4
store	23	yes	66.08831	66.19126	66.22629	66.32923	0.0411024	4
store	23	no	67.14393	67.51552	67.52360	67.89520	0.2060739	4
store	40	yes	58.90895	59.12529	59.21659	59.43293	0.4320148	4
store	40	no	58.76884	58.96347	58.99050	59.18513	0.1202191	4

Table 3: Least Squares Means

Brand	Temp	Stirred	emmean	SE	df	lower.CL	upper.CL
name	6	yes	76.20241	0.5374175	36	75.11248	77.29235
store	6	yes	77.33703	0.5374175	36	76.24709	78.42696
name	23	yes	72.69145	0.5374175	36	71.60152	73.78138
store	23	yes	66.19126	0.5374175	36	65.10132	67.28119
name	40	yes	65.85343	0.5374175	36	64.76350	66.94337
store	40	yes	59.12529	0.5374175	36	58.03535	60.21522
name	6	no	78.99061	0.5374175	36	77.90068	80.08055
store	6	no	79.49240	0.5374175	36	78.40247	80.58233
name	23	no	76.36351	0.5374175	36	75.27358	77.45344
store	23	no	67.51552	0.5374175	36	66.42559	68.60546
name	40	no	70.55511	0.5374175	36	69.46518	71.64505
store	40	no	58.96347	0.5374175	36	57.87354	60.05341

Table 4: Contrast Stirred and Brand

contrast	estimate	SE	df	lower.CL	upper.CL
stirred	-2.413294	0.3102781	36	-3.042567	-1.784021
branding	5.338595	0.3102781	36	4.709322	5.967868

Table 5: Contrast Stirred versus Brand

contrast	estimate	SE	df	lower.CL	upper.CL
stirredbrand stirredstore	0.,_00_0	0.4387996 0.4387996			

Table 6: Contrast Temperatures

contrast	estimate	SE	df	lower.CL	upper.CL
temp6_23	7.3151767	0.3800116	36	6.254195	8.3761584
$temp6_40$	14.3812861	0.3800116	36	13.320305	15.4422678
$temp23_40$	7.0661094	0.3800116	36	6.005128	8.1270910
$temp6_rest$	10.8482314	0.3290997	36	9.929394	11.7670685
$temp23_rest$	-0.1245337	0.3290997	36	-1.043371	0.7943034
$temp40_rest$	-10.7236978	0.3290997	36	-11.642535	-9.8048607

Table 7: Model 1: ANOVA Table

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Brand	1	342.007	342.007	296.041	0.000
Temp	2	1654.737	827.368	716.169	0.000
Stirred	1	69.888	69.888	60.495	0.000
Brand:Temp	2	231.852	115.926	100.345	0.000
Brand:Stirred	1	20.510	20.510	17.753	0.000
Temp:Stirred	2	0.125	0.062	0.054	0.948
Brand:Temp:Stirred	2	9.056	4.528	3.919	0.029
Residuals	36	41.590	1.155	NA	NA

Table 8: Model 1: Type III ANOVA Table

Sum Sq	Df	F value	Pr(>F)
23227.231	1	20105.451	0.000
2.575	1	2.229	0.144
221.582	2	95.901	0.000
15.548	1	13.458	0.001
80.110	2	34.672	0.000
0.400	1	0.347	0.560
3.668	2	1.588	0.218
9.056	2	3.919	0.029
41.590	36	NA	NA
	23227.231 2.575 221.582 15.548 80.110 0.400 3.668 9.056	23227.231 1 2.575 1 221.582 2 15.548 1 80.110 2 0.400 1 3.668 2 9.056 2	23227.231 1 20105.451 2.575 1 2.229 221.582 2 95.901 15.548 1 13.458 80.110 2 34.672 0.400 1 0.347 3.668 2 1.588 9.056 2 3.919

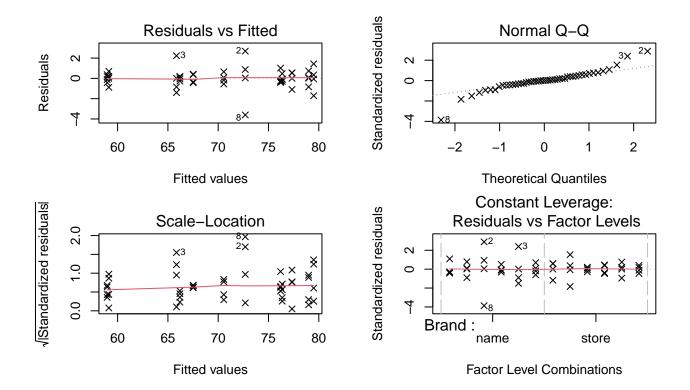


Table 9: Model 2: ANOVA Table

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Brand	1	342.00715	342.007154	196.71962	0e+00
Temp	2	1654.73655	827.368276	475.89522	0e + 00
Stirred	1	69.88787	69.887866	40.19891	1e-07
Brand:Temp	2	231.85191	115.925956	66.67963	0e + 00
Residuals	41	71.28061	1.738551	NA	NA

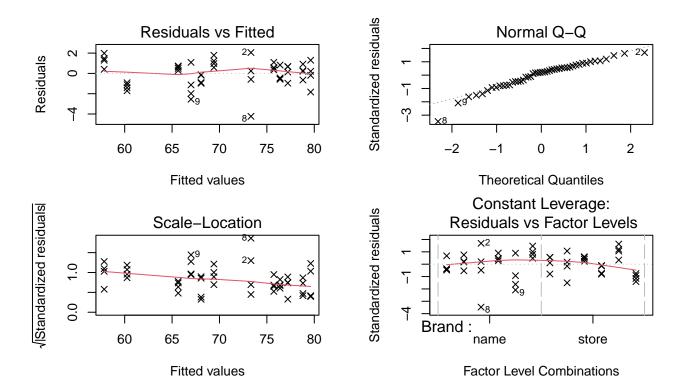


Table 10: Model 3: ANOVA Table

	Df	$\operatorname{Sum}\operatorname{Sq}$	Mean Sq	F value	Pr(>F)
Brand	1	342.00715	342.007154	48.514451	0.0000000
Temp	2	1654.73655	827.368276	117.363970	0.0000000
Stirred	1	69.88787	69.887866	9.913744	0.0029802
Residuals	43	303.13252	7.049593	NA	NA

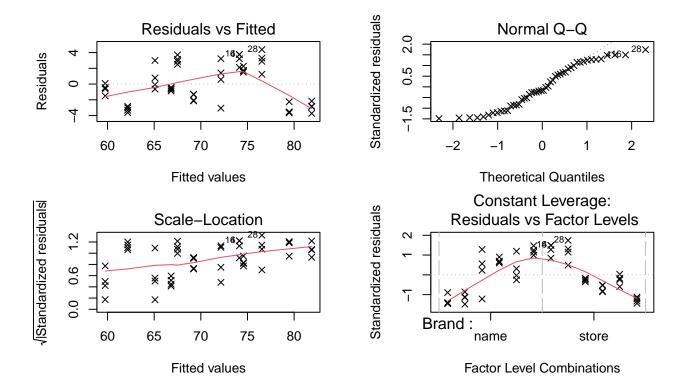


Table 11: Model 7: ANOVA Table

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Brand	1	342.0071543	342.0071543	201.4523573	0.0000000
Temp	2	1654.7365514	827.3682757	487.3444529	0.0000000
Stirred	1	69.8878657	69.8878657	41.1660257	0.0000001
Order	1	0.9059095	0.9059095	0.5336076	0.4693512
Brand:Temp	2	234.3183134	117.1591567	69.0102180	0.0000000
Residuals	40	67.9082953	1.6977074	NA	NA

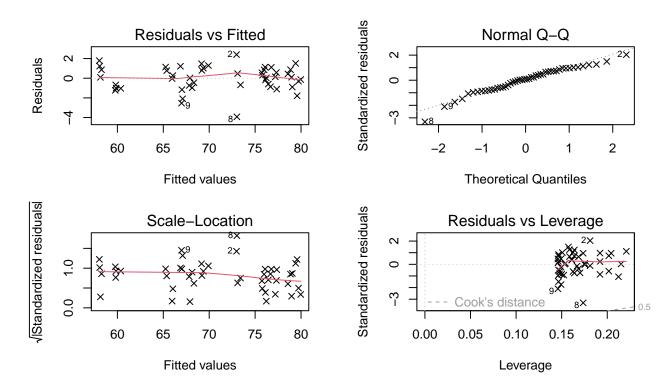
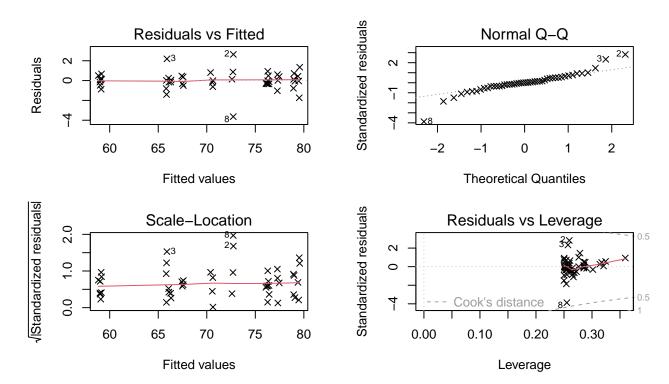


Table 12: Model 8: ANOVA Table

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Brand	1	342.0071543	342.0071543	289.5117212	0.0000000
Temp	2	1654.7365514	827.3682757	700.3736925	0.0000000
Stirred	1	69.8878657	69.8878657	59.1606229	0.0000000
Order	1	0.9059095	0.9059095	0.7668595	0.3871609
Brand:Temp	2	234.3183134	117.1591567	99.1761391	0.0000000
Brand:Stirred	1	17.2952414	17.2952414	14.6405566	0.0005144
Temp:Stirred	2	0.0420436	0.0210218	0.0177951	0.9823712
Brand:Temp:Stirred	2	9.2246692	4.6123346	3.9043772	0.0294693
Residuals	35	41.3463412	1.1813240	NA	NA



Appendix: Code

```
library(tidyverse)
library(emmeans)
library(lme4)
library(lmerTest)
library(olsrr)
library(car)
df_eff <- read_csv('effervescence.csv', col_types = 'fffnnn')</pre>
df_stats <-
df_eff %>% group_by(Brand, Temp, Stirred) %>%
summarise('25%' = quantile(Time, probs = 0.25),
          'Mean' = mean(Time),
          'Median' = median(Time),
          '75%' = quantile(Time, probs = 0.75),
          'Var' = var(Time),
          'n' = n()
#knitr::kable(df_stats)
df_eff %>% ggplot() + geom_boxplot(aes(fill = Brand, y = Time, x = Temp)) +
 facet_grid(cols = vars(Stirred)) + labs(title = "Stirred") + theme(
  plot.title = element_text(hjust = 0.5)
##3 factor interaction plot based on HW7 code
par(mfrow=c(1,2), mar = c(3.5,3.5,2,2))
with(df_eff%>%filter(Stirred=="yes"),interaction.plot(Temp,Brand,Time,
            type="b", pch=19, col=c(2,4), ylab="", xlab = "",
            main="Mean Time vs. Temp: Stirred = Yes",
            cex.main = 0.75, legend = FALSE))
legend("topright",
       title = "Brand",
       c("Name", "Store"),
       cex = 0.7,
       col = c("#DF536B", "#2297E6"),
       pch = c(19,19), lty = c(2,1)
title(xlab = "Temperature", ylab = "Mean Dissolving Time (Minutes)", line = 2.25, cex.lab = 0.9)
#```{r, echo=FALSE, message=FALSE, error=FALSE, fig.dim=c(6,3), dpi=250}
with(df_eff%>%filter(Stirred=="no"),interaction.plot(Temp,Brand,Time,
          type="b", pch=19, col=c(2,4), ylab="", xlab = "",
          main="Mean Time vs. Temp: Stirred = No",
          cex.main = 0.75, legend = FALSE))
legend("topright",
       title = "Brand",
       c("Name", "Store"),
       cex = 0.7,
       col = c("#DF536B", "#2297E6"),
       pch = c(19,19), lty = c(2,1)
title(xlab = 'Temperature', ylab = "Mean Dissolving Time (Minutes)", line = 2.25, cex.lab = 0.9)
aov_eff <- aov(lm_eff <- lm(Time ~ Brand * Temp * Stirred, data = df_eff))</pre>
```

```
#cooksD_values <- cooks.distance(lm_eff)</pre>
\#qqplot() + qeom_col(aes(y = cooksD_values, x = 1:length(cooksD_values)), width = 0.025, col = 'red')
             qeom\_point(aes(y = cooksD\_values, x = 1:length(cooksD\_values))) + xlab('Sample Points') + ylab("CooksD\_values)))
             qeom_hline(yintercept = 0.25, lty = 2) + labs(title = "Cook's Distance for each sample point")
ols_plot_cooksd_chart(lm_eff)
qqnorm(lm_eff$resid, pch = 20)
qqline(lm eff$resid, col = "maroon", lwd = 2)
means_eff <- emmeans(aov_eff, specs = c('Brand', 'Temp', 'Stirred'))</pre>
#summary(means_eff)
cont_str_brd <-</pre>
contrast(means_eff, list(stirred = c(1/6, 1/6, 1/6, 1/6, 1/6, 1/6, -1/6, -1/6, -1/6, -1/6, -1/6, -1/6, -1/6)
                                                                   branding = rep(c(1/6,-1/6), 6)
                        )
cont_strbrd <-</pre>
contrast(means_eff, list(stirredbrand = c(1/3, 0, 1/3, 0, 1/3, 0, -1/3, 0, -1/3, 0, -1/3, 0),
                                                                  stirredstore = c(0, 1/3, 0, 1/3, 0, 1/3, 0, -1/3, 0, -1/3, 0, -1/3)
                        )
cont_temp <-
contrast(means_eff, list(temp6_23 = c(1/4, 1/4, -1/4, -1/4, 0, 0, 1/4, 1/4, -1/4, -1/4, 0, 0),
                                                                  temp6_40 = c(1/4, 1/4, 0, 0, -1/4, -1/4, 1/4, 1/4, 0, 0, -1/4, -1/4),
                                                                  temp23_40 = c(0, 0, 1/4, 1/4, -1/4, -1/4, 0, 0, 1/4, 1/4, -1/4, -1/4),
                                                                  temp6\_rest = c(1/4, 1/4, -1/8, -1/8, -1/8, -1/8, 1/4, 1/4, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8,
                                                                  temp23_rest = c(-1/8, -1/8, 1/4, 1/4, -1/8, -1/8, -1/8, -1/8, 1/4, 1/4, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8, -1/8
                                                                  temp40_rest = c(-1/8, -1/8, -1/8, -1/8, 1/4, 1/4, -1/8, -1/8, -1/8, -1/8, 1/4,
                                                                  ), options=list(adjust="bonferroni")
#knitr::kable(confint(cont_str_brd))
#knitr::kable(confint(cont_strbrd))
#knitr::kable(confint(cont_temp))
\#par(mfrow=c(2,2), mar = c(5,5,2,2))
#plot(aov_eff)
#knitr::kable(summary(aov_eff)[[1]], 'simple', caption = 'Model 1 ANOVA Results')
#model with stirred as block effect without interaction
#model2
aov_block_eff <- aov(lm_block_eff <- lm(Time ~ Brand * Temp + Stirred, data = df_eff))</pre>
#model3
aov_block_eff_noint <- aov(lm_block_eff <- lm(Time ~ Brand + Temp + Stirred, data = df_eff))</pre>
#summary(lm block eff)
#knitr::kable(summary(aov_block_eff)[[1]], caption = "Model 2: ANOVA Table")
\#par(mfrow=c(2,2), mar = c(5,5,2,2))
#plot(aov_block_eff)
#ols_plot_cooksd_chart(lm_block_eff)
#added covariate Order model with stirred as block effect without interaction
#model7
aov_block_order_eff <- aov(lm_block_order_eff <- lm(Time ~ Brand * Temp + Stirred + Order, data = df_ef
#summary(lm_block_order_eff)
#knitr::kable(summary(aov_block_order_eff)[[1]], caption = "Model 3: ANOVA Table")
#Anova(aov_block_order_eff, type=3) # type 3 SS
```

```
\#par(mfrow=c(2,2), mar = c(5,5,2,2))
#plot(lm_block_order_eff)
#ols_plot_cooksd_chart(lm_block_order_eff)
#added covariate Order to model with 3 factor interaction
#mode1.8
aov_three_order_eff <- aov(lm_three_order_eff <- lm(Time ~ Brand * Temp * Stirred + Order, data = df_ef
#summary(lm_three_order_eff)
#knitr::kable(summary(aov_three_order_eff)[[1]], 'simple', caption = "Model 7: ANOVA Table")
#Anova(aov_three_order_eff, type=3) # type 3 SS
\#par(mfrow=c(2,2), mar = c(5,5,2,2))
#plot(lm_three_order_eff)
RMSE_function <- function(df_aov){</pre>
    r_mse <- sqrt(sum(df_aov$residuals^2)/df_aov$df)</pre>
    r_s \leftarrow 1 - tail(summary(df_aov)[1][[1]][[2]], n = 1) / sum(summary(df_aov)[1][[1]][2])
    a_r_s \leftarrow 1 - (1 - r_s)*(nrow(df_aov$model) - 1)/(df_aov$df)
    output_stats <- c(
        r_mse,
        r_s,
        a_r_s
    return(output stats)
}
model1 <- RMSE_function(aov_eff)</pre>
model2 <- RMSE_function(aov_block_eff)</pre>
model3 <- RMSE_function(aov_block_eff_noint)</pre>
model7 <- RMSE_function(aov_block_order_eff)</pre>
model8 <- RMSE_function(aov_three_order_eff)</pre>
knitr::kable(df_stats, caption = "Data Summary Table")
knitr::kable(summary(means_eff), caption = "Least Squares Means")
knitr::kable(confint(cont_str_brd), caption = "Contrast Stirred and Brand")
knitr::kable(confint(cont_strbrd), caption = "Contrast Stirred versus Brand")
knitr::kable(confint(cont_temp), caption = "Contrast Temperatures")
knitr::kable(summary(aov_eff)[[1]], 'simple', digits = 3, caption = 'Model 1: ANOVA Table')
knitr::kable(Anova(aov_eff, type=3), 'simple', digits = 3, caption = 'Model 1: Type III ANOVA Table') #
par(mfrow=c(2,2), mar = c(5,5,2,2))
plot(aov_eff, pch = 4)
knitr::kable(summary(aov_block_eff)[[1]], 'simple' , caption = "Model 2: ANOVA Table")
par(mfrow=c(2,2), mar = c(5,5,2,2))
plot(aov_block_eff, pch = 4)
knitr::kable(summary(aov_block_eff_noint)[[1]], 'simple', caption = "Model 3: ANOVA Table")
par(mfrow=c(2,2), mar = c(5,5,2,2))
plot(aov_block_eff_noint, pch = 4)
knitr::kable(summary(aov_block_order_eff)[[1]], caption = "Model 7: ANOVA Table")
#Anova(aov_block_order_eff, type=3) # type 3 SS
par(mfrow=c(2,2), mar = c(5,5,2,2))
plot(aov_block_order_eff, pch = 4)
knitr::kable(summary(aov_three_order_eff)[[1]], 'simple', caption = "Model 8: ANOVA Table")
#Anova(aov_three_order_eff, type=3) # type 3 SS
```

```
par(mfrow=c(2,2), mar = c(5,5,2,2))
plot(lm_three_order_eff, pch = 4)
```