

# Lab Exercise 9 - SI Units for Patriot Missile Launcher Rotation System (Simplified Academic Model)

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This is a famous surface-to-air missile defence system.

We will NOT model weapons — only the **launcher rotation mechanism**, which is a safe electromechanical academic system.

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## OBJECTIVE OF THIS LAB

Simulate a **missile launcher azimuth rotation system** using:

- DC Voltage Source
- Resistor
- Inductor
- DC Motor (simplified equations)
- Rotational Inertia
- Damper

We will write everything in **text editor mode (no graphical view)**.

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## PHYSICAL IDEA OF THE SYSTEM

The launcher rotates left or right to aim toward a target.

Power → Motor → Shaft → Launcher Platform

The motor generates torque.

The platform has inertia.

Friction resists motion.

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## MATHEMATICAL MODEL

Electrical side:

$$V = R i + L \frac{di}{dt} + k \omega$$

Mechanical side:

$$J \frac{d\omega}{dt} = k i - b \omega$$

Where:

$V$  = applied voltage

$i$  = current

$\omega$  = angular velocity

$J$  = inertia

$b$  = damping

$k$  = motor constant

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## STEP 1: CREATE A NEW MODEL

Open OEdit

File → New Modelica Class

Name: **PatriotLauncherSystem**

Type: **Model**

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## STEP 2: COMPLETE MODEL CODE

Paste the following complete code:

```
model PatriotLauncherSystem
  import Modelica.SIunits;

  parameter SIunits.Resistance R = 2 "Armature resistance (Ohm)";
  parameter SIunits.Inductance L = 0.5 "Armature inductance (H)";
  parameter SIunits.Inertia J = 5 "Launcher inertia (kg.m2)";
  parameter Real k = 0.8 "Motor constant (Nm/A)";
  parameter Real b = 1 "Damping coefficient (Nms)";

  SIunits.Current i(start=0);
  SIunits.AngularVelocity w(start=0);
  SIunits.Angle theta(start=0);

  SIunits.Voltage V;

equation
```

```
// Input voltage (step command to rotate launcher)
V = if time < 1 then 0 else 24;

// Electrical equation
L*der(i) + R*i + k*w = V;
// Mechanical equation
J*der(w) = k*i - b*w;
// Angular position
der(theta) = w;
end PatriotLauncherSystem;
```

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### STEP 3: SIMULATION SETTINGS

Simulation → Setup

Start Time = 0

Stop Time = 5

Click Simulate.

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### STEP 4: PLOT RESULTS

Plot:

- theta (angular position)
- w (angular velocity)
- i (current)