

Code the below question in c++

Given two integer array A and B of size N each.

A sum combination is made by adding one element from array A and another element of array B.

Return the maximum K valid sum combinations from all the possible sum combinations.

Note : Output array must be sorted in non-increasing order.

Example 1:

Input:

N = 2

K = 2

A [] = {3, 2}

B [] = {1, 4}

Output: {7, 6}

Explanation:

7 -> (A : 3) + (B : 4)

6 -> (A : 2) + (B : 4)

Example 2:

Input:

N = 4

K = 3

A [] = {1, 4, 2, 3}

B [] = {2, 5, 1, 6}

Output: {10, 9, 9}

Explanation:

10 -> (A : 4) + (B : 6)

9 -> (A : 4) + (B : 5)

9 -> (A : 3) + (B : 6)

Your Task:

You don't need to read input or print anything. Your task is to complete the function `maxCombinations()` which takes the integer N, integer K and two integer arrays A [] and B [] as parameters and returns the maximum K valid distinct sum combinations .

Expected Time Complexity:  $O(N \log(N))$

Expected Auxiliary Space:  $O(N)$

Constraints:

$1 \leq N \leq 105$

$1 \leq K \leq N$

$1 \leq A[i], B[i] \leq 104$



To solve this problem, we can use the following approach:

### Approach:

1. **Sort both arrays A and B:** This will allow us to efficiently generate the largest sum combinations, as the largest sums will come from the largest elements of both arrays.
2. **Use a Max-Heap (Priority Queue):** The goal is to find the maximum K sums. A max-heap will allow us to quickly extract the largest sums. In C++, the `priority_queue` is a max-heap by default.
3. **Generate sum combinations:** Start by adding the largest element of A with the largest element of B. After that, we will generate possible sum combinations by moving one element from A and one element from B while ensuring that the combinations are distinct.
4. **Store the results in a heap:** We will maintain a max-heap to keep track of the largest combinations. As we generate combinations, we insert them into the heap and extract the top K largest combinations.

### Steps:

1. Sort arrays A and B in descending order.
2. Push the sum of the largest elements of A and B into the heap.
3. For each combination, push the next possible combinations into the heap, and track the already visited indices to avoid duplicates.
4. Extract the top **K** sums from the heap.

### Code Implementation:

```
cpp Copy code

#include <iostream>
#include <vector>
#include <queue>
#include <set>

using namespace std;

vector<int> maxCombinations(int N, int K, vector<int>& A, vector<int>& B) {
    // Sort both arrays in descending order
    sort(A.begin(), A.end(), greater<int>());
    sort(B.begin(), B.end(), greater<int>());

    // Max-Heap to store the combinations
    priority_queue<pair<int, pair<int, int>>> maxHeap;

    // Set to track visited pairs of indices
    set<pair<int, int>> visited;

    // Insert the first combination (A[0] + B[0]) into the max-heap
    maxHeap.push({A[0] + B[0], {0, 0}});
    visited.insert({0, 0});

    vector<int> result;

    // Generate the top K combinations
    while (K-- > 0) {
        // Get the current max combination
        auto top = maxHeap.top();
        maxHeap.pop();

        int sum = top.first;
        int i = top.second.first;
        int j = top.second.second;

        // Add the sum to the result
        result.push_back(sum);

        // Try to add the next element from A or B to the current sum combination
        if (i + 1 < N && visited.find({i + 1, j}) == visited.end()) {
            maxHeap.push({A[i + 1] + B[j], {i + 1, j}});
            visited.insert({i + 1, j});
        }

        if (j + 1 < N && visited.find({i, j + 1}) == visited.end()) {
            maxHeap.push({A[i] + B[j + 1], {i, j + 1}});
            visited.insert({i, j + 1});
        }
    }

    return result;
}

int main() {
    // Example 1
    vector<int> A1 = {3, 2};
    vector<int> B1 = {1, 4};
```

```

int N1 = 2;
int K1 = 2;
vector<int> result1 = maxCombinations(N1, K1, A1, B1);
for (int val : result1) {
    cout << val << " ";
}
cout << endl; // Output: 7 6

// Example 2
vector<int> A2 = {1, 4, 2, 3};
vector<int> B2 = {2, 5, 1, 6};
int N2 = 4;
int K2 = 3;
vector<int> result2 = maxCombinations(N2, K2, A2, B2);
for (int val : result2) {
    cout << val << " ";
}
cout << endl; // Output: 10 9 9

return 0;
}

```

### Explanation:

1. **Sorting:** Both **A** and **B** are sorted in descending order so that the largest elements are considered first when generating combinations.
2. **Max-Heap:** We use a max-heap (priority queue) to store the sum of elements from **A[i] + B[j]**, along with the indices **(i, j)** to track which elements from **A** and **B** were used to form the sum. This allows efficient extraction of the maximum sum combination.
3. **Visited Set:** A **set** is used to ensure that we don't revisit the same index pair **(i, j)** multiple times, avoiding duplicate combinations.
4. **Main Logic:**
  - Initially, we push the largest combination **(A[0] + B[0])** into the heap.
  - Then we generate new sums by incrementing either the index in **A** or in **B** and push these combinations into the heap.
  - The top **K** largest sums are extracted from the heap and returned as the result.

### Time Complexity:

- Sorting both arrays takes  $O(N \log N)$ .
- The priority queue operations (insertions and deletions) take  $O(\log N)$ , and we perform at most **K** such operations.
- Overall, the time complexity is dominated by  $O(N \log N)$  due to the sorting step.

### Space Complexity:

- We use a priority queue and a set to store combinations, so the space complexity is  $O(N)$ .

### Edge Cases:

- If **K = 1**, we should return just the single largest combination.
- If **N = 1**, only one sum combination will be possible.



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