

L16. M-Coloring Problem | Backtracking

Day10: (Recursion and Backtracking)

1. Print all Permutations of a string/array

https://www.youtube.com/watch?v=f2ic2Rsc9pU&list=PLgUwDviBIf0p4ozDR_kJJkONnb1wdx2Ma&index=52

2. N queens Problem

https://www.youtube.com/watch?v=i05Ju7AftcM&list=PLgUwDviBIf0p4ozDR_kJJkONnb1wdx2Ma&index=57

3. Sudoku Solver

https://www.youtube.com/watch?v=FWAIf_EVUKE&list=PLgUwDviBIf0p4ozDR_kJJkONnb1wdx2Ma&index=58

4. M coloring Problem

5. Rat in a Maze

6. Word Break (print all ways)

M-Coloring Problem

Medium Accuracy: 33.66% Submissions: 6921 Points: 4

Given an undirected graph and an integer **M**. **The task is to determine if the graph** can be colored with at most M colors such that no two adjacent vertices of the graph are colored with the same color. Here coloring of a graph means the assignment of colors to all vertices. Print 1 if it is possible to colour vertices and 0 otherwise.

Example 1:

Input:

N = 4

M = 3

E = 5

Edges[] = {(1,2),(2,3),(3,4),(4,1),(1,3)}

Output: 1

Explanation: It is possible to colour the given graph using 3 colours.

M-Coloring Problem**Medium** Accuracy: 33.66% Submissions: 6921 Points: 4

Given an undirected graph and an integer **M**. The task is to determine if the graph can be colored with at most M colors such that no two adjacent vertices of the graph are colored with **the same color**. Here coloring of a graph means the assignment of colors to all vertices. Print 1 if it is possible to colour vertices and 0 otherwise.

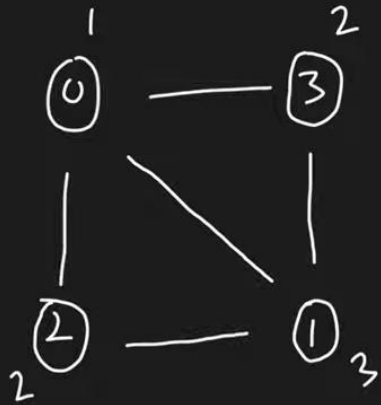
Example 1:**Input:** $N = 4$ $M = 3$ $E = 5$ $\text{Edges[]} = \{(1,2), (2,3), (3,4), (4,1), (1,3)\}$ **Output:**

Explained: It is possible to colour the graph using 3 colours.

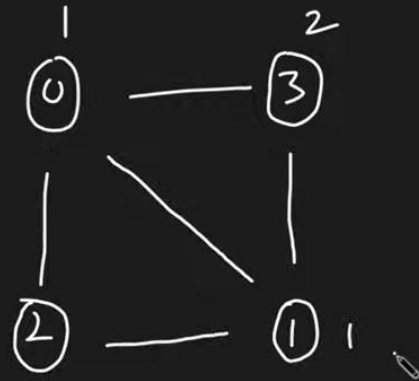
0:40 / 24:36



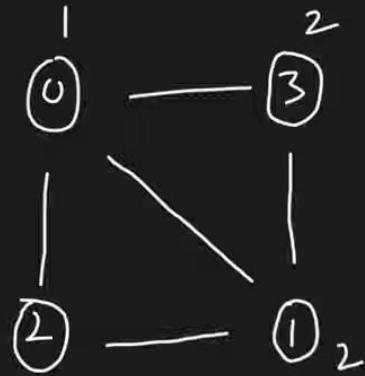
TUF



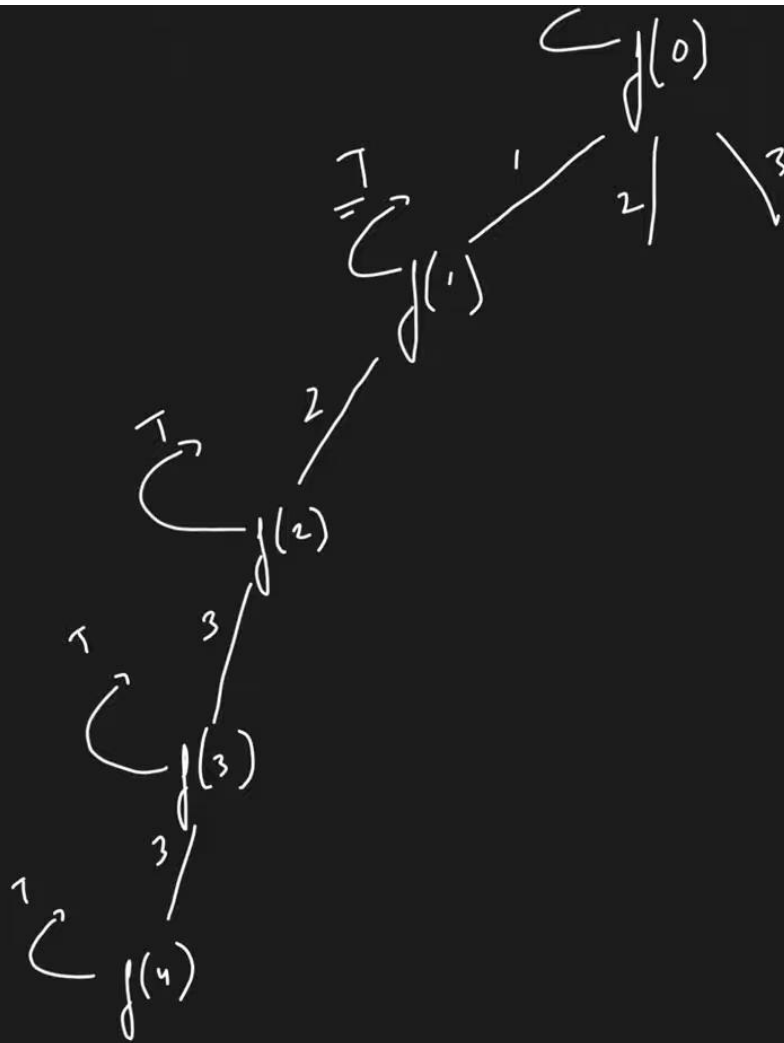
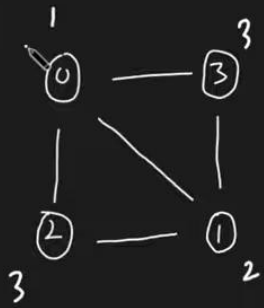
$$\underline{M = 3}$$



$$M = 2$$

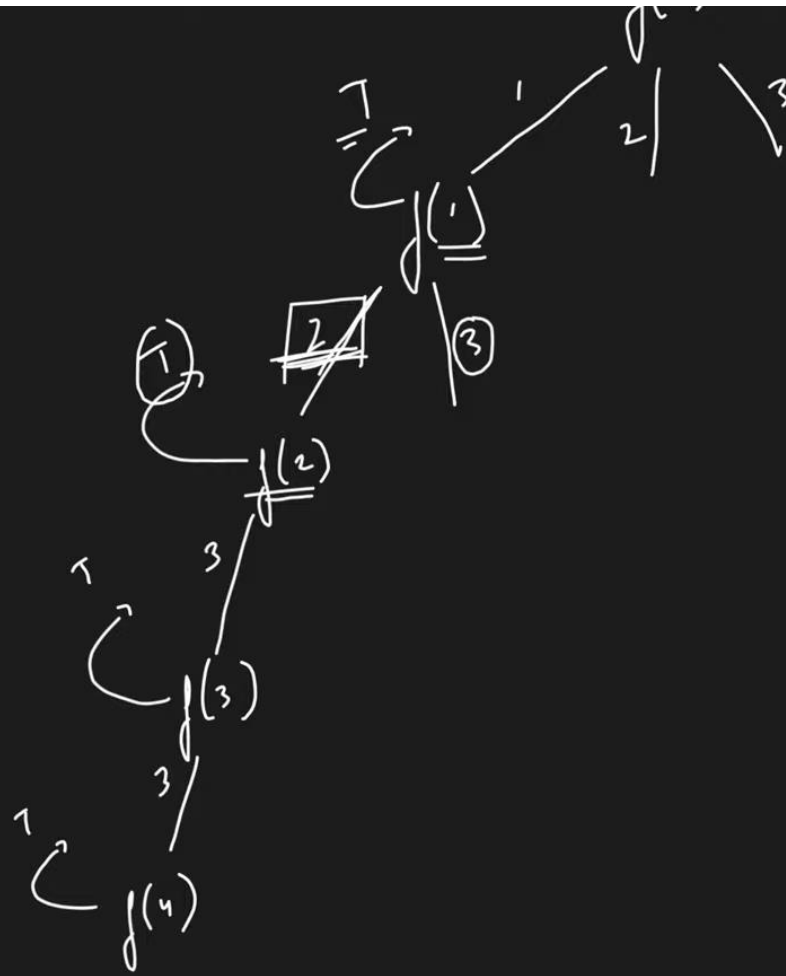
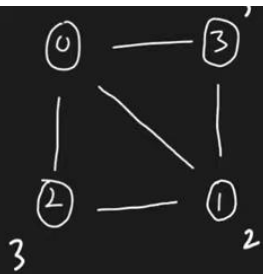


$$\underline{M \approx 2}$$



M=3

N=4



$f(\text{node})$

{
if (node == N) return T;
}

for (col = 1 → m)

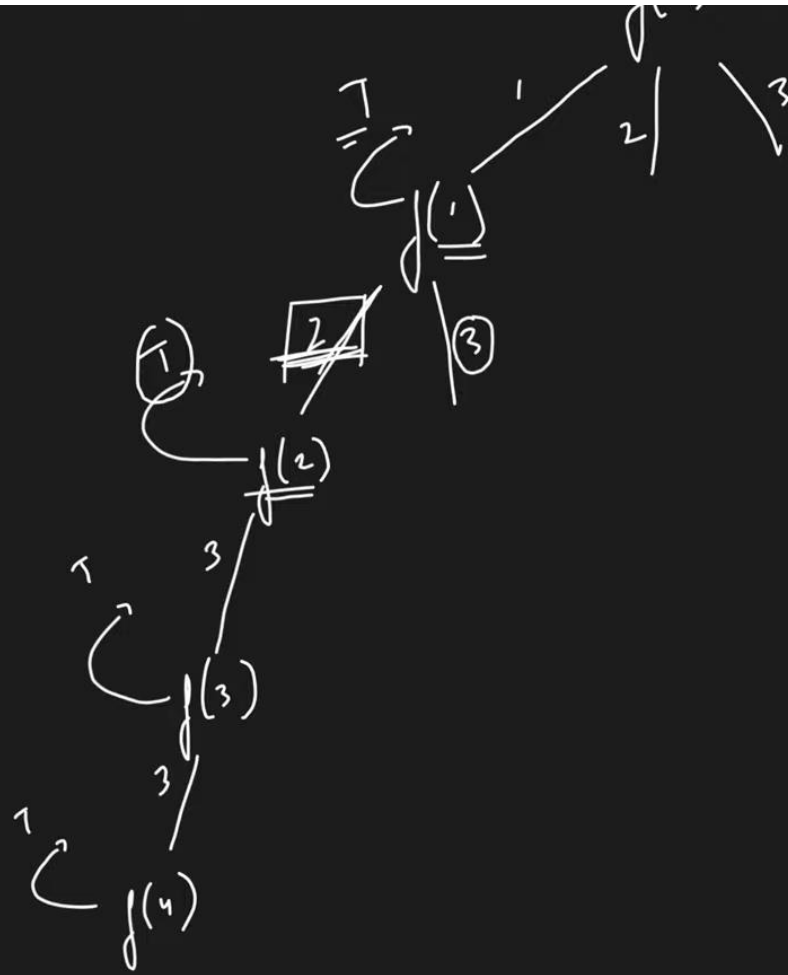
{
if (possible → ✓)

{
color[node] = col;

if (f(node + 1) == T)
return T;

{
color[node] = 0;

}



$g(\text{node} == N)$ return T ;

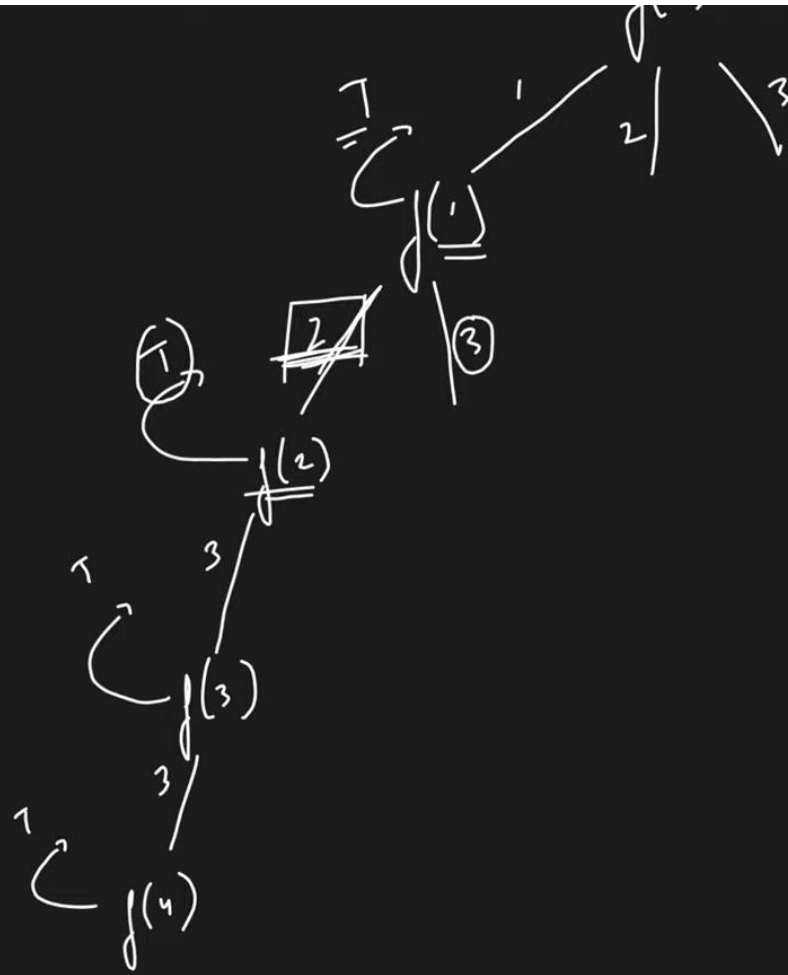
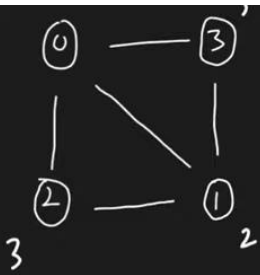
for $\{ \underline{col} = (\underline{1} \rightarrow \underline{n}) \}$
if (possible $\rightarrow \checkmark$)

$$\{ \text{column}[node] = col_j$$
$$if (j(\text{node} + 1) = -1)$$

```

3   color [node] = 0;

```



$f(\underline{\text{node}})$

{
if (node == N) return T;

for (col = 1 → m)

{
if (possible → ✓)

{
column[node] = col;

if (f(node + 1) == T)

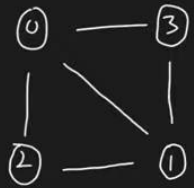
return T;

{
column[node] = 0;

{
return F;

N=3

N=4



$M=3^2$

$N=4$

$f(\text{node})$

{
if (node == N) return T;

for (col = (1 → m))

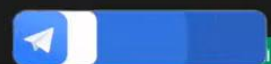
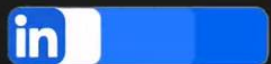
{
if (possible → ✓)

{
color[node] = col;

if (f(node+1) == T)
return T;

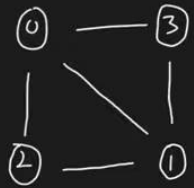
{
color[node] = 0;

}
return F;



1 changes saved!

TUF



$$\boxed{M=3^2}$$

$$\underline{\underline{N=4}}$$

f(node)

{ if (node == N) return T;

for (col = (1 → m))

{ if (possible → ✓)

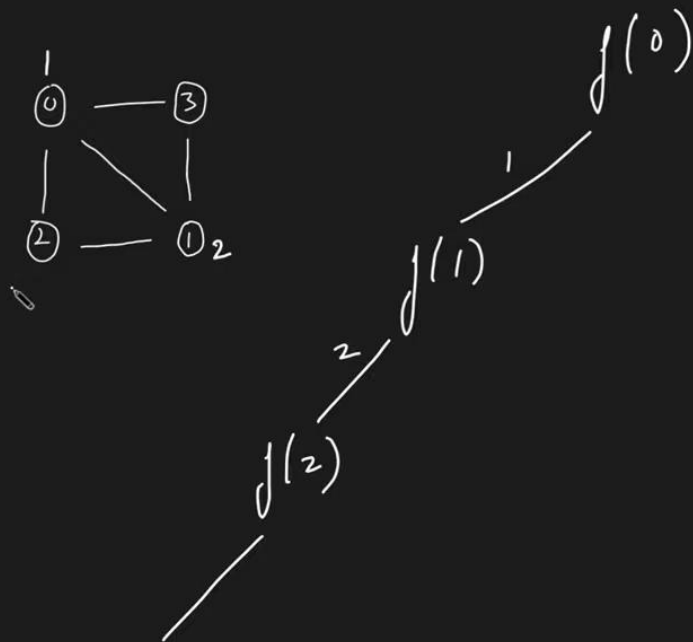
{ color[node] = col;

if (f(node+1) == T)

return T;

{ color[node] = 0;

{ return F;



$$\boxed{N=3^2}$$

$$\underline{N=4}$$

$$f(\underline{node})$$

$$\{ \text{if } (node == N) \text{ return } T;$$

$$f(\underline{col} = (1 \rightarrow m))$$

$$\{ \text{if } (possible \rightarrow \checkmark)$$

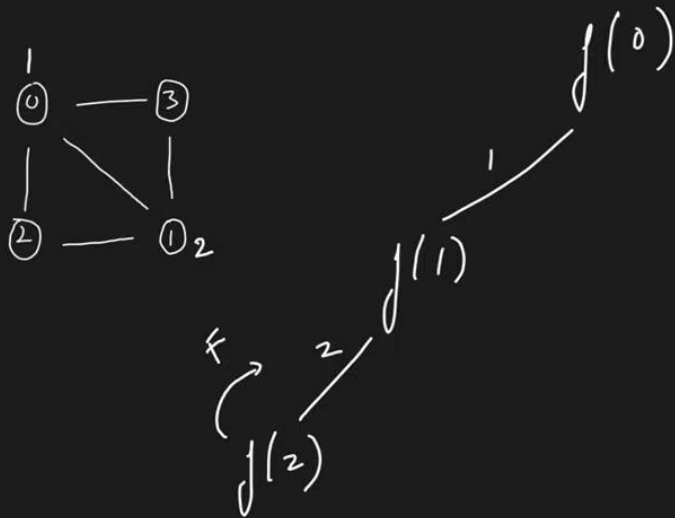
$$\{ \text{color}[node] = col;$$

$$\text{if } (f(node+1) == T)$$

$$\underline{\text{return } T};$$

$$\{ \text{color}[\underline{node}] = 0;$$

$$\{ \text{return } F;$$



$$\frac{14-3^2}{2}$$

$$\underline{N=7}$$

f(node)

{ if (node == N) return T;

for (col = (1 → m))

{ if (possible → ✓)

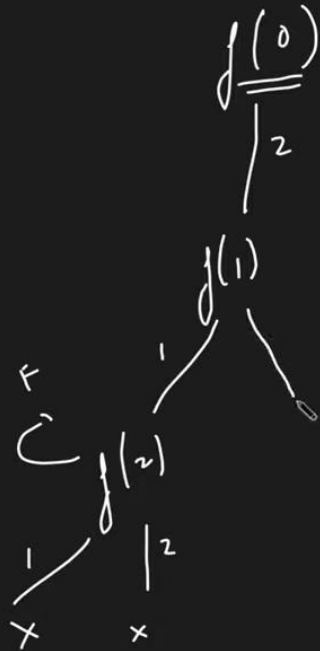
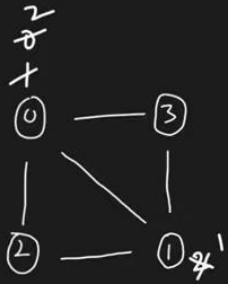
{ color[node] = col;

if (f(node+1) == T)

return T;

{ color[node] = 0;

{ return F;



$$\boxed{N=3^2}$$

$$\underline{\underline{N=9}}$$

```
f(node)
{
    if (node == N) return T;

```

```
    for (col = 1 -> m)
    {
        if (possible -> ✓)
        {

```

```
            color[node] = col; ✓
            if (f(node+1) == T)
            {
                return T;
            }
            color[node] = 0;
        }
    }
    return F;

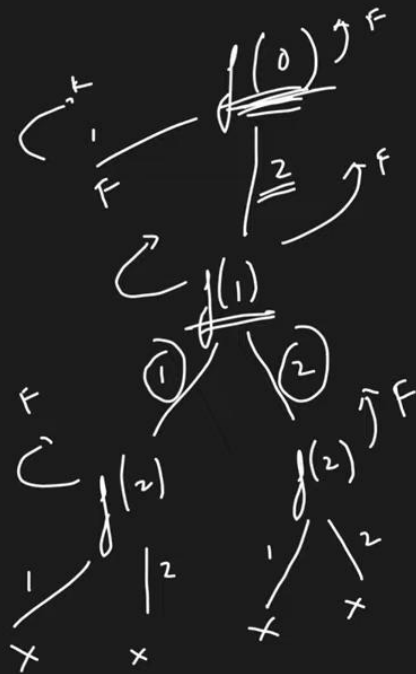
```

f(2) is possible ?

At f(1), we cannot use color 2, since adjacent nodes cannot have same color, I in a hurry just drew the tree of f(2), ignore that

```
    }
    return F;

```

$$\boxed{14-3^2}$$
$$N=4$$

for (col = (1 → m))
 if (possible → ✓)

$\{ \text{column}[\text{node}] = \text{col}; \checkmark_F$
 $\text{if } (j(\text{node} + 1) == 7)$
 $\quad \boxed{\text{return } T};$
 $\quad \text{column}[\text{node}] = 0;$

$$\rightarrow \underbrace{\text{return } F}_{\{ \}};$$

```

37
38
39 class solve
40 {
41     private static boolean isSafe(int node, List<Integer>[] G, int[] color, int n, int col) {
42         for(int it: G[node]) {
43             if(color[it] == col) return false;
44         }
45         return true;
46     }
47     private static boolean solve(int node, List<Integer>[] G, int[] color, int n, int m) {
48         if(node == n) return true;
49
50         for(int i = 1; i <= m; i++) {
51             if(isSafe(node, G, color, n, i)) {
52                 color[node] = i;
53                 if(solve(node+1, G, color, n, m) == true) return true;
54                 color[node] = 0;
55             }
56         }
57         return false;
58     }
59     public static boolean graphColoring(List<Integer>[] G, int[] color, int i, int m)
60     {
61         int n = G.length;
62         if(solve(i, G, color, n, m) == true) return true;
63         return false;
64         // Your code here
65     }
66 }
67
68

```

```

37
38
39 class solve
40 {
41     private static boolean isSafe(int node, List<Integer>[] G, int[] color, int n, int col) {
42         for(int it: G[node]) {
43             if(color[it] == col) return false;
44         }
45         return true;
46     }
47     private static boolean solve(int node, List<Integer>[] G, int[] color, int n, int m) {
48         if(node == n) return true;
49
50         for(int i = 1; i <= m; i++) {
51             if(isSafe(node, G, color, n, i)) {
52                 color[node] = i;
53                 if(solve(node+1, G, color, n, m) == true) return true;
54                 color[node] = 0;
55             }
56         }
57         return false;
58     }
59     public static boolean graphColoring(List<Integer>[] G, int[] color, int i, int m)
60     {
61         int n = G.length;
62         if(solve(i, G, color, n, m) == true) return true;
63         return false;
64         // Your code here
65     }
66 }
67
68

```

```

9
10
11- bool isSafe(int node, int color[], bool graph[101][101], int n, int col) {
12-     for(int k = 0; k < n; k++) {
13-         if(k != node && graph[k][node] == 1 && color[k] == col) {
14-             return false;
15-         }
16-     }
17-     return true;
18- }
19- bool solve(int node, int color[], int m, int N, bool graph[101][101]) {
20-     if(node == N) {
21-         return true;
22-     }
23-
24-     for(int i = 1; i <= m; i++) {
25-         if(isSafe(node, color, graph, N, i)) {
26-             color[node] = i;
27-             if(solve(node+1, color, m, N, graph)) return true;
28-             color[node] = 0;
29-         }
30-     }
31-     return false;
32- }
33-
34-
35- //Function to determine if graph can be coloured with at most M colours such
36- //that no two adjacent vertices of graph are coloured with same colour.
37- bool graphColoring(bool graph[101][101], int m, int N)
38- {
39-     int color[N] = {0};
40-     if(solve(0, color, m, N, graph)) return true;
41-     return false;
42- }
43- // } Driver Code Ends

```