

## 4nodes\_3

April 12, 2019

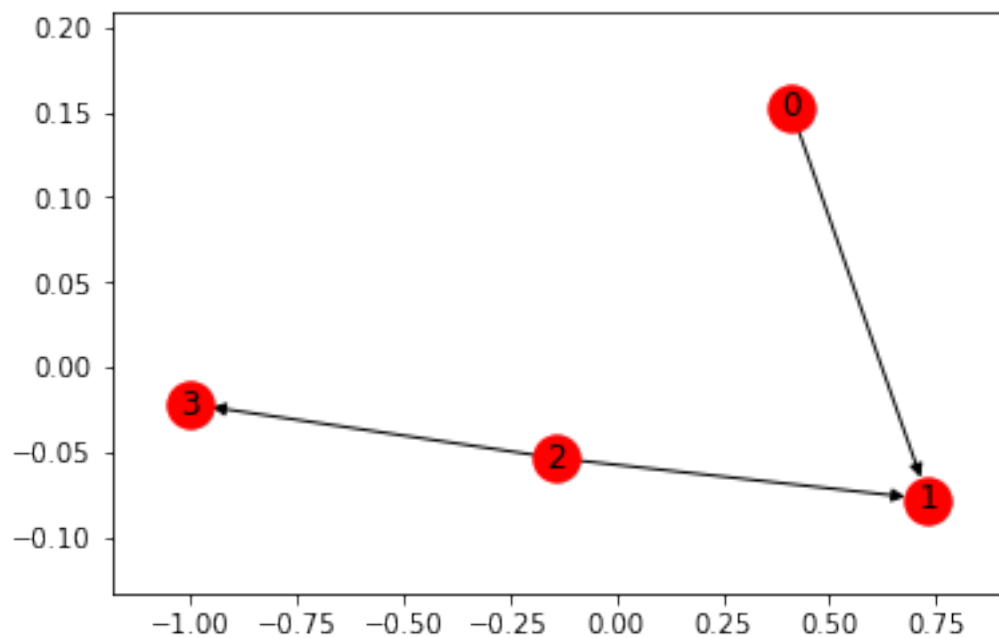
### 0.1 4 nodes

```
In [1]: %run ../imports.py
```

```
In [2]: G = nx.DiGraph()
```

```
In [3]: G.add_nodes_from([0,1,2,3])
        G.add_edges_from([
            (0,1),
            (2,1),
            (2,3)
        ])
```

```
In [4]: nx.draw_networkx(G)
```



```
In [5]: L = out_degree_laplacian(G)
        np.linalg.matrix_rank(L)
```

Out [5]: 2

```
In [6]: Q = orth_matrix(L).T
rL = np.matmul(Q, np.matmul(L, np.transpose(Q)))
sigma = solve_lyapunov(rL, np.identity(np.linalg.matrix_rank(L)))
x = 2*np.matmul(np.transpose(Q), np.matmul(sigma, Q))
eqL = np.linalg.pinv(x)
```

In [7]: Q

```
Out [7]: matrix([[ 0.09200377, -0.48173799,  0.77946844, -0.38973422],
                 [-0.73279591,  0.55980626,  0.3459793 , -0.17298965]])
```

In [8]: sigma

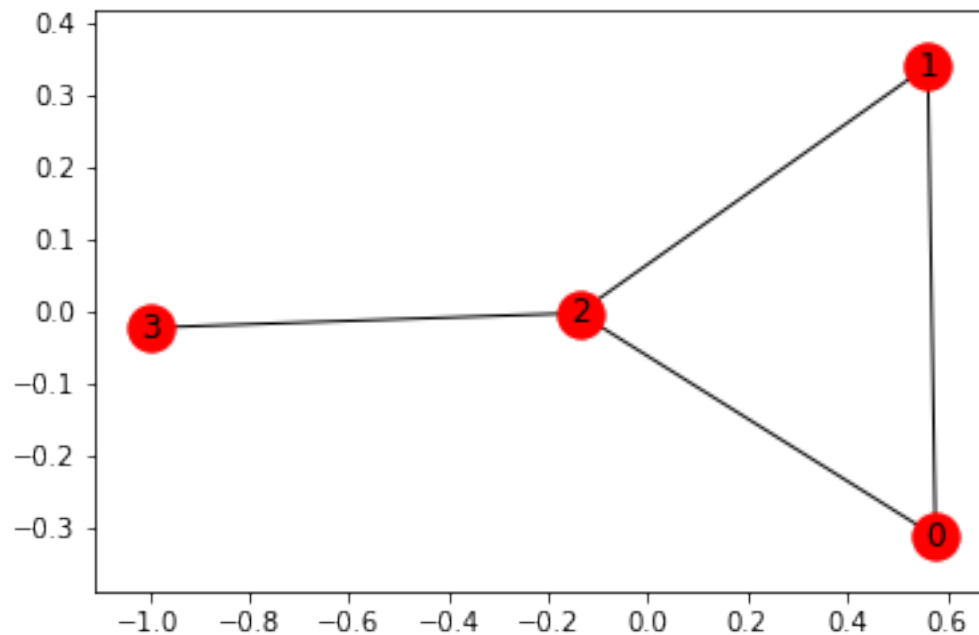
```
Out [8]: array([[ 0.26020852, -0.05618332],
                [-0.05618332,  0.49736724]])
```

In [9]: eqL

```
Out [9]: matrix([[ 0.54, -0.42, -0.24,  0.12],
                 [-0.42,  0.66, -0.48,  0.24],
                 [-0.24, -0.48,  1.44, -0.72],
                 [ 0.12,  0.24, -0.72,  0.36]])
```

In [10]: posG, negG = separate\_graphs(eqL)

In [12]: nx.draw\_networkx(posG)



```
In [13]: nx.draw_networkx(negG)
```

