

Ma323-LAB 09

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This Lab assignment was done by using the values of $\mu = 0.0002981060700200021$ and $\sigma^2 = 0.000496475360718651$ and $S(0)=185.399994$ as calculated in Lab 7.

For simulating the BSM model with the ratio of asset price after and before a jump should follow the log-normal distribution $LN(\mu, \sigma^2)$, I have used the first approach i.e. Simulating the dates to generate the path of stock prices $S(t)$.

The stock prices $S(t)$ were generated for $N \sim \text{Poisson}(\lambda)$ for $\lambda = 0.1$.

Mean and variance of the price of avg price Asian put option calculated without using control variate with the payoff formula given in the lab assignment, and are tabulated below:

$\hat{\mu}$ (sampling mean)	$\hat{\sigma}$ (sampling variance)
21.524791304962715	623.9950622528808

The calculated **95% Confidence interval** is: $[-17.15082334522346, 60.200405955148895]$

Mean and variance of the same avg price Asian put option calculated by using the price of an European put option as the control variate are tabulated below:

$\hat{\mu}$	$\hat{\sigma}$
21.524791304962715	214.19639211420284

Note:

- After introducing the control variate the variance decreases from 623.9950622528808 to 214.19639211420284.
- It can be seen that even after introducing the control variate the $\hat{\mu}$ remains same which shows that the control variate (European put option price) is an unbiased estimator.

The output of the code can be seen below:

```
TERMINAL  PROBLEMS 4  OUTPUT  DEBUG CONSOLE  1: cmd
C:\Users\harshy\Desktop\Ma323_Monte_Carlo_Simulation\Lab9>python 180123015-harsh.py
Mean of the price of avg price Asian put option calculated without using control variate is: 21.524791304962715
Variance of the price of avg price Asian put option calculated without using control variate is: 623.9950622528808
Confidence Interval: [ -17.15082334522346 , 60.200405955148895 ]
Mean of the same avg price Asian put option calculated by using the price of an European put as the control variate is: 21.524791304962715
Variance of the same avg price Asian put option calculated by using the price of an European put as the control variate is: 214.19639211420284
C:\Users\harshy\Desktop\Ma323_Monte_Carlo_Simulation\Lab9>
```

Reference for data: <https://finance.yahoo.com/quote/SBIN.NS/history/>