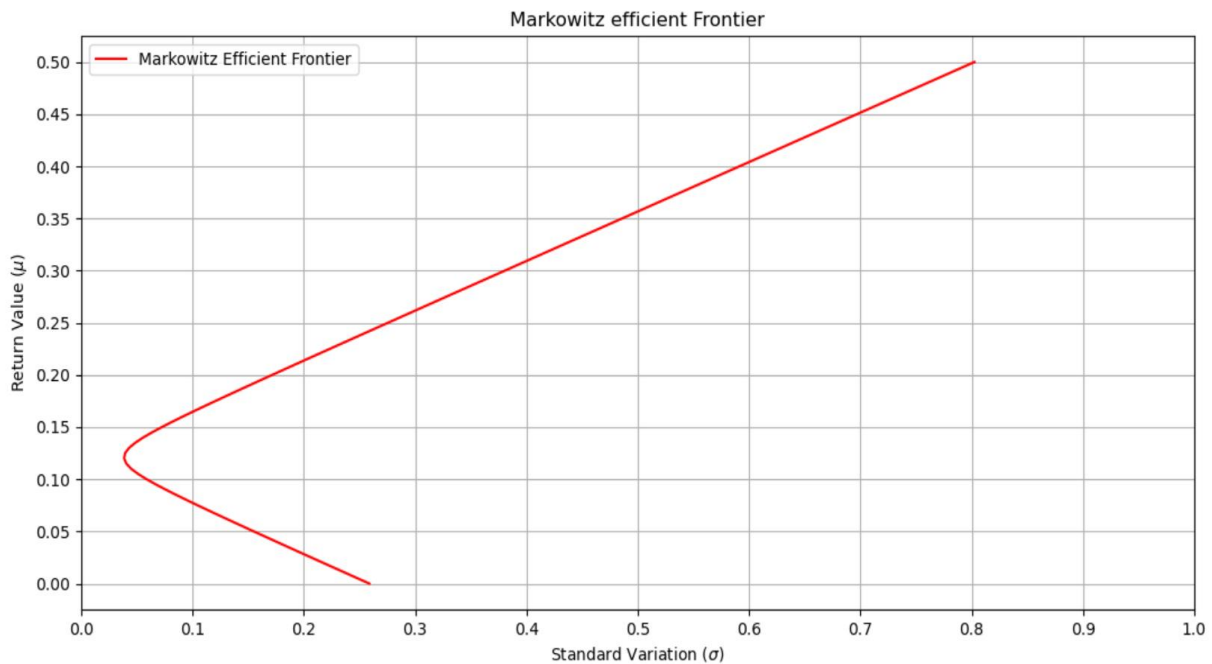


## Ma374-LAB 04

**Name:** Harsh Yadav **Roll. No.:** 180123015 **Dept.:** Mathematics and Computing  
**Submission Date:** 11-02-2021

### Question 1:

- i. The Markowitz efficient frontier for the given mean return vector and covariance matrix is shown below:



- ii. The weights, return and risk of the portfolios for 10 different values on the efficient frontier are tabulated below:

Return	Risk (SD)	w1	w2	w3
0.0	0.259	2.55	-0.45	-1.101
0.05	0.155	1.835	-0.165	-0.67
0.1	0.059	1.119	0.119	-0.239
0.15	0.072	0.404	0.404	0.193
0.2	0.171	-0.312	0.688	0.624
0.25	0.276	-1.028	0.972	1.055
0.3	0.381	-1.743	1.257	1.486
0.35	0.486	-2.459	1.541	1.917
0.4	0.591	-3.174	1.826	2.349
0.45	0.697	-3.89	2.11	2.78
0.5	0.803	-4.606	2.394	3.211

- iii. For a 15% risk, the maximum return is 0.1896  
Corresponding Portfolio:  $w_1 = -0.1624$   $w_2 = 0.6287$   $w_3 = 0.5338$

For a 15% risk, the minimum return is 0.0524  
Corresponding Portfolio:  $w_1 = 1.7998$   $w_2 = -0.1512$   $w_3 = -0.6486$

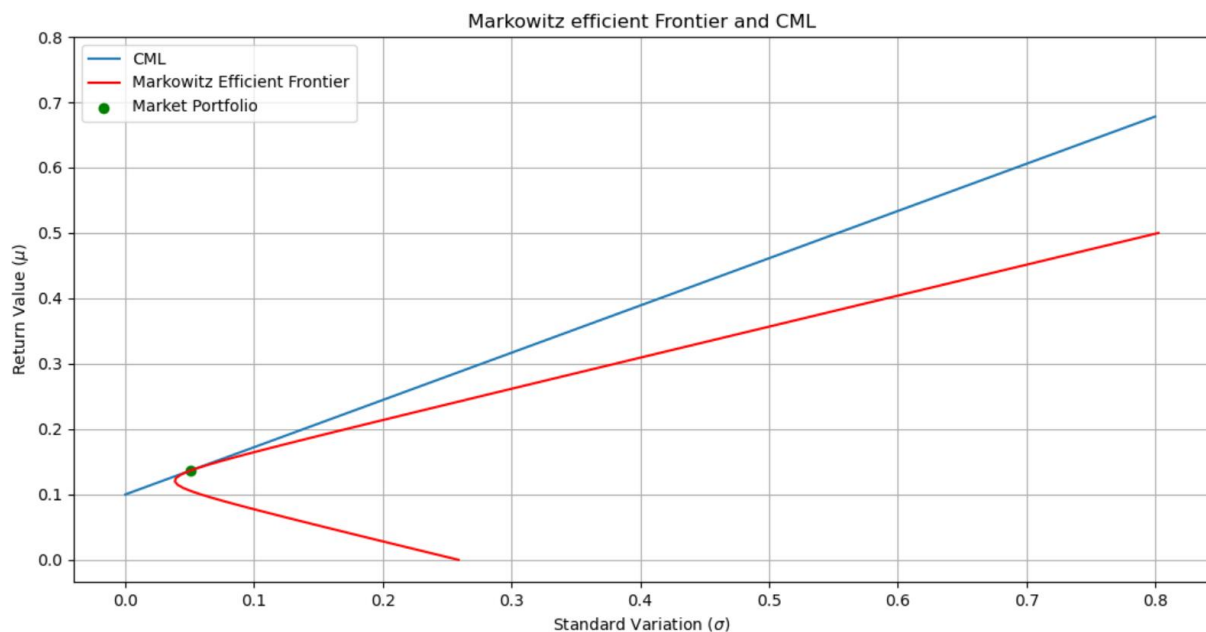
- iv. For a 18% return, the minimum risk is 13.0568 %  
Corresponding Portfolio:  $w_1 = -0.0257$   $w_2 = 0.5743$   $w_3 = 0.4514$

**v. Market Portfolio:**

For a 10% risk free return, the return on market portfolio is 0.1367

For a 10% risk free return, the risk on market portfolio is 5.0811 %

Corresponding Portfolio:  $w_1 = 0.5938$   $w_2 = 0.3281$   $w_3 = 0.0781$

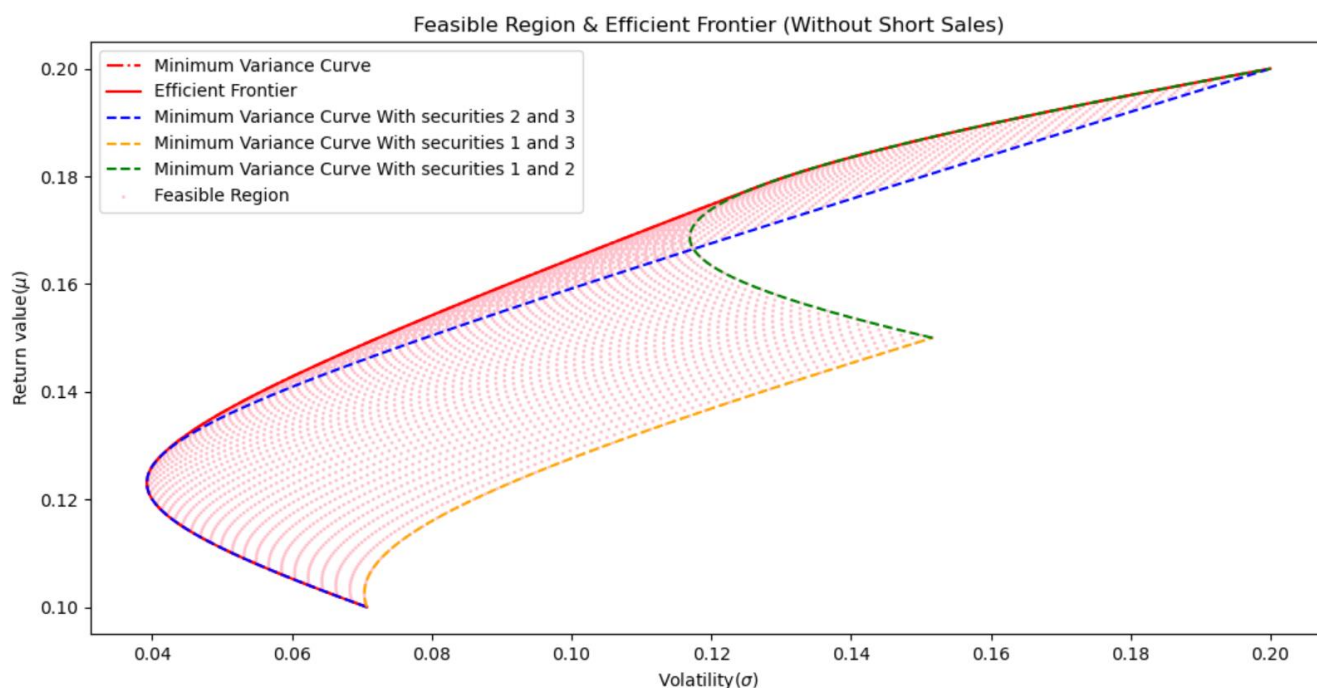


- vi. For a 10% risk free return, the required portfolio is:  
Corresponding Portfolio (Risky Asset):  $w_1 = 1.1685$   $w_2 = 0.6458$   $w_3 = 0.1538$   
Corresponding Portfolio (RiskFree Asset):  $w = -0.9681$

For a 25% risk free return, the required portfolio is:  
Corresponding Portfolio (Risky Asset):  $w_1 = 2.9213$   $w_2 = 1.6144$   $w_3 = 0.3844$   
Corresponding Portfolio (RiskFree Asset):  $w = -3.9202$

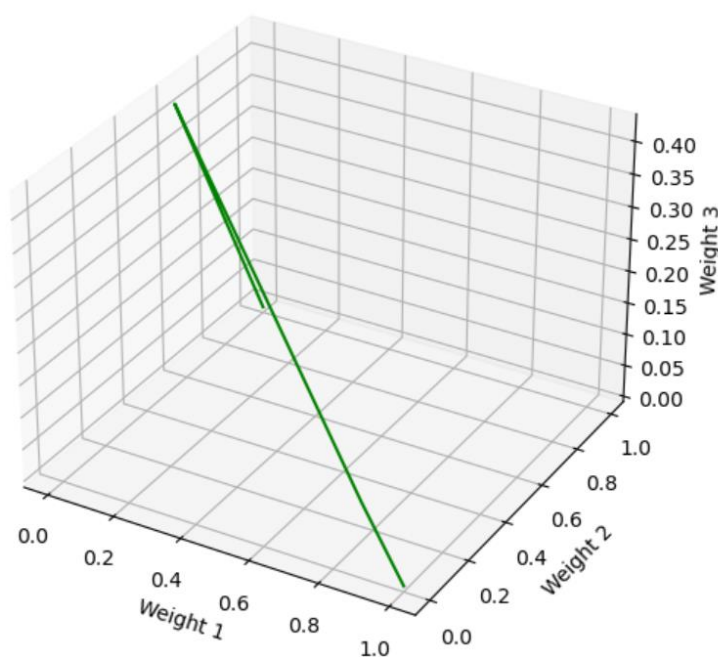
## Question 2:

- Assuming short selling is not allowed the efficient frontier, the minimum variance curve and the feasible region for the given mean return vector and covariance matrix were plotted in the same graph and is shown below. Also the minimum variance curves taking two-securities at a time were also plotted in the same plot.



- Weights of securities corresponding to Minimum Variance Curve with 3-securities:  
Equation:  $w_1 + w_2 + w_3 = 1$

Weights Corresponding to Minimum Variance Curve



- Plotting weights of two securities corresponding to the Minimum Variance Curve of the portfolio with 3 securities:

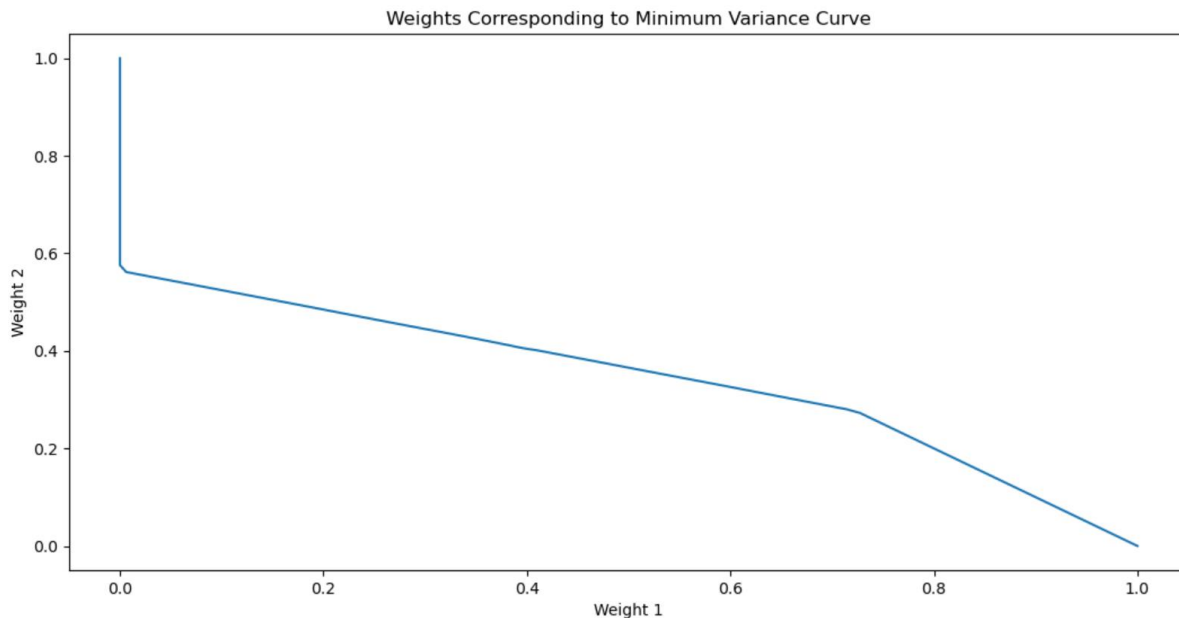
Equations:

$$w_1=0, 0.569 \leq w_2 \leq 1$$

$$w_1 = 2.484w_2 - 1.413, 0.278 \leq w_2 \leq 0.569$$

$$w_1 = 1 - 0.996w_2, 0 \leq w_2 \leq 0.278$$

$$w_3 = 1 - (w_1 + w_2)$$



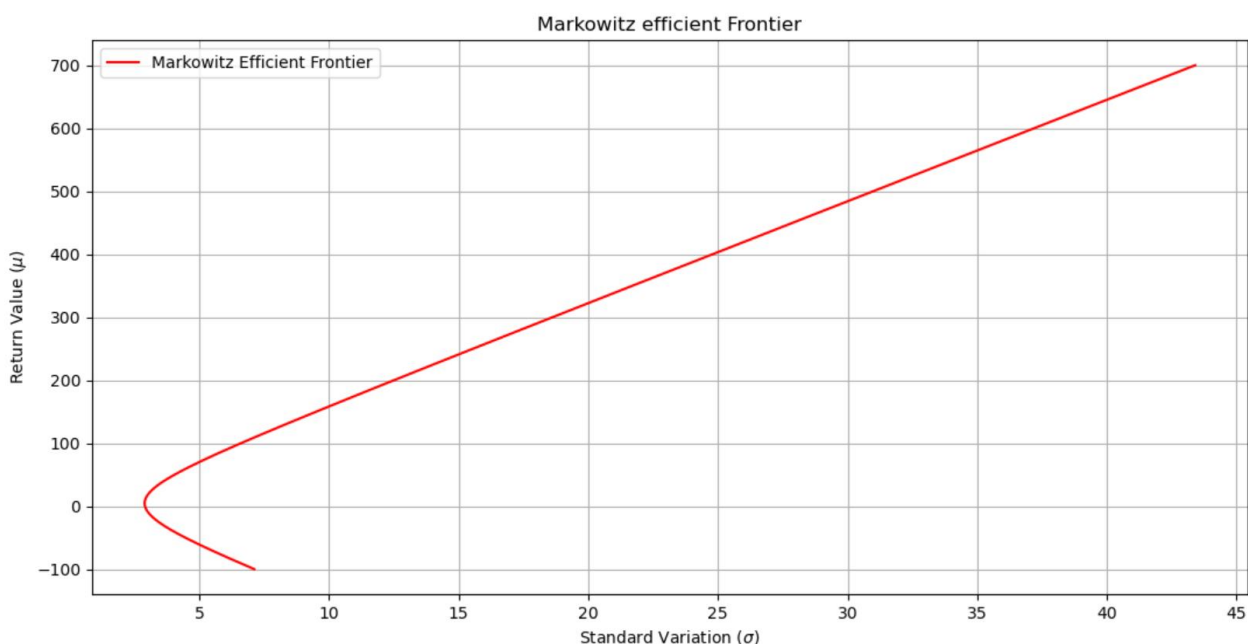
### Question 3:

For this particular question, we collected the monthly stock prices of the following companies: ["Google", "Airtel", "Microsoft", "Apple", "Tesla", "SBI", "Amazon", "Infosys", "Facebook", "Reliance"].

Mean return vector (M): [[1143 98 117 55 133 20 1664 52 178 32]]

Covariance matrix: printed on the console and can be seen from the output once code is executed

- The Efficient Frontier for the aforementioned assets is plotted below:



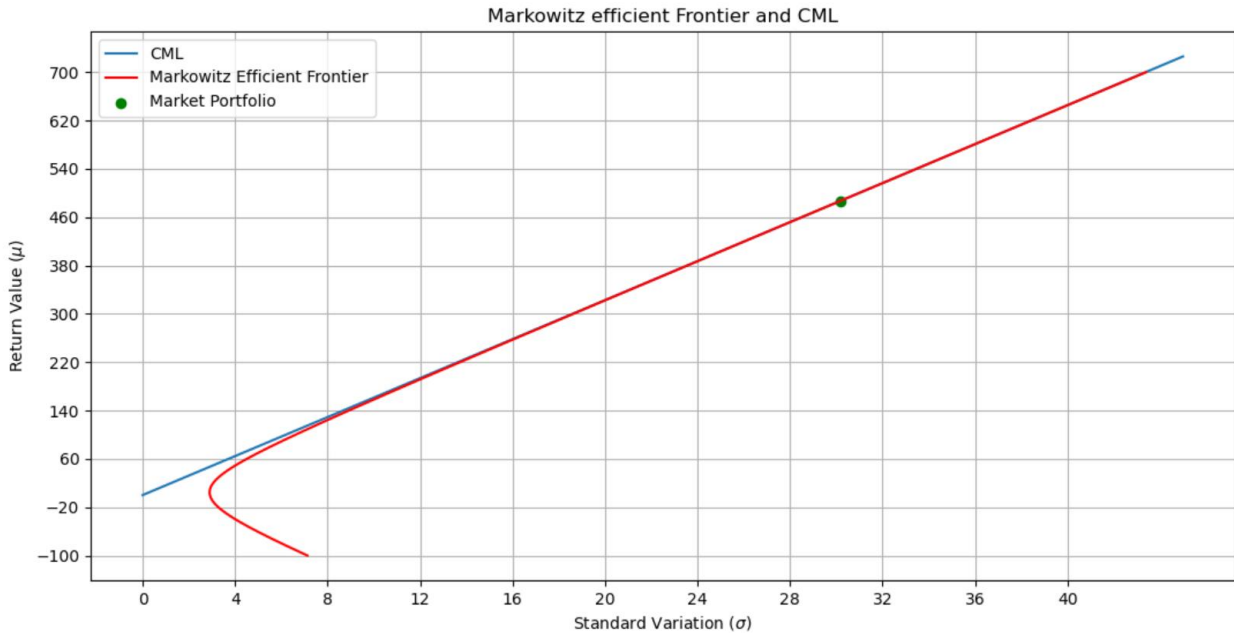
## ii. The Market Portfolio:

For a 5% risk free return, the return 486.8074

For a 5% risk free return, the risk 30.1702

$w_1 = 0.3562$  ,  $w_2 = 2.0556$  ,  $w_3 = -2.219$  ,  $w_4 = -0.3661$  ,  $w_5 = -0.1254$ ,  $w_6 = 0.1356$  ,  $w_7 = 0.081$  ,  
 $w_8 = -3.4991$  ,  $w_9 = 0.4965$  ,  $w_{10} = 4.0846$

iii. Capital Market Line and the Market Portfolio are plotted below:



iv.

