RBE549 - Midterm Exam

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Problem 1

In this problem we are presented with a Hough transform problem, wherein x, y, b, and m are positive or negative real numbers. 2 points are given in (m, b) space by $P_1 : (m, b) = (0.5, 4)$ and $P_2 : (m, b) = (0.9, 0)$.

\mathbf{A}

What line L_1 in (m, b) space through P_1 and P_2 ?

We can set the line equation (y = mx + b) for P_1 and P_2 equal to eachother to solve this.

$$P_1 = P_2 \tag{1}$$

$$0.5x + 4 = 0.9x + 0 \tag{2}$$

$$4 = 0.4x \tag{3}$$

$$10 = x \tag{4}$$

...and then we plug in x to solve for y:

$$0.5(10) + 4 = y \tag{5}$$

$$y = 9 \tag{6}$$

...thus the equation for L_1 , a line that passes through points P_1 and P_2 , is b = -10m + 9.

\mathbf{B}

The point P_3 in (x, y) space that corresponds to line L_1 is the point (10, 9), as calculated above in part A. We can also just deduce it from our solved equation mentioned in A - specifically that since y = mx + b for b = -mx + y, and we stated that b = -10m + 9, we can also deduce that (x, y) = (10, 9).

\mathbf{C}

Since it is a horizontal line, which means the slope m must be m = 0, we now know that the resulting point, P_4 , must fall along the line we calculated earlier, L_1 , specifically where m = 0, or the vertical axis of (m, b) space. Thus we can solve:

$$b = -10m + 9 \tag{7}$$

$$b = -10 * 0 + 9 \tag{8}$$

$$b = 9 \tag{9}$$

...thus we know that P_4 will fall on (m,b)=(0,9). This means that the equation for L_2 is y=9.

Problem 2

Problem 3

In this problem we are solving equations having to do with image focus and lenses.

\mathbf{A}

We aim to prove that for a thin lens, the image is in focus when:

$$\frac{1}{-z_O} + \frac{1}{z_c} = \frac{1}{f} \tag{10}$$