

Horizontal bar chart comparing the number of nodes generated by different heuristics across 15 test cases. The x-axis is logarithmic, ranging from 1 to 1,000,000. The y-axis lists test cases: PE1, PE2, PE3, PE4, PE5, PM1, PM2, PM3, PM4, PM5, PH1, PH2, PH3, PH4, PH5. The legend includes: No heuristic (blue), Forward Checking (green), Minimum Remaining Value (orange), Naked Pairs (red), FC + LCV + MRV + NT (light blue), Least Constraining Value (yellow), and Nakes Triples (purple).

Test Case	No heuristic	Forward Checking	Minimum Remaining Value	Naked Pairs	FC + LCV + MRV + NT	Least Constraining Value	Nakes Triples
PE1	~500,000	~200,000	~400,000	~400,000	~300,000	~400,000	~400,000
PE2	~400,000	~200,000	~400,000	~400,000	~300,000	~400,000	~400,000
PE3	~1,500,000	~500,000	~1,500,000	~1,500,000	~500,000	~1,500,000	~1,500,000
PE4	~800,000	~300,000	~800,000	~800,000	~300,000	~800,000	~800,000
PE5	~400,000	~200,000	~300,000	~300,000	~200,000	~300,000	~300,000
PM1	~800,000	~1,100,000	-	-	-	-	-
PM2	~400,000	-	-	-	-	-	-
PM3	~500,000	~900,000	-	-	-	-	-
PM4	~400,000	~1,500,000	-	-	-	-	-
PM5	~1,000,000	~1,100,000	-	-	-	-	-
PH1	~800,000	~1,100,000	-	-	-	-	-
PH2	~1,000,000	~900,000	-	-	-	-	-
PH3	~800,000	-	-	-	-	-	-
PH4	~500,000	-	-	-	-	-	-
PH5	~800,000	-	-	-	-	-	-

As you can see from our graph about it is clear that on average our Forward Checking, LCV, MRV and Naked Triples algorithm runs the fastest. More proof of this can be seen when looking at the statistics of running time/backtracks for each of the different algorithms:

No Heuristics: 33% Success Rate

PE1.txt : 0.13

PE2.txt : 0.13

PE3.txt : 0.02

PE4.txt : 0.03

PE5.txt : 0.13

The rest fail

Forward Checking: 78% Success Rate

PE1.txt : 2.7

PE2.txt : 2.625

PE3.txt : 0.58

PE4.txt : 2.07

PE5.txt : 2.5

PM1.txt : 0.308

PM2.txt : Failed to find solution

PM3.txt : 0.46

PM4.txt : 0.36

PM5.txt : 0.37

PH1.txt : 0.38

PH2.txt : 0.77

PH3.txt : Failed to Find Solution

PH4.txt : Failed to Find Solution

PH5.txt : Failed to Find Solution

LCV: 33% Success Rate

PE1.txt : 0.13

PE2.txt : 0.13

PE3.txt : 0.02

PE4.txt : 0.03

PE5.txt : 0.13

The rest fail

MRV: 33% Success Rate

PE1.txt : 0.13

PE2.txt : 0.13

PE3.txt : 0.02

PE4.txt : 0.03

PE5.txt : 0.13

The rest fail

Naked Pairs: 33% Success Rate

PE1.txt : 0.13

PE2.txt : 0.13

PE3.txt : 0.02

PE4.txt : 0.03

PE5.txt : 0.13

The rest fail

Forward Checking, LCV, MRV, Naked Triples 100% Success Rate

PE1.txt : 24.0

PE2.txt : 1.82

PE3.txt : 1.53

PE4.txt : 9.7

PE5.txt : 19.0

PM1.txt : 0.84

PM2.txt : 6.9

PM3.txt : 2.5

PM4.txt : 102

PM5.txt : 0.55

PH1.txt : 334

PH2.txt : 1.18

PH3.txt : 1.06

PH4.txt : 1.02

PH5.txt : 1.04

These values show that overall the amount of backtracks is on average lower than the total running time of the algorithm. Comparing these values with the values in the graph above it is evident that the Forward Checking, LCV, MRV, Naked Triples algorithm provides the best results for us.